

Difference in fuel consumption between automatic and manual transmission automobiles

Summary

The purpose of this study is use linear regression to explore the relationship between fuel consumption, expressed in miles per gallon (mpg), and 10 other automobile design and performance aspects(features) for 32 automobiles manufactured in the years 1973 and 1974. The design features include the transmission (manual or automatic) of the automobile, the number of engine cylinders, its weight, rear axle ratio, number of foward gears, number of carburators and displacement ratio. The performance features include the fuel consumption, the gross horse power and the quarter-mile time.

Data

The *mtcars* dataset was used in the study, and is available in the R library. The R commands in Appendix A: can be used to load the mtcars and display the first three(3) observations in the dataset. All variables are recorded as numeric values. For this analysis some of the variables will be used a categorical(factor) variables.

Exploratory Analysis

The dataset contains 19 automatic and 13 manual transmission automobiles. Figure A1.0 in appendix A: shows that the average fuel consumption for automatic transmission automobiles appears to be higher (17.1 miles per gallon) compared to the manual transmission automobiles (24.4 miles per gallon) . Appendix **Figure B1.0:** shows pairwise plot and the correlation factors between all the variables in the dataset. It should be noted that the pairwise plot also shows that colinearity between the predictor variables. Some of the correlations, for example between fuel consumption and engine horse power ($R=0.78$), appear to be non-linear.

Linear Regression Model

Initial model

Using R commands shown in Appendix C: we can build a linear model that expressses the relationship between the miles per gallon and the other disign and performance aspects of an automobile. The initial model includes all the variables, and using a 5% significance level, we observe from the summary that some of the variables have p-values greater than 5% and could potentially be removed from the model.

Best Model Selection Strategy

Using a backward selection strategy, we can build a more parsimonious model (refer to code in Appendix C:) than the model obtained in the previous section. A summary of the model parameters is shown in **Appendix C:**. Based on the model, the relationship between the fuel consumption, in miles per gallon (mpg), and the predictor variables (**cyl**, **hp**, **wt**, and **am**) can be expressed using the following linear regression function:

$$mpg = 33.71 - 3.03cyl/6 - 2.16cyl/8 - 0.03hp - 2.50wt + 1.81am$$

Interpretation of the Regression Model

All other factors held constant and on average, we observe that the predicts a reduction of only 0.03 miles per gallon for every unit increase in engine horse power. In terms of the number of cylinders, the model predicts that the miles per gallon (mpg) for 6 cylinder engine automobiles is 3.03 miles per gallon lower, on average, than 4 cylinder engine automobiles. Similarly, the model predicts that the miles per gallon (mpg) for 6 cylinder engine automobiles is 2.16 miles per gallon lower, on average, than 4 cylinder engine automobiles. The difference between the 6 and 8 cylinder engines is 0.87 miles per gallon, and this can be interpreted to mean that on average 6 cylinder engine automobiles travel 0.87 more miles per gallon than 8 cylinder engines. Furthermore, the model predicts that the miles per gallon decreases by 2.5 miles for each unit increase in weight.

Finally, In terms of type of engine transmission (automatic or manual), the model predicts that all things held constant, the miles per gallon (mpg) for manual transmission automobiles is 1.81 higher, on average, than automatic transmission engine automobiles. Appendix D: shows the model data in a conditional plot, and We observe that the interpretation provided above is to a large extent consistent with data shown on the conditional plot.

Diagnostics

Appendix E: shows some of the diagnostic plot for the fitted model. The residuals plot shows relatively constant variability of the residuals against the fitted values with a few outliers. The quantile plot also shows normal errors with a bit of skew around the outlying points.

Conclusion

The data provides evidence that automatic transmission automobile consume more gallons of fuel per mile compared to manual transmission engines. However the data may be biased since we observe from the plot in Appendix C: that the majority (63%) of the automatic automobiles in the dataset use 8 cylinder engines which, according to the model, tend to weigh more and hence consume for fuel.

APPENDIX

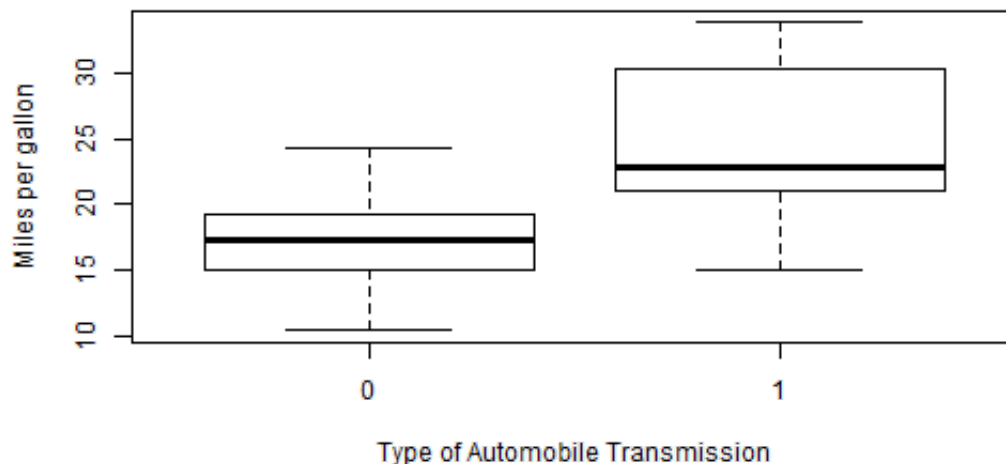
Appendix A:

