

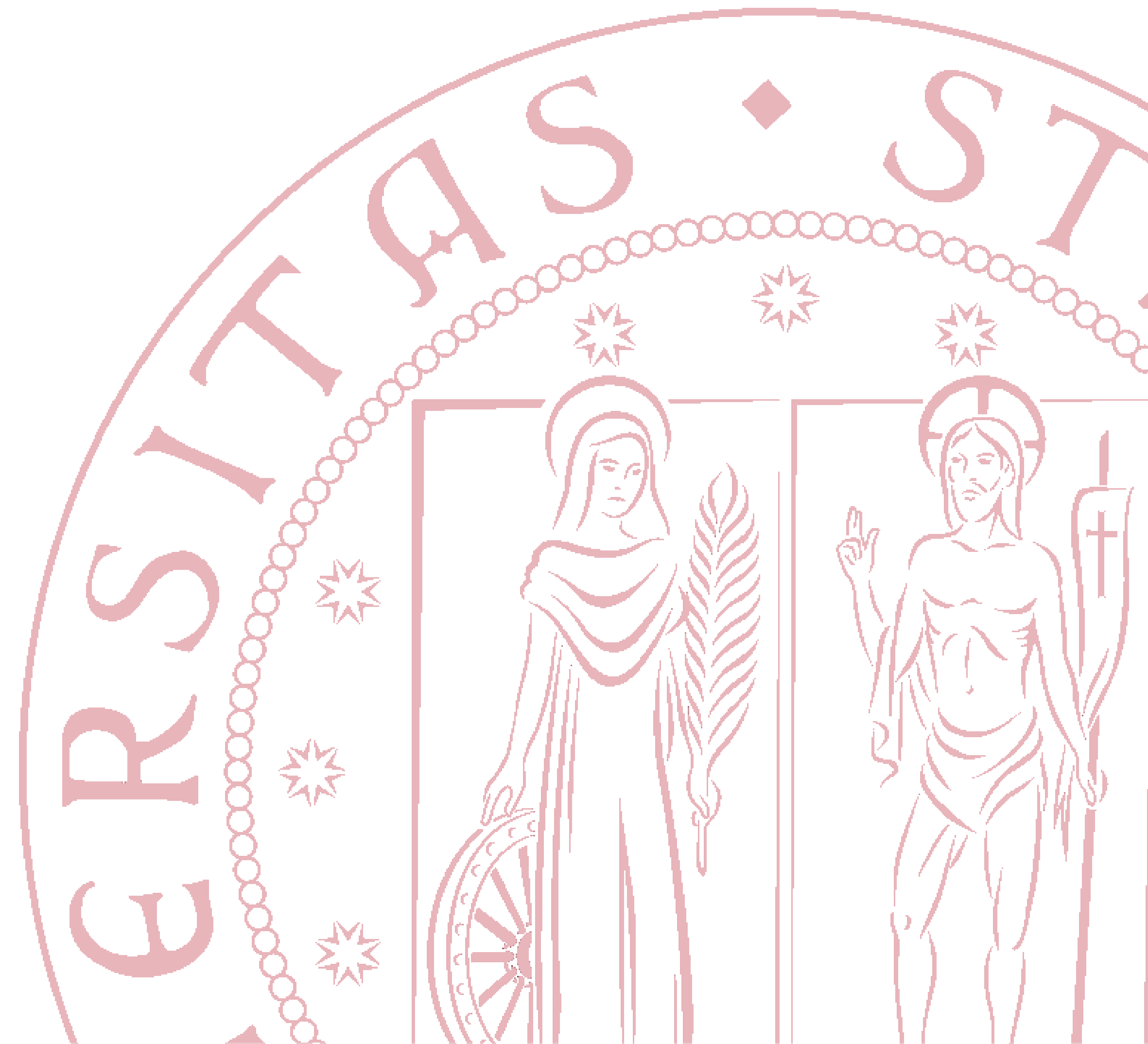
Solving Problems by Searching in Python: Extra exercises

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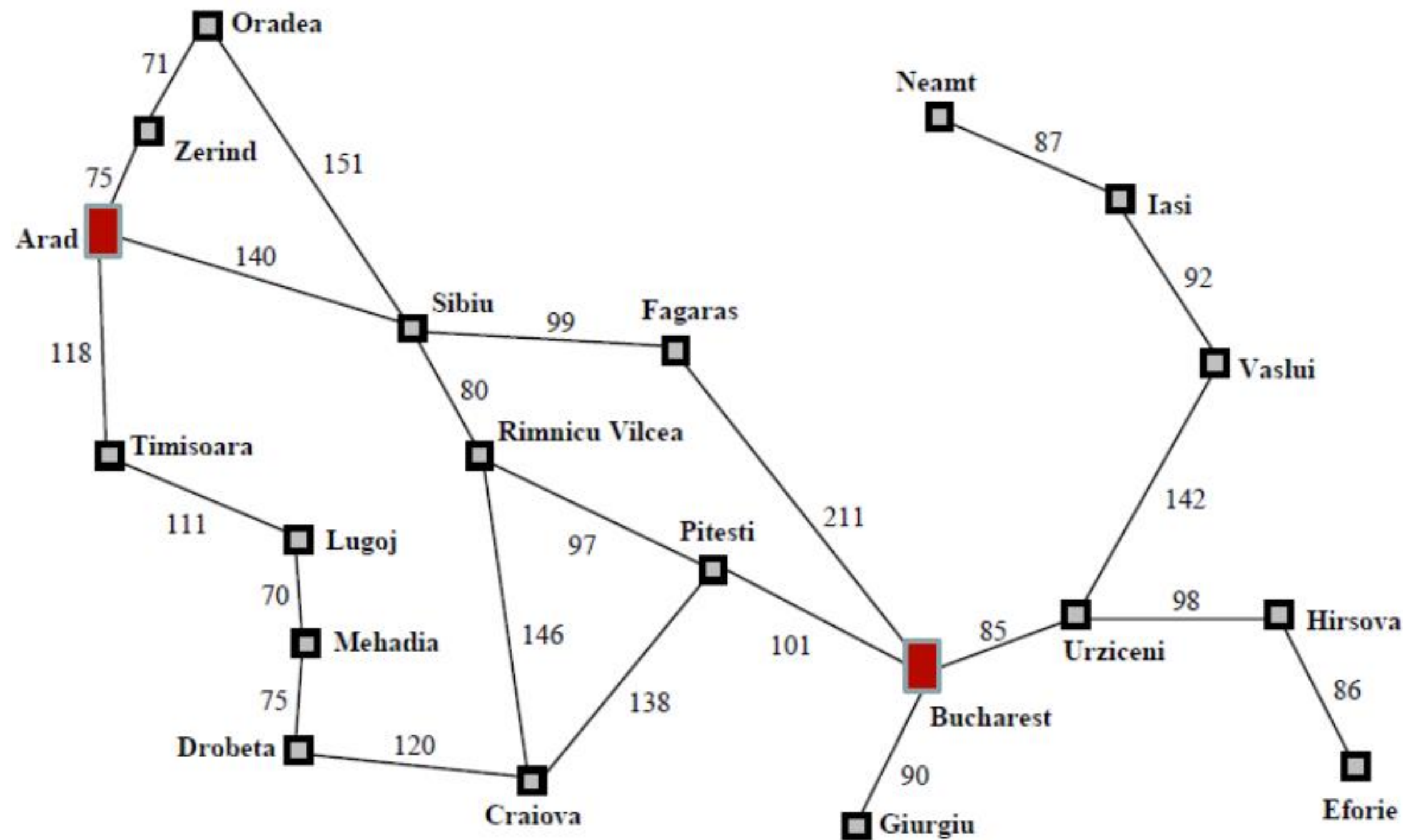
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Topics:

- Route Finding Problems
- Map class
- Pancake Sorting Problems
- Gap heuristic
- CountCalls
- Report



Route Finding Problems



In a RouteProblem, the **states** are names of "cities" (or other locations), like `'A'` for Arad.

The **actions** are also city names; `'Z'` is the action to **move to city** `'Z'`.

The layout of cities is given by a separate data structure, a **Map**, which is a **graph** where there are vertexes (cities), links between vertexes, distances (costs) of those links (if not specified, the default is 1 for every link), and optionally the 2D (x, y) location of each city can be specified.

A RouteProblem takes **this Map as input** and allows **actions to move among linked cities**. The default heuristic is straight-line distance to the goal, or is uniformly zero if locations were not given.

Map

Map, which is a graph where there are **vertexes** (cities), **links** between vertexes, **distances (costs)** of those links (if not specified, the default is 1 for every link), and **optionally** the 2D (x, y) location of each city can be specified.

```
class Map:
    """A map of places in a 2D world: a graph with vertexes and links between them.
    In `Map(links, locations)`, `links` can be either [(v1, v2)...] pairs,
    or a {(v1, v2): distance...} dict. Optional `locations` can be {v1: (x, y)}
    If `directed=False` then for every (v1, v2) link, we add a (v2, v1) link."""

    def __init__(self, links, locations=None, directed=False):
        if not hasattr(links, 'items'): # Distances are 1 by default
            links = {link: 1 for link in links}
        if not directed:
            for (v1, v2) in list(links):
                links[v2, v1] = links[v1, v2]
        self.distances = links
        self.neighbors = multimap(links)
        self.locations = locations or defaultdict(lambda: (0, 0))

def multimap(pairs) -> dict:
    """Given (key, val) pairs, make a dict of {key: [val,...]}."""
    result = defaultdict(list)
    for key, val in pairs:
        result[key].append(val)
    return result
```

hasattr() function returns True if the specified object has the specified attribute, otherwise False.

