Epoch, Iteration, and Batch size



1 epoch is to pass an entire dataset through the neural network once.



Iteration is the number of minibatch.



Batch size is the total number of training samples present in a single min-batch.



Gradient Descent

- Gradient descent is an optimization algorithm used to minimize some functions by moving in a certain direction.
- Gradient descent in machine/deep learning is used to update the parameters of models. (weights in neural networks)
- Gradient descent is very useful for supervised learning.



Yann LeCun

@ylecun

I've been trying to convince many of my more theoryoriented colleagues of the unbelievable power of gradient descent for close to 4 decades. 1/2

M Chris Olah @ch402 · Jun 4

The elegance of ML is the elegance of biology, not the elegance of math or physics.

Simple gradient descent creates mind-boggling structure and behavior, just as evolution creates the awe inspiring complexity of nature. twitter.com/banburismus_/s...

Show this thread

9:11 AM · Jun 5, 2022 · Twitter for Android

x	у
2	4
3	6
4	8
5	10
6	12

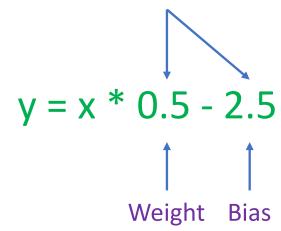
$$y = x * 2$$

x	У
2	6
3	9
4	12
5	15
6	18

$$y = x * 3$$

x	у
2	-1.5
3	-1
4	-0.5
5	0
6	0.5

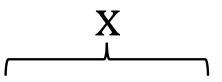
Gradient Descent helps you find these parameters.



x	у
2	8
3	11
4	14
5	17
6	20

$$y = x * 3 + 2$$

Binary Classification



У

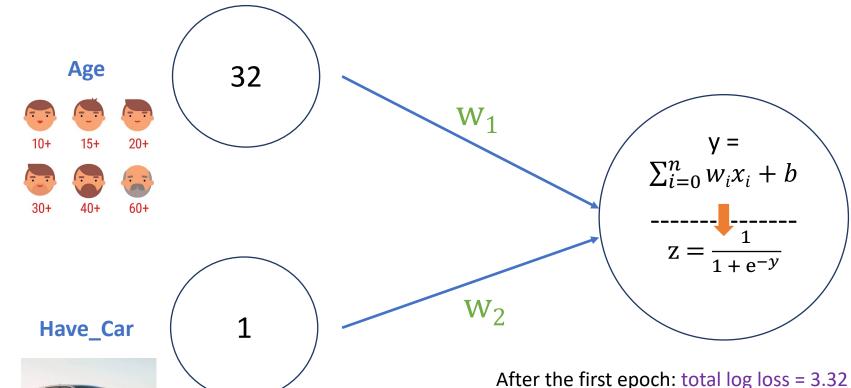
Age	Have_Car	Have_Insurance
21	0	0
48	1	1
28	0	0
19	0	0
56	1	1
65	1	1
32	1	0
24	0	1
43	1	0
22	0	0
53	1	1

$$y = f(x)$$

Binary Cross Entropy (Log Loss) =

$$-\frac{1}{n}\sum_{i=0}^{n} y_i * \log(\hat{y}_i) + (1 - y_i) * \log(1 - (\hat{y}_i))$$

Have_Car	Have_Insurance
0	0
1	1
0	0
0	0
1	1
1	1
1	0
0	1
1	0
0	0
1	1
	0 1 0 0 1 1 1 0



 $y = w_1 * X_1 + w_2 * X_2 + bias$

$$w_1 = w_1 - learning rate * \partial / \partial w_1$$

$$w_2 = w_2 - learning rate * \partial / \partial w_2$$

$$w_3 = w_3 - learning rate * \partial / \partial w_3$$

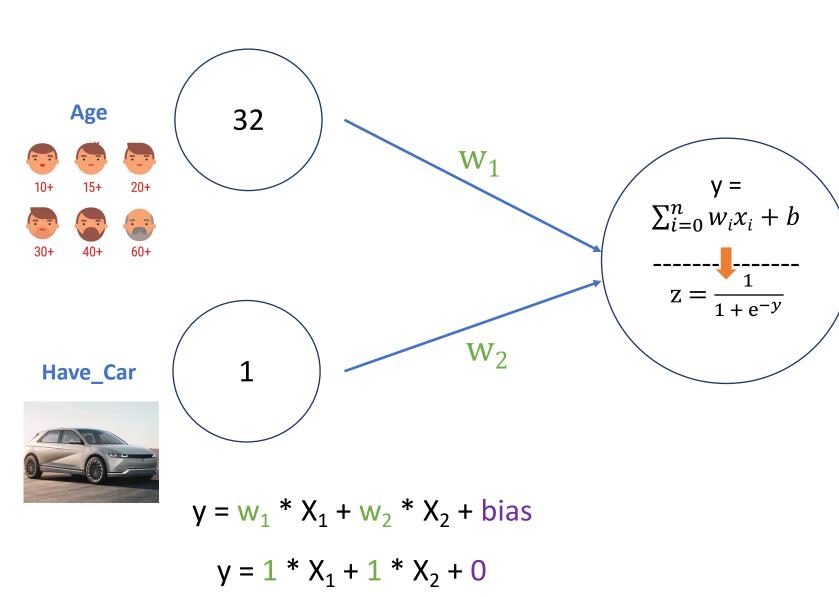
$$b = b - learning rate * \partial / \partial b$$

