

# Clusterkit Manual

## Description about initial version

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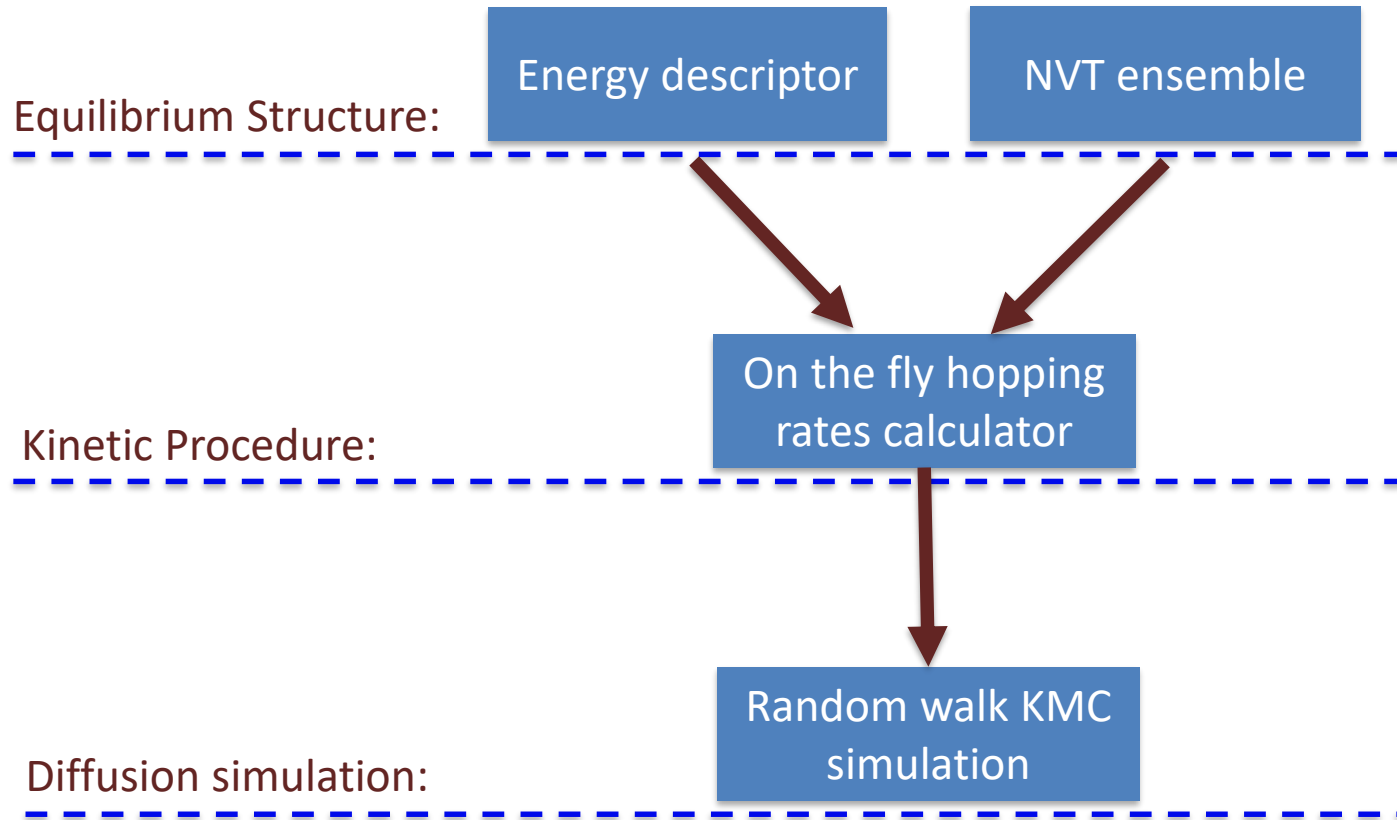
Code page: <https://github.com/Jeff-oakley/Clusterkit/>

Profile: <http://bouyang.wixsite.com/road-to-mse>

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# Computational framework



# Implementation of cluster algorithms

Equilibrium Structure:

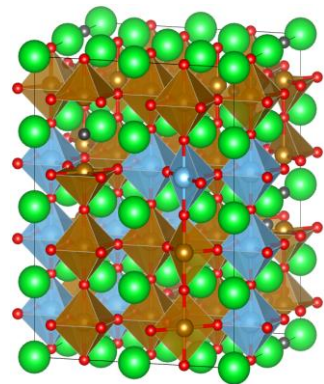
Energy descriptor

NVT ensemble

The idea of cluster expansion (CE):