<https://docs.python.org/3/library/functions.html#hasattr>

If it is missing items (e.g., the costs of the links), this means that link-cost is 1 per default

If is not directed, for every (v1, v2) link, we add a (v2, v1) link

The neighbors is represented as the multimap namely a dict (see the second function)

The 2D locations can be given or are represented by a dict with (0,0)

Map

The neighbors is represented as the multimap namely a dict (see the second function)

```
def multimap(pairs) -> dict:
    "Given (key, val) pairs, make a dict of {key: [val,...]}."
    result = defaultdict(list)
    for key, val in pairs:
        result[key].append(val)
    return result

from collections import defaultdict, deque, Counter
result = defaultdict(list)
print(result)
links = {('O', 'Z'): 71, ('O', 'S'): 151, ('A', 'Z'): 75, ('A', 'S'): 140, ('A', 'T'): 118, ('L', 'T'): 111, ('L', 'M'): 70, ('D', 'M'): 75, ('C', 'D'): 120,
multimap(links)

defaultdict(<class 'list'>, {})
defaultdict(list,
  {'O': ['Z', 'S'],
   'A': ['Z', 'S', 'T'],
   'L': ['T', 'M'],
   'D': ['M'],
   'C': ['D', 'R', 'P'],
   'R': ['S'],
   'F': ['S'],
   'B': ['F', 'P', 'G', 'U'],
   'H': ['U'],
   'E': ['H'],
   'U': ['V'],
   'I': ['V', 'N'],
   'P': ['R']})
```



Route Finding Problems

```
class RouteProblem(Problem):
    """A problem to find a route between locations on a `Map`.
    Create a problem with RouteProblem(start, goal, map=Map(...)).
    States are the vertexes in the Map graph; actions are destination states."""

    def actions(self, state):
        """The places neighboring `state`."""
        return self.map.neighbors[state]

    def result(self, state, action):
        """Go to the `action` place, if the map says that is possible."""
        return action if action in self.map.neighbors[state] else state

    def action_cost(self, s, action, s1):
        """The distance (cost) to go from s to s1."""
        return self.map.distances[s, s1]

    def h(self, node):
        """Straight-line distance between state and the goal."
        locs = self.map.locations
        return straight_line_distance(locs[node.state], locs[self.goal])

def straight_line_distance(A, B):
    """Straight-line distance between two points."
    return sum(abs(a - b)**2 for (a, b) in zip(A, B)) ** 0.5
```

zip() function produces tuples with an item from each one
<https://docs.python.org/3/library/functions.html#zip>

The **actions** are also city names; `'Z'` is the action to **move to city** `'Z'`.

```
defaultdict(list,
    {'O': ['Z', 'S'],
     'A': ['Z', 'S', 'T'],
     'L': ['T', 'M'],
     'D': ['M'],
     'C': ['D', 'R', 'P'],
     'R': ['S'],
     'F': ['S'],
     'B': ['F', 'P', 'G', 'U'],
     'H': ['U'],
     'E': ['H'],
     'U': ['V'],
     'I': ['V', 'N'],
     'P': ['R']})
```

The cities where it is possible to move (i.e., destinations) from a current city = state. They are stored in the Map (neighbors).

The **result** method returns the action if the action (i.e., destinations) are inside the Map otherwise returns the state (i.e., current city)

The **action_cost** method returns the cost of applying the action from the current state. In this example the cost is the distance.

The default **heuristic** is straight-line distance to the goal, or is uniformly zero if locations were not given. In **h** method (i.e., heuristic) the straight-line distance is computed as specified in the problem description

Route Finding Problems

```
class Map:
    """A map of places in a 2D world: a graph with vertexes and links between them.
    In `Map(links, locations)`, `links` can be either [(v1, v2)...] pairs,
    or a {(v1, v2): distance...} dict. Optional `locations` can be {v1: (x, y)}
    If `directed=False` then for every (v1, v2) link, we add a (v2, v1) link."""

    def __init__(self, links, locations=None, directed=False):
```

```
romania = Map(
    {('O', 'Z'): 71, ('O', 'S'): 151, ('A', 'Z'): 75, ('A', 'S'): 140, ('A', 'T'): 118,
    ('L', 'T'): 111, ('L', 'M'): 70, ('D', 'M'): 75, ('C', 'D'): 120, ('C', 'R'): 146,
    ('C', 'P'): 138, ('R', 'S'): 80, ('F', 'S'): 99, ('B', 'F'): 211, ('B', 'P'): 101,
    ('B', 'G'): 90, ('B', 'U'): 85, ('H', 'U'): 98, ('E', 'H'): 86, ('U', 'V'): 142,
    ('I', 'V'): 92, ('I', 'N'): 87, ('P', 'R'): 97},
    {'A': ( 76, 497), 'B': (400, 327), 'C': (246, 285), 'D': (160, 296), 'E': (558, 294),
    'F': (285, 460), 'G': (368, 257), 'H': (548, 355), 'I': (488, 535), 'L': (162, 379),
    'M': (160, 343), 'N': (407, 561), 'O': (117, 580), 'P': (311, 372), 'R': (227, 412),
    'S': (187, 463), 'T': ( 83, 414), 'U': (471, 363), 'V': (535, 473), 'Z': (92, 539)})
```

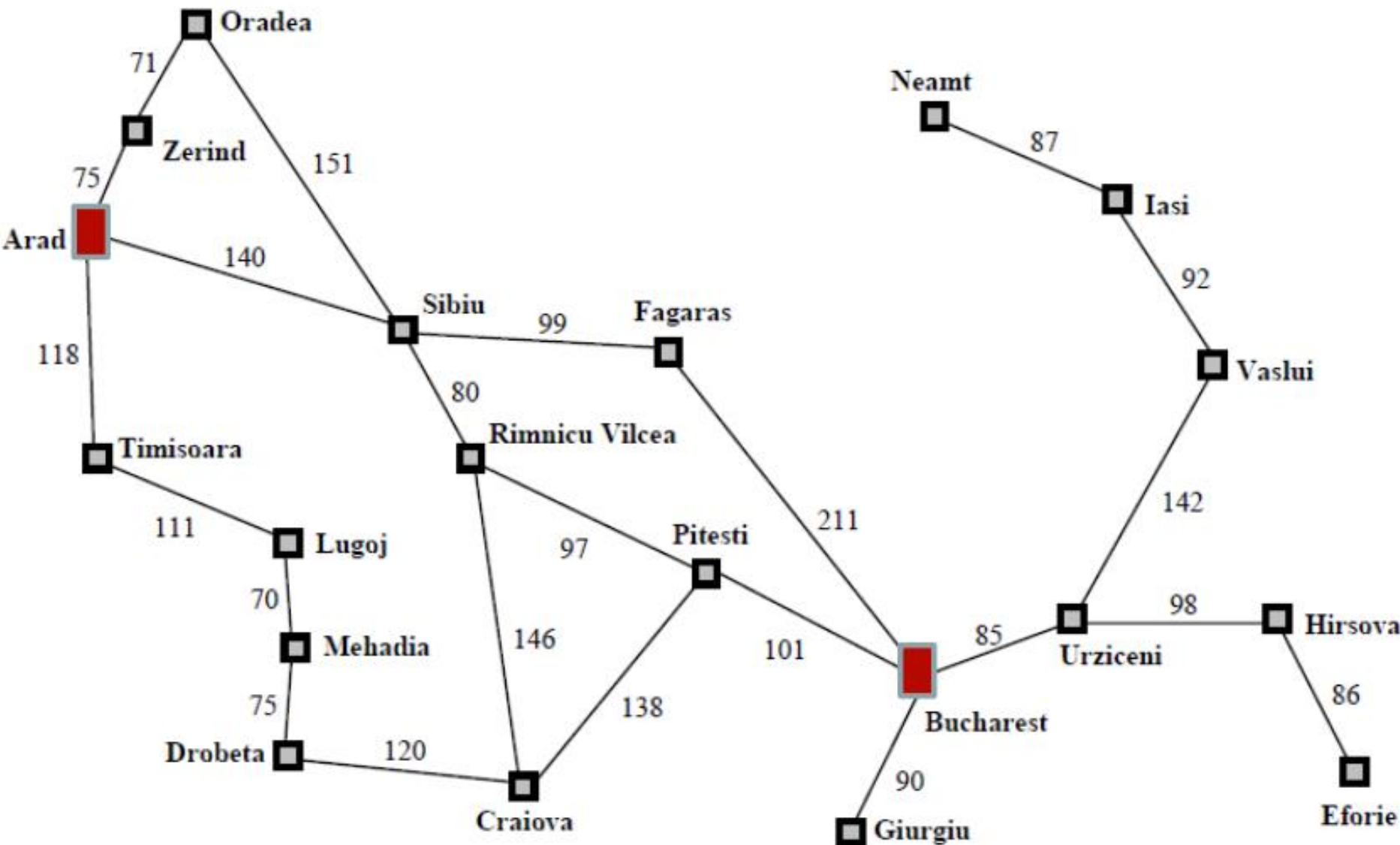
```
r0 = RouteProblem('A', 'A', map=romania)
r1 = RouteProblem('A', 'B', map=romania)
r2 = RouteProblem('N', 'L', map=romania)
r3 = RouteProblem('E', 'T', map=romania)
r4 = RouteProblem('O', 'M', map=romania)
```