$$w_1 = w_1 - learning rate * \partial / \partial w_1$$

$$\partial/\partial \mathbf{w}_1 = \frac{1}{n} \sum_{i=1}^n x_i (\hat{y}_i - yi)$$

$$b = b - learning rate * \partial / \partial b$$

$$\partial/\partial \mathbf{b} = \frac{1}{n} \sum_{i=1}^{n} (\hat{y}_i - yi)$$



$$w_1 = w_1 - learning rate * \partial / \partial w_1$$

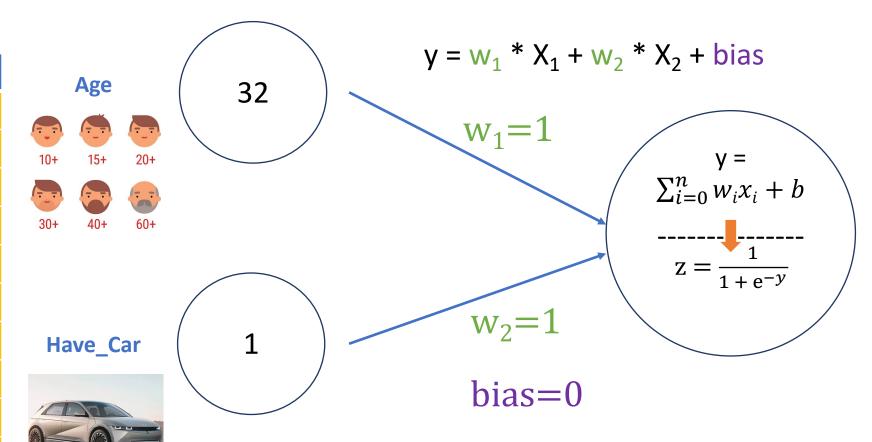
 $w_1 = 1 - 0.2 = 0.8$
 $w_2 = w_2 - learning rate * \partial / \partial w_2$
 $w_2 = 0.9 - 0.15 = 0.75$

 $b = b - learning rate * \partial / \partial b$

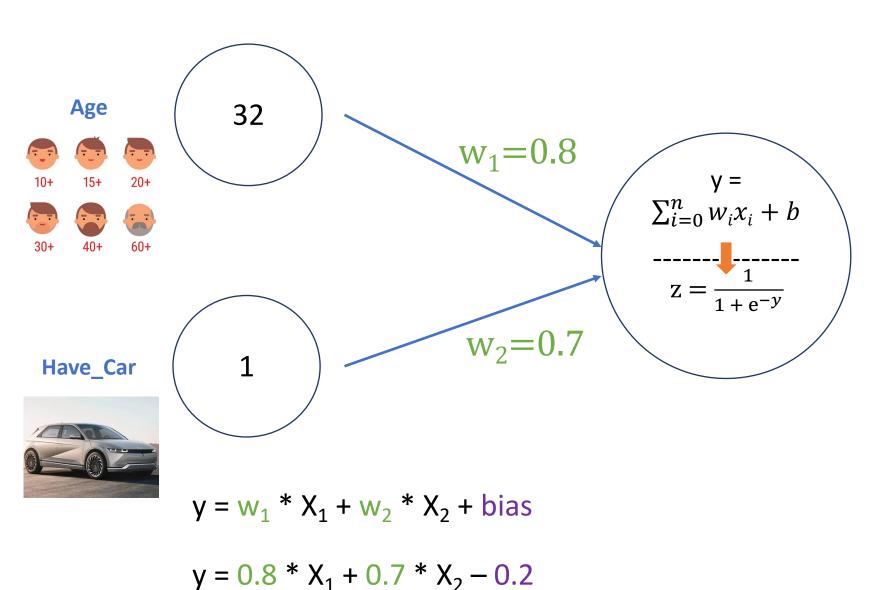
b = 0 - 0.2 = -0.2

$$MAE = \frac{1}{n} \sum_{i=0}^{n} abs(y_i - \hat{y}_i)$$

Age	Have_Car	Have_Insurance
21	0	0
48	1	1
28	0	0
19	0	0
56	1	1
65	1	1
32	1	0
24	0	1
43	1	0
22	0	0
53	1	1



