

Question	Answer	Marks	Guidance
(a)	Using the correct process find the scalar product of direction vectors of $l$ and $\mathbf{OA}$	<b>M1</b>	$(1, 5, 6) \cdot (-1, 2, 3) = -1 + 10 + 18$
	Using the correct process for the moduli, divide the scalar product by the product of the moduli and find the inverse cosine of the result	<b>M1</b>	<i>Their</i> scalar product $\div [\sqrt{1^2 + 5^2 + 6^2} \sqrt{(-1)^2 + 2^2 + 3^2}]$ . Angle = $\cos^{-1} \frac{27}{\sqrt{62} \sqrt{14}}$ .
	Obtain answer $23.6^\circ$ .	<b>A1</b>	AWRT $23.6^\circ$ . $23.5889^\circ$ . Radians 0.412 scores A0 (0.4117...).
		<b>3</b>	
(b)	Taking a general point $P$ on $l$ , state $\mathbf{AP}$ (or $\mathbf{PA}$ ) in component form, e.g. $(3 - \lambda, -5 + 2\lambda, -5 + 3\lambda)$	<b>B1</b>	Note: $(4, 1, 0)$ or $(4, 1, 1)$ , for $4\mathbf{i} + \mathbf{k}$ is not MR, but M1 possible.
	<i>Either</i> equate scalar product of $\mathbf{AP}$ and direction vector of $l$ to zero and solve for $\lambda$ <i>or</i> use Pythagoras in a relevant triangle and solve for $\lambda$	<b>M1</b>	$(3 - \lambda, -5 + 2\lambda, -5 + 3\lambda) \cdot (-1, 2, 3) = 0$ $-3 - 10 - 15 + \lambda + 4\lambda + 9\lambda = 0$ or let $\mathbf{OQ} = (4, 0, 1)$ so $\mathbf{AQ} = (3, -5, -5)$ , $\mathbf{QP} = (-\lambda, 2\lambda, 3\lambda)$ , $\mathbf{AP} = (3 - \lambda, -5 + 2\lambda, -5 + 3\lambda)$ hence $3^2 + (-5)^2 + (-5)^2 =$ $(3 - \lambda)^2 + (-5 + 2\lambda)^2 + (-5 + 3\lambda)^2 + (-\lambda)^2 + (2\lambda)^2 + (3\lambda)^2$ Other alternative approaches are possible, e.g. minimise $AP$ or $AP^2$ , either by completing the square or by differentiating.
	Obtain $\lambda = 2$	<b>A1</b>	$\lambda = 2$
	State that the position vector $\mathbf{OP}^*$ of the foot is $2\mathbf{i} + 4\mathbf{j} + 7\mathbf{k}$	<b>A1</b>	OE Condone coordinates.
		<b>4</b>	

Question	Answer	Marks	Guidance
(c)	Set up a correct method for finding the position vector of the reflection of $A$ in $l$	<b>M1</b>	For all methods, allow a sign error in one component only: $\mathbf{OA}' = \mathbf{OP}^* + (\mathbf{OP}^* - \mathbf{OA})$ <i>their</i> $(2, 4, 7) + (\text{their } 2, 4, 7 - 1, 5, 6)$ or $\mathbf{OA}' = \mathbf{OP}^* - (\mathbf{OA} - \mathbf{OP}^*)$ <i>their</i> $(2, 4, 7) - (1, 5, 6 - \text{their } 2, 4, 7)$ or $\mathbf{OA}' = \mathbf{OA} + 2(\mathbf{OP}^* - \mathbf{OA})$ $\begin{pmatrix} 1 + 2(\text{their } 2 - 1) \\ 5 + 2(\text{their } 4 - 5) \\ 6 + 2(\text{their } 7 - 6) \end{pmatrix}$ or midpoint $\mathbf{OP}^* = (\mathbf{OA} + \mathbf{OA}')/2$ with <i>their</i> $\lambda$ value substituted. $\frac{1+x}{2} = \text{their } 2$ $\frac{5+y}{2} = \text{their } 4$ $\frac{6+z}{2} = \text{their } 7$
	Obtain answer $3\mathbf{i} + 3\mathbf{j} + 8\mathbf{k}$ or $3\left(\mathbf{i} + \mathbf{j} + \frac{8}{3}\right)$	<b>A1</b>	OE Condone coordinates $x = 3, y = 3, z = 8$ A1. No method shown and correct answer 2/2.
		<b>2</b>	