initial
state

goal

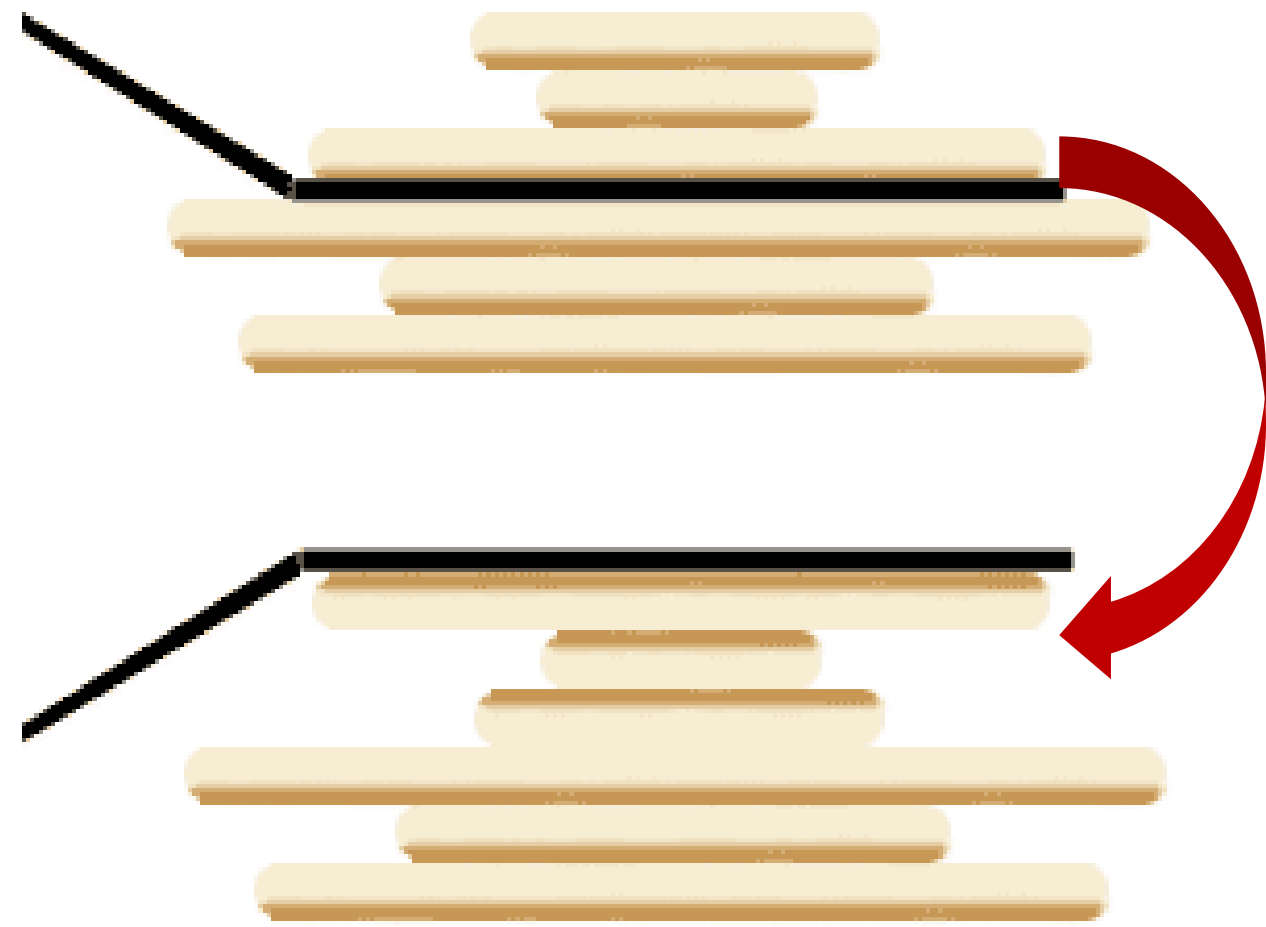
LINKS

LOCATIONS



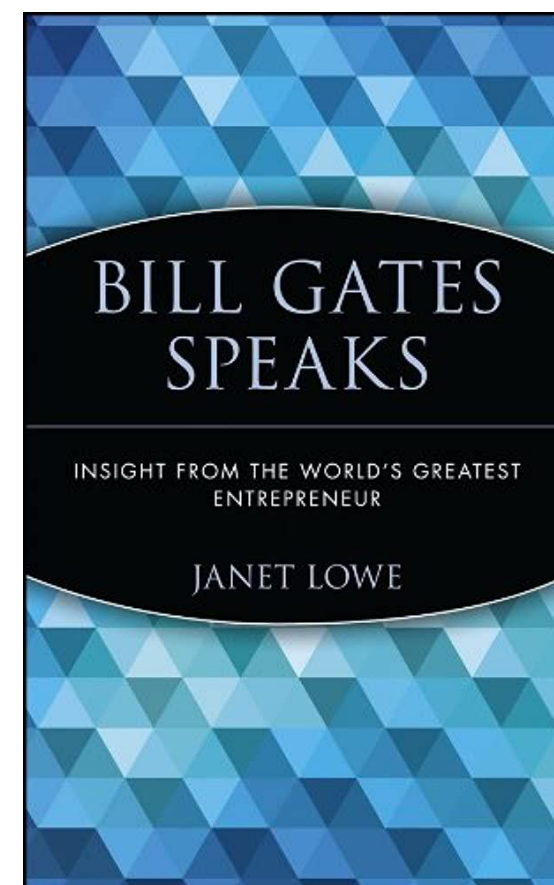
Pancake Sorting Problems

Given a stack of pancakes of various sizes, can you sort them into a stack of decreasing sizes, largest on bottom to smallest on top? You have a spatula with which you can **flip the top i pancakes**.



This is shown below for $i = 3$; on the top the spatula grabs the first three pancakes; on the bottom we see them flipped.

How many flips will it take to get the whole stack sorted? → **SORTING PROBLEM**



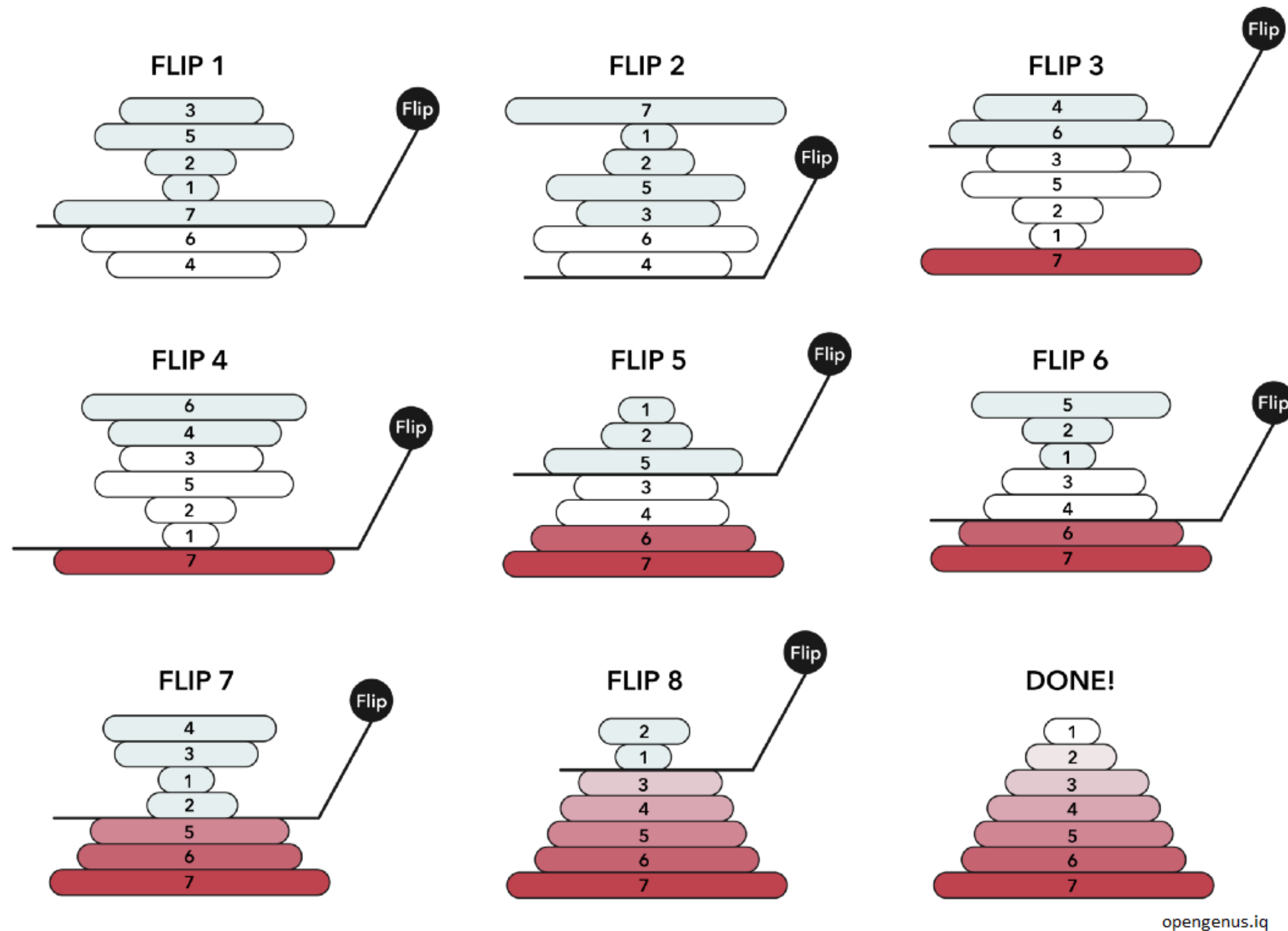
Pag 19

<https://www.npr.org/templates/story/story.php?storyId=92236781>



Source: Neil Jones and Pavel Pevzner, 2004 "Introduction to Bioinformatics Algorithms".

Pancake Sorting Problems



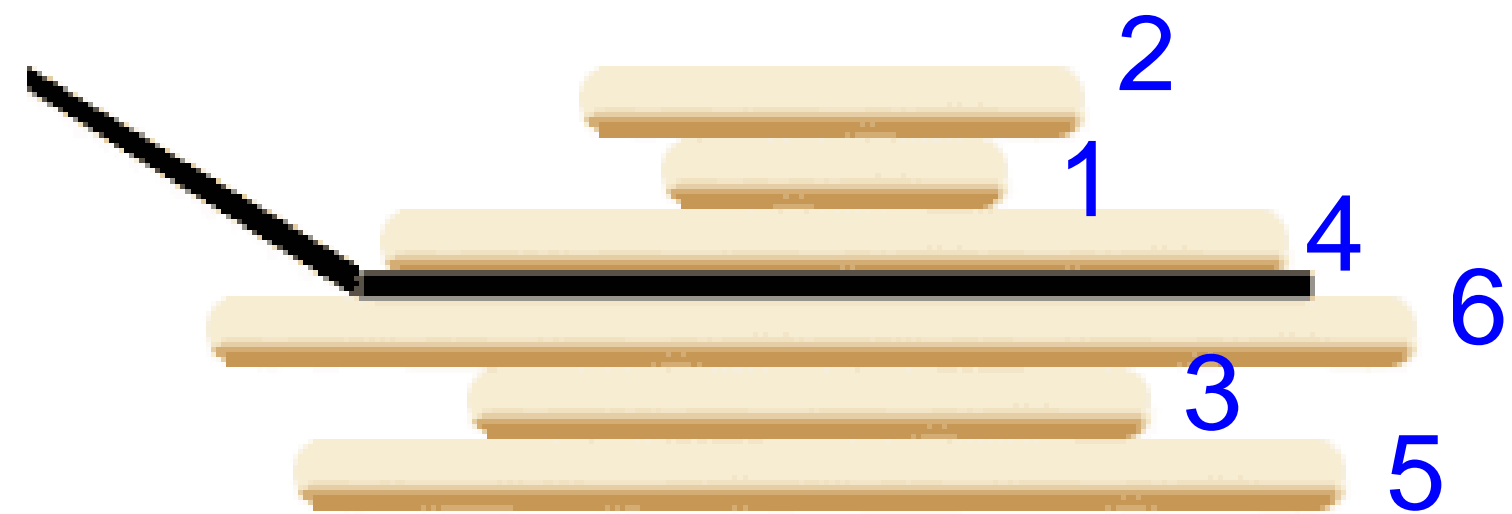
A reasonable heuristic for this problem is:
the *gap heuristic*

If we look at neighboring pancakes, if, say, the 2nd smallest is next to the 3rd smallest, that's good; they should stay next to each other.

