Markov Decision Processes in Python

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Topics:

- Utility recap
- Example: Time for coffee?
- Example: Time for coffee?- Maximax Maximin
- MDP toolbox
- Exercise: Solving a simple MDP using the MDP toolbox
- Value iteration algorithm recap
- Policy iteration algorithm recap
- Value iteration algorithm via MDP toolbox
- Policy iteration algorithm via MDP toolbox
- Q-Learning via MDP toolbox





Expected utility: Recap

Expected utility

- Let's call U(s) the utility of being in a certain state s
- U(s) is a sort of numerical "score" assigned to s i.e. how desirable is to reach that particular state (e.g. money earned in the quiz game)
- The **expected utility** of an action, EU(a), is then the average utility value of the outcomes, weighted by the probability that the outcome occurs:

$$EU(a) = \sum_{s'} P(RESULT(a) = s') \ U(s')$$

MEU principle: choose the action that <u>maximizes expected utility</u>

I have half an hour to spare in my busy schedule, and I have a choice between working quietly in my office and going out for a coffee.

If I stay in my office, three things can happen:

- I can get some work done (Utility = 8),
- I can get distracted looking at the latest news (Utility = 1),
- A colleague might stop by to talk about some work we are doing (Utility = 5).
 If I go out for coffee, I will most likely enjoy a good cup of smooth caffeination (Utility = 10), but there is also a chance I will end up spilling coffee all over myself (Utility = −20).

The probability of getting work done if I choose to stay in the office is 0.5, while the probabilities of getting distracted, and a colleague stopping by are 0.3 and 0.2 respectively.

If I go out for a coffee, my chance of **enjoying my beverage is 0.95**, and the chance of **spilling my drink is 0.05**.

QUESTION 1(a): What is the expected utility of staying in my office?

QUESTION 1(b): What is the expected utility of going out for a coffee?

QUESTION 1(c): By the principle of maximum expected utility, what should I do?





QUESTION 1(a): What is the expected utility of staying in my office?

SOLUTION 1(a):

Staying in the office means that I will either work, get distracted, or talk with a colleague.

These states have the following utilities:

$$U(work) = 8$$

 $U(distracted) = 1$
 $U(colleague) = 5$

and the probabilities of these happening, given I stay in the office are:

$$P(work|office) = 0.5$$

 $P(distracted|office) = 0.3$
 $P(colleague|office) = 0.2$

Let's declare these as Python arrays



Let's declare these as Python arrays

```
import numpy as np
# Setup arrays with: symbolic names for outcomes (not currently used), utilities of outcomes, and
# probabililites of those outcomes
                                                         label
office_outcomes = ["work", "distracted", "colleague"]
print('office_outcomes = ', office_outcomes)
                                                         utilities
u_office_outcomes = np.array([8, 1, 5])
print('U(office_outcomes) = ', u_office_outcomes)
                                                         probabilities
p_office_outcomes_office = np.array([0.5, 0.3, 0.2])
print('P(office outcomes office) =', p office outcomes office)
office_outcomes = ['work', 'distracted', 'colleague']
U(office\_outcomes) = [8 1 5]
P(office\_outcomes|office) = [0.5 0.3 0.2]
```

The **expected utility** of an action, EU(a), is then the average utility value of the outcomes, weighted by the probability that the outcome occurs:

$$EU(a) = \sum_{s'} P(RESULT(a) = s') U(s')$$

SOLUTION 1(a):

$$EU(office) = 0.5 * 8 + 0.3 * 1 + 0.2 * 5 = 5.3$$

SOLUTION 1(a):

Now let's implement this in Python:

```
# The weighted utility ofeach outcome is each to compute by pairwise multiplication
eu_office_outcomes = u_office_outcomes * p_office_outcomes_office
print('EU by outcome =', eu_office_outcomes)
# Summing the weighted utilities gets us the expected utility
eu_office = np.sum(eu_office_outcomes)
print('EU(office) = ', eu_office)
```

EU by outcome = [4. 0.3 1.]EU(office) = 5.3

So the expected utility of staying in the office is 5.3



QUESTION 1(b): What is the expected utility of going out for a coffee?

