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#### Short Communication

# Surface-tethered polymers in polymeric matrices

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Abstract. — Recently Budkowski et al. used nuclear reaction analysis to study polymer brushes consisting of end-tethered deuterated polystyrene tails within a polystyrene homopolymer matrix. They measured the concentration-depth profile as a function of the surface coverage  $\sigma$  of tails and the degree of polymerisation of the matrix. For the matrix with the largest degree of polymerisation, the variation of the effective brush thickness L with  $\sigma$  can be fitted by the apparent power law  $L \propto \sigma^q$  with  $q = 0.54 \pm 0.06$ . This scaling law is not expected theoretically for surface-tethered polymers exposed to a polymeric matrix consisting of chemically identical chains ( $\chi = 0$ , where  $\chi$  is the interaction parameter). In the present note we would like to propose an explanation based on the fact that mixtures of deuterated and protonated polystyrene chains are characterized by a small (but non-zero) value of  $\chi$ .

#### 1. Introduction.

Polymer chains tethered by one end to a flat solid surface at high enough coverage stretch away from the surface forming a polymer "brush". Being a central model in many important problems in polymer science, polymer brushes have been the subject of numerous theoretical and experimental studies [1] in the last 15 years. The pioneering work of Alexander and de Gennes [2, 3], based on scaling arguments, was followed more recently by computer simulations [4, 5] and self-consistent field calculations [6-9]. Most of the existing experimental studies focus on polymer brushes exposed to a low molecular weight solvent and much less is known of the behavior of surface-tethered polymers in polymeric matrices. Very recently, Budkowski et al. [10] studied, using nuclear reaction analysis, polymer brushes consisting of end-tethered deuterated polystyrene tails (N monomers per tail) in a polystyrene homopolymer matrix. They measured the concentration-depth profiles as a function of the surface coverage  $\sigma$  of tails and the degree of polymerization P of the polymer matrix. For the most part, the experimental result for the variation of the brush thickness L with  $\sigma$  and P are consistent with scaling and

mean-field models. The variation of L with  $\sigma$  for the highest P matrix used in the experiment is however very intriguing: for  $\sigma > 4 \times 10^{-3}$ , the data can be fitted by the apparent power law

$$L \propto \sigma^q \qquad q = 0.54 \pm 0.06 \tag{1}$$

This scaling law is not expected theoretically for surface-tethered polymers exposed to a polymeric matrix consisting of chemically identical chains ( $\chi=0$ , where  $\chi$  is the interaction parameter). In order to solve this apparent contradiction, the authors, who implicitly assumed a zero interaction parameter, suggested that the power law (1) may indicate a cross over region between the predicted regimes  $L \propto \sigma^0$  and  $L \propto \sigma^1$  (see Sect. 2) in the present letter we would like to propose another possible explanation based on the fact that mixtures of deuterated and protonated polystyrene chains are characterized by a small (but non zero) value of  $\chi$ , as shown by Bates and co-workers [11]. The paper is organized as follows: we first recall the brush conformation in the case of a chemically indentical polymer matrix (Sect. 2). We then consider the effect of a small chemical mismatch (Sect. 3). The paper ends with a short discussion.

Throughout this paper we adopt the Alexander-de Gennes scaling picture [2, 3]; in particular, we assume a steplike concentration profile and impose that all free ends be at the same distance from the surface.

# 2. The chemically identical case $(\chi = 0)$ .

Consider a brush made of chains, with degree of polymerization N, terminally grafted onto a flat surface and exposed to a solvent made of chemically identical chains, with degree of polymerization P [3]. The number of terminally grafted chains per unit area is  $\sigma a^{-2}$ , where a is the monomer size. The average distance between two grafting sites is given by  $D = a\sigma^{-1/2}$ .

At sufficiently low  $\sigma$ , the grafted polymers do not overlap (the so-called mushroom regime [3]). The brush thickness L is given by  $L \cong aN^{1/2}$  for  $P > N^{1/2}$  and  $L \cong aN^{3/5}P^{-1/5}$  for  $P < N^{1/2}$  (see regions (1) and (2) in Fig.1).

As  $\sigma$  increases, the different chains begin to overlap for  $D \cong L$ . This defines an overlap concentration:  $\sigma_{\rm OV} \cong N^{-1}$  for  $P > N^{1/2}$  and  $\sigma_{\rm OV} \cong P^{2/5}N^{-6/5}$  for  $P < N^{1/2}$  In a Flory type approach, the free energy per chain is then given by:

$$\frac{F}{kT} \cong \frac{L^2}{a^2 N} + \frac{a^3}{P} \frac{N^2}{LD^2} + \frac{a^6}{P} \frac{N^3}{(LD^2)^2}$$
 (2)

The second term in equation (2) corresponds to two-body interactions while the third term corresponds to three-body interactions (we omit higher order interactions). These two terms correspond to an osmotic contribution. The origin of the screening factors  $P^{-1}$  in equation (2) is explained in appendix 2. The first term in equation (2) represents the elastic contribution.