But if the 2nd smallest is next to the 4th smallest, that's bad: we will require at least one move to separate them and insert the 3rd smallest between them.

The *gap heuristic* counts the number of neighbors that have a gap like this.

Pancake Sorting Problems



The **gap heuristic** counts the number of neighbors that have a **gap** like this.

In our specification of the problem, pancakes are ranked by size: the smallest is 1, the 2nd smallest 2, and so on, and

The representation of **a state** is a **tuple of these rankings**, from the top to the bottom pancake.

Thus the goal state is always $(1, 2, \dots, n)$

The initial (top) state in the diagram above is: **(2, 1, 4, 6, 3, 5)**.

Pancake Sorting Problems

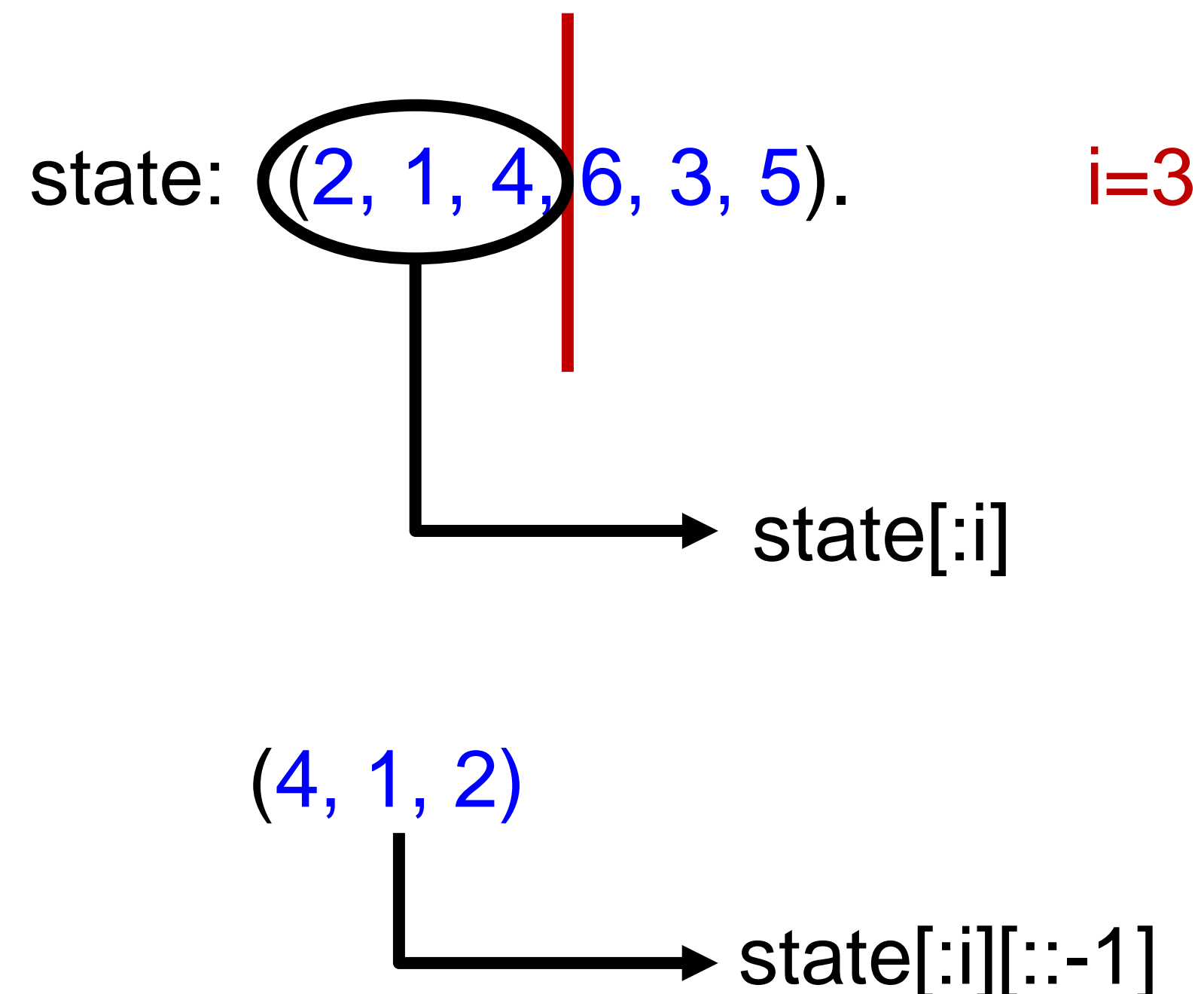
```
class PancakeProblem(Problem):
    """A PancakeProblem the goal is always `tuple(range(1, n+1))`, where the
    initial state is a permutation of `range(1, n+1)`. An act is the index `i`
    of the top `i` pancakes that will be flipped."""

    def __init__(self, initial):
        self.initial, self.goal = tuple(initial), tuple(sorted(initial))

    def actions(self, state): return range(2, len(state) + 1)

    def result(self, state, i): return state[:i][::-1] + state[i:]

    def h(self, node):
        "The gap heuristic."
        s = node.state
        return sum(abs(s[i] - s[i - 1]) > 1 for i in range(1, len(s)))
```

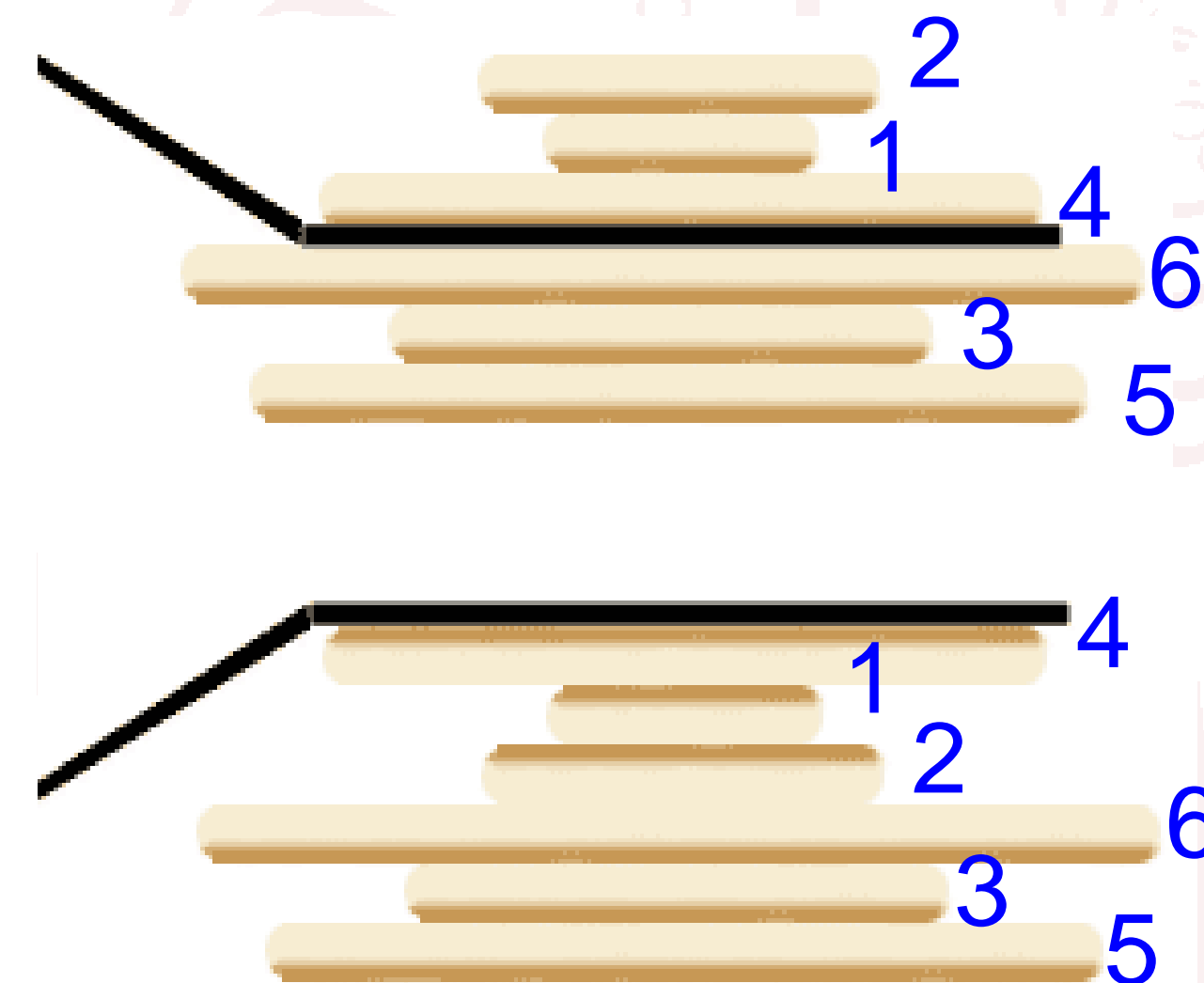


The representation of a state is a tuple of these rankings, from the top to the bottom pancake.

