

# COMP90048: Workshop 7

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Logic Programming, but better

# Intro

- In Prolog, it can be easy to accidentally write very inefficient code.
- There are two tricks: **tail recursion** and **asymptotic complexity**.

# Tail recursion and the stack

- What happens when you call a function in C?

```
int n = 2;
int x;
x = factorial(n);
// x = 2

int factorial(int n) {
    return n <= 1
        ? 1
        : (n * factorial(n - 1));
}
```

The stack



# Tail recursion and the stack

- What happens when you call a function in C?

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→ int n = 2;  
   int x;  
   x = factorial(n);  
   // x = 2  
  
   int factorial(int n) {  
       return n <= 1  
           ? 1  
           : (n * factorial(n - 1));  
   }
```

The stack\*

n (4 bytes)

\* it grows downwards by convention

# Tail recursion and the stack

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The stack

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x (4 bytes)

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The stack

n (4 bytes)
x (4 bytes)
return address (8 bytes)
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The stack

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x (4 bytes)
return address (8 bytes)
n (4 bytes)
return address (8 bytes)
n - 1 (4 bytes)

# Tail recursion and the stack

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The stack

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// x = 2
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```
int factorial(int n) {  
    return n <= 1  
    →      ? 1  
          : (n * factorial(n - 1));  
}
```

The stack

n (4 bytes)
x (4 bytes)
return address (8 bytes)
n (4 bytes)
<del>return address (8 bytes)</del>
<del>n 1 (4 bytes)</del>

popped

# Tail recursion and the stack

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int x;  
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// x = 2
```

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int factorial(int n) {  
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# Tail recursion and the stack

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→ // x = 2
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int factorial(int n) {  
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        ? 1  
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}
```

The stack

n (4 bytes)
x (4 bytes)

# Tail recursion and the stack

- We've got two stack entries per call...

```
int n = 2;  
int x;  
x = factorial(n);  
// x = 2
```

```
→ int factorial(int n) {  
    return n <= 1  
        ? 1  
        : (n * factorial(n - 1));  
}
```

The stack

n (4 bytes)
x (4 bytes)
return address (8 bytes)
n (4 bytes)
return address (8 bytes)
n - 1 (4 bytes)

# Tail recursion and the stack

- Now with tail recursion!

```
int n = 2;  
int x;  
x = factorial(n);  
// x = 2
```

```
→ int factorial(int n) {  
    return n <= 1  
        ? 1  
        : (n * factorial(n - 1));  
}
```

The stack

n (4 bytes)
x (4 bytes)
return address (8 bytes)
n (4 bytes)



# Tail recursion and the stack

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```
int n = 2;  
int x;  
x = factorial(n);  
// x = 2
```

```
int factorial(int n) {  
    return n <= 1  
        ? 1  
        : (n * factorial(n - 1));  
→ }  
}
```

The stack

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return address (8 bytes)
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# Tail recursion and the stack

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int x;  
x = factorial(n);  
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```
int factorial(int n) {  
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→ }  
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The stack

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# Tail recursion and the stack

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int n = 2;  
int x;  
x = factorial(n);  
→ // x = 2
```

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int factorial(int n) {  
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The stack

n (4 bytes)
x (4 bytes)
<del>return address (8 bytes)</del>
<del>n * (n - 1) (4 bytes)</del>
<del>n - 1 (4 bytes)</del>

# Tail recursion and the stack

- By reducing stack use, we save both memory and time.

```
int n = 2;  
int x;  
x = factorial(n);  
→ // x = 2
```

```
int factorial(int n) {  
    return n <= 1  
        ? 1  
        : (n * factorial(n - 1));  
}
```

The stack

n (4 bytes)
x (4 bytes)

# Tail recursion and the stack

- By reducing stack use, we save both memory and time.

The stack (no tail recursion)

n (4 bytes)
x (4 bytes)
return address (8 bytes)
n (4 bytes)
return address (8 bytes)
n - 1 (4 bytes)

The stack (tail recursion)

n (4 bytes)
x (4 bytes)
return address (8 bytes)
n * (n - 1) (4 bytes)
n - 1 (4 bytes)

# Tail recursion and the stack

- We can do this because **recursion is the last step**.

```
int factorial(int n) {  
    return n <= 1  
        ? 1  
        : (n * factorial(n - 1));  
}
```

# Tail recursion in Prolog

- Prolog works in much the same way! Consider:

```
prodlist([], 1).
```

```
prodlist([N|Ns], Prod):-  
    prodlist(Ns, Prod0),  
    Prod is N * Prod0.
```

- This is **not** tail recursive.

# Tail recursion in Prolog

- We introduce an **accumulator** (and a helper predicate).

```
prodlist(List,Prod):-  
    prodlist_acc(List, 1, Prod).
```

```
prodlist_acc([], Prod, Prod).  
% to be continued
```

- The idea: `prodlist_acc` holds when its accumulator is the sum.



# Tail recursion in Prolog

- We introduce an **accumulator** (and a helper predicate).

```
prodlist(List, Prod):-  
    prodlist_acc(List, 10, Prod).  
  
prodlist_acc([], Prod, Prod).  
prodlist_acc([N|Ns], Acc, Prod):-  
    Prod0 is Acc * N,  
    prodlist_acc(Ns, Prod0, Prod).
```

# Avoiding append

- Similarly to Haskell, `append/3` is  $O(n)$ . We try to avoid it where we can. Consider:

```
reverse([], []).
```

```
reverse([A|BC], CBA):-  
    reverse(BC, CB),  
    append(CB, [A], CBA).
```

# Avoiding append

- We can use the accumulator approach here too!

```
reverse([], A, A).
```

DCBAcc is the reversed list, with Acc on the end



```
reverse([B|CD], Acc, DCBAcc) :-  
    reverse(CD, [B|Acc], DCBAcc).
```

# Avoiding append

- We can use the accumulator approach here too!

```
reverse([], A, A).
```

DCBAcc is the reversed list, with Acc on the end

```
reverse([B|CD], Acc, DCBAcc) :-  
    reverse(CD, [B|Acc], DCBAcc).
```

peel B from the **front** of the original list BCD and  
stick it at the **back** of the new list DCBAcc

# Avoiding append

- We can use the accumulator approach here too!

```
reverse([], A, A).
```

```
reverse([B|CD], Acc, DCBAcc):-  
    reverse(CD, [B|Acc], DCBAcc).
```

- This is a general method for working with lists.

Continue with Grok Workshop 7  
(Week 8).