

**Exercise 1:** Generate simulated data that is similar to the

**Exercise 2 (Divide by four rule):** Test the divide by four rule on the support for same-sex marriage data set by performing a linear regression on the binned data and comparing the coefficients to the logistic regression output. Clearly explain why this tests the divide by four rule.

**Exercise 3**

```
pd.read_csv("https://raw.githubusercontent.com/washingtonpost/data-homicides/master/homicide-data-py")
> data["victim_age"] = pd.to_numeric(data["victim_age"], errors="coerce")
>
> disp_new = []
> disp = data["disposition"].values
> for d in disp:
>     if d == "Closed by arrest":
>         disp_new.append(1)
>     else:
>         disp_new.append(0)
> data["arrest"] = disp_new
> data = data.dropna()
```

**Exercise 4 (Water contamination model):** Suppose we have data consisting of the longitude ( $X_1$ ) and latitude ( $X_2$ ) of water samples along with whether or not the sample tested positive for a toxin ( $Y$ ). We believe that there has been a leak and want to identify the region within which there is more than a 1% chance the water is contaminated.

How do we frame this problem as a logistic regression? We need to introduce features so that the contours of equal  $q$  (the chance to be contaminated as a function of  $X_1$  and  $X_2$ ) are ellipses. Recall the equation is

$$(1) \quad W = a_1X_1 + a_2X_2 + a_3X_1^2 + a_4X_2^2 + a_5X_1X_2$$

The function  $W(X_1, X_2)$  is constant along the curves.

This means that  $h(W)$  is constant along these curves, where  $h$  is the logistic function. In other words,  $h$  will be largest at the center and decay.