$E_{\text{total}}$  of the system can be regarded as summation of atom clusters with 1 atom to N atoms

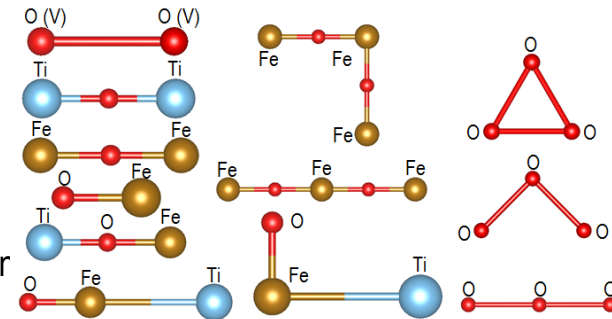
$$E = \sum_i n_i \varepsilon_i + \sum_{i>j} n_{ij} \varepsilon_{ij} + \sum_{i>j>k} n_{ijk} \varepsilon_{ijk} + \sum_{i>j>k>l} n_{ijkl} \varepsilon_{ijkl} \dots\dots$$



Made of clusters



**Monomer:** Sr, Fe, Ti, O  
**Dimer:** Sr-Fe, Fe-Fe, Ti-Ti, O-O, Fe-O et al.  
**Trimer:** Fe-Fe-Fe, O-O-O and Fe-Ti-O et al.  
 >> Fe-Ti-O: long chain, short chain, right triangle  
 >> Fe-Fe-Fe: triangle, chain  
 >> O-O-O: equilateral triangle, right triangle, chair  
**Tetramers and beyond.**



The idea of Metropolis Monte Carlo (MC):

Random sample within configurational space with acceptance rate according to energy criterion

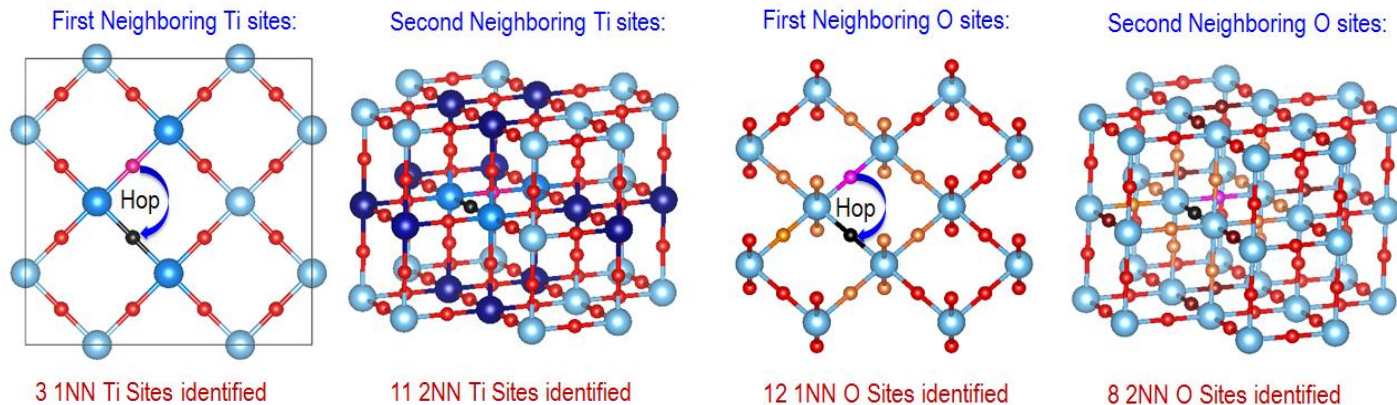
$$P = \exp\left(\frac{\Delta E}{k_B T}\right)$$

# Estimation of kinetic barrier

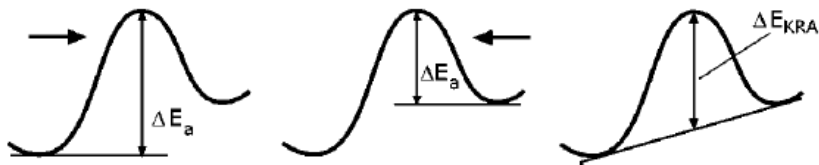
On the fly hopping  
rates calculator

Kinetic Procedure:

Finite sampling of local cluster interactions:



