

DHAKA COLLEGE

DEPT. OF PHYSICS

Honours 3rd Year

Incourse - 2020

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Session : 2017 - 2018

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Ans to the Q.N. 2

Newton Raphson method:

$$f(x) = x^2 - 3x + 2$$

$$\Rightarrow f'(x) = 2x - 3$$

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

$$= \frac{2x_n^2 - 3x_n - x_n^2 + 3x_n - 2}{(2x_n - 3)}$$

$$\therefore x_{n+1} = \frac{(x_n^2 - 2)}{(2x_n - 3)}$$

$$x_0 = 0,$$

$$x_1 = 0.667$$

$$x_2 = 0.9334$$

$$x_3 = 0.996$$

$$x_4 = 0.999$$

$$x_5 = 0.999$$

Hence the required root is 0.999

Ans

Solving with C++ :

#include <bits/stdc++.h>

#define EPSILON 0.001

// The function is $x^2 - 3x + 2$

```
double func(double x)
{
    return x*x - 3*x + 2;
}
```

// Derivative of the above function, which is $2x - 3$

```
double derivfunc(double x)
{
    return 2*x - 3;
}
```

// Function to find the root

```
void newton Raphson (double x)
```

```
{
    double h = func(x) / derivFunc(x);
    while (abs(h) >= EPSILON)
    {
        h = func(x) / derivFunc(x);
    }
}
```



```

//  $x(i+1) = x(i) - f(x)/f'(x)$ 
     $x = x - h;$ 
}
count << "The value of the root is:" << x;
}

```

// Driver program to test above

```

int main()
{
    double x0 = 0; // Initial values assumed
    Newton Raphson(x0);
    return 0;
}

```

output:

The value of root is : 0.999

Ans

Ans to the Q.N. 3

▣ Simpson's ($\frac{1}{3}$) method:

Let, $y = f(x) = 2x$

Here, $a=0$, $b=1$, We shall divide the interval into six equal parts.

$$\text{Hence, } h = \frac{b-a}{n} = \frac{1}{6}$$

$$\text{Now, } x_0 = 0 \longrightarrow y_0 = 0$$

$$x_1 = x_0 + h = \frac{1}{6} \longrightarrow y_1 = \frac{1}{3}$$

$$x_2 = \frac{1}{3} \longrightarrow y_2 = \frac{2}{3}$$

$$x_3 = \frac{1}{2} \longrightarrow y_3 = 1$$

$$x_4 = \frac{2}{3} \longrightarrow y_4 = \frac{4}{3}$$

$$x_5 = \frac{5}{6} \longrightarrow y_5 = \frac{5}{3}$$

$$x_6 = b = 1 \longrightarrow y_6 = 2$$

From,

Simpson's ($\frac{1}{3}$) rule is,

$$\begin{aligned} \int_0^1 2x \, dx &= \frac{1}{3} \left[(y_0 + y_6) + 4(y_1 + y_3 + y_5) + 2(y_2 + y_4) \right] \\ &= \frac{1}{18} (2 + 12 + 4) \end{aligned}$$

$$\therefore \int_0^1 2x \, dx = 1 \quad (\text{Ans})$$

Solving with C++:

include <iostream>

include <math.h>

// Function to calculate f(x)

float func (float x)

{
return log(x);
}

// Function for approximate integral

float simpson's- (float ll, float ul, int n)

{
// calculating the value of h

float h = (ul - ll) / n;

// Array for storing value of x and f(x)

float x[10]; float f[10];

// calculating values of x and f(x)

for (int i=0; i<=n; i++)

{
x[i] = ll + i * h;

f[i] = func(x[i]);

}

// Calculating result

```
float res = 0;
for (int i = 0; i <= n; i++)
{
    if (i == 0 || i == n)
        res += f[x[i]];
    else if (i % 2 != 0)
        res += 4 * f[x[i]];
    else
        res += 2 * f[x[i]];
}
res = res * (h/3);
return res;
```

// Driver program

```
int main()
{
    float lower-limit = 0;
    float upper-limit = 1;
    int n = 6;
    cout << simpsons - (lower-limit, upper-limit, n);
    return 0;
}
```

Output: The root is 1

Ans