Total Error = $error_1 + error_2 + error_3 + ...$



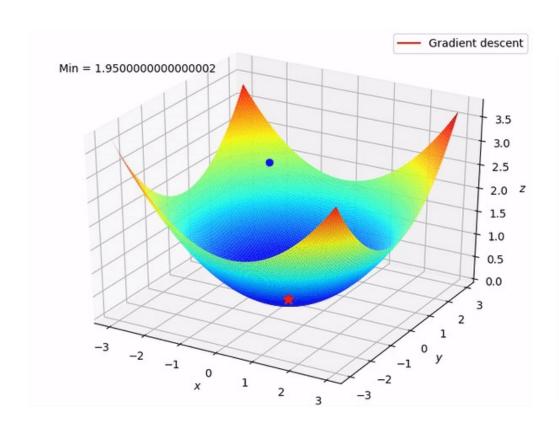
$$w_1 = w_1 - \text{learning rate } * \partial / \partial w_1$$

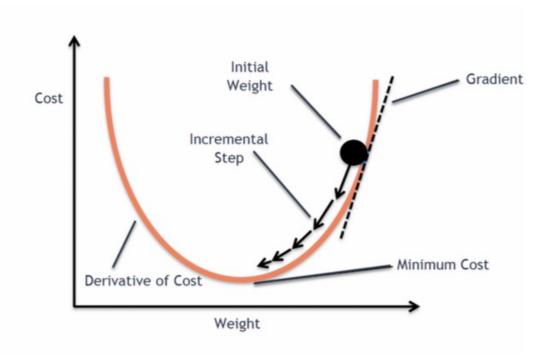
 $w_1 = 0.8 - 0.1 = 0.7$
 $w_2 = w_2 - \text{learning rate } * \partial / \partial w_2$
 $w_2 = 0.7 - 0.15 = 0.55$

 $b = b - learning rate * \partial / \partial b$

b = -0.2 - 0.1 = -0.3

Gradient Descent





Gradient Descent

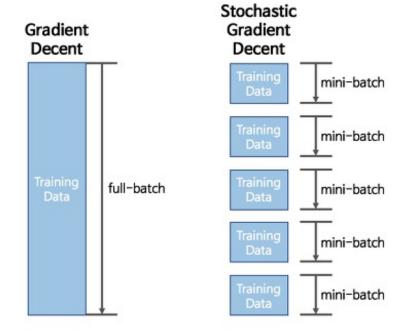


Batch Gradient Descent updates parameters for the entire training dataset.