The initial state is the tuple representing the pancake stack

The goal is the sorted tuple

<https://docs.python.org/3/howto/sorting.html>



Pancake Sorting Problems

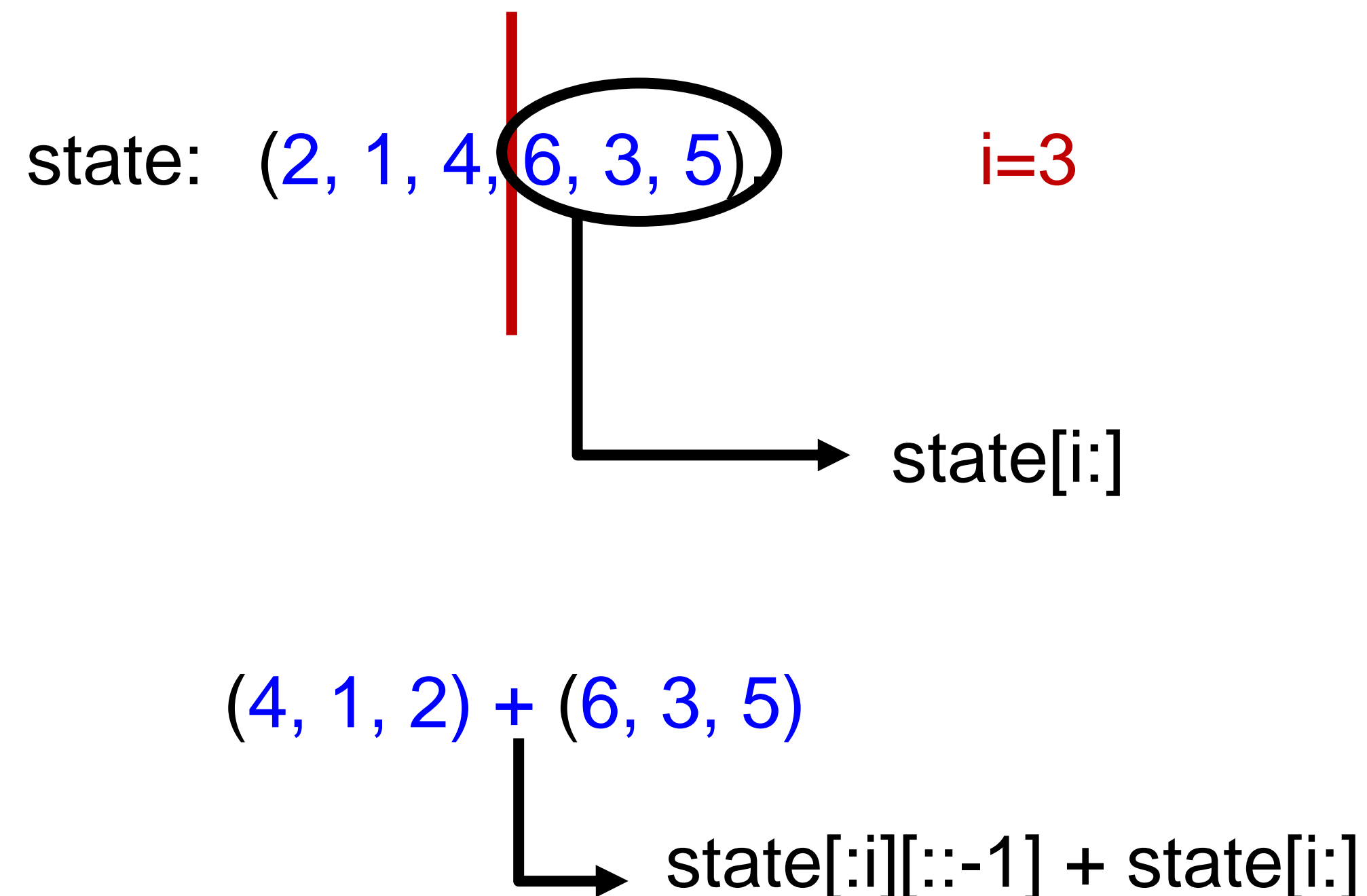
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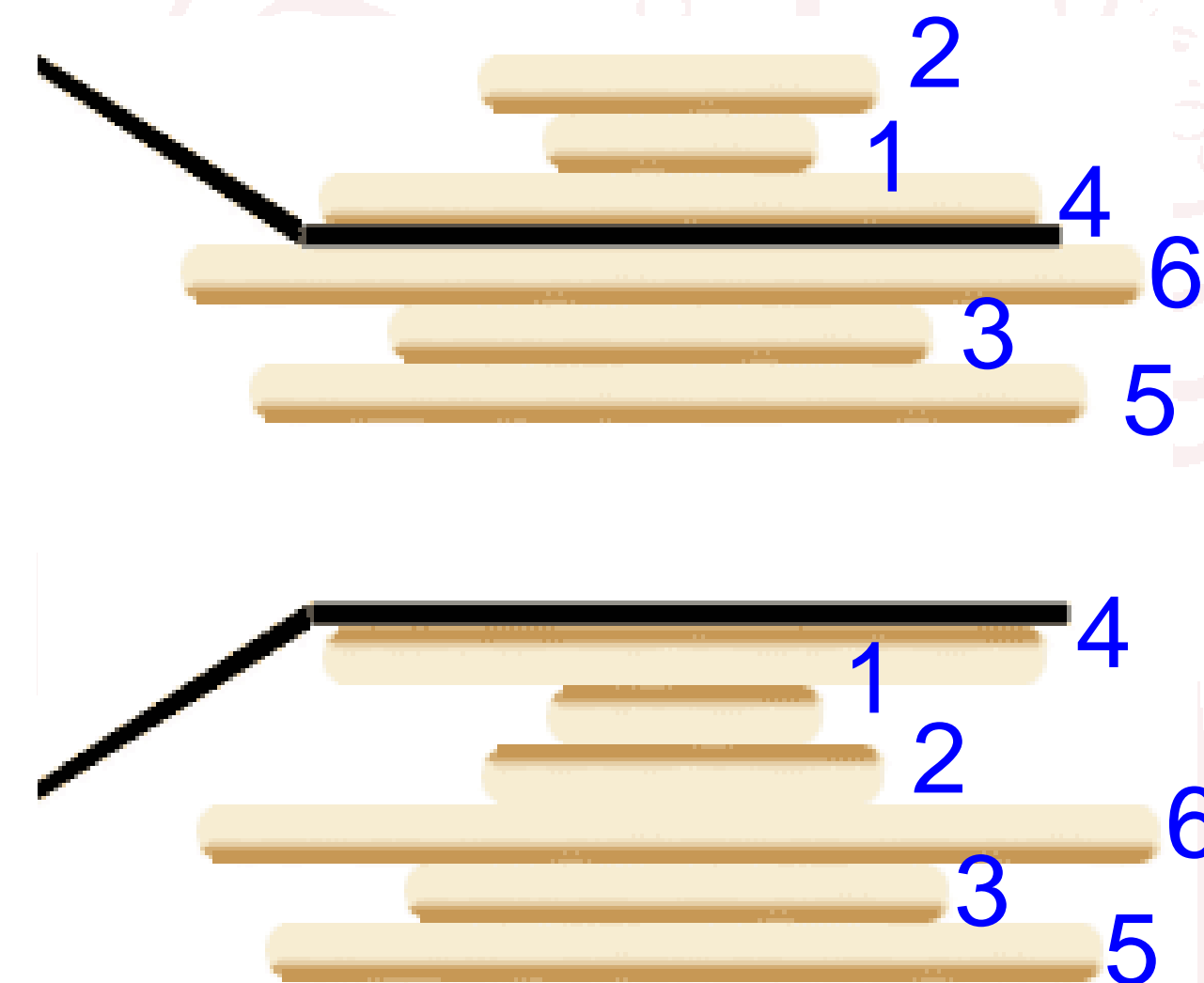


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Pancake Sorting Problems

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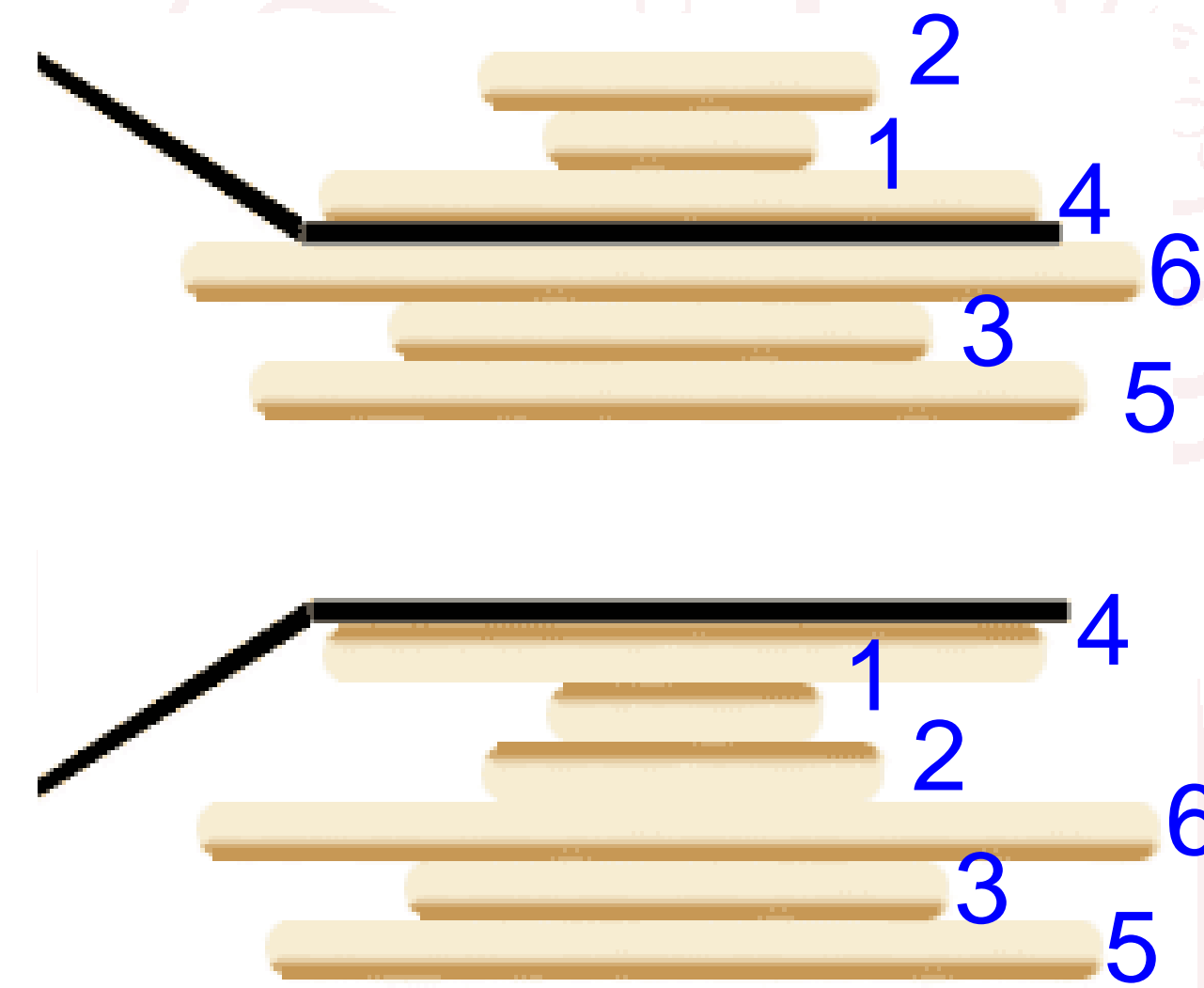
The **gap heuristic** counts the number of neighbors that have a gap like this.

