t [Eq. (3.101)]

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s treated in Secigure 3.26, charnind the cylinder, er is the same as al result that the

n that studied in preover, the drag o. For a viscous tion 1.7) clearly lds number. The gure 3.44, which  $(\infty d)/\mu_{\infty}$ , where or the extremely  $\approx 300,000$ . At a value near 1 to te: These results , contrasting  $C_D$ ecipitous drop in led answer must Part 4. However, sition of laminar bulent boundary

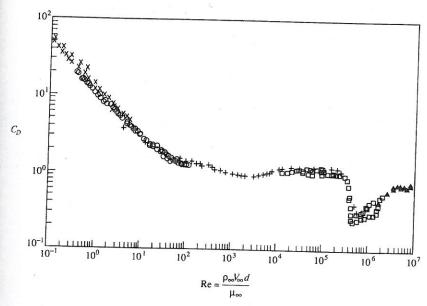


Figure 3.44 Variation of cylinder-drag coefficient with Reynolds number. (Source: Experimental data as compiled in Panton, Ronald, Incompressible Flow, Wiley-Interscience, New York, 1984.)

layer at the higher values of Re. Why does a turbulent boundary layer result in a smaller  $C_D$  for this case? Stay tuned; the answer is given in Chapter 4.

The variation of  $C_D$  shown in Figure 3.44 across a range of Re from  $10^{-1}$  to  $10^7$  is accompanied by tremendous variations in the qualitative aspects of the flow field, as itemized, and as sketched in Figure 3.45.

- 1. For very low values of Re, say, 0 < Re < 4, the streamlines are almost (but not exactly) symmetrical, and the flow is attached, as sketched in Figure 3.45a. This regime of viscous flow is called *Stokes flow*; it is characterized by a near balance of pressure forces with friction forces acting on any given fluid element; the flow velocity is so low that inertia effects are very small. A photograph of this type of flow is shown in Figure 3.46, which shows the flow of water around a circular cylinder where Re = 1.54. The streamlines are made visible by aluminum powder on the surface, along with a time exposure of the film.
- 2. For 4 < Re < 40, the flow becomes separated on the back of the cylinder, forming two distinct, stable vortices that remain in the position shown in Figure 3.45b. A photograph of this type of flow is given in Figure 3.47, where Re = 26.
- 3. As Re is increased above 40, the flow behind the cylinder becomes unstable; the vortices which were in a fixed position in Figure 3.45b now are alternately shed from the body in a regular fashion and flow downstream.