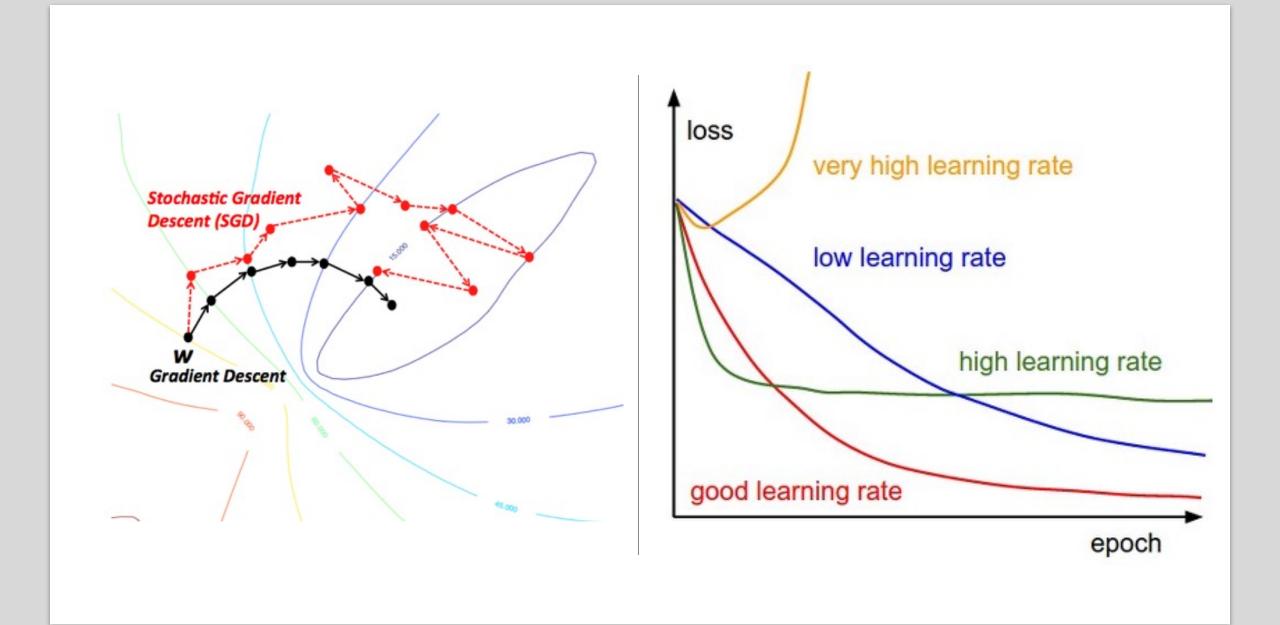


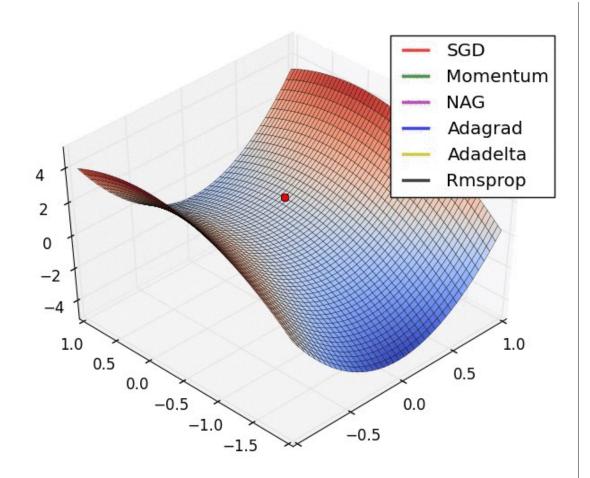
Stochastic Gradient Descent

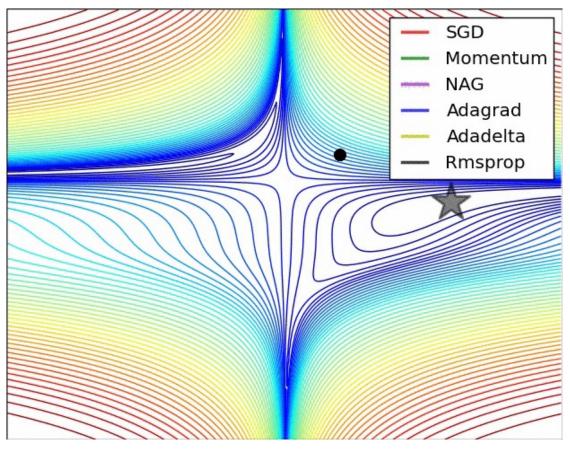
updates parameters for each training example and label.



Mini-batch Gradient Descent is a mixture of Batch Gradient Descent and Stochastic Gradient Descent.







Batch Gradient Descent (BGD)

```
for i in range(m):
    gradient=evaluate_gradient(training_data)
    weight=weight-learning_rate * gradient
```

Stochastic Gradient Descent (SGD)

```
for i in range(m):
    np.random.shuffle(training_data)
    for one_data in training_data:
        gradient=evaluate_gradient(one_data)
        weight=weight-learning_rate * gradient
```

Mini-batch Gradient Descent

```
for i in range(m):
    np.random.shuffle(training_data)
    for one_batch in get_mini_batches(training_data,one_batch_size=32):
        gradient=evaluate_gradient(one_batch)
        weight=weight-learning_rate * gradient
```

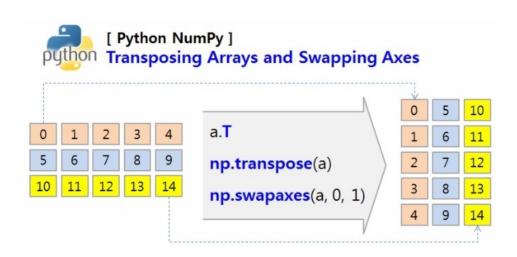
PyTorch: Optimizer

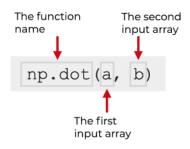
- optimizer = optim.SGD(model.parameters(), Ir=0.01, momentum=0.9)
- optimizer = optim.Adam([var1, var2], lr=0.0001) (https://pytorch.org/docs/stable/optim.html)

TensorFlow-Keras: Optimizer

- tf.keras.optimizers.SGD
- tf.keras.optimizers.Adam
- https://pytorch.org/docs/stable/optim.html#module-torch.optim

NumPy: transpose() / dot()





numpy.dot(3, 4)



 3×4