

# A Novel Discrete Particle Swarm Optimization to Solve Traveling Salesman Problem

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**Abstract**—Particle Swarm Optimization (PSO), which simulates the unpredictable flight of a bird flock, is one of the intelligent computation algorithms. PSO is well-known to solve the continuous problems, yet by proper modification, it can also be applied to discrete problems, such as the classical test model: Traveling Salesman Problem (TSP). In this paper, a novel discrete PSO call C3DPSO for TSP, with modified update formulas and a new parameter  $c_3$  (called mutation factor, to help to keep the balance between exploitation and exploration), is proposed. In the new algorithm, the particle is not a permutation of numbers but a set of edges, which is different from most other algorithms for TSP. However, it still keeps the most important characteristics of PSO that the whole swarm is guided by *pbest* and *gbest*. According to some benchmarks in TSP lib, it is proved that the proposed PSO works well even with 200 cities.

**Index Terms**—Traveling Salesmen Problem (TSP), Swarm Intelligent, Particle Swarm Optimization (PSO), Mutation Factor

## I. INTRODUCTION

### A. Traveling Salesman Problem

Traveling salesman problem (TSP) is a well-known NP-complete problem as a benchmark for new algorithms. This problem can be simply described as follow: Suppose that there is one salesman who wants to visit  $n$  cities, and his object is finding out the shortest Hamilton cycle through which he can visit all the cities once and only once, and finally return to the start one. It's obvious that the computation cost of exhausting permutations for TSP is  $O(n!)$ . By now, many studies on TSP has been presented, such as genetic algorithms (GA)[1], simulated annealing (SA)[2], neural network(NN)[3] and ant colony system (ACO)[4], etc.

### B. Particle Swarm Optimization

Particle Swarm Optimization (PSO), as a new evolutionary algorithms was first proposed by Eberhart and Kennedy [5][6] in 1995. It use a simplified model of the social system of flying birds, in which each bird (called particle) will search the whole space guided both by its previous best position (*pbest*) and the best position of the swarm (*gbest*). Due to its high performance and simple implementation, PSO has been successfully used to optimize a wide range of continuous problems [7]~[10]. Meanwhile, some researchers have tried to

extend PSO to discrete areas and gotten some achievements [11][12][13]. However, in solving TSP, PSO has seldom showed its magic power. In 2000, Maurice Clerc [14] first tried to adapt PSO to resolve TSP. It was feasible but not very efficient. In [15][16][17], some Chinese scholars also proposed several different discrete PSO for TSP. However, only a few results with benchmarks less than 100 cities are given in these papers, and most of these algorithms required considerable computation cost.

In this paper, a novel discrete PSO called C3DPSO with less computation cost and higher precision is proposed. In the algorithm, a particle represents a set of edges, which will make up a whole Hamilton cycle. So the update formulas should be modified to fit this change. Utteriorly, to prevent the algorithm trapped in a local optimality, a new parameter  $c_3$ , called mutation factor, is introduced.

Following the introduction, the basic PSO algorithm and the novel discrete PSO are illustrated in part II & III. In part IV, analysis how the new parameter  $c_3$  improve discrete PSO is presented. Part 5 displays result of experiments, and the last part draws a conclusion.

## II. BASIC PARTICLE SWARM OPTIMIZATION ALGORITHM

In the basic PSO model, a particle swarm stands for a bird flock and searches the solution in a D-dimension real space. Each particle has its own position vector (a valid solution) and velocity vector (decides the particle's next action), which are both D-dimension. What's more, the fitness of each particle should be calculated by a special function to estimate the quality of a particle.

For more detail, the algorithm in pseudo code follows:

```
1) Randomly initialize the whole swarm
2) For( $i = 0$ ;  $i < \text{size of swarm}$ ;  $i++$ )
3) Evaluate  $f(x_i)$ 
4) While(termination criterion is not met){
5) For( $i = 0$ ;  $i < \text{size of swarm}$ ;  $i++$ ){
6) if( $f(x_i) > f(pbest_i)$ )  $pbest_i = x_i$ ;
7) if( $f(x_i) > f(gbest)$ )  $gbest = x_i$ ;
8) Update( $x_i, v_i$ );
9) Evaluating  $f(x_i)$ 
10) }
11) }
```

In line 3),  $f(x_i)$  is the fitness function to estimate the quality of solution. And the line 8) is the most important part of PSO. The particles update as follow:

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$$v_{id}^{k+1} = w * v_{id}^k + c_1 rand() * (pbest_{id}^k - x_{id}^k) + c_2 rand() * (gbest_{id}^k - x_{id}^k) \quad ①$$

$$x_{id}^{k+1} = x_{id}^k + v_{id}^{k+1} \quad ②$$

Here  $i$  indicates the number of particle and  $d$  is for the number of dimension. In formula ①,  $w$  is called inertia weight and decide how much the pre-velocity will affected the new one.  $c_1$  and  $c_2$  are constant value called learning factors, which decide the degree of affection of  $pbest_i$  and  $gbest$ . And  $rand()$  devote to a random number between 0 and 1.

