

Assignment 2

Due to: 30.11.2023 23:59

In floating point addition/subtraction, due to the shift operations to align the mantissas, some errors may occur. Write a C program to show that, in floating-point arithmetic, the result of $(A+B)-B$ may not always be equal to A . That is, after the following operations, D may not be equal to A .

$$\begin{aligned} C &\leftarrow A+B \\ D &\leftarrow C-B \end{aligned}$$

1. First, select two numbers for A and B such that when you run your code, the result can be calculated without an error (that is D is equal to A).

2. Then, select different numbers for A and B and show that D is not equal to A .

In both cases, print A , B , C and D .

In selecting the numbers A and B , make sure that the numbers can be represented in the binary accurately.

For example:

$(0.6875)_{10}$ can be accurately represented in 32-bit floating format since

$$1 * 2^{-1} + 1 * 2^{-3} + 1 * 2^{-4} = 0.5 + 0.125 + 0.0625 = 0.6875 = 0.1011$$

Hence, its 32-bit floating point representation would be 0 01111110 011000000000000000000000

However, $(1.36)_{10}$ cannot be accurately represented in 32-bit floating format, since the fractional part $0.36 = 0.01011100001010001111\dots$ repeats itself. Hence, its 32-bit floating point representation would be 0 01111101 01110 00010100 011110101

Therefore, you must select numbers A and B such that their fractional parts can be accurately represented in 32-bit floating format, as in number $(0.6875)_{10}$.

Some helpful links:

- Online Binary-Decimal Converter <http://www.binaryconvert.com/>
- Floating Point Number Representation in C https://www.cprogramming.com/tutorial/floating_point/understanding_floating_point_representation.html

The following code may help you to find the desired numbers:

```
#include <stdio.h>
#include <stdlib.h>
#include <ieee754.h>

int main(){
    float a;
    for(;;){
        printf("\n\nENTER the value of a:\n");
        scanf("%f", &a);
        union ieee754_float *p_a;
        unsigned int a_exp;
        unsigned int a_negative;
        unsigned int a_mantissa;
        p_a = (union ieee754_float*)&a;
        a_exp = p_a->ieee.exponent;
        a_negative = p_a->ieee.negative;
        a_mantissa = p_a->ieee.mantissa;
        printf("exponent of a: %x\n", a_exp);
        printf("negative of a: %x\n", a_negative);
        printf("mantissa of a: %x\n", a_mantissa);
    }
    return 0;
}
```

Submission:

Submit your C program, outputs of the two runs, and your comments on the results. For what kind of numbers inaccurate results are obtained?