The operation is equivalent to the following:

```
count = 0
for i in range(1, len(s)):
    diff = abs(s[i] - s[i-1])
    if diff > 1:
        count+=1
```

(2, 1, 4, 6, 3, 5).

1



Pancake Sorting Problems

```
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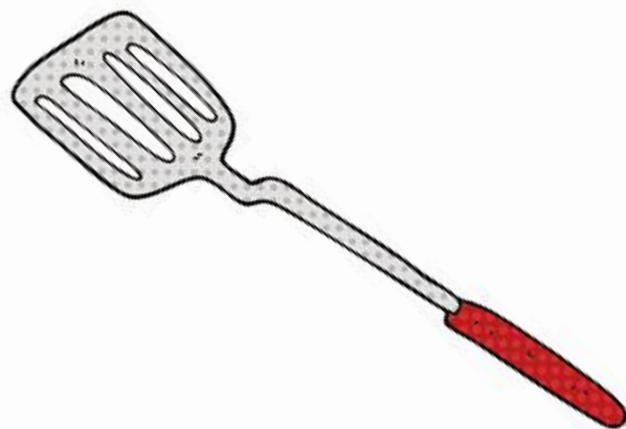
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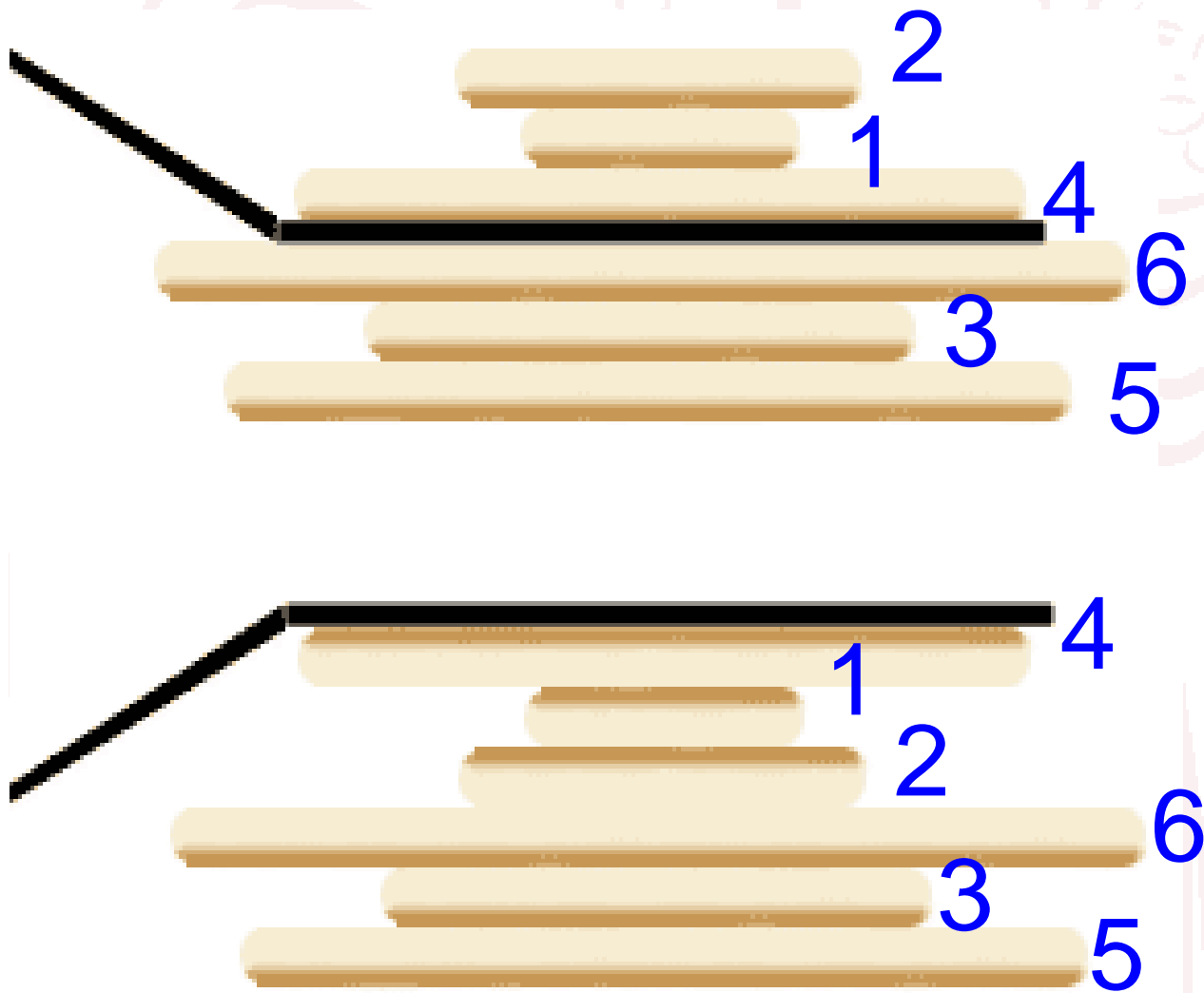
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count = 0
for i in range(1, len(s)):
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```

(2, 1, 4, 6, 3, 5).

3



+1



Pancake Sorting Problems

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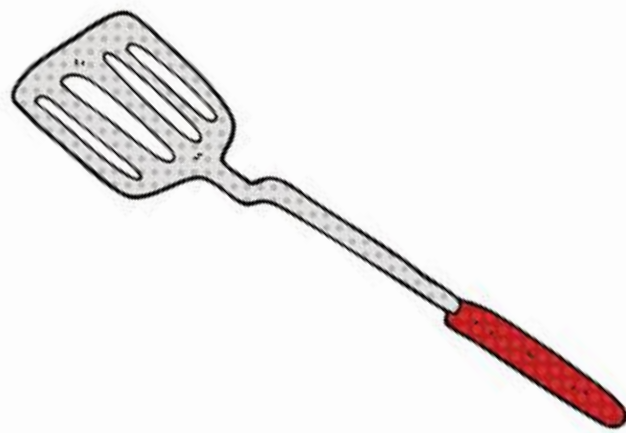
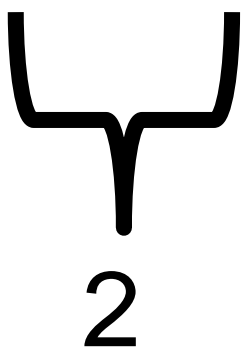
    def h(self, node):
        "The gap heuristic."
        s = node.state
        return sum(abs(s[i] - s[i - 1]) > 1 for i in range(1, len(s)))
```

The gap heuristic counts the number of neighbors that have a gap like this.

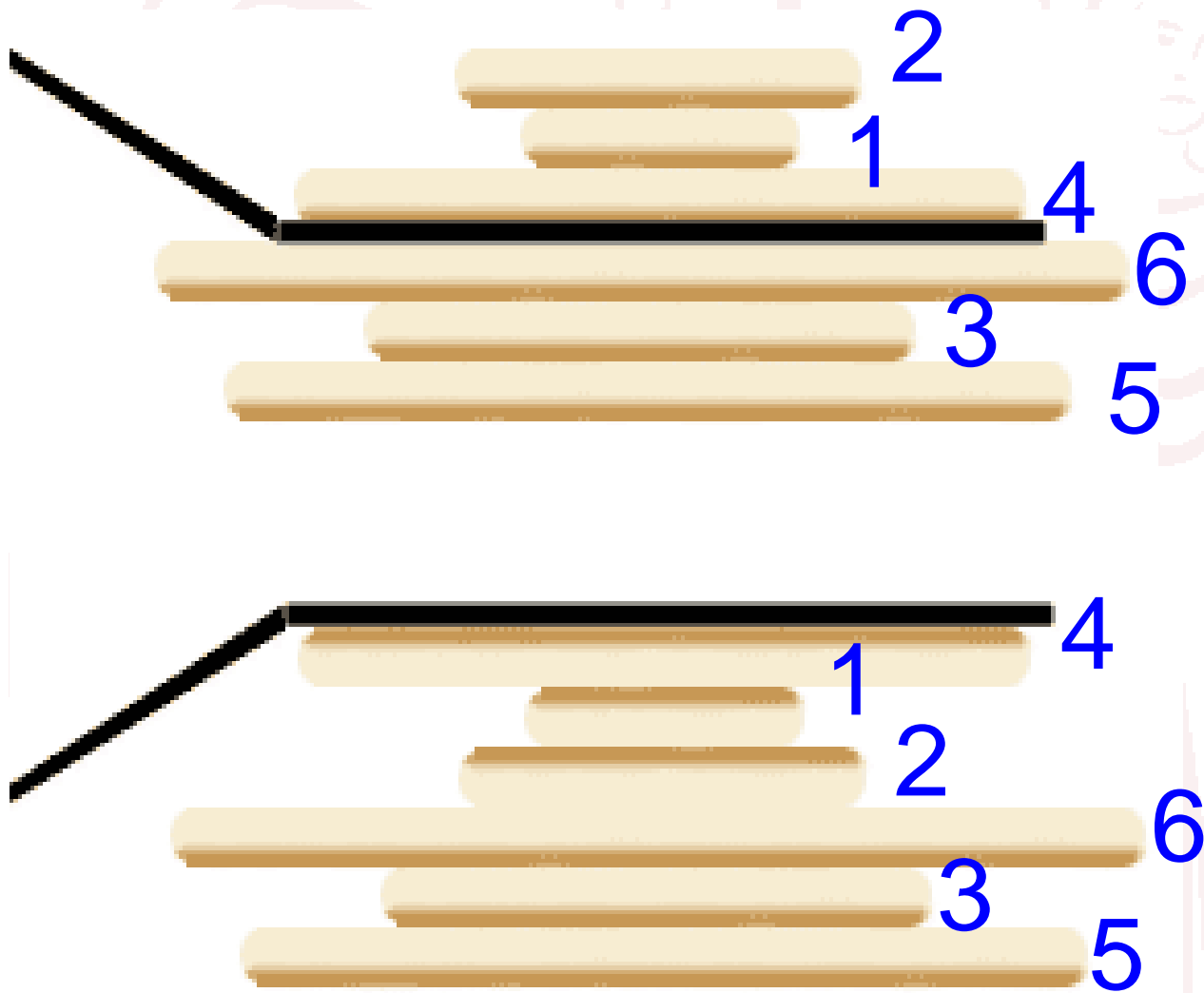
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```