SOLUTION 1(b):

Going out for a coffee means that I will either enjoying my beverage, or spilling my drink. These states have the following utilities:

$$U(caffeination) = 10$$

 $U(spillage) = -20$

and the probabilities of these happening, given I stay in the office are:

$$P(caffeination|coffee) = 0.95$$

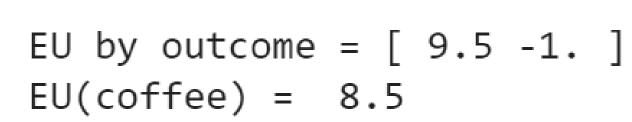
 $P(spillage|coffee) = 0.05$

Let's implement these in Python using the same notation as before



SOLUTION 1(b):

```
# The coffee calculation is the same as the office calculation, first set up arrays
coffee_outcomes = ["caffeination", "spillage"]
print('coffee_outcomes = ', coffee_outcomes)
u_coffee_outcomes = np.array([10, -20])
print('U(coffee_outcomes) = ', u_coffee_outcomes)
p_coffee_outcomes_coffee = np.array([0.95, 0.05])
print('P(coffee_outcomes coffee) =', p_coffee_outcomes_coffee)
print('\n')
# Then compute the expected utility
eu_coffee_outcomes = u_coffee_outcomes * p_coffee_outcomes_coffee
print('EU by outcome =', eu_coffee_outcomes)
eu_coffee = np.sum(eu_coffee_outcomes)
print('EU(coffee) = ', eu_coffee)
coffee_outcomes = ['caffeination', 'spillage']
U(coffee\_outcomes) = [10 - 20]
P(coffee_outcomes | coffee) = [0.95 0.05]
```



So the expected utility of going out for coffee is 8.5

QUESTION 1(c): By the principle of maximum expected utility, what should I do?

SOLUTION 1(c):

MEU principle: choose the action that maximizes expected utility

Clearly in the case of numbers in the example, the option of *going out for coffee* is the one with the maximum expected utility.

However, we will also program it in Python so that we can see what happens as the probabilities of the outcomes vary:

```
if eu_office > eu_coffee:
    print('Office is the MEU choice')
else:
    print('Coffee is the MEU choice')
```

Coffee is the MEU choice

Expected utility: Example Time for coffee? - Maximax

Revisit the decision for the coffee example using the maximax decision criterion

SOLUTION:

The maximax decision criterion rates each choice by the utility of its best outcome, and then picks the choice with best utility.

In Python we would do this calculation as follows

```
# The utility of each choice is the max utility of their outcomes
max_u_office = np.max(u_office_outcomes)
print('MaxU(office) =', max u office)
max_u_coffee = np.max(u_coffee_outcomes)
print('MaxU(coffee) =', max_u_coffee)
print('\n')
# The decision criterion is then to pick the outcome with the highest utility:
if max_u_office > max_u_coffee:
    print('Office is the Maximax choice')
else:
    print('Coffee is the Maximax choice')
MaxU(office) = 8
MaxU(coffee) = 10
```



Expected utility: Example Time for coffee? - Maximin

Revisit the decision for the coffee example using the maximin decision criterion

SOLUTION:

The maximin decision criterion rates each choice by the utility of its worst outcome, and then picks the choice with the best utility.

In Python we would do this calculation as follows

```
# The utility of each choice is the max utility of their outcomes
min_u_office = np.min(u office outcomes)
print('MinU(office) =', min_u_office)
min_u_coffee = np.min(u_coffee_outcomes)
print('MinU(coffee) =', min_u_coffee)
print('\n')
# The decision criterion is then to pick the outcome with the highest utility:
if min_u_office > min_u_coffee:
    print('Office is the Maximin choice')
else:
    print('Coffee is the Maximin choice')
MinU(office) = 1
MinU(coffee) = -20
```



MDP toolbox

Python Markov Decision ProcessToolbox

Search docs

Markov Decision Process (MDP)
Toolbox

Markov Decision Process (MDP)
Toolbox: mdp module

Markov Decision Process (MDP)
Toolbox: util module

Markov Decision Process (MDP)
Toolbox: example module

The MDP toolbox provides classes and functions for the resolution of discrete-time Markov Decision Processes.