Kinetic cluster expansion:



$$\Delta E_{KRA} = E_{saddle} - \frac{1}{n} \sum_{j=1}^n E_{e_j}$$

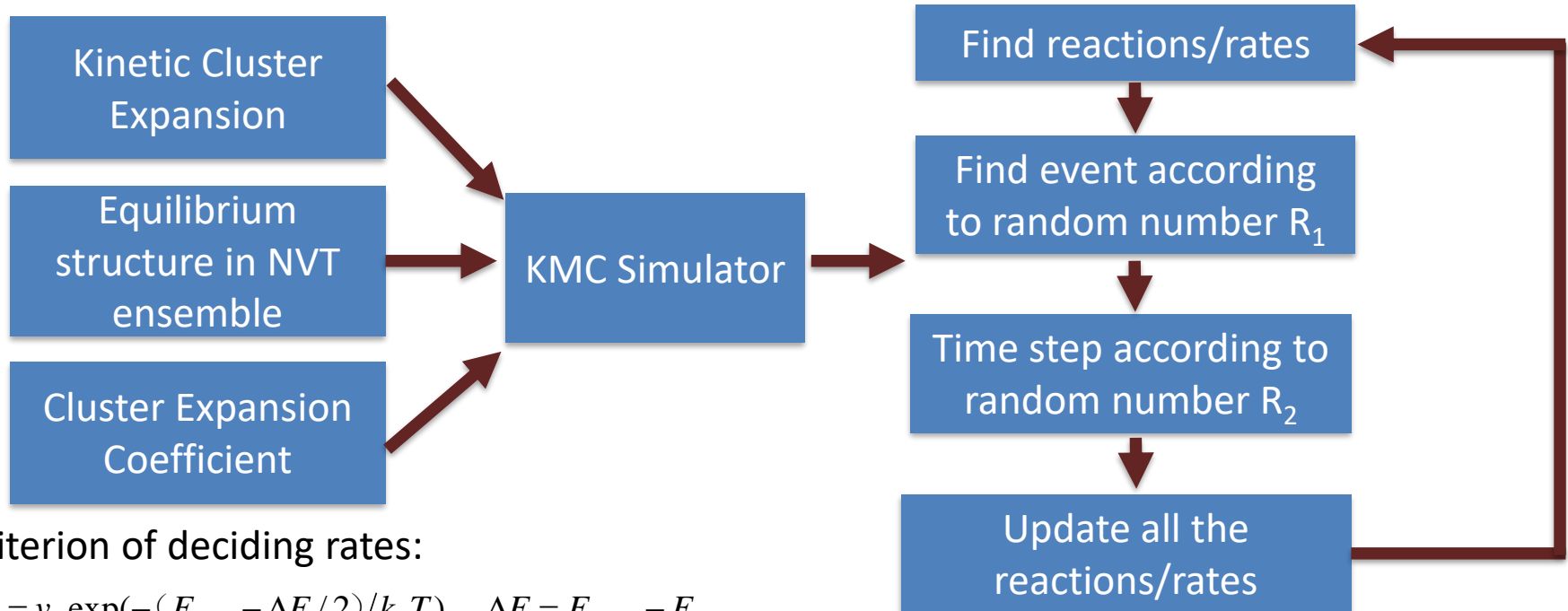
$$\Delta E_{KRA} = E_0 + \sum_{\alpha} n_{\alpha} \varepsilon_{\alpha}$$

$$\Delta E_a = \Delta E_{KRA} + \frac{1}{n} \left( \sum_{j=1}^n E_{e_j} \right) - E_{e_1}$$

# KMC simulation for diffusion process

Diffusion simulation:

Random walk KMC  
simulation



Criterion of deciding rates:

$$\Gamma_m = v_0 \exp(-(E_{KRA} - \Delta E / 2) / k_B T), \quad \Delta E = E_{Final} - E_{Initial}$$

Criterion of deciding jump phenomenon:

$$\frac{1}{\Gamma_{tot}} \sum_{m=1}^{k-1} \Gamma_m < R_1 \leq \frac{1}{\Gamma_{tot}} \sum_{m=1}^k \Gamma_m$$

Criterion of updating diffusion time:

$$\Delta t = -\frac{1}{\Gamma_{tot}} \ln \xi$$

# What can be done using Clusterkit?

1. Automatic workflow of cluster algorithms.
2. Cluster expansion description of solid solution system
3. Measurement of thermodynamic properties under NVT/NPT ensemble.
4. Construction of equilibrium structure at finite temperature.
5. Predicting of kinetic energy using kinetic cluster expansion.
6. Simulation of diffusion process with non-dilute concentration of diffusors and vacancies.

