

Tabla de parametros.

Link	a_i	α_i	d_i	θ_i
0	0	0	0	θ_1
1	L_1	0	L_1	θ_2
2	L_2	90°	0	θ_3

Joint No	Type	Joint offset	Joint angle	Link length
1	revolute	0	θ_1	0
2	revolute	L_1	θ_2	L_1
3	revolute	0	θ_3	L_2

Joint No	Twist angle α	initial Value (3v) system	Final value	Param master simulation
1	0	0		
2	0	0		
3	90°	0		

$$A_0 = \begin{bmatrix} C(\theta_1) & -C(0)S(\theta_1) & S(0)S(\theta_1) & 0C(\theta_1) \\ S(\theta_1) & C(0)C(\theta_1) & -S(0)C(\theta_1) & 0S(\theta_1) \\ 0 & S(0) & \cos(0) & d_1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_0 = \begin{bmatrix} C(\theta_1) & -S(\theta_1) & 0 & 0 \\ S(\theta_1) & C(\theta_1) & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_1 = \begin{bmatrix} C(\theta_2) & -S(\theta_2) & 0 & L_1 \cos(\theta_2) \\ S(\theta_2) & C(\theta_2) & 0 & L_1 \sin(\theta_2) \\ 0 & 0 & 1 & L_1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_2 = \begin{bmatrix} C(\theta_3) & -C(90^\circ) S(\theta_3) & S(90^\circ) S(\theta_3) & L_2 C\theta_3 \\ S(\theta_3) & C(90^\circ) C(\theta_3) & -S(90^\circ) C(\theta_3) & L_2 S\theta_3 \\ 0 & S(90^\circ) & C(90^\circ) & L_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_2 = \begin{bmatrix} C(\theta_3) & 0 & S(\theta_3) & L_2 C(\theta_3) \\ S(\theta_3) & 0 & -C(\theta_3) & L_2 S(\theta_3) \\ 0 & 1 & 0 & L_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$H_2^0 = A_0 * A_1 * A_2$$

$$C_{11} = C(\theta_1) C(\theta_2) - S(\theta_1) S(\theta_2)$$

$$A_0 * A_1 = C_{12} = C(\theta_1) (-S(\theta_2)) - S(\theta_1) C(\theta_2)$$

$$= -C$$

$$C_{13} = 0$$

$$C_{14} = C(\theta_1)(L_1 C(\theta_2)) - S(\theta_1)(L_1 S(\theta_2))$$

$$C_{21} = S(\theta_1) C(\theta_2) + C(\theta_1) S(\theta_2)$$

$$C_{22} = -S(\theta_2) S(\theta_1) + C(\theta_1) C(\theta_2)$$

$$C_{23} = 0$$

$$C_{24} = S(\theta_1)(L_1 \cos(\theta_2)) + C(\theta_1)(L_1 \sin(\theta_2))$$

$$C_{31} = 0 \quad ; \quad C_{32} = 0 \quad ; \quad C_{33} = 1 \quad ; \quad C_{34} = L_1$$

$$C_{41} = 0 \quad ; \quad C_{42} = 0 \quad ; \quad C_{43} = 0 \quad ; \quad C_{44} = 1$$

$$A_0 \cdot A_1 = \begin{bmatrix} C(\theta_1)C(\theta_2) - S(\theta_1)S(\theta_2) & -S(\theta_2)C(\theta_1) - S(\theta_1)C(\theta_2) \\ S(\theta_1)C(\theta_2) + C(\theta_1)S(\theta_2) & -S(\theta_2)S(\theta_1) + C(\theta_1)C(\theta_2) \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{bmatrix} \cdot \begin{bmatrix} C(\theta_1)(L_1 C(\theta_2)) - S(\theta_1)(L_1 S(\theta_2)) \\ S(\theta_1)(L_1 C(\theta_2)) + C(\theta_1)(L_1 S(\theta_2)) \\ L_1 \\ 1 \end{bmatrix}$$

$$(A_0 \cdot A_1) \cdot A_2 = \begin{bmatrix} C_{11} = [C(\theta_3)[C(\theta_1)C(\theta_2) - S(\theta_1)S(\theta_2)]] \\ C_{12} = [C(\theta_3)[-S(\theta_2)C(\theta_1) - S(\theta_1)C(\theta_2)]] \\ C_{13} = S(\theta_3) \end{bmatrix}$$