The list of algorithms that have been implemented includes backwards induction, linear programming, policy iteration, q-learning and value iteration along with several variations.

The documentation is available at:

https://pymdptoolbox.readthedocs.io/en/latest/index.html

We need to install it using:

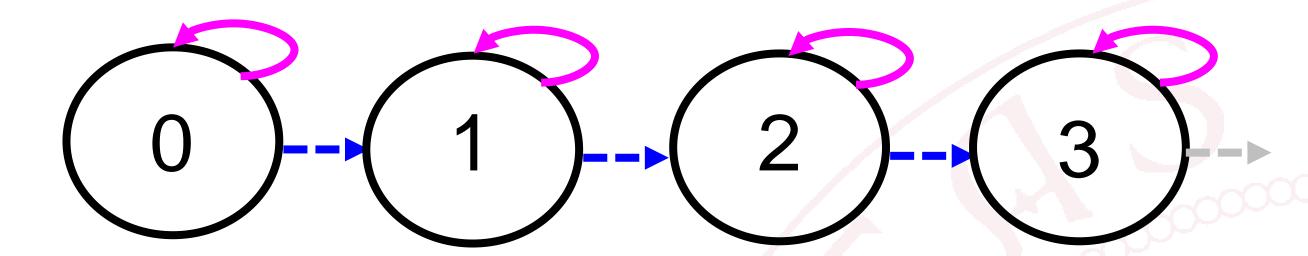
pip install pymdptoolbox

Let's start with a really simple problem.

We have 4 states and two actions.

There are two actions:

- 0 is "Stay",
- 1 is "Right".



0 always succeeds and leaves the agent in the same state.

1 moves the agent right with probability 0.8, stays in place with probability 0.2.

The states are 0, 1, 2, 3.

0 is left of 1, which is left of 2 and so on.

(Thus the states are in a line which runs 0, 1, 2, 3 from left to right.)

The agent remains in state 3 with probability 1.

State 3 has a reward of 1, and the cost of any action is -0.04.

The MDP Toolbox defines MDPs through a probability array and a reward array.

The probability array has shape (A, S, S), where A are actions and S are states.

For **each action** specify the **transitions probabilities** of reaching the **second state** by applying that action in the **first state**.

```
!pip install pymdptoolbox
import mdptoolbox
import numpy as np
# The MDP Toolbox defines MDPs through a probability array and a reward array.
# The probability array has shape (A, S, S), where A are actions and S
# are states. For each action specify the transitions probabilities of reaching
# the second state by applying that action in the first state.
# So, to implement the action model described above, we need:
P1 = np.array([[[1, 0, 0, 0],
                [0, 1, 0, 0],
                [0, 0, 1, 0],
               [0, 0, 0, 1]],
              [[0.2, 0.8, 0, 0],
               [0, 0.2, 0.8, 0],
               [0,
                     0, 0.2, 0.8],
               [0, 0, 0, 1]]])
```

