

Multinomial Logistic Regression with R

Multinomial Logistic Regression

- ▶ We use the `multinom` function from the **nnet** package to estimate a multinomial logistic regression model.
- ▶ Remark - There are other functions in other R packages capable of multinomial regression, such as the **mlogit** package.
- ▶ The `multinom` function does not require the data to be reshaped (as the **mlogit** package does)
- ▶ (Similar format to example code found in Hilbe's *Logistic Regression Models*).

Multinomial Logistic Regression with R

Multinomial logistic regression

- ▶ We must choose the level of our outcome that we wish to use as our **baseline** and specify this in the `relevel` function.
Let's choose "academic".
- ▶ Then, we run our model using *multinom*.
- ▶ The `multinom` command does not include p-value calculation for the regression coefficients.
- ▶ (We can calculate p-values using Wald tests or z-tests).

Multinomial Logistic Regression with R

```
ml$prog2 <- relelevel(ml$prog, ref = "academic")  
test <- multinom(prog2 ~ ses + write, data = ml)  
  
# weights:  15 (8 variable)  
initial    value 219.722458  
iter   10 value 179.982880  
final      value 179.981726  
converged
```

Multinomial Logistic Regression with R

```
summary(test)
```

Call:

```
multinom(formula = prog2 ~ ses + write,  
          data = ml)
```

Coefficients:

	(Intercept)	sesmiddle	seshigh	write
general	2.852	-0.5333	-1.1628	-0.05793
vocation	5.218	0.2914	-0.9827	-0.11360

Multinomial Logistic Regression with R



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Std. Errors:

	(Intercept)	sesmiddle	seshigh	write
general	1.166	0.4437	0.5142	0.02141
vocation	1.164	0.4764	0.5956	0.02222

Residual Deviance: 360

AIC: 376

Multinomial Logistic Regression with R

Wald Test

- ▶ The Wald test in the context of logistic regression is used to determine whether a certain predictor variable X is significant or not.
- ▶ It rejects the null hypothesis of the corresponding coefficient being zero.
- ▶ The test consists of dividing the value of the coefficient by standard error

Multinomial Logistic Regression with R

```
# Coefficients Divided by Standard Errors
# Then Compute p-values.
# 2-tailed z test
# p.values
```

	(Intercept)	sesmiddle	seshigh	write
general	1.448e-02	0.2294	0.02374	6.819e-03
vocation	7.299e-06	0.5408	0.09895	3.176e-07

Multinomial Regression with R

- ▶ Remark: Some output is generated by running the model, even though we are assigning the model to a new R object.
- ▶ This model-running output includes some iteration history and includes the final **negative log-likelihood** (+ 179.981726).
- ▶ This value multiplied by two is then seen in the model summary as the **Residual Deviance** and it can be used in comparisons of nested models (360).

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- ▶ As with many summary outputs, the output contains a column of coefficients and a column of standard errors.
- ▶ Each of these blocks has one row of values corresponding to a model equation.
- ▶ Focusing on the block of coefficients, we can look at the first row comparing `prog = "general"` to our baseline `prog = "academic"` and the second row comparing `prog = "vocation"` to our baseline *prog = "academic"*.

Multinomial Regression with R

- ▶ If we consider our coefficients from the first row to be b_1 and our coefficients from the second row to be b_2 , we can write our model equations:

$$\ln \left(\frac{P(\text{prog} = \text{gen.})}{P(\text{prog} = \text{acad.})} \right) = b_{10} + b_{11}(\text{ses} = 2) + b_{12}(\text{ses} = 3) + b_{13}\text{write}$$

$$\ln \left(\frac{P(\text{prog} = \text{voc.})}{P(\text{prog} = \text{acad.})} \right) = b_{20} + b_{21}(\text{ses} = 2) + b_{22}(\text{ses} = 3) + b_{23}\text{write}$$

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- ▶ A one-unit increase in the variable **write** is associated with the decrease in the log odds of being in general program vs. academic program in the amount of 0.058 (b_{13}).
- ▶ A one-unit increase in the variable **write** is associated with the decrease in the log odds of being in vocation program vs. academic program in the amount of 0.1136 (b_{23}).

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- ▶ The log odds of being in general program vs. in academic program will decrease by 1.163 if moving from *ses="low"* to *ses="high"* b_{12} .
- ▶ The log odds of being in general program vs. in academic program will decrease by 0.533 if moving from *ses="low"* to *ses="middle"* b_{11} , although this coefficient is not significant.

Multinomial Regression with R

- ▶ The log odds of being in vocation program vs. in academic program will decrease by 0.983 if moving from $\text{ses} = \text{"low"}$ to $\text{ses} = \text{"high"}$ (b_{22}).
- ▶ The log odds of being in vocation program vs. in academic program will increase by 0.291 if moving from $\text{ses} = \text{"low"}$ to $\text{ses} = \text{"middle"}$ (b_{21}), although this coefficient is not significant.