From equation (2) one can easily construct the  $(P, \sigma)$  diagram represented in figure 1 (for more details see [15]):

- in region (3), two body interactions dominate the osmotic contribution and the brush thickness is given by:  $L \cong aNP^{-1/3}\sigma^{1/3}$
- in region (4), repulsive interactions are not sufficient to swell the brush and the structure remains Gaussian:  $L \cong aN^{1/2}$

At higher  $\sigma$ , we reach region (6) where the P chains are almost completely expelled from the brush: the brush is "dry". In this region the volume fraction of the grafted polymer is of order unity and  $L \cong aN\sigma$ .

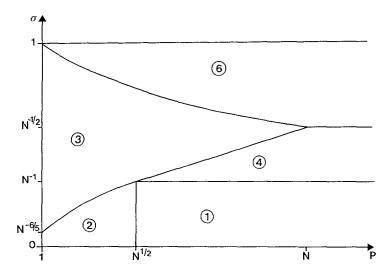


Fig. 1. — Schematic  $(P, \sigma)$  diagram for a brush exposed to a chemically identical  $(\chi = 0)$  high molecular weight solvent. The thickness of the brush in the different regions is given by: (1):  $L \cong aN^{1/2}$ ; (2):  $L \cong aN^{3/5}P^{-1/5}$ ; (3):  $L \cong aNP^{-1/3}\sigma^{1/3}$ ; (4):  $L \cong aN^{1/2}$ ; (6):  $L \cong aN\sigma$ . The cross over between the different regions are given in the appendix 2.

# 3. Influence of a small chemical difference $(\chi > 0)$ .

We now consider the less familiar case of small chemical mismatch between the grafted polymer and the polymer matrix. This case was first considered by Zhulina and Borisov [16]. The chemical mismatch is expressed in terms of a non-zero interaction parameter  $\chi$ , which generates a new term in the Flory free energy:

$$\frac{F}{kT} \cong \frac{L^2}{a^2N} + \frac{a^3}{P}(1 - 2P\chi)\frac{N^2}{LD^2} + \frac{a^6}{P}\frac{N^3}{(LD^2)^2}$$
(3)

We assume both the interaction parameter  $\chi$  and the second virial coefficient  $(1-2P\chi)/P$  to be positive.

The overall shape of the  $(P, \sigma)$  diagram is not drastically affected by this change as long as the three-body interactions are negligeable. Indeed, at low  $\sigma$ , we can build the  $(P, \sigma)$  diagram figure 2 by simply considering the substitution  $P \leftrightarrow P/(1-2P\chi)$ .

However, if we increase  $\sigma$ , we reach a region (5') where three-body interactions become the dominant term in the osmotic contribution and the previous substitution ceases to be valid. In this region the free energy is given by:

$$\frac{F}{kT} \cong \frac{L^2}{a^2 N} + \frac{a^6}{P} \frac{N^3}{(LD^2)^2} \tag{4}$$

Minimizing equation (4) leads to:

$$L \cong aNP^{-1/4}\sigma^{1/2} \tag{5}$$

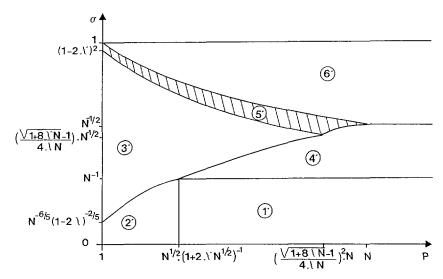


Fig. 2. — Schematic  $(P, \sigma)$  diagram for a brush exposed to a high molecular weight solvent in the case of a small chemical mismatch. The thickness of the brush in the different regions is given by: (1'):  $L \cong aN^{1/2}$ ; (2'):  $L \cong aN^{3/5}P^{-1/5}(1-2P\chi)^{1/5}$ ; (3'):  $L \cong aNP^{-1/3}\sigma^{1/3}(1-2P\chi)^{1/3}$ ; (4'):  $L \cong aN^{1/2}$ ; (5'):  $L \cong aNP^{1/4}\sigma^{1/2}$ ; (6'):  $L \cong aN\sigma$ . The cross over between the different regions are given in the appendix 2.

The lower limit of the region (5') arises when two-body and three-body interactions are comparable:

$$\sigma_{\rm CO} \cong \frac{(1 - 2P\chi)^2}{P^{1/2}} \tag{6}$$

(where the subscript CO stands for cross over). The upper limit of this region is obtained by considering  $\phi$ , the volume fraction of grafted chains. From equation (5) we obtain  $\phi \cong P^{1/4}\sigma^{1/2}$ , and when  $\phi = 1$  we reach the dry brush region:

$$\sigma_{\rm CO} \cong \frac{1}{P^{1/2}} \tag{7}$$

If we increase P, we reach region (4') where repulsive interactions do not affect the conformation of the brush. In region (5') the perturbation parameter is  $\xi \equiv a^6 N^3 / P \left(R_0^2 D^2\right)^2$  Setting  $\xi \cong 1$  gives us the thrird limit of region (5'):

$$\sigma_{\rm CO} \cong \frac{P^{1/2}}{N} \tag{8}$$

Since  $\chi \neq 0$ , the cross over equations (6) and (7) are different and define a new region (5'). A small chemical difference can thus drastically affect the  $(P, \sigma)$  diagram by generating a new region (region (5')). In this region, some P chains are still present in the brush and the osmotic contribution is dominated by three-body interactions; this leads to  $L \propto \sigma^{1/2}$  Note that this region vanishes for P > N.