The R code for loading dataset and displaying first three(3) observations:

```
data(mtcars)
head(mtcars, 3)
```

```
##           mpg cyl  disp  hp  drat   wt  qsec vs am
gear carb
## Mazda RX4      21.0   6  160  110  3.90  2.620  16.46  0  1
4       4
## Mazda RX4 Wag  21.0   6  160  110  3.90  2.875  17.02  0  1
4       4
## Datsun 710     22.8   4  108   93  3.85  2.320  18.61  1  1
4       1
```

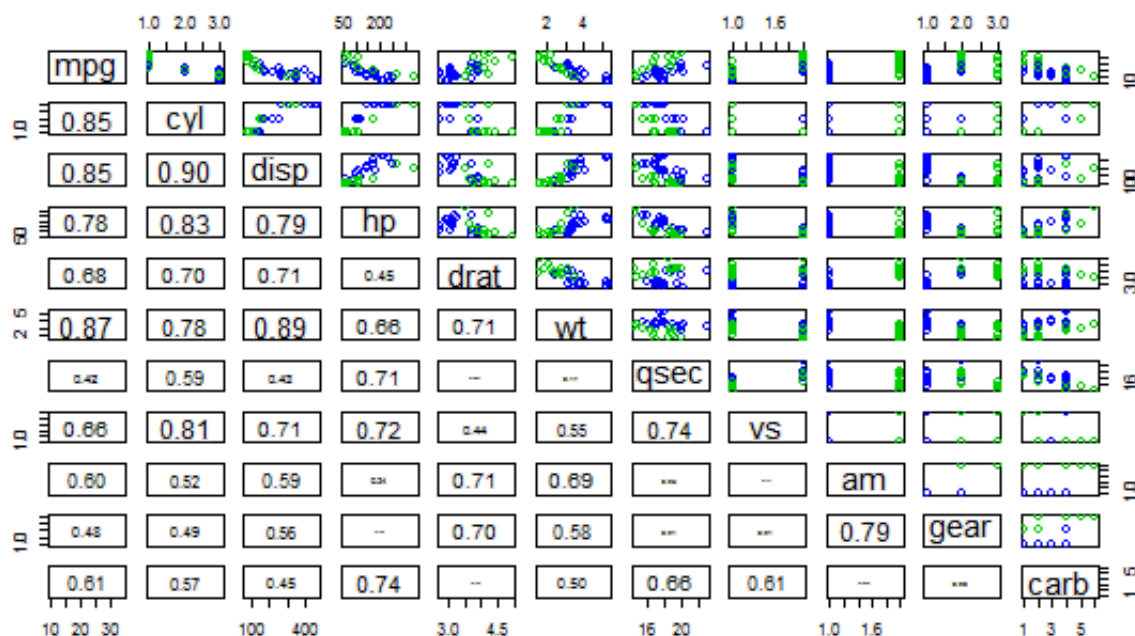
Figure A1.0 : Fuel Consumption



Appendix B:

A pairwise plot for the provided data. The **blue** points correspond to automatic transmission automobiles and the **green** points correspond to manual transmission automobiles.

Figure B1.0: Pairwise plot and Correlation factors



Appendix C:

Initial model: **model1**

```
model1 <- lm(mpg ~ ., data = mtcars) # initial model
including all variables
## summary(model1) -- commented out to reduce number of
pages coef(model1) --
## -- commented out to reduce number of pages
```

Best fit model: **model2**

```
library(MASS)
model2 <- stepAIC(model1, method = "backward") #
iterative results too long; not echoed
## summary(model2)-- commented out to reduce number of
pages
```

```
coef(model2)
```

```
## (Intercept)          cyl6          cyl8          hp
wt          am1
##      33.70832      -3.03134      -2.16368      -0.03211
-2.49683      1.80921
```

Appendix D:

```
require(graphics)
coplot(mpg ~ wt | cyl, data = mtcars, panel =
panel.smooth, rows = 1, col = 3 +
      (mtcars$am == 0), main = "Figure c1.0")
```



The figure displays four diagnostic plots for a linear regression model, arranged in a 2x2 grid. The top row contains the 'Residuals vs Fitted' and 'Normal Q-Q' plots. The bottom row contains the 'Scale-Location' and 'Residuals vs Leverage' plots. The y-axis for the top row is 'Residuals' and for the bottom row is 'Standardized residuals'. The x-axis for the left column is 'Fitted values' and for the right column is 'Leverage'. The 'Normal Q-Q' plot shows the distribution of standardized residuals against theoretical quantiles. The 'Scale-Location' plot shows the square root of the absolute value of standardized residuals against fitted values. The 'Residuals vs Leverage' plot shows standardized residuals against leverage, with Cook's distance contours indicated by dashed lines.