CS370 Midterm F2005

$$| \cdot \alpha \rangle |_{1}(x) = \frac{(x-1)(x-2)}{(-1)(-1)}$$

$$| \cdot \alpha \rangle |_{1}(x) = \frac{x(x-2)}{(1-2)}$$

$$| \cdot \alpha \rangle |_{2}(x) = \frac{x(x-1)}{2(2-1)}$$

$$\rho_{1}(x) = 5L_{1}(x) + \frac{5}{2}L_{2}(x) + L_{3}(x)$$

$$= \frac{5}{2}(x-1)(x-2) - \frac{5}{2}x(x-2) + \frac{1}{2}x(x-1)$$

$$= 5 - 3x + \frac{1}{2}x^{2}$$

b)
$$p(0) = 5 \rightarrow c_0 = 5$$

 $p(1) = \frac{5}{2} \rightarrow c_0 + c_1 + c_2 = \frac{5}{2}$
 $p(2) = 1 \rightarrow c_0 + 2c_1 + 4c_2 = 1$
 $p_2(x) = 5 - 3x + \frac{1}{2}x^2$

(x) p1(x) and p2(x) are the same polynomial.

2. a) i.
$$S_{1}'(1) = S_{2}'(1)$$

ii. $S_{1}''(1) = S_{2}''(1)$

b)
$$S_1(1) = S_2(1) \rightarrow 0.917 - 5.917 + \alpha_1 = b_3 + b_2 + b_1 + 5.375$$

 $S_1'(1) = S_2'(1) \rightarrow 2.757 - 5.617 = 3b_3 + 2b_2 + b_1$
 $S_1''(1) = S_2''(1) \rightarrow 5.502 = 6b_3 + 2b_2$

$$S''(3) = 0 \implies 2b_2 = 0$$

- [Not covered on midterm]
- 4. [Not covered]
- 5. a) 0.00001 · 10-5
 - b) 0.25790·104
 - c) 5912.32 @ 4087.50

- = 0.99998 . 104
- The distance between consecutive floating point numbers in the interval [1, 2) is

$$\Delta = 10^{1-5} = 10^{-4}$$

Hence there are $1/10^{4} = 10^{4}$ numbers in the interval [1, 2).

6. a)
$$2^{4}-2^{-23} \otimes 2^{5}+2^{-21}$$

$$= f(2^{9} + 2^{-18} - 2^{-18} - 2^{-45})$$

$$=2^9$$

b) RelErr =
$$\frac{|a \otimes b - ab|}{|ab|eps} = \frac{|2^{9} - (2^{9} - 2^{-45})|}{(2^{9} - 2^{-45})2^{-52}}$$

- **7**. [Not covered]
- **%.** [Not covered]