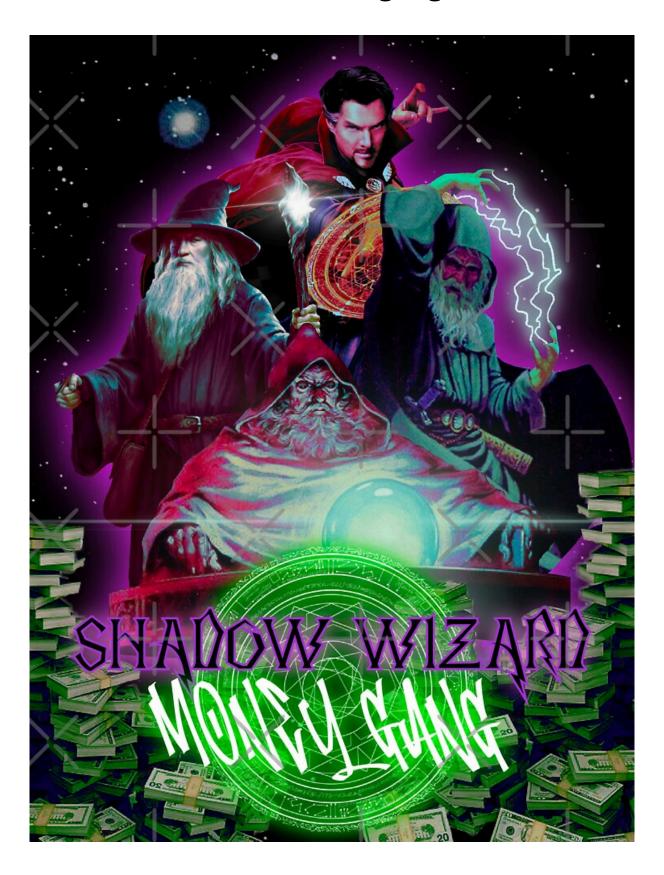
Functional Languages



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Intro

What makes a language functional? The fact that "functions are first class citizen of the language". This means that functions can be passed as arguments to other functions, returned as values from other functions, and assigned to variables or data structures.

Some basics

- Statements are single line of code of type statement
- Expressions are entities that can be evaluated and have a type

Let's describe (not completely) the C grammar in BNF notation:

```
constant ::= 0 | 1 | 2 | 3 | ...
expr ::= constant
                                       | 'a' | 'b' | ...
        (expr)
                                          1.0 | 2.45 | ...
        Χ
                                          "string..."
       expr++
        ++expr
                             block ::= statement ;
      expr--
                                    | statement ; block
        --expr
       expr = expr
                             cases ::= case constant: block
      expr + expr
      expr += expr
                                       case constant: block cases
                                    expr - expr
                             statement ::= return expr
        expr -= expr
        expr * expr
                                       | if (expr) { block }
                                        | if (expr) { block } else { block }
      expr *= expr
       expr / expr
                                          for (statement ; expr ; expr ) { block }
                                          while (expr) { block }
        expr /= expr
        expr % expr
                                           do { block } while (expr)
      | expr %= expr
                                           switch (expr) { cases }
        expr << expr
                                           break
       expr <<= expr
                                           continue
        expr >> expr
                                           goto x
        expr >>= expr
                             NOTE: this notation is called Backus-Naur Form.
        expr & expr
        expr &= expr
                             It is used to describe context-free grammars and syntax of
        expr | expr
                             languages.
        expr |= expr
        expr ^ expr
        expr ^= expr
        ~ expr
        - expr
        ! expr
        expr && expr
        expr || expr
        expr == expr
        expr < expr
        expr <= expr
        expr > expr
        expr >= expr
        & expr
        * expr
        expr ? expr : expr
        f(expr1, ..., exprN)
        expr[expr]
        expr.x
```

Reduction

Reduction is the evaluation of an expression. With this process every part of the expression is "reduced" to a smaller form until we get to a *ground value*. Let's take 1 + 2 * 4 as example:

$$\underbrace{1+2*4}_{\text{int}}$$

On the lower brackets we can see the result of the evaluation of the arithmetical operations. From the upper brackets instead we can see that the reduction preserves the types of the expression.

Declaration, assegnation, binding

In imperative languages there are some core concepts like **declaration** and **assignment** or **initialiation**. So for example in C

```
int x;  // declaration

x = 7;  // assignment

int answer = 42;  // declaration with initialiation
```

In the context of functional languages, following the syntax of mathematics, we use only the last option, declaration with initialization, and we call it *binding*.

Binding answer to 42 in F# will be let answer = 42

Syntax vs Semantics... and types

Let's take for example this code int x = &42, a declaration with inizialitation in C.

