

CSE 151A Intro to Machine Learning

Lecture 14 – Part 01
Boosting

So Far in CSE 151A

- Learn a single (sometimes complex) model:
 - Logistic Regression
 - SVMs
 - ► LDA/QDA
 - Decision Trees
 - **.**..

Today

Can we combine very simple models and get good results?

Yes: boosting.

Weak Learners

- A weak classifier is one which performs only a little better than chance.
- A learning algorithm capable of consistently producing weak classifiers is called a **weak learner**.
- Usually very simple, fast.

A decision stump is a weak classifier.



► **Weak learner**: the strategy discussed last time for picking question.

► The full decision tree learning algorithm is a **strong learner**.

The Question

Can we "boost" the quality of a weak learner?

Boosting: The Idea

- ► Train a weak classifier, $H_1: \mathcal{X} \rightarrow [-1, 1]$.
- Increase weight (importance) of misclassified points, train another classifier H_2 .
- Repeat, creating more classifiers, updating weights.
- Final classifier: a linear combination of $H_1, ..., H_k$.

The Details

▶ Q1: How do we measure the performance of a classifier on a weighted data set?

Q2: How do we update the point weights?

Q3: How do we combine the classifiers?

AdaBoost

- Yoav Freund (UCSD) and Robert Schapire.
- A theoretically-sound answer to these questions.

Q1: Measuring Performance

- Suppose weights at step t are in $\vec{w}^{(t)}$.
 - Assume normalized s.t. weights add to one.
- We use weights to learn a classifier $H_t: \mathcal{X} \to [-1, 1]$.
- The "margin":

$$r_t = \sum_{i=1}^n \omega_i^{(t)} y_i H_t(\vec{x}^{(i)}) \in [-1, 1]$$

Q1: Measuring Performance

▶ The **performance** of H_t :

$$\alpha_t = \frac{1}{2} \ln \frac{1 + r_t}{1 - r_t}$$

Q2: Updating Weights

- We use weights to learn a classifier $H_t: \mathcal{X} \to [-1, 1]$.
- Weigh misclassified points more heavily.
- Point is misclassified if $y_i H_t(\vec{x}^{(i)}) < 0$

Q2: Updating Weights

► This will do the trick:

$$\omega_i^{(t+1)} \propto \omega_i^{(t)} \cdot \exp\left(-\alpha_t y_i H_t(\vec{x}^{(i)})\right)$$

Q3: Combining Classifiers

► The final classifier:

$$H_t(\vec{x}) = \sum_{t=1}^{T} \alpha_t H_t(\vec{x})$$

AdaBoost

Given data $(\vec{x}^{(1)}, y_1), ..., (\vec{x}^{(n)}, y_n)$, labels in $\{-1, 1\}$.

- Initialize weight vector, $\vec{\omega}^{(1)} = (\frac{1}{n}, \frac{1}{n}, \dots, \frac{1}{n})^T$
- Repeat:
 - ► Give data and weights $\vec{\omega}^{(t)}$ to weak learner. Receive a classifier, $H_{+}: \mathcal{X} \to \{-1, 1\}$ back.
 - ► Calculate "performance", $\alpha_t = \frac{1}{2} \ln \frac{1+r_t}{1-r_t}$
 - ▶ Update $\vec{\omega}^{(t+1)} \propto \omega_i^{(t)} \cdot \exp(-\alpha_t y_i H_t(\vec{x}^{(i)}))$
- Final classifier: $H_t(\vec{x}) = \sum_{t=1}^{T} \alpha_t H_t(\vec{x})$

Example: Decision Stumps

- ightharpoonup To learn decision stump, given data and $\vec{\omega}^{(t)}$.
- Try all features, thresholds.
- Choose that which maximizes the margin:

