Parent-Teacher conferences

Knowledge and Data Mining Project

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The task



- Schedule parent-teacher conferences
- Each meeting between parent(s) and a teacher lasts for the same fixed amount of time for convenience, we want to find a schedule so that every person's conferences occur in consecutive time slots
- Input: **n** teachers, **m** parents, and a $m \times n$ matrix S_{ij} : $S_{ij} = 1$ if teacher j has a student whose parent is i otherwise is equal to 0

The variables



- Matrix S generated randomly, T = 4 and P = 5 (P > T since students have more than one teacher)
- The maximum number of slots avaliable per teacher is given by the max number of parent a teacher should meet w.r.t. S. This variable is saved as *spots*.
- Use variable $m_{t,p,s}$ with 3 different indices return a single variable following the rule:

$$m_{t,p,s} = 1 + p \cdot T \cdot spots + s \cdot T + t$$

Example: (0,0,0) is encoded in 1, (1,0,0) is encoded in 2.

Encoding

Only one meeting for each pair teacher-parent

$$\forall s' \neq s \quad m_{t,p,s} \rightarrow \neg m_{t,p,s'} \quad \mathsf{CNF:} \ \neg m_{t,p,s} \lor \neg m_{t,p,s'}$$

■ A parent cannot meet more than one teacher per slot

$$\forall t' \neq t \quad m_{t,p,s} \rightarrow \neg m_{t',p,s} \quad \mathsf{CNF:} \ \neg m_{t,p,s} \lor \neg m_{t',p,s}$$

■ A Teacher cannot meet more than one parent per slot

$$\forall p' \neq p \quad m_{t,p,s} \rightarrow \neg m_{t,p',s} \quad \mathsf{CNF:} \ \neg m_{t,p,s} \lor \neg m_{t,p',s}$$

■ Choose 1 $m_{t,p,s}$ w.r.t to the 1 in S[p,t]:

$$\forall t, p \quad AtMost(\bigvee_{s=1}^{spots} m_{t,p,s}; S[p,t])$$

First result



- With Pysat implementation of RC2 algorithm
- WCNFPlus support cardinality constraints

First Result

	Teacher 0	Teacher 1	Teacher 2	Teacher 3
Slot 0	Parent 1	Parent 2		Parent 0
Slot 1	Parent 2	Parent 0	Parent 4	Parent 1
Slot 2		Parent 4	Parent 0	Parent 2
Slot 3		Parent 1		Parent 4
Slot 4	Parent 4		Parent 1	Parent 3

Soft constraints

Encoding the preference as a soft constraint

Encoding

lacksquare If a slot s is occupied than the slot s+1 should be occupied

$$\forall t, p \quad m_{t,p,s} \rightarrow m_{t,p,s+1}$$

■ The CNF in this case is:

$$\neg m_{t,p,s} \lor m_{t,p,s+1}$$
 with positive weight

Final result



Consecutive time-slots

	Teacher 0	Teacher 1	Teacher 2	Teacher 3
Slot 0				Parent 0
Slot 1		Parent 4		Parent 1
Slot 2	Parent 2	Parent 1	Parent 0	Parent 4
Slot 3	Parent 4	Parent 0	Parent 1	Parent 2
Slot 4	Parent 1	Parent 2	Parent 4	Parent 3