This respects the grammar of the language because it is **syntactically correct**, in fact this can be described as Type ID = expr. We can also expand that expression in expr = &expr, which is the address extraction of a variable, where the internal expr is the constant expressions 42. But speaking about **semantics** this is **wrong**!

To understand why this is incorrect we have to analyze the types of the expression. The address extraction operation transform types like that & $\tau \rightsquigarrow \tau *$, so in our example it transforms int to an int*.

Characteristics of functional languages

Functional languages:

- have only expressions
- have variable definition
- have function definition
 - Note: in the C grammar described before is missing function definition

They have to offer the minimum to be Turing-complete, so a way of looping is needed. This structure is missing in this type of languages, but covered by *recursion*.

Syntactical vs Lexical

Lexicon: collection of words. In programming language is the set of keywords and values that can be used.

So, for example, –7 is different from -expr where the expression is 7.

In expr + expr there are two expression and the operator + which is a keyword in the lexicon of the language.

Functional vs Imperative

We have to consider that "to assing" means to modify. This is why functional languages lacks of assignment operation, meaning anything that can modify data directly.

```
int x = 3; // declaration with initialiation -> a BINDING in FL x = 4; // assignment -> MISSING in FL
```

Polymorphism

When the type of an expression is not important we can use some form of **polymorphism**. For example it could be **subtyping**, such as the possibility of interchange sub and base classes in OOP. Another way to implement polymorphism is by **parametric polymorphism**, with techniques like Java Generics and C++ Templates (this is the way F# follows).

Function applications

The line in the C grammar that allow us to do function calls is $f(e_1,...,e_n)$. In functional languages we use to call this *application* of the function and usually it is called just by writing the name of the function followed by the arguments.

The "functional grammar" for the application is expr ::= expr expr.

Take for example the function (fun x -> x) 7. This is the identity function, so from something it returns the exactly same thing. In this case types $\underline{\text{are not}}$ explicit, so the compiler create some "generic" anonymous types.

(fun x -> x) 7	F# function
$f: `a \rightarrow `a$	Anonymous type generated by the compiler
$f: \mathrm{int} \to \mathrm{int}$	Types by inferred the compiler using the type of the argument

Note: in application the left part must be an arrow (a function). We can say that <u>lambdas create</u> and <u>applications remove</u> arrows.

After the application, the type is inferred by the compiler. It understands that we are passing a integer, so the function becomes "*monomorphic at time of application*" over the type int.

Binding of parameters

```
let succ x = x + 1 // Syntactic sugar for this: let succ = fun x \rightarrow x + 1
let seven = f 6 // 6 is bounded to x then the function is computed
```

That 6 in the function applications replaces every occurrency of x in the scope of the parameter.

Errors accepted by the grammar

If we look at the grammar for function application application (but not only in that) we can see that it is possible to create something that is <u>syntactically correct but that will produce an error</u>. For this we need to use the power of **types** and **type check** what we create with our grammar.

Currying

Currying is the technique of translating the evaluation of a function that takes multiple arguments into evaluating a sequence of functions, each with a single argument.

```
// curry : ('a -> 'b -> 'c) -> 'a * 'b -> 'c
let curry f (x, y) = f x y

// uncurry : ('a * 'b -> 'c) -> 'a -> 'b -> 'c
let uncurry f x y = f (x, y)
```

Let's define the addition over integers in both forms:

• Uncurried form:

```
// uncurry_add : int * int -> int
let uncurry_add = fun (x, y) -> x + y
let result = uncurry_add (7, 8)
```

It accepts only pair of integers as arguments and after the application it returns the result.

• Curried form:

```
// curry_add : int -> (int -> int)
let curry_add = fun x -> fun y -> x + y

// partial_application : int -> int
let partial_application = curry_add 7

// final_application : int
let final_application = z 1

// total_application : int -> int -> int
let total application = addition 7 1
```

With this form we can pass single integers as arguments and make "partial" applications of the function. It is automatically applied associativity on the left.

Currying is preferred in libraries. Instead pairs and more generally speaking tuples are used to express simple data types, such as point in space like (x,y,z).

Let's make another example of a curried function and analyze the types:

```
let curried_f f (x, y) = f x y
// Syntactic sugar for
// let curried_f = fun f -> fun (x, y) -> f x y
```

The curried_f function uses f that is a binary curried function. So it applies f to x and then to y, decomposing the pair (x, y) that gets as input and returns the same type of f. Its type is curried_f: (`a -> `b -> `c) -> (`a * `b) -> `c, where the first two comes blocks comes from the type of the arguments f and (x, y) and the last is the return type of the applied function f.

Instead the uncurried version uses a function f that is non curried because it takes as an input a pair and returns the same type as the input function, like before.

```
let uncurried_f f x y = f (x, y)
// We have 3 parameters, so there will be 3 arrows
// uncurried_f : (`a * `b -> `c) -> `a -> `b -> `c
// I : f I:x I:y 0
```