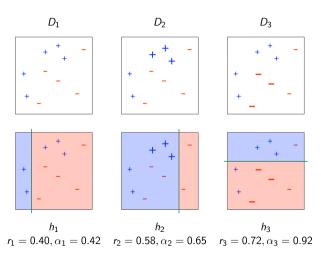
$$r_t = \sum_{i=1}^n \omega_i^{(t)} y_i H_t(\vec{x}^{(i)}) \in [-1, 1]$$

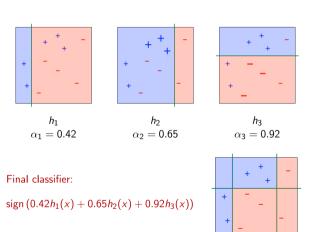
Example: Decision Stumps

- ightharpoonup To learn decision stump, given data and $\vec{\omega}^{(t)}$.
- Try all features, thresholds.
- Equivalently, choose that which maximizes the performance:

$$\alpha_t = \frac{1}{2} \ln \frac{1 + r_t}{1 - r_t}$$

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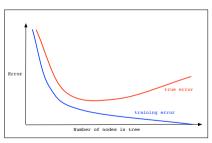


Theory

Suppose that on each round t, the weak learner returns a rule H_t whose error on the step t weighted data is $\leq \frac{1}{2} - \gamma$. Then after T rounds, the training error of the combined rule H is at most $e^{-\gamma^2 T/2}$.

Generalization

Boosted decision stumps are really resistant to overfitting.



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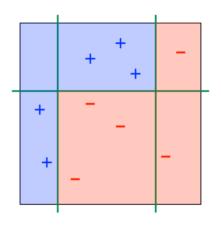
Why not?

Why use weak learners?

What if we replace decision stumps with SVMs or logistic regression?

Why not?

- Why use weak learners?
- What if we replace decision stumps with SVMs or logistic regression?
- You can, but weak learners are fast to learn.
- The point of boosting is that weak learners are "just as good" as strong learners.



CSE 151A Intro to Machine Examing

Lecture 14 – Part 02
Random Forests

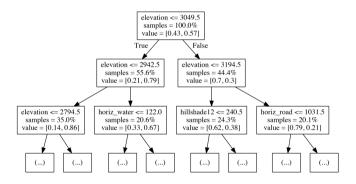
Let's Try

- Decision trees are susceptible to overfitting.
- Let's try using boosted decision trees.

Example: Forest Cover Type

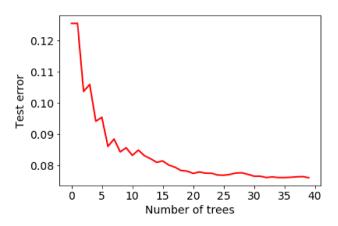
- Goal: predict forest type.
 - Spruce-fir
 - Lodgepole pine
 - etc. 7 classes in total.
- ► 54 cartographic/geological features.
 - Elevation, slope, amount of shade, distance to water, etc.

Decision Tree

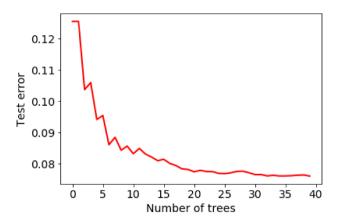


Depth 20. Training error: 1%. Test error: 12.6%.

Boosted Decision Trees



Boosted Decision Trees



Depth 20: Test error: 8.7%. Slow!

Another Idea

- Prevent decision trees from overfitting by "hiding data" randomly.
- Train a bunch of trees, quickly.
- Average them to make a final prediction.

Random Forests

- For t = 1 to T
 - Choose n' training points randomly, with replacement.
 - Fit a decision tree, H_t .
 - At each node, restrict to one of k features, chosen randomly.
- Final classifier: majority vote of $H_1, ..., H_T$.
- Common settings: n' = n (bootstrap), $k = \sqrt{d}$.

Forest Cover Type

▶ Decision trees: 12.6% error.

- Boosted decision trees: 8.7% error (but slow!)
- Random forests: 8.8% error.
 - ▶ 50% of features dropped.
 - Each individual tree H₁,..., H_t has test error around 15%.