

Question	Answer	Marks	Guidance
(a)	$y = \frac{x^2 - 4}{x^2 + 4}$ leading to $(x^2 + 4)y = (x^2 - 4)$ leading to $x^2y + 4y = x^2 - 4$	<b>*M1</b>	For clearing denominator and expanding brackets. If swap variables first, look for $y^2x + 4x = y^2 - 4$ .
	$x^2y - x^2 = -4y - 4$ leading to $x^2(1 - y) = 4y + 4$ leading to $x^2 = \dots$	<b>DM1</b>	For making $x^2$ the subject. If swap variables first, look for $y^2(1 - x) = 4x + 4 \Rightarrow y^2 = \dots$
	$x^2 = \frac{4y + 4}{1 - y}$ leading to $x = \sqrt{\frac{4y + 4}{1 - y}}$ leading to $[f^{-1}(x)] = \sqrt{\frac{4x + 4}{1 - x}}$	<b>A1</b>	OE e.g. $\sqrt{\frac{-4x - 4}{x - 1}}$ without $\pm$ in final answer.
	<b>Alternative method for Q6(a)</b>		
	$x = \frac{y^2 - 4}{y^2 + 4}$ leading to $x = 1 - \frac{8}{y^2 + 4}$ leading to $x - 1 = \frac{-8}{y^2 + 4}$	<b>*M1</b>	For division and reaching $x - 1 = \dots$ (or $y - 1 = \dots$ )
	$y^2 + 4 = \frac{-8}{x - 1}$ leading to $y^2 = \frac{-8}{x - 1} - 4$	<b>DM1</b>	For making $y^2$ (or $x^2$ ) the subject.
	$[y =][f^{-1}(x)] = \sqrt{\frac{-8}{x - 1} - 4}$	<b>A1</b>	OE without $\pm$ in final answer.
		<b>3</b>	

Question	Answer	Marks	Guidance
(b)	$1 - \frac{8}{x^2 + 4} = \frac{x^2 + 4}{x^2 + 4} - \frac{8}{x^2 + 4} \left[ = \frac{x^2 + 4 - 8}{x^2 + 4} \right] = \frac{x^2 - 4}{x^2 + 4}$	<b>M1 A1</b>	Using common denominator or division to reach 1. Remainder -8. WWW
	$0 < f(x) < 1$	<b>B1 B1</b>	B1 for each correct inequality. B0 if contradictory statement seen. Accept $f(x) > 0$ , $f(x) < 1$ ; $1 > f(x) > 0$ ; $(0, 1)$ <b>SC B1</b> for $0 \leq f(x) \leq 1$ .
		<b>4</b>	
(c)	Because the range of f does not include the whole of the domain of f (or any of it)	<b>B1</b>	Accept an answer that includes an example outside the domain of f, e.g. $f(4) = \frac{12}{20}$ . Must refer to the domain or $> 2$ . Need not explicitly use the term 'domain' but must not refer just to the range.
		<b>1</b>	

