Find the complex numbers w which satisfy the equation $w^2 + 2iw^* = 1$ and are such that $\operatorname{Re} w \leqslant 0$. Give your answers in the form $x + iy$, where x and y are real. [6]