$$C_{14} = [C(\theta_3)[C(\theta_1)(L_1 C(\theta_2)) - S(\theta_1)(L_1 S(\theta_2))] + [S(\theta_3) L_1] + [L_2 C(\theta_3)]$$

simplificación

$$C_{11} = C_{\theta_1} C_{\theta_2} (C_{\theta_3} - C_{\theta_3} S_{\theta_1} S_{\theta_2}) \\ C_{\theta_3} (C_{\theta_2} C_{\theta_1} - S_{\theta_1} S_{\theta_2})$$

$$C_{14} = C_{\theta_3} C_{\theta_1} L_1 C_{\theta_2} - C_{\theta_3} S_{\theta_1} L_1 S_{\theta_2} + \\ S_{\theta_3} L_1 + L_2 C_{\theta_3}$$

$$C_{\theta_3} L_1 (C_{\theta_1} C_{\theta_2} - S_{\theta_1} S_{\theta_2}) + S_{\theta_3} L_1 + L_2 C_{\theta_3}$$

$$C_{21} = S_{\theta_3} (S_{\theta_1} C_{\theta_2} + C_{\theta_1} S_{\theta_2})$$

$$C_{22} = -S_{\theta_3} (S_{\theta_2} C_{\theta_1} + S_{\theta_1} C_{\theta_2})$$

$$C_{23} = -C_{\theta_3}$$

$$C_{24} = L_1 S_{\theta_3} (C_{\theta_1} C_{\theta_2} - S_{\theta_1} S_{\theta_2}) - C_{\theta_3} L_1 \\ + L_2 S_{\theta_3}$$

$$C_{31} = S_{\theta_1} C_{\theta_2} + C_{\theta_1} S_{\theta_2}$$

$$C_{32} = C_{\theta_1} C_{\theta_2} - S_{\theta_2} S_{\theta_1}$$

$$C_{33} = 0; C_{34} = L_1 (S_{\theta_1} C_{\theta_2} + C_{\theta_1} S_{\theta_2}) + L_2$$

$$C_{41} = 0; C_{42} = 0; C_{43} = 0; C_{44} = 1;$$

$$\begin{bmatrix}
 \cos(\theta_2 \cos \theta_1 - \sin \theta_1 \sin \theta_2) & -\cos(\sin \theta_2 \cos \theta_1 + \sin \theta_1 \cos \theta_2) & \sin \theta_3 \\
 \sin(\sin \theta_1 \cos \theta_2 + \cos \theta_1 \sin \theta_2) & -\sin(\sin \theta_2 \cos \theta_1 + \sin \theta_1 \cos \theta_2) & -\cos \theta_3 \\
 \sin \cos \theta_2 + \cos \theta_1 \sin \theta_2 & \cos \cos \theta_2 - \sin \theta_2 \sin \theta_1 & 0
 \end{bmatrix}$$

$A_0^* =$
 $A_1^* =$
 A_2

$$\begin{bmatrix}
 \cos L_1 (\cos \theta_2 - \sin \theta_1 \sin \theta_2) + \sin \theta_3 L_1 + L_2 \cos \theta_3 \\
 L_1 \sin(\cos \theta_1 \cos \theta_2 - \sin \theta_1 \sin \theta_2) - \cos \theta_3 L_1 + L_2 \sin \theta_3 \\
 L_1 (\sin \cos \theta_2 + \cos \sin \theta_2) + L_2
 \end{bmatrix}$$

1

C. link 1 = 630 mm ; link 2 = 374 mm
 Rotación 45° en cada joint

$$H_2^0 \begin{bmatrix} 0 & -\frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \left(630 \left(\frac{\sqrt{2}}{2} \right) \right) \\ 0 & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{2} & \frac{\sqrt{2}}{2} \left(630 \left(\frac{\sqrt{2}}{2} \right) \right) \\ 1 & 0 & 0 & 187 + 187 + 445.48 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$H_2^0 \begin{bmatrix} 0 & -\frac{\sqrt{2}}{4} & \frac{\sqrt{2}}{2} & 315 \\ 0 & -\frac{\sqrt{2}}{4} & -\frac{\sqrt{2}}{2} & 315 \\ 1 & 0 & 0 & 819.48 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$H_2^0 \begin{bmatrix} 0 & -0.35 & 0.70 & 315 \\ 0 & -0.35 & -0.70 & 315 \\ 1 & 0 & 0 & 819.48 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$