# 4. Concluding remarks.

As shown in section 3, a small chemical mismatch is able to bring about a new region in the  $(P, \sigma)$  diagram where the brush thickness scales as  $\sigma^{1/2}$ . This might provide an explanation for the apparent power law equation (1) observed by Budkowski et al. [10]. Moreover, the experimental results indicate that some P chains are still present in the brush, in agreement with our predictions. From the study of Bates and coworkers we know that the experimental interaction parameter  $\chi$  for a binary mixture of fully deuterated and protonated polystyrenes behaves as  $\chi = (0.20 \pm 0.01)T^{-1} - (2.9 \pm 0.4) \times 10^{-4}$  where T is the temperature [11, 17]. In the experimental conditions of Budkowski et al. we expect  $\chi \cong 1.1 \times 10^{-4}$ ; this value enables us to check that the experiment of the reference [10] take place within the correct range of  $\sigma$  values. We are aware of the fact that in the experiment of Budkowski et al. the length of the chains in the matrix is greater than the length of the tails  $(P \cong 3N)$  and, strictly speaking, we should not expect  $L \propto \sigma^{1/2}$ . Nevertheless, we think that our explanation remains plausible since, in our Flory type approach, all numerical factors are undetermined while they could well be relevant in the interpretation of the experiment.

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# Appendix 1

Consider an isolated linear chain, with degree of polymerization N, dissolved in a melt of shorter chains (degree of polymerization P < N). The monomer-monomer interactions of the N-chain are screened out by the P-chains. As a consequence, the bare excluded-volume parameter  $v_0 = a^3(1-2\chi)$  is replaced by the effective parameter  $v = a^3(P^{-1}-2\chi)$ . This result was first stated by Flory [12], but its physical interpretation in terms of screening is due to Edwards [13]. It can be simply deduced from the Flory-Huggins free energy of polymer mixtures [14]:

$$\frac{F_{\text{site}}}{kT} = \frac{\varphi_N}{N} \text{Ln} \varphi_N + \frac{1 - f_N}{P} \text{Ln} (1 - \varphi_N) + \chi \varphi_N (1 - \varphi_N)$$
 (9)

where  $\varphi_N$  is the volume fraction of the N monomers. In the limit of small  $\varphi_N$ , equation (9) leads to

$$\frac{F_{\text{site}}}{kT} = \frac{\varphi_N}{N} \text{Ln} \varphi_N + \frac{1}{2} \left( \frac{1}{P} - 2\chi \right) \varphi_N^2 + \frac{1}{6P} \varphi_N^3 + . \tag{10}$$

Equation (10) shows that second virial coefficient (i.e. the excluded-volume parameter) is indeed given by  $a^3 (P^{-1} - 2\chi)$ . It also indicates that the third virial coefficient is equal to  $a^6/P$ . Hence equations (2) and (3) for  $\chi = 0$  and  $\chi \neq 0$  respectively.

#### Appendix 2

We give here the cross over between the differents regions of the  $(P, \sigma)$  diagram: Diagram of figure 1: (1)/(2):  $P_{\text{CO}} \equiv N^{1/2}$ ; (2)/(3):  $P^{2/5}N^{-6/5}$ ; (1)/(4):  $\sigma_{\text{CO}} \equiv N^{-1}$ ; (3)/(4):  $\sigma_{\text{CO}} \equiv P^{N^{-3/2}}$ ; (3)/(6):  $\sigma_{\text{CO}} \equiv P^{-1/2}$ ; (4)/(6):  $\sigma_{\text{CO}} \equiv N^{-1/2}$ ;

Diagram of figure 2: (1')/(2')  $P_{\text{CO}} \equiv N^{1/2} \left(1 + 2N^{1/2}\chi\right)^{-1}$ ; (2')/(3')  $\sigma_{\text{CO}} \equiv P^{2/5}N^{-6/5}(1 - 2P\chi)^{-2/5}$ ; (1')/(4')  $\sigma_{\text{CO}} \equiv N^{-1}$ ; (3')/(4')  $\sigma_{\text{CO}} \equiv PN^{-3/2}(1 - 2P\chi)^{-1}$ ; (3')/(5')  $\sigma_{\text{CO}} \equiv (1 - 2P\chi)^2P^{-1/2}$ ; (4')/(5')  $\sigma_{\text{CO}} \equiv P^{1/2}N^{-1}$ ; (4')/(6')  $\sigma_{\text{CO}} \equiv N^{-1/2}$ ; (5')/(6')  $\sigma_{\text{CO}} \equiv P^{-1/2}$ 

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