(2, 1, 4, 6, 3, 5).



+2



Pancake Sorting Problems

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        return sum(abs(s[i] - s[i - 1]) > 1 for i in range(1, len(s)))
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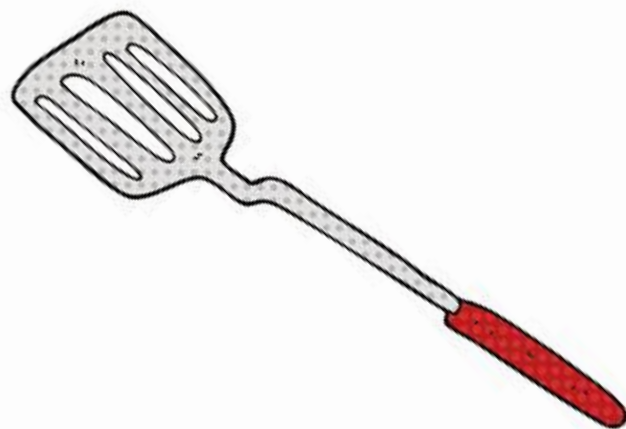
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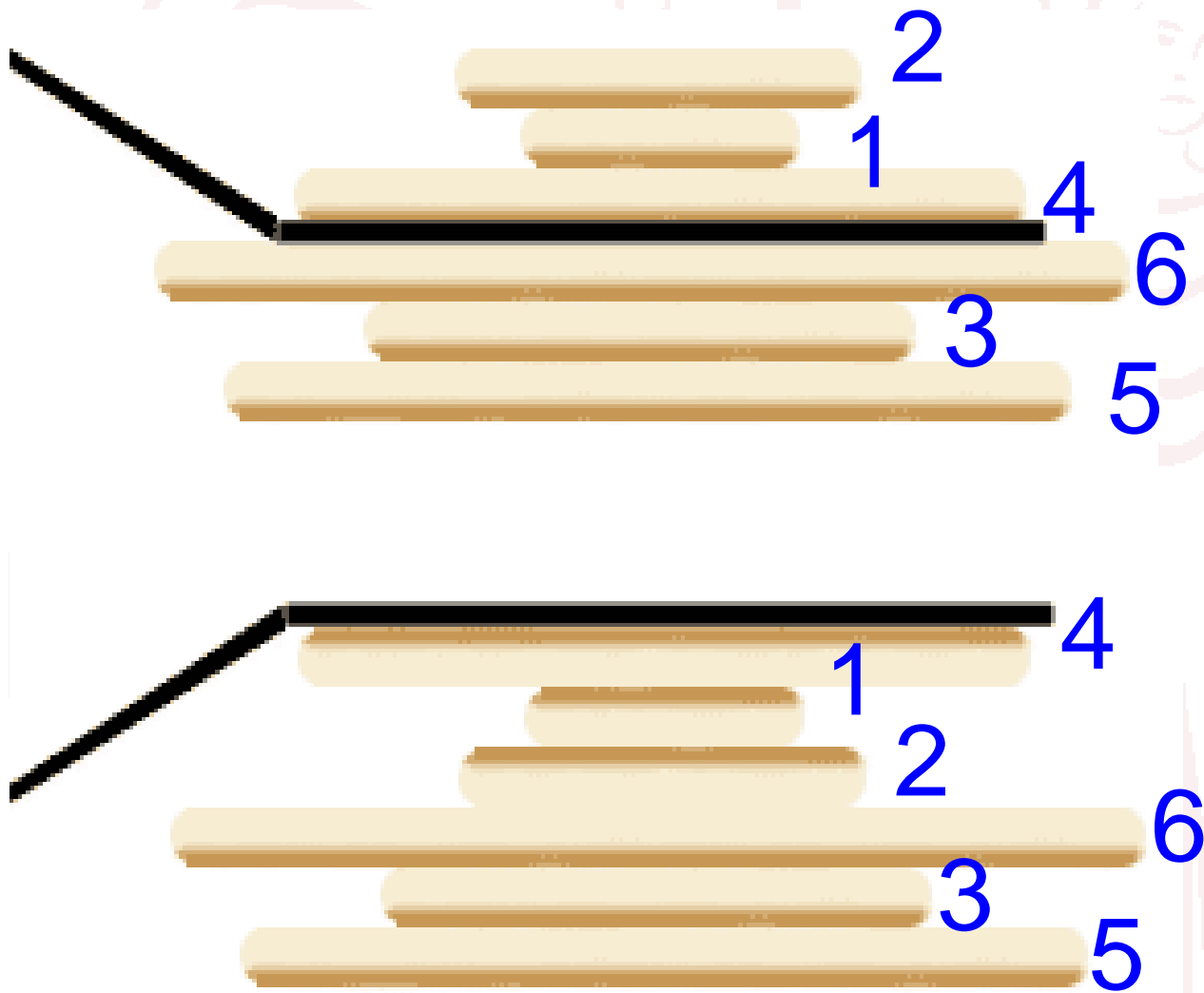
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    diff = abs(s[i] - s[i-1])
    if diff > 1:
        count+=1
```

(2, 1, 4, 6, 3, 5).

3



+3



Pancake Sorting Problems

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class PancakeProblem(Problem):
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        s = node.state
        return sum(abs(s[i] - s[i - 1]) > 1 for i in range(1, len(s)))
```