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# the second state by applying that action in the first state.
# So, to implement the action model described above, we need:
P1 = np.array([[[1, 0, 0, 0],
               [0, 0, 0, 1]],
                                        Right
                          0, 1]]])
```

The MDP Toolbox defines MDPs through a probability array and a reward array.

The probability array has shape (A, S, S), where A are actions and S are states.

For **each action** specify the **transitions probabilities** of reaching the **second state** by applying that action in the **first state**.

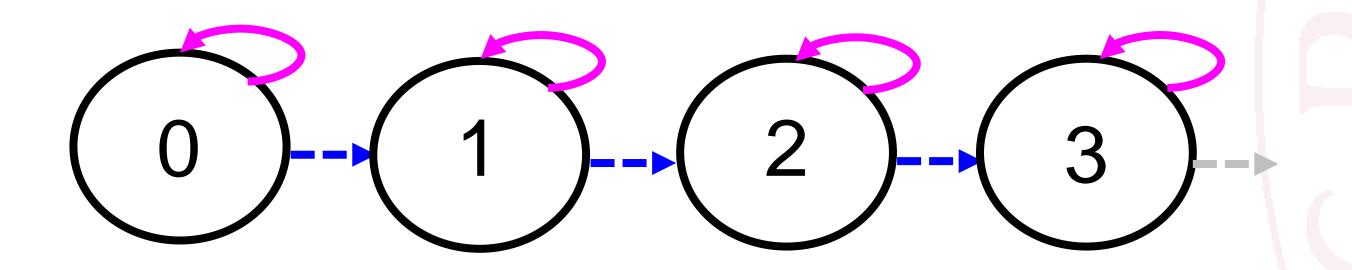
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# The probability array has shape (A, S, S), where A are actions and S
# are states. For each action specify the transitions probabilities of reaching
# the second state by applying that action in the first state.
# So, to implement the action model described above, we need:
P1 = np.array([[[1, 0, 0, 0],
                                  Stay
               [0, 1, 0, 0],
                [0, 0, 1, 0],
               [0, 0, 0, 1]],
               [0.2, 0.8, 0,
                     0.2, 0.8, 0],
                                       Right
                          0.2, 0.8],
                          0, 1]]])
```

The first matrix is that for the action "Stay" (when executed in a given state the agent stays there) and the second is for the action "Right" (which shifts the agent right with probability 0.8 except in state 3 when the agent remains in state 3 with probability 1).

The reward array has **shape** (**S**, **A**), so there is a set of S vectors, one for each state, and each is a vector with one element for each the actions --- **each element is the reward for executing the relevant action in the state** (so this is really modelling cost of the action).

```
R1 = np.array([[-0.04, -0.04], [-0.04, -0.04], [-0.04, -0.04], [1, 1]]) # R1 says that executing either action in states 0, 1, or 2 has a reward # of -0.04, and executing either action in state 3 has reward 1.
```

R1 says that executing either action in states 0, 1, or 2 has a **reward of -0.04**, and executing either action in **state 3 has reward 1**.



The util.check() function checks that the reward and probability matrices are well-formed, and match.

Success is silent, failure provides somewhat useful error messages.

```
The util.check() function checks that the reward and probability matrices
   are well-formed, and match.
#
   Success is silent, failure provides somewhat useful error messages.
mdptoolbox.util.check(P1, R1)
                                                                              mdptoolbox.util.check(P, R)
                                                                                                         [source]
                                                                                Check if P and R define a valid Markov Decision Process (MDP).
                                                                                Let s = number of states, A = number of actions.
                                                                                                • P (array) - The transition matrices It can be a three dimensional array with a
                                                                                                 shape of (A, S, S). It can also be a one dimensional arraye with a shape of (A, ),
                                                                                                 where each element contains a matrix of shape (S, S) which can possibly be
                                                                                                 sparse.
                                                                                                 R (array) - The reward matrix It can be a three dimensional array with a shape of
                                                                                                 (S, A, A). It can also be a one dimensional array with a shape of (A, ), where each
                                                                                                 element contains matrix with a shape of (S, S) which can possibly be sparse. It can
                                                                                                 also be an array with a shape of (S, A) which can possibly be sparse.
https://pymdptoolbox.readthedocs.io/en/latest/api/util.html
```

Notes

Raises an error if P and R do not define a MDP.

Value iteration algorithm recap

Value iteration algorithm

- The iteration step, called a Bellman update, looks like this
- Update is assumed to be applied simultaneously to all the states at each iteration, where

function Q-VALUE(
$$mdp, s, a, U$$
) **returns** a utility value **return** $\sum_{s'} P(s'|s,a)[R(s,a,s') + \gamma U[s']]$