# Installation

Download the source code at:

<https://github.com/Jeff-oakley/Clusterkit/blob/bluewater/dist/Clusterkit-0.1.tar.gz> or  
<https://github.com/Jeff-oakley/Clusterkit>

Prerequisite:

numpy==1.11.1

pyyaml==3.12

And extract (if start with the tarball):

```
tar xvfz Clusterkit-0.1.tar.gz
```

```
cd Clusterkit-0.1/
```

Building using setup.py:

```
python setup install --user
```

Modify PYTHONPATH and PATH:

```
export PYTHONPATH=INSTALLDIR/lib/python2.7/site-packages:$PYTHONPATH
```

```
export PATH = INSTALLDIR/bin: $PATH
```

For automatic loading for each running:

Add the path variables in your .bashrc (or maybe .bash\_profile), .zshenv, or other script for the other shells.

# Utilities

ClusterFind (Identify stoichiometry independent clusters):

usage: ClusterFind [-h] -Sub SUBLATT [--NCut NCUT] [--Ref REF]

Script for running CEMC.

optional arguments:

- h, --help show this help message and exit
- Sub SUBLATT Tell projection of sublattice with respect to reference lattice. We are expecting something like "[[0,1],[2,3],[4,5]]", which tells the code that we have two types of atoms for each of the three sublattices
- NCut NCUT The cutoff of cluster size (default: 3)
- Ref REF Reference lattice (default: POSCAR\_Primary)



# Utilities

CEExtract (extract cluster information from samples DFT calculations):

usage: CEExtract [-h] -Des CLUSTERDES -Comp COMP -Tag TAG [--RN RDNUM]  
                  [--O OUTFILE] [--P PRECONF] [--Pos POSNAME]

Script for extracting CE data.

optional arguments:

- h, --help      show this help message and exit
- Des CLUSTERDES   Tell the description of each cluster
- Comp COMP        Composition list used for making dir
- Tag TAG          Tag list used for each composition
- RN RDNUM        Number of random structures for each composition, can be one digit or list
- O OUTFILE      Out put file name (default: CEDat.yaml)
- P PRECONF      Prefix of each configuration name (default: POSCARRand)
- Pos POSNAME    Name of the position file to read (default: POSCAR)

# Utilities

CERegress (Performing regressing of cluster coefficient):

usage: CERegress [-h] [--DF CEDATAFILE] [--I CINDLST] [--O OUTFILE]

Script for performing regression.

optional arguments:

- h, --help show this help message and exit
- DF CEDATAFILE Tell yaml data file, usually generated from CEExtract (default: CEDat.yaml)
- I CINDLST Effective indexes used in regressing
- O OUTFILE

# Utilities

## CEMC (Running cluster expansion Monte Carlo simulations):

usage: CEMC [-h] -des CLUSTERDES -coef CLUSTERCOEF -t TEMP [--GrpLst GRPLST]  
          [--N NLST] [--bias BIAS] [--ini INITCONF]

Script for running CEMC.

optional arguments:

- h, --help       show this help message and exit
- des CLUSTERDES   Tell the description of each cluster
- coef CLUSTERCOEF Tell the coefficient fitted for cluster expansion
- t TEMP           Tell the temperature of the simulation
- GrpLst GRPLST   group the sublattices with swap possibilities (default:  
                  [[1,2],[3,4]])
- N NLST          Tell the number of iterations required, 1st: outer loop,  
                  2st: inner loop; 3st: step size of outputting structure  
                  (default: [20,1500,500])
- bias BIAS       Tell the bias parameter (default: 0.0)
- ini INITCONF    Starting Configuration (default: POSCAR\_Primary)

# Utilities

KCEPre (Prepare NEB calculations given KCE descriptions):

```
usage: KCEPre [-h] -Sub SUBLATT -Ele ELENAME -Diff DIFFLATT [--NCut NCUT]
             [--DCut DCUT] [--N NBARRIER] [--C CONF] [--P PNTLST]
             [--O OUTFILE] [--MV MAXVAC]
```

Script for preparing KCE calculations.

optional arguments:

- h, --help show this help message and exit
- Sub SUBLATT Tell effective sublattice in reference cell
- Ele ELENAME List of elements with substitution
- Diff DIFFLATT Tell the diffuser sublattice, should be a integer in this version
- NCut NCUT The cutoff of cluster size (default: 2)
- DCut DCUT Cutoff distance of inteaction, default is half cell size (default: Half)
- N NBARRIER Number of random NEB calculations to be created
- C CONF Reference structures (default: POSCARRef)
- P PNTLST The StaInd and FinInd reference, should be a list of two index: StaInd and FinInd (default: Center)
- O OUTFILE Output file for the KCE informations (default: KCEConf.yaml)
- MV MAXVAC Set maximum NVac to avoid significant thrinkage (default: 6)