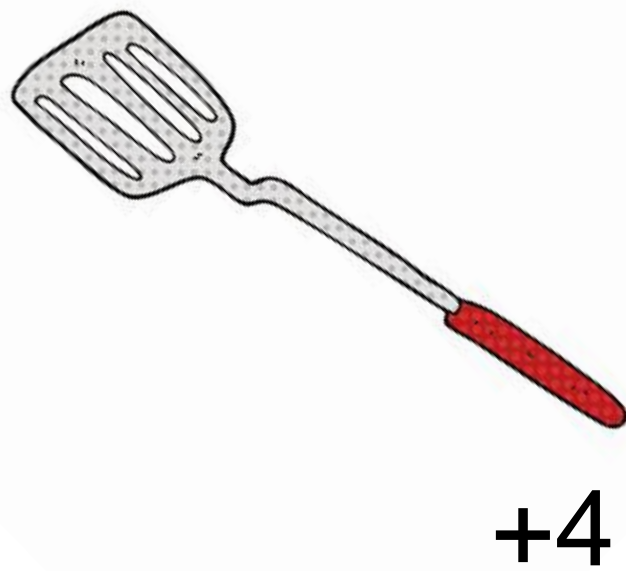
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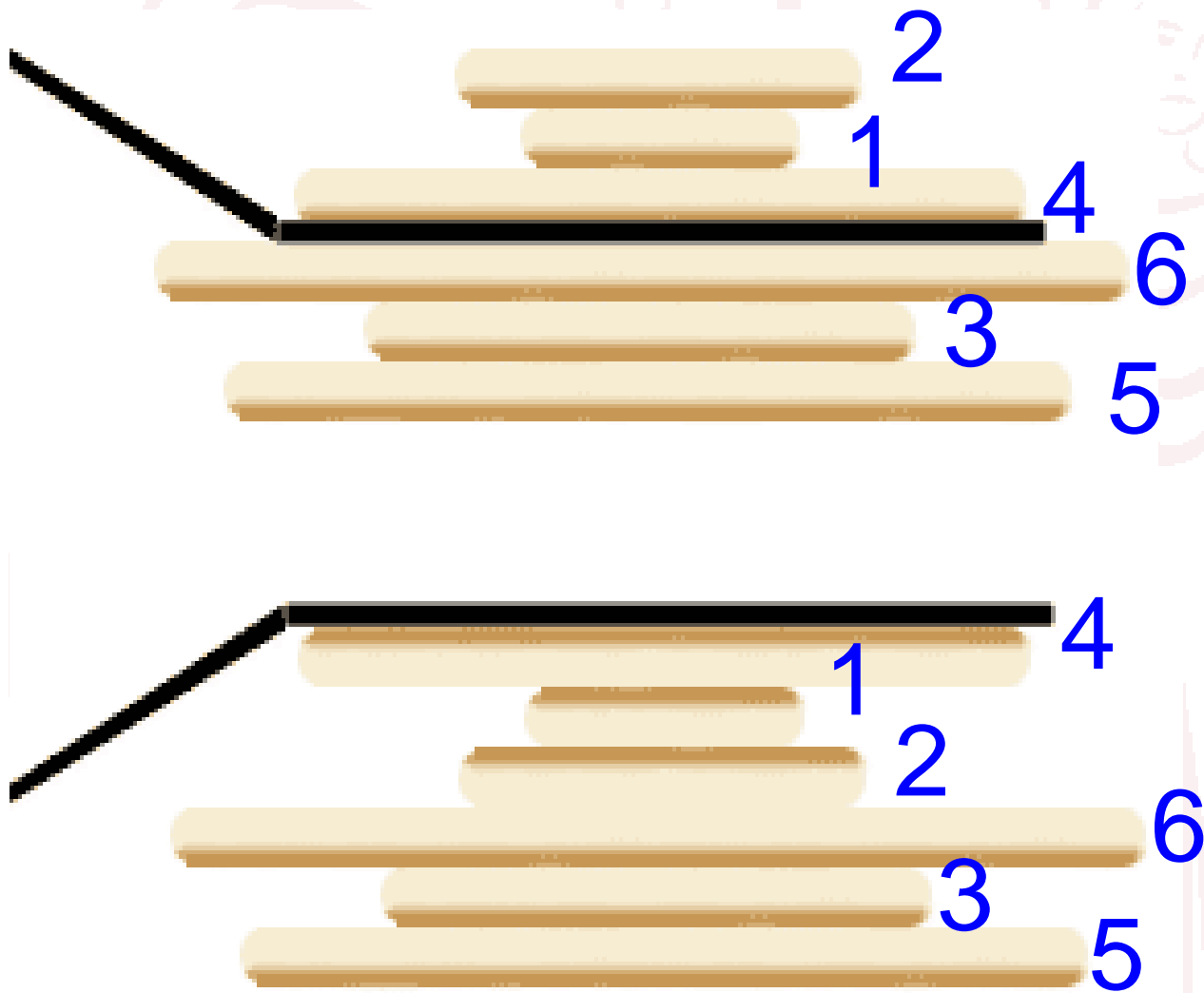
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count = 0
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    diff = abs(s[i] - s[i-1])
    if diff > 1:
        count+=1
```

(2, 1, 4, 6, 3, 5).

2



+4



CountCalls

We'll use CountCalls to wrap a Problem object in such a way that calls to its methods are delegated to the original problem, but each call increments a counter.

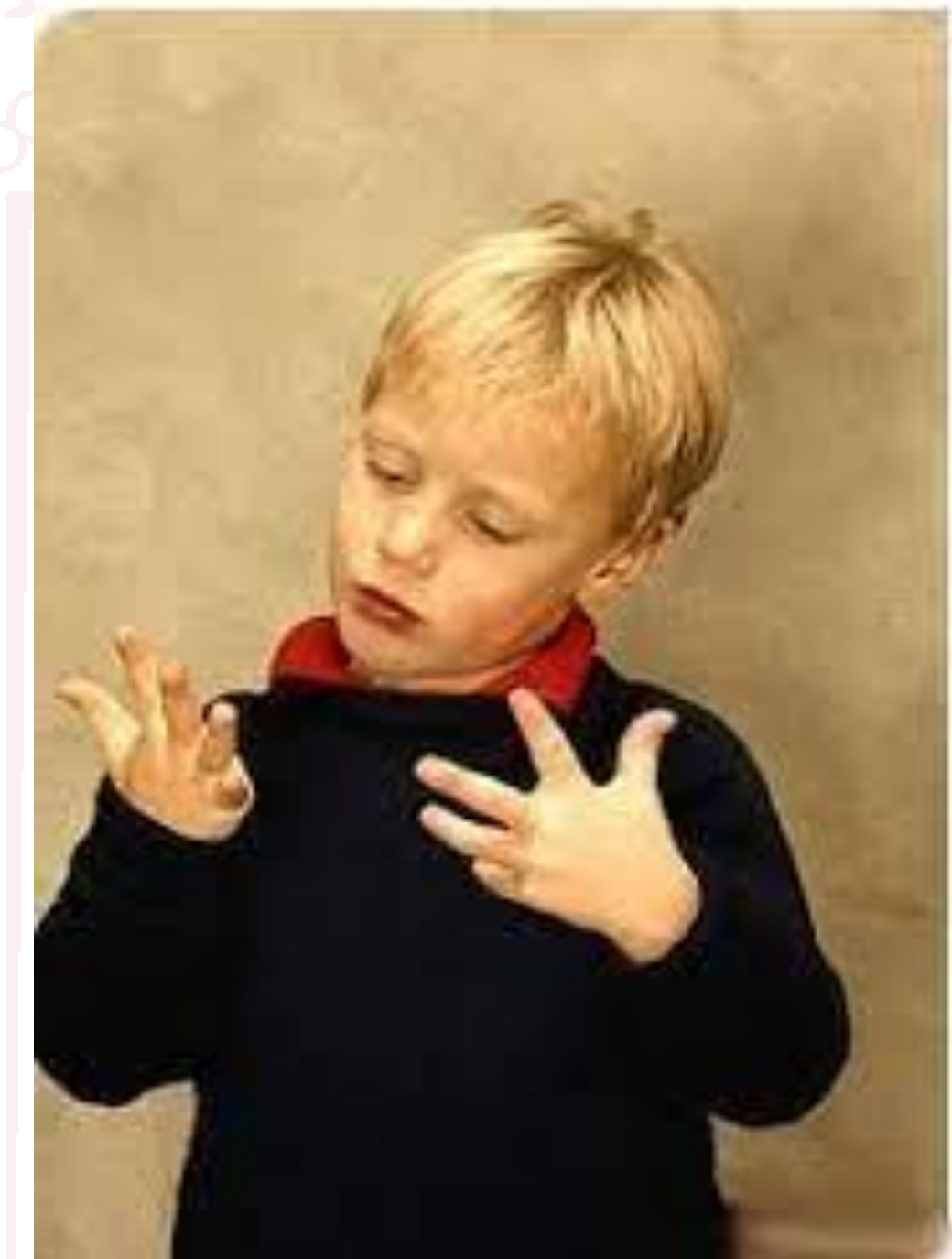
```
class CountCalls:
    """Delegate all attribute gets to the object, and count them in ._counts"""
    def __init__(self, obj):
        self._object = obj
        self._counts = Counter()

    def __getattr__(self, attr):
        "Delegate to the original object, after incrementing a counter."
        self._counts[attr] += 1
        return getattr(self._object, attr)
```

<https://docs.python.org/3/library/collections.html#collections.Counter>

Called when the default attribute access fails with an [AttributeError](#) (either [__getattr__\(\)](#) raises an [AttributeError](#) because *name* is not an instance attribute or an attribute in the class tree for self; or [__get__\(\)](#) of a *name* property raises [AttributeError](#)).

https://docs.python.org/3/reference/datamodel.html#object.__getattr__



Report

Now let's gather some metrics on how well each algorithm does.

```
def report(searchers, problems, verbose=True):
    """Show summary statistics for each searcher (and on each problem unless verbose is false)."""
    for searcher in searchers:
        print(searcher.__name__ + ':')
        total_counts = Counter()
        for p in problems:
            print(p)
            prob = CountCalls(p)
            soln = searcher(prob)
            counts = prob._counts;
            counts.update(actions=len(soln), cost=soln.path_cost)
            total_counts += counts
            if verbose: report_counts(counts, str(p)[:40])
        report_counts(total_counts, 'TOTAL\n')

def report_counts(counts, name):
    """Print one line of the counts report."""
    print('{:9,d} nodes |{:9,d} goal |{:5.0f} cost |{:8,d} actions | {}'.format(
        counts['result'], counts['is_goal'], counts['cost'], counts['actions'], name))
```

searchers is an iterable object (e.g., list)

Report

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    for searcher in searchers:
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        total_counts = Counter()
        for p in problems:
            print(p)
            prob = CountCalls(p)
            soln = searcher(prob)
            counts = prob._counts;
            counts.update(actions=len(soln), cost=soln.path_cost)
            total_counts += counts
            if verbose: report_counts(counts, str(p)[:40])
        report_counts(total_counts, 'TOTAL\n')

def report_counts(counts, name):
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    print('{:9,d} nodes |{:9,d} goal |{:5.0f} cost |{:8,d} actions | {}'.format(
        counts['result'], counts['is_goal'], counts['cost'], counts['actions'], name))
```

→ *problems* is an iterable object (e.g., list)

Report

Now let's gather some metrics on how well each algorithm does.

```
def report(searchers, problems, verbose=True):
    """Show summary statistics for each searcher (and on each problem unless verbose is false)."""
    for searcher in searchers:
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        for p in problems:
            print(p)
            prob = CountCalls(p)
            soln = searcher(prob)
            counts = prob._counts;
            counts.update(actions=len(soln), cost=soln.path_cost)
            total_counts += counts
            if verbose: report_counts(counts, str(p)[:40])
        report_counts(total_counts, 'TOTAL\n')

def report_counts(counts, name):
    """Print one line of the counts report."""
    print('{:9,d} nodes |{:9,d} goal |{:5.0f} cost |{:8,d} actions | {}'.format(
        counts['result'], counts['is_goal'], counts['cost'], counts['actions'], name))
```

solve the problem using the *searcher*

Report

Now let's gather some metrics on how well each algorithm does.

```
def report(searchers, problems, verbose=True):
    """Show summary statistics for each searcher (and on each problem unless verbose is false)."""
    for searcher in searchers:
        print(searcher.__name__ + ':')
        total_counts = Counter()
        for p in problems:
            print(p)
            prob = CountCalls(p)
            soln = searcher(prob)
            counts = prob._counts;
            counts.update(actions=len(soln), cost=soln.path_cost)
            total_counts += counts
            if verbose: report_counts(counts, str(p)[:40])
        report_counts(total_counts, 'TOTAL\n')

def report_counts(counts, name):
    """Print one line of the counts report."""
    print('{:9,d} nodes |{:9,d} goal |{:5.0f} cost |{:8,d} actions | {}'.format(
        counts['result'], counts['is_goal'], counts['cost'], counts['actions'], name))
```

update([iterable-or-mapping])

Elements are counted from an *iterable* or added-in from another *mapping* (or counter).

<https://docs.python.org/3/library/collections.html#collections.Counter>

Questions