 The algorithm stops when the difference between old and updated utilities is below a certain threshold



$$U_{i+1}(s) \leftarrow \max_{a \in A(s)} \sum_{s'} P(s'|s,a) [R(s,a,s') + \gamma U_i(s')],$$

```
function VALUE-ITERATION(mdp, \epsilon) returns a utility function inputs: mdp, an MDP with states S, actions A(s), transition model P(s'|s,a), rewards R(s,a,s'), discount \gamma
\epsilon, the maximum error allowed in the utility of any state local variables: U, U', vectors of utilities for states in S, initially zero \delta, the maximum relative change in the utility of any state repeat U \leftarrow U'; \delta \leftarrow 0 for each state s in S do U'[s] \leftarrow \max_{a \in A(s)} Q\text{-VALUE}(mdp, s, a, U) if |U'[s] - U[s]| > \delta then \delta \leftarrow |U'[s] - U[s]| until \delta \leq \epsilon (1 - \gamma)/\gamma return U
```

Value iteration algorithm via MDP toolbox

class mdptoolbox.mdp.ValueIteration(transitions, reward, discount, epsilon=0.01, max_iter=1000, initial_value=0, skip_check=False) [source]

Bases: mdptoolbox.mdp.MDP

A discounted MDP solved using the value iteration algorithm.

ValueIteration applies the value iteration algorithm to solve a discounted MDP. The algorithm consists of solving Bellman's equation iteratively. Iteration is stopped when an epsilon-optimal policy is found or after a specified number (max_iter) of iterations. This function uses verbose and silent modes. In verbose mode, the function displays the variation of v (the value function) for each iteration and the condition which stopped the iteration: epsilon-policy found or maximum number of iterations reached.

Parameters:

- transitions (array) ransition probability matrices. See the documentation for the MDP class for details.
- reward (array) Reward matrices or vectors. See the documentation for the MDP class for details.
- **discount** (*float*) Discount factor. See the documentation for the MDP class for details.
- **epsilon** (*float*, *optional*) Stopping criterion. See the documentation for the MDP class for details. Default: 0.01.
- max_iter (int, optional) Maximum number of iterations. If the value given is greater than a computed bound, a warning informs that the computed bound will be used instead. By default, if discount is not equal to 1, a bound for max_iter is computed, otherwise max_iter = 1000. See the documentation for the MDP class for further details.
- initial_value (array, optional) The starting value function. Default: a vector of zeros.
- **skip_check** (*bool*) By default we run a check on the **transitions** and **rewards** arguments to make sure they describe a valid MDP. You can set this argument to True in order to skip this check.
- Attributes (Data) -
- -----
- V (tuple) The optimal value function.
- **policy** (*tuple*) The optimal policy function. Each element is an integer corresponding to an action which maximises the value function in that state.
- iter (int) The number of iterations taken to complete the computation.
- time (float) The amount of CPU time used to run the algorithm.

run() [source]

Do the algorithm iteration.

To run value iteration we create a value iteration object, and run it.

Note that the discount value is 0.9

```
# To run value iteration we create a value iteration object, and run it. Note that
# discount value is 0.9
vi1 = mdptoolbox.mdp.ValueIteration(P1, R1, 0.9)
vi1.run()
```

https://pymdptoolbox.readthedocs.io/en/latest/api/mdp.html

class mdptoolbox.mdp.ValueIteration(transitions, reward, discount, epsilon=0.01, max_iter=1000, initial_value=0, skip_check=False) [source]

Bases: mdptoolbox.mdp.MDP

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- reward (array) Reward matrices or vectors. See the documentation for the MDP class for details.
- **discount** (*float*) Discount factor. See the documentation for the MDP class for details.
- **epsilon** (*float*, *optional*) Stopping criterion. See the documentation for the MDP class for details. Default: 0.01.
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- initial_value (array, optional) The starting value function. Default: a vector of zeros.
- **skip_check** (*bool*) By default we run a check on the **transitions** and **rewards** arguments to make sure they describe a valid MDP. You can set this argument to True in order to skip this check.
- Attributes (Data) -
- -----
- V (tuple) The optimal value function.
- policy (tuple) The optimal policy function. Each element is an integer
- corresponding to an action which maximises the value function in that state.
- iter (int) The number of iterations taken to complete the computation.
- time (float) The amount of CPU time used to run the algorithm.

