$\begin{array}{c} {\rm Matematika} \ 3 \\ {\rm Quiz} \ 2 \end{array}$



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Quiz 2

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Score: **97.5**

Material 10

1. What is the difference between vectors and vector spaces?

Vectors is an entity that has magnitude or length and direction. Vector space is a set of vectors that can be added and multiplied by a scalar.

2. Determine the size of the vector $\vec{PQ} = 5i + 8j + 3k$ and $\vec{RS} = 9i + 4j + 5k$

$$\vec{PQ} = 5i + 8j + 3k$$
$$|\vec{PQ}| = \sqrt{5^2 + 8^2 + 3^2}$$
$$= \sqrt{25 + 64 + 9}$$
$$= \sqrt{98}$$
$$= 7\sqrt{2}$$

$$\vec{RS} = 9i + 4j + 5k$$

 $|\vec{RS}| = \sqrt{9^2 + 4^2 + 5^2}$
 $= \sqrt{81 + 16 + 25}$
 $= \sqrt{102}$

3. Known $\vec{u} = (1, 2, 3, 5)$ and $\vec{v} = (4, 7, 6, 2)$ determine the length of each vector

$$\vec{u} = (1, 2, 3, 5)$$

 $||\vec{u}|| = \sqrt{1^2 + 2^2 + 3^2 + 5^2}$
 $= \sqrt{39}$

$$\vec{v} = (4, 7, 6, 2)$$

 $||\vec{v}|| = \sqrt{4^2 + 7^2 + 6^2 + 2^2}$
 $= \sqrt{105}$

4. Known $\vec{u} = (2, 1, 3, 1)$ and $\vec{v} = (3, 3, 1, 2)$ determine the distance between the two vectors.

$$\vec{u} = (2, 1, 3, 1)$$

$$\vec{v} = (3, 3, 1, 2)$$

$$||\vec{u} - \vec{v}|| = \sqrt{(2 - 3)^2 + (1 - 3)^2 + (3 - 1)^2 + (1 - 2)^2}$$

$$= \sqrt{1 + 4 + 4 + 1}$$

$$= \sqrt{10}$$

Material 12

5. Determine the direction cosine [l, m, n] from vector $\vec{r} = 2i - 2j + 7k$

$$r = \sqrt{2^2 - 2^2 + 7^2}$$

$$= \sqrt{4 + 4 + 49}$$

$$= \sqrt{57}$$

$$l = \frac{2}{\sqrt{57}}$$
$$m = \frac{-2}{\sqrt{57}}$$
$$n = \frac{7}{\sqrt{57}}$$

6. What is the scalar product of two vectors if a=3, b=5 and $\theta = 45$?

$$\vec{a} = 3$$

$$\vec{b} = 5$$

$$\theta = 45$$

$$\vec{a} \cdot \vec{b} = ab \cos \theta$$

$$= 3 \times 5 \times \cos 45$$

$$= 15 \times \frac{\sqrt{2}}{2}$$

$$= \frac{15\sqrt{2}}{2}$$

7. What is the vector product of $p \times q = \begin{bmatrix} i & j & k \\ 3 & 4 & 2 \\ 1 & 5 & 2 \end{bmatrix}$

$$p \times q = \begin{bmatrix} i & j & k \\ 3 & 4 & 2 \\ 1 & 5 & 2 \end{bmatrix}$$

$$= i \begin{vmatrix} 4 & 2 \\ 5 & 2 \end{vmatrix} - j \begin{vmatrix} 3 & 2 \\ 1 & 2 \end{vmatrix} + k \begin{vmatrix} 3 & 4 \\ 1 & 5 \end{vmatrix}$$

$$= i(8 - 10) - j(6 - 2) + k(15 - 4)$$

$$= -2i - 4j + 11k$$

- 8. If a = 3i + 2j + 2k and b = 2i + 1j + 4k. Determine
 - (a) a.b
 - (b) $a \times b$
 - (a)

$$a = 3i + 2j + 2k$$

$$b = 2i + 1j + 4k$$

$$a \cdot b = (3 \times 2) + (2 \times 1) + (2 \times 4)$$

$$= 6 + 2 + 8$$

$$= 16$$

(b)

$$a \times b = \begin{bmatrix} i & j & k \\ 3 & 2 & 2 \\ 2 & 1 & 4 \end{bmatrix}$$

$$= i \begin{vmatrix} 2 & 2 \\ 1 & 4 \end{vmatrix} - j \begin{vmatrix} 3 & 2 \\ 2 & 4 \end{vmatrix} + k \begin{vmatrix} 3 & 2 \\ 2 & 1 \end{vmatrix}$$

$$= i(8 - 2) - j(12 - 4) + k(3 - 4)$$

$$= 6i - 8j - k$$

Material 12

9. Determine the angle between vectors:

$$p = 3i + 2j + 2k$$
$$q = 3i - 2j + 2k$$

(a) First determine the direction cosine [l, m, n] (for p) and [l', m', n'] (for q).

$$p = 3i + 2j + 2k$$

$$||p|| = \sqrt{3^2 + 2^2 + 2^2}$$

$$= \sqrt{9 + 4 + 4}$$

$$= \sqrt{17}$$

$$l = \frac{3}{\sqrt{17}}$$

$$m = \frac{2}{\sqrt{17}}$$

$$n = \frac{2}{\sqrt{17}}$$

$$q = 3i - 2j + 2k$$

$$||q|| = \sqrt{3^2 + (-2)^2 + 2^2}$$

$$= \sqrt{9 + 4 + 4}$$

$$= \sqrt{17}$$

$$l' = \frac{3}{\sqrt{17}}$$

$$m' = \frac{-2}{\sqrt{17}}$$

$$n' = \frac{2}{\sqrt{17}}$$

(b) Then look for $\cos \theta = l \cdot l' + m \cdot m' + n \cdot n'$

$$\cos \theta = l \cdot l' + m \cdot m' + n \cdot n'$$

$$= \frac{3}{\sqrt{17}} \times \frac{3}{\sqrt{17}} + \frac{2}{\sqrt{17}} \times \frac{-2}{\sqrt{17}} + \frac{2}{\sqrt{17}} \times \frac{2}{\sqrt{17}}$$

$$= \frac{9}{17} - \frac{4}{17} + \frac{4}{17}$$

$$= \frac{9}{17}$$

10. What is vector direction ratio?

Vector direction ratio is the ratio of the direction of a vector to the direction of the x, y, and z axes.