| (a) | By sketching the graphs of  |
|-----|---|
|     | $y =  5 - 2x  \qquad \text{and} \qquad y = 3 \ln x$                                     |
|     | on the same diagram, show that the equation $ 5 - 2x  = 3 \ln x$ has exactly two roots. |
|     |   |
|     |   |
|     |   |
|     |   |
|     |   |
|     |   |
|     |   |

[3]

| <b>(b)</b> | Show that the value of the larger root satisfies the equation $x = 2.5 + 1.5 \ln x$ . [1] |
|------------|---|
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|         |   |        |   |   |   |            |                      |        |       |   |   |
| • • • • | ••••••                                  | •••••  | • | •••••                                   |   | •••••      | •••••                | •••••  | ••••• | •••••                                   | • • • • • • •                           |
|         |   |        |   |   |   |            |                      |        |       |   |   |
| ••••    | •                                       | •••••• | ••••••                                  | ••••••                                  | • | ••••••     | ••••••               | •••••• |       | •••••                                   | • • • • • • •                           |
|         |   |        |   |   |   |            |                      |        |       |   |   |
|         |   |        |   |   |   |            |                      |        |       |   |   |
| •••     |   |        |   |   |   |            |                      |        |       | •••••                                   |   |
|         |   |        |   |   |   |            |                      |        |       |   |   |
| ••••    |   | •••••  | •••••                                   | • |   | •••••      |                      | •••••  |       | •••••                                   | • • • • • • •                           |
|         |   |        |   |   |   |            |                      |        |       |   |   |
| ••••    | • | •••••  | ••••••                                  | ••••••                                  | • |            | •••••                | •••••  |       | •••••                                   | • • • • • • •                           |
|         |   |        |   |   |   |            |                      |        |       |   |   |
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| •••     |   | •••••  |   |   |   |            |                      |        | ••••• |   | • |
|         |   |        |   |   |   |            |                      |        |       |   |   |
| ••••    |   | •••••  | ••••••                                  | •••••                                   |   | •••••      |                      | •••••  | ••••• | •••••                                   | • • • • • • • •                         |
|         |   |        |   |   |   |            |                      |        |       |   |   |
| ••••    | • | •••••  | ••••••                                  | ••••••                                  | • | ••••••     | ••••••               | •••••• |       | • | • • • • • • •                           |
|         |   |        |   |   |   |            |                      |        |       |   |   |
|         | e an iterat                             |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         | e an iterat                             |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |
|         |   |        |   |   |   | ntion in p | oart ( <b>b</b> ), t |        |       | of the l                                | arge                                    |