XThe probability wass function of a binomial random variable XuBinomial(n,p) is: $P_{r}[X=L] = \binom{n}{r} p^{L} (1-p)^{r-L}$ i = 0,1,...,n.

Mhy ? BOES

- The probability of any sequence of noutcomes with i successes and n-i failures is p'(1-p) because the trials are assumed to be independent.
 - e.g. Suppose you flip a biased coin with Pr[heads] = p and Pr[toils] = 1-p three times to a Compute the probability of any sequence with 2 heads and I tail.

 $Pr[HHT] = p^{2}(1-p)$ Pr[H|T|H] = p(1-p)p(1-p)each has probability = $p^{2}(1-p).(x)$ Pr[THH] = (1-p)p

Pr[HHT] = Pr[heads on 1st flip 1 heads on 2nd flip 1 tails on 3rd flip] outcome of one = Pr[heads on 1st flip] Pr[heads on 2nd Alip] Pr[tails on 3rd Alip] ton esob gilt influence the 20 smost of · (1-p).

- There are (n) distinct sequences of the n outcomes leading to isuccesses
- e.g. Continuing the example above, X~ Binomial (3, p) on any thip is p

P-[X=2] = P-[HHT U HTH U THH] = P-[HHT] + P-[HTH] + P-[THH]

(each is) _ p2(1-p) + p2(1-p) + p2(1-p) + (5ee *) 3 different ways) $= 3p^2(1-p)$ $\binom{3}{2} = \binom{3}{2} = \binom{3}{2} p^2 (1-p)$.

Prepared by: M. Charman 7/1/2017