# Utilities

KCEExtract (Extract KCE information from NEB calculations):

usage: KCEExtract [-h] -Des KCLUSTERDES -Conf CONFLST -Map MAPDIC  
[--Pre PREFIX] [--Ref POSREF] [--O OUTFILE]

Script for extracting KCE data.

optional arguments:

- h, --help show this help message and exit
- Des KCLUSTERDES Tell the description of each cluster
- Conf CONFLST Configuration list used for making dir
- Map MAPDIC Dictionary for position remapping
- Pre PREFIX Prefix of sample folders
- Ref POSREF Reference POSCAR with out doping
- O OUTFILE Out put file name (default: KCEDat.yaml)

# Utilities

CVChk (Cross validation of CE and KCE regression):

Under developments...

The cross validation on clusters and samples are necessary, however this can be done conveniently using a extra script for specific system. A general utility will is under development to offer calculation of cross validations scores in one shot.

# Utilities

## KMC (Performance kinetic Monte Carlo simulations)

usage: KMC [-h] -des CLUSTERDES -coef CLUSTERCOEF -kdes KCLUSTERDES -kcoef  
KCLUSTERCOEF -t TEMP -sitelst SITELST -r RADIUS -fre FRE0  
[--ini INITCONF] [--ref REF] [--IsNew ISNEW]

Script for running KMC simulation.

optional arguments:

- h, --help show this help message and exit
- des CLUSTERDES Tell the description of each cluster
- coef CLUSTERCOEF Tell the coefficient fitted for cluster expansion
- kdes KCLUSTERDES Tell the description of each kinetic cluster
- kcoef KCLUSTERCOEF Tell the coefficient fitted for kinetic cluster expansion
- t TEMP Tell the temperature of the simulation
- sitelst SITELST List of site information, 1st: sublattice list that contain vacancy2nd:  
sublattice in Ref containing vacancy
- r RADIUS Radius that atomic jump can happen
- fre FRE0 Attempt frequency of a certain atom
- ini INITCONF Starting Configuration (default: POSCAR\_Primary)
- ref REF Reference configuration for vacancy identification (default: POSCAR\_Ref)
- IsNew ISNEW If this is a new calculation (default: 1)

# Utilities

## KMCPost (Post processing of KMC simulations)

usage: KMCPost [-h] [--KF KMCOUTFILE] [--P POSFILE] [--O OUTFILE]

Script for extracting the DOSCAR.

optional arguments:

-h, --help show this help message and exit

--KF KMCOUTFILE Tell file of KMC simulation results (default:  
Trace.dat)

--P POSFILE Initial configuration for KMC simulation (default:  
POSCAR\_Primary)

--O OUTFILE Output the processed diffusion results (default:  
Diffusion.dat)



# Input files

Primary lattice file in POSCAR format in VASP code for initialize Cluster expansion:

Currently we support only format of VASP with all methods implemented in Vasp.py. However this can be easily extended to other DFT code.

For instance, for the simulation of  $\text{ABO}_3$ , what we need is a POSCAR file with one specie in A and B site. A example is given below:

```
Sr1 Ti1 O3
1.000000
11.158513 0.000000 0.000000
0.000000 11.158513 0.000000
0.000000 0.000000 15.780520
Sr Ti O
32 32 96
Direct
0.000000 0.000000 0.000000
0.000000 0.000000 0.250000
0.000000 0.000000 0.500000
0.000000 0.000000 0.750000
0.000000 0.500000 0.000000
0.000000 0.500000 0.250000
0.000000 0.500000 0.500000
0.000000 0.500000 0.750000
0.250000 0.250000 0.000000
0.250000 0.250000 0.250000
0.250000 0.250000 0.500000
0.250000 0.250000 0.750000
0.250000 0.750000 0.000000
0.250000 0.750000 0.250000
```

