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Math 201 - Lecture Participation Assignment Week 12

### Theorems

1) If  $\lambda_1 \neq \lambda_2$  are the eigenvalues of  $T$ , then  $E_T(\lambda_1) \cap E_T(\lambda_2) = \{0\}$  <sup>zero vector of  $T$</sup>

2)  $T: V \rightarrow V$  be linear. Let  $\lambda_1, \lambda_2, \dots, \lambda_k$  be distinct eigenvalues of  $T$ .

If  $v_1, v_2, \dots, v_k$  are the eigenvectors of  $T$  such that  $T(v_i) = \lambda_i v_i$  for  $i=1, \dots, k$ .

Then  $\{v_1, v_2, \dots, v_k\}$  is a linearly independent subset of  $V$ .

3) Let  $T: V \rightarrow V$  be linear with  $\dim V = n < \infty$ . If  $T$  has  $n$  distinct eigenvalues, then  $T$  is diagonalizable.

4)  $T: V \rightarrow V$  be linear with  $\dim V = n < \infty$ .

$T$  is diagonalizable  $\iff$  (i)  $P_T(\lambda)$  has  $n$  roots (counted with multiplicities)

(ii)  $A_M(\lambda) = G_M(\lambda)$  for each eigenvalue of  $T$ .

$\iff$  There exists an eigenbasis  $B$  of  $V$ .