### III. A NOVEL DISCRETE PARTICLE SWARM OPTIMIZATION FOR TRAVELING SALESMAN PROBLEM

Now basic PSO will be partly modified for TSP. Suppose there are  $N$  cities to visit. First,  $x_i$  should represent a set of edges. So it's not a common vector in  $N$ -dimensional space and some definitions must be introduced to modify the update formulas.

**Definition 1:**  $X(x, y)$  represents an edge  $(x, y)$  connected city  $x$  and  $y$ , with chosen probability  $X$ . When updating, a random number  $R$  between 0 and 1 will be given, and if  $R \leq X$ , this edge will be chosen while the opposite if  $R > X$ . As only symmetric TSP is discussed in this paper,  $(x, y)$  makes no difference from  $(y, x)$ ;

**Definition 2:** Velocity  $v$  is a set of elements as  $X(x, y)$ , such as  $\{A(a, b), B(a, c), C(f, g), \dots\}$ ;

**Definition 3:** A substitution between two position vectors is defined as a set of edges which exist in  $x_1$  but not in  $x_2$ , and the probability of 100% is added to these edges, to make it uniform as velocity. For example,  $x_1 = \{(1, 2), (2, 3), (3, 4), (4, 5), (5, 1)\}$ ,  $x_2 = \{(1, 2), (2, 4), (4, 3), (3, 5), (5, 1)\}$ , then  $x_1 - x_2 = \{(1, 2, 3), 1(4, 5)\}$ .

**Definition 4:** A multiplication between a real number and a set of edges is defined like this:  $A * \{B(2, 3), C(3, 5)\} = \{A * B(2, 3), A * C(3, 5)\}$ , where  $B$  and  $C$  indicates the probability of corresponding edges;

**Definition 5:** The result of  $v_1 + v_2$  is a set of  $v_1 \square v_2$ . In particular, each city can appear at most 4 times in one velocity, if overflows, some edges may be discarded to prevent the velocity from a tremendous set. And the same edges can exist in one velocity, like  $(a, b)$  in follow example 2.

e.g.1:  $\{A(a, b), B(e, f)\} + \{C(h, i)\} = \{A(a, b), B(e, f), C(h, i)\}$ ,  
e.g.2:  $\{A(a, b), B(a, c), C(a, d)\} + \{D(a, b), E(a, f)\} = \{A(a, b), B(a, c), C(a, d), D(a, b)\}$

**Definition 6:** The new parameter  $c_3$  is introduced here and the reason why  $c_3$  is much necessary is given in part IV. The formula ② is converted to formula ④ and contains three steps. First, choose edges depending on their corresponding probabilities in  $v_i$  to construct  $x_i'$ . Second, select edges from  $x_i$  according to the probability to complete the  $x_i'$ . Third, if the first two steps can't make a whole Hamilton cycle, add the absent edges with nearest principle. Specially, in the first two step, if a chosen edge will make  $x_i'$  illegal (for instance, no city can exist in more than three edges), it will be discarded. Thus it is obvious that edges in front of set  $v_i$  get more opportunity to be selected because of its priority position. So we change the order of formulas to make algorithm guided by  $gbest$  rather than  $pbest$  and pre-velocity. The new update formulas

are like this:

$$v_{id}^{k+1} = c_3 rand() * (gbest_{id}^k - x_{id}^k) + c_1 rand() * (pbest_{id}^k - x_{id}^k) + w * v_{id}^k \quad ③$$

$$x_{id}^{k+1} = v_{id}^{k+1} \oplus c_3 rand() * x_{id}^k \quad ④$$

Here if  $c_1, c_2, c_3$  is bigger than 1, the probability of some edges after multiplied a random number may be larger than 100%. According to Definition 1, the probability would be limit to 100% forcedly in this case.