We can then display the values (utilities) computed, and look at the policy:

```
# We can then display the values (utilities) computed, and look at the policy:
print('Values:\n', vi1.V)
print('Policy:\n', vi1.policy)
```

```
Values:
(2.766226988084275, 3.7438891127976524, 4.857502678650809, 6.12579511)
Policy:
(1, 1, 1, 0)
```

This says that the optimum policy is to go Right in every state until reaching state 3, then Stay.

https://pymdptoolbox.readthedocs.io/en/latest/api/mdp.html

Policy iteration algorithm recap

Policy iteration algorithm

- How to do POLICY-EVALUATION?
- Action in each state is fixed by the policy
 - At the i^{th} iteration, the policy π_i specifies the action $\pi_i(s)$ in state s

$$U_i(s) = \sum_{s'} P(s' | s, \pi_i(s)) [R(s, \pi_i(s), s') + \gamma U_i(s')].$$

- Basically a simplified version of Bellman eq. relating the utility of s (with π_i) to those of its neighbors
 - No "max" operator ⇒ linear equations



```
function Policy-Iteration(mdp) returns a policy inputs: mdp, an MDP with states S, actions A(s), transition model P(s'|s,a) local variables: U, a vector of utilities for states in S, initially zero \pi, a policy vector indexed by state, initially random repeat U \leftarrow \text{Policy-Evaluation}(\pi, U, mdp) unchanged? \leftarrow \text{true} for each state s in S do a^* \leftarrow \underset{a \in A(s)}{\operatorname{argmax}} Q\text{-Value}(mdp, s, a, U) \underset{a \in A(s)}{\operatorname{af}} Q\text{-Value}(mdp, s, a^*, U) > Q\text{-Value}(mdp, s, \pi[s], U) then \pi[s] \leftarrow a^*; unchanged? \leftarrow \text{false} until unchanged? return \pi
```

Policy iteration algorithm via MDP toolbox

class mdptoolbox.mdp.PolicyIteration(transitions, reward, discount, policyO=None, max_iter=1000, eval_type=0, skip_check=False) Bases: mdptoolbox.mdp.MDP A discounted MDP solved using the policy iteration algorithm. Parameters: • transitions (array) - Transition probability matrices. See the documentation for the MDP class for details. • reward (array) - Reward matrices or vectors. See the documentation for the MDP class for details. • discount (float) - Discount factor. See the documentation for the MDP class for details. policy0 (array, optional) – Starting policy. • max_iter (int, optional) - Maximum number of iterations. See the documentation for the MDP class for details. Default is 1000. • eval_type (int or string, optional) - Type of function used to evaluate policy. O or "matrix" to solve as a set of linear equations. 1 or "iterative" to solve iteratively. Default: 0. • skip_check (bool) - By default we run a check on the transitions and rewards arguments to make sure they describe a valid MDP. You can set this argument to True in order to skip this check. Attributes (Data) -• V (tuple) - value function • policy (tuple) - optimal policy • iter (int) - number of done iterations • time (float) - used CPU time

Although we have been looking at the policy, we go it through value iteration.

Solving the same problem using policy iteration is easy with the MDP Toolbox:

```
# To run policy iteration we create a policy iteration object, and run it. Note that
# discount value is 0.9
pi1 = mdptoolbox.mdp.PolicyIteration(P1, R1, 0.9)
pi1.run()
```

https://pymdptoolbox.readthedocs.io/en/latest/api/mdp.html

class mdptoolbox.mdp.PolicyIteration(transitions, reward, discount, policyO=None, max_iter=1000,
eval_type=0, skip_check=False) [source]

Bases: mdptoolbox.mdp.MDP

A discounted MDP solved using the policy iteration algorithm.

Parameters:

- transitions (array) Transition probability matrices. See the documentation for the MDP class for details.
- reward (array) Reward matrices or vectors. See the documentation for the documentation for the class for details.
- discount (float) Discount factor. See the documentation for the MDP class for details.
- policy0 (array, optional) Starting policy.
- max_iter (int, optional) Maximum number of iterations. See the documentation for the MDP class for details. Default is 1000.
- eval_type (int or string, optional) Type of function used to evaluate policy. 0 or "matrix" to solve as a set of linear equations. 1 or "iterative" to solve iteratively.
 Default: 0.
- **skip_check** (*bool*) By default we run a check on the **transitions** and **rewards** arguments to make sure they describe a valid MDP. You can set this argument to True in order to skip this check.
- Attributes (Data) -
- -----
- V (tuple) value function
- policy (tuple) optimal policy
- iter (int) number of done iterations
- time (float) used CPU time

Although we have been looking at the policy, we go it through value iteration.