# Output files

Configuration database for cluster expansion: CeDat.yaml

This file with YAML format is used to consolidate the data generated from DFT training set. In this case we just need to keep on single file on base of hundreds/thousands of DFT calculations. Meanwhile, all information of cluster expansion would be stored in the same file.

```
A12B20:
  POSCARRand0:
    Cluster Expansion: [-1029.2888, 12, 48, 74, 32, 14, 74, 54, 14, 50, 42, 43, 171,
      19, 16, 26, 18, 182, 548, 274]
    Position File:
      AtomNum: [32, 12, 20, 86, 10]
      AtomSum: 160
      Base:
        - [11.272991, -0.008624, 0.00052]
        - [-0.008341, 11.251252, -0.005254]
        - [0.00073, -0.007529, 15.870263]
      CellName: 'Sr1 Ti1 O3 '
      EleName: [Sr, Ti, Fe, O, Vac]
      EleNum: 5
      IsSel: 0
      LatType: Direct
      LattConst: 1.0
      LattPnt:
        - [0.0, 0.0, 0.0]
        - [0.0, 0.0, 0.25]
        - [0.0, 0.0, 0.5]
        - [0.0, 0.0, 0.75]
        - [0.0, 0.5, 0.0]
        - [0.0, 0.5, 0.25]
        - [0.0, 0.5, 0.5]
```

# OutputFiles

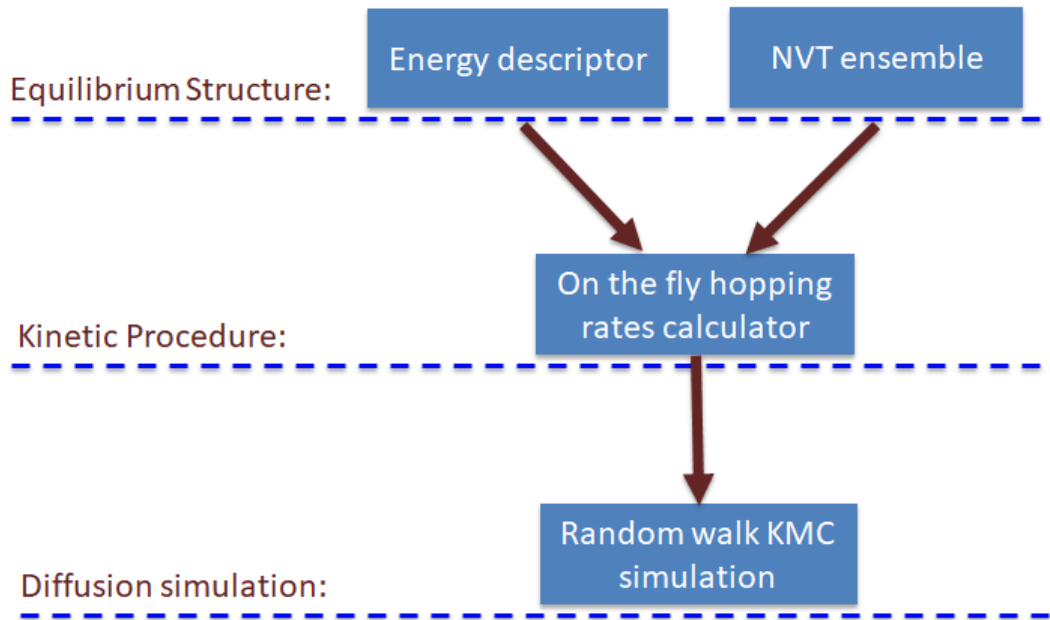
Configuration database for cluster expansion: KCEConf.yaml

This file with YAML format is used to describe the local atomic environment, diffusing atoms, effective local atoms for diffusions

```
DCut: 5.8792564999999999
EffPntLst:
- []
- [32, 33, 36, 37, 40, 41, 44, 45, 46, 48, 49, 50, 52, 53, 60, 61]
- [65, 66, 69, 70, 72, 73, 76, 77, 78, 80, 81, 82, 85, 89, 90, 92, 93, 95, 96, 99,
  101, 103, 104, 105, 107, 108, 111, 112, 113, 116, 117, 119, 120, 123, 124, 127]
KClusterDes:
- - [Sta, 1]
  - &id001 [5.029073801039524]
- - [Sta, 2]
  - *id001
- - [Sta, 1]
  - &id002 [4.184442368805207]
```

```
NCut: 2
Pnt:
- [0.375, 0.375, 0.375]
- [0.25, 0.5, 0.25]
PntLst:
- !!python/object/apply:numpy.core.multiarray.scalar
  - &id006 !!python/object/apply:numpy.dtype
    args: [i8, 0, 1]
```

# Summary



1. Automatic workflow of cluster algorithms.
2. (Kinetic) Cluster expansion description of solid solution system.
3. Statistic measurement of thermodynamic properties.
4. Diffusion simulation