Further more,  $pbest_i$  and  $gbest$  easily become the same after iteration. So the  $pbest_i$  won't be replaced by  $x_i$  with same length of  $gbest$ , in order to keep diversity. This is different from basic PSO.

Finally, the fitness function can be simple defined as the length of Hamilton cycle, and the smaller, the better.

Here is an example of update process, supposing  $w=0.5, c_1=1, c_2=0.4, c_3=1$ . The upper three graphs of Figure 1 show  $pbest_i, gbest$  and  $x_i$  before updating. And the lower ones indicate how to build the new  $x_i'$  follow the three steps.

Before update:

$pbest_i$ :  $\{(1, 2), (2, 3), (3, 4), (4, 5), (5, 6), (6, 7), (7, 8), (8, 9), (9, 10), (10, 1)\}$  (see the first graph of figure1)

$gbest$ :  $\{(1, 3), (3, 2), (2, 5), (5, 6), (6, 7), (7, 8), (8, 9), (9, 10), (10, 4), (4, 1)\}$  (see the second graph of figure1)

$x_i$ :  $\{(1, 2), (2, 4), (4, 5), (5, 6), (6, 7), (7, 8), (8, 10), (10, 9), (9, 3), (3, 1)\}$  (see the third graph of figure1)

$v_i$ :  $\{0.3(2, 4), 0.4(3, 5), 0.6(7, 9)\}$

Update process:

$gbest - x_i = \{1(2, 3), 1(2, 5), 1(8, 9), 1(10, 4), 1(4, 1)\}$ , suppose  $rand()=0.5$ ;

$pbest_i - x_i = \{1(2, 3), 1(3, 4), 1(8, 9), 1(10, 1)\}$ , suppose  $rand()=0.6$ , then

$v_i' = \{0.2(2, 3), 0.2(2, 5), 0.2(8, 9), 0.2(10, 4), 0.2(4, 1), 0.6(2, 3), 0.6(3, 4), 0.6(8, 9), 0.6(10, 1), 0.15(2, 4), 0.2(3, 5), 0.3(7, 9)\}$

$v_i' \oplus c_3 rand() * x_i$ , suppose  $rand()=0.7$

step 1: select edges from  $v_i'$  depend on probability, and  $x_i' = \{(2, 3), (2, 5), (3, 4), (8, 9), (10, 1), (7, 9)\}$

step 2: add edges from  $x_i$  depend on probability ( $c_3 * 0.7$  here), so  $x_i' = \{(2, 3), (2, 5), (3, 4), (8, 9), (10, 1), (7, 9), (8, 10), (6, 7)\}$

step 3: add the absent edges with nearest principle, then  $x_i' = \{(2, 3), (2, 5), (3, 4), (8, 9), (10, 1), (7, 9), (8, 10), (6, 7), (5, 6), (1, 4)\}$

Italics letter indicates edges which join in  $x_i'$  at current step. So in the end,  $x_i' = \{(1, 4), (4, 3), (3, 2), (2, 5), (5, 6), (6, 7), (7, 9), (9, 8), (8, 10), (10, 1)\}$

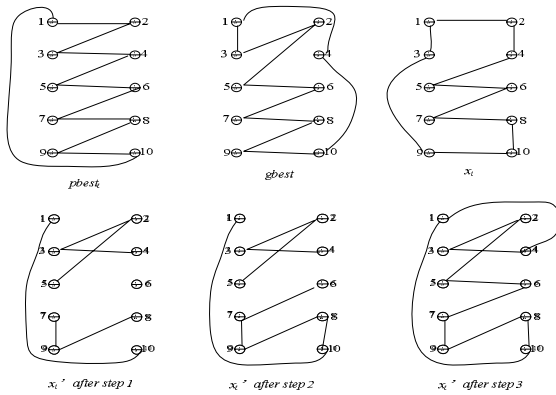


Fig. 1. An whole example for the update of a particle  $i$

#### IV. ANALYSIS OF MUTATION FACTOR, $C_3$

Figure 2 shows that how many edges come from the 3 steps in benchmark KroA100 without  $c_3$ , that is say,  $c_3 * rand()$  is set to 100% and the other parameters are set as description in part V. As a result, edges will be chosen from  $x_i$  in step 2 as much as possible. In figure 2, the middle line indicates that the number of edges from  $v_i$  decrease with the increasing of iteration, while the ones from  $x_i$  is opposite, as the top line shows. The reason is that  $pbest_i$ ,  $gbest$  and  $x_i$  become very similar in the later phase (see in figure 3), so new edges added to  $v_i$  become fewer and fewer according to formula ③ in part III. Ulteriorly, as the probabilities are 100%, edges in  $x_i$  will be surely chosen to  $x_i'$  if it is possible (see definition 6 in part III). So, after step 1 & 2,  $x_i'$  is very likely to  $x_i$ , and few new edges are brought into  $x_i'$  in step 3, as showed by the lowest line in figure 2. It will probably make the swarm premature and stop searching a better path. The experiment results in part V also demonstrate this.