Solving the same problem using policy iteration is easy with the MDP Toolbox:

```
# We can then display the values (utilities) computed, and look at the policy:
print('Values:\n', pi1.V)
print('Policy:\n', pi1.policy)
```

```
Values:
```

```
(6.6402692938291725, 7.6180844735276665, 8.731707317073173, 10.0000000000000000)
Policy:
(1, 1, 1, 0)
```

Note that the methods disagree on the value while agreeing on the policy.

https://pymdptoolbox.readthedocs.io/en/latest/api/mdp.html

Q-Learning algorithm via MDP toolbox

class mdptoolbox.mdp.QLearning(transitions, reward, discount, n_iter=10000, skip_check=False) Bases: mdptoolbox.mdp.MDP A discounted MDP solved using the Q learning algorithm. Parameters: • transitions (array) - Transition probability matrices. See the documentation for the MDP class for details. reward (array) - Reward matrices or vectors. See the documentation for the MDP class for details. • **discount** (*float*) - Discount factor. See the documentation for the MDP class for details. • n_iter (int, optional) - Number of iterations to execute. This is ignored unless it is an integer greater than the default value. Defaut: 10,000. • skip_check (bool) - By default we run a check on the transitions and rewards arguments to make sure they describe a valid MDP. You can set this argument to True in order to skip this check. Attributes (Data) - Q (array) – learned Q matrix (SxA) V (tuple) – learned value function (S). policy (tuple) – learned optimal policy (S). • mean_discrepancy (array) - Vector of V discrepancy mean over 100 iterations. Then the length of this vector for the default value of N is $100 \, (N/100)$.

Solving a problem using reinforcement learning (well, the **Q-learning** kind of Reinforcement Learning)

Action-utility function, or Q-function: Q(s, a)

- expected utility of taking a given action in a given state
- related to utilities in the obvious way →

is also easy using the MDP Toolbox:

```
# To run q-learning we create a q-learning object, and run it. Note that
# discount value is 0.9
ql1 = mdptoolbox.mdp.QLearning(P1, R1, 0.9)
ql1.run()
```

class mdptoolbox.mdp.QLearning(transitions, reward, discount, n_iter=10000, skip_check=False) [source]

Bases: mdptoolbox.mdp.MDP

A discounted MDP solved using the Q learning algorithm.

Parameters:

- **transitions** (*array*) Transition probability matrices. See the documentation for the MDP class for details.
- reward (array) Reward matrices or vectors. See the documentation for the documentation for the class for details.
- discount (float) Discount factor. See the documentation for the MDP class for details.
- **n_iter** (*int*, *optional*) Number of iterations to execute. This is ignored unless it is an integer greater than the default value. Defaut: 10,000.
- **skip_check** (*bool*) By default we run a check on the transitions and rewards arguments to make sure they describe a valid MDP. You can set this argument to True in order to skip this check.
- Attributes (Data) -
- -----
- Q (array) learned Q matrix (SxA)
- **V** (tuple) learned value function (S).
- policy (tuple) learned optimal policy (S).
- mean_discrepancy (array) Vector of V discrepancy mean over 100 iterations.
 Then the length of this vector for the default value of N is 100 (N/100).

Solving a problem using reinforcement learning (well, the **Q-learning** kind of Reinforcement Learning) is also easy using the MDP Toolbox:

```
# We can then display the values (utilities) computed, and look at the policy:
print('Values:\n', ql1.V)
print('Policy:\n', ql1.policy)

Values:
  (0.26457661943006405, 2.0695643950241327, 6.421037194032352, 9.999999762119485)
Policy:
  (1, 1, 1, 0)
```

Note that the methods disagree on the value while agreeing on the policy.

Questions

