1 Exercise Set 1.1

My answers

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- **a.** Is there an integer n such that n has a remainder of 2 when divided by 5, and a remainder of 3 when divided by 6?
- **b.** Does there exist a number n, such that if n is divided by 5 the *remainder* is 2 and if n is divided by 6 the remainder is 3?

3. Given any two distinct real numbers, there is a real number in between them

- a. Given any two distinct real numbers a and b, there is a real number c such that c is in between a and b. (a < c > b)
- b. For any two real numbers a,b there is a real number in between, c such that c is between a and b.

4. Given any real number, there is a real number that is greater.

- **a.** Given any real number r, there is another number s such that s is greater than r.
- **b.** For any real number r, there is a real number s greater than r such that s > r.

5. The reciprocal of any positive real number is positive.

- **a.** Given any positive real number r, the reciprocal of r is positive.
- **b.** For any real number r, if r is positive, then its reciprocal is positive.
- **c.** If a real nubmer r is positive, then the reciprocal of r is positive.

6. The cube root of any negative real number is negative.

- a. Given any negative real number s, the cube root of s is negative.
- b. For any real number s, if s is negative, then the cube root of s is negative.
- c. If a real number s is negative, then s cube root is negative.

7. Rewrite the following statements less formally, without using variables. Determine, as best as you can, whether the statements are true or false. a. False, if u < v, then u + v > u - v

- b. True
- c. True, take for example $n = 1, 1^2 = 1 \ge 1$
- d. True.