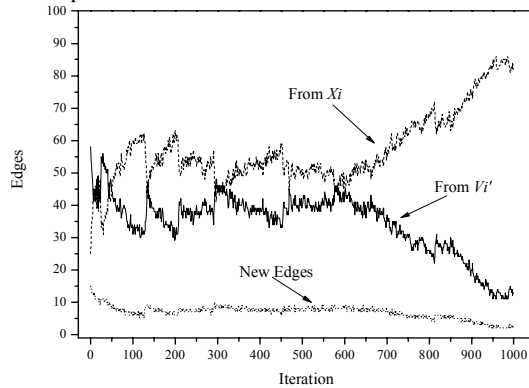


Fig. 2. Distribution of edges in KroA100 in 3 steps without  $c_3$ .

To avoid premature, parameter  $c_3$  is introduced to step 2.  $c_3$ , multiplied by a random number between 0 and 1, is the probability of an edge in  $x_i$  being selected. That is said, not all the legal edges in  $x_i$  will be chosen in step 2. So,  $x_i'$  after the first two steps is probably lack of some edges, and new edges will be added in step 3. Figure 4 illustrates that about 10% new edges are added to  $x_i'$ , like mutation. And figure 5 shows that  $x_i$  always keep different from  $gbest$  at least 3%~5% rate,

which indicates  $x_i$  maintaining to search the solution space. So  $c_3$  is also called mutation factor and it will help to keep balance between exploration and exploitation of this algorithm.

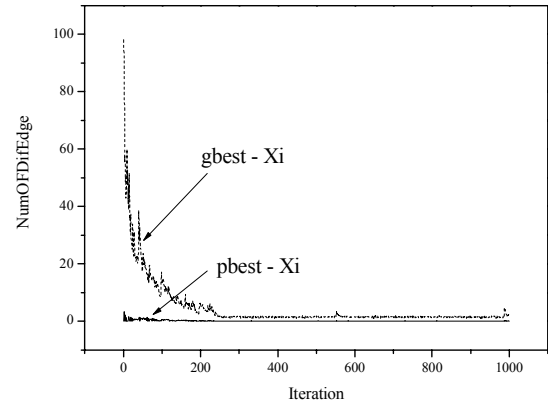


Fig. 3. Average number of different edges among  $gbest$ ,  $pbest$ , and  $x_i$  in algorithm without  $c_3$  in KroA100

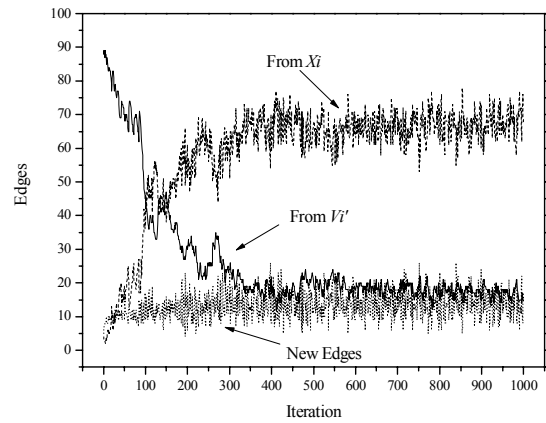


Fig. 4. Distribution of edges in KroA100 in 3 steps with  $c_3$ .

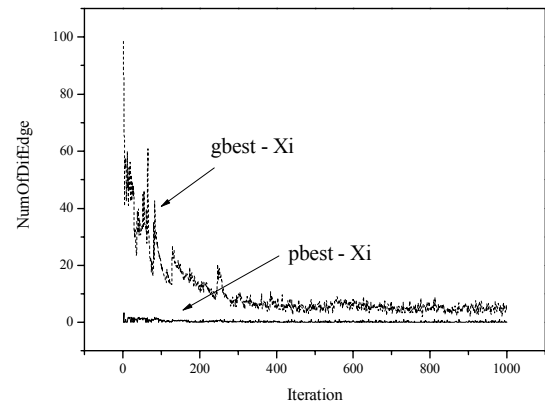


Fig. 5. Average number of different edges among  $gbest$ ,  $pbest$ , and  $x_i$  in algorithm with  $c_3$  in KroA100

