

The complex number  $u$  is defined by  $u = \frac{\sqrt{2} - a\sqrt{2}i}{1 + 2i}$ , where  $a$  is a positive integer.

- (a) Express  $u$  in terms of  $a$ , in the form  $x + iy$ , where  $x$  and  $y$  are real and exact. [3]

[illegible]

It is now given that  $a = 3$ .

- (b) Express  $u$  in the form  $re^{i\theta}$ , where  $r > 0$  and  $-\pi < \theta \leq \pi$ , giving the exact values of  $r$  and  $\theta$ . [2]

[illegible]

- (c) Using your answer to part (b), find the two square roots of  $u$ . Give your answers in the form  $re^{i\theta}$ , where  $r > 0$  and  $-\pi < \theta \leq \pi$ , giving the exact values of  $r$  and  $\theta$ . [3]

[illegible]