## V. EXPERIMENT RESULTS

### A. Related Settings of the Experiment

Six classic TSP benchmarks from TSP lib have been tested by using the novel discrete PSO and ACO [18] (for comparison) algorithm, which are Burma14, Eil51, Berlin52, Eil76, KroA100 and KroA200. Because there are only a few researchers who have optimized TSP with PSO, and almost all of their benchmarks are smaller than 100 cities. So Burma14, Eil51, Berlin52 and Eil76 are adapted to compare with the other discrete PSO, and KroA100, 200 are used to prove the efficiency of our algorithm in solving larger TSP.

Each test has run for 50 times. And the computer system for test is consisted of Celeron 2.26GHz and 256 MB memory with Windows XP.

In C3DPSO, parameters  $w$ ,  $c_1$ ,  $c_2$ ,  $c_3$ ,  $n$ ,  $iter$  are set to 0.6, 1.5, 2, 2, 30,  $N*10$ , respectively.  $n$  and  $N$  are the size of the swarm and the number of cities, respectively.  $iter$  represent number of iteration.

In ACO,  $\alpha=0.1$ ,  $\rho=0.1$ ,  $\beta=2$ ,  $q_0=0.9$ ,  $n=10$ , as recommended in [18]. And  $iter$  is set to  $N*30$ , so the numbers of computing the length of Hamilton cycle in the two algorithms are the same.

### B. Results

The average and best result, relative error, running time and percentage of success computed by the two algorithms are showed in table 2. In this table, “average” is the average length of 50 running, while the “best” is the best one. “Error” is (“average” – “optima” / “optima”), where the “optima” is given by TSP Lib. And “Time” is the average cost of 50 running, estimated by milliseconds. “Success” here is defined as  $sucTimes/runningTimes$ . And “sucTimes” is the number of Hamilton cycles whose lengths are shorter than “limitation”.  $limitation = ((\text{floor}(N/50) + 1) * 0.01 + 1) * \text{optimal}$ .

Here “floor(x)” means the largest integer smaller than x.

For example, in Eil76,  $limitation = (\text{floor}(76/50) + 1) * 0.01 + 1 * 538 = 1.02 * 538 = 549$ .

For there are seldom results of PSO in solving TSP presented, only those in [16] are used for comparison in table 2, which was made by PSO-TS, PSO-TS-2opt, PSO-TS-CO and PSO-TS-CO-2opt. The reason to choose it is that it gives more and harder benchmarks than other papers we have found out.

In table 2, results made by discrete PSO proposed in this paper without  $c_3$ , that is say  $c_3 * \text{rand}()$  in formula (4) is always 100%, are presented first. It proved that when  $N \leq 76$ , the algorithm performs not bad, with relative error smaller than 20%. But its precision decreases rapidly with growing  $N$ .

C3DPSO are much more effective in all benchmarks than other algorithms, as showed in table 2, whose relative error are low than 5% even in KroA100 and KroA200. Figure 6, 7 & 8 denote the convergence of the proposed PSO with and without  $c_3$  in Berlin52, Eil76 and KroA200. They make it evident the mutation factor  $c_3$  play an important role to enhance the searching ability of the algorithm. Compared to other discrete PSO done in [16], C3PSO improves greatly either in precision

or computational cost. In particularly, there may be some mistakes in Burma14 give by [16], because the lengths are much shorter than those given by TSPLib.

In table 2, the boldfaced and italic numbers denote the winner between C3DPSO and ACO. It's obvious that C3DPSO makes advantages in most benchmarks with the same computational cost. Specially, the running times of C3DPSO increase slower than ACO. That is, C3DPSO will perform better and better than ACO as  $N$  becomes bigger and bigger.

TABLE 2  
EXPERIMENT RESULTS ARE SHOWED IN THE TABLE. BOLD AND ITALIC NUMBERS ARE THE BEST ONES IN THE COLUMN.

		Burma14	Eil51	Berlin52	Eil76	KroA100	KroA200
PSO without $c_3$	Average	3342.88	473.34	8730.18	626.94	27725.4	41204.5
	Best	3323	443	7724	566	24343	36464
	Error (%)	0.60	11.11	15.75	16.53	30.27	40.30
	Suc (%)	86	0	0	0	0	0
	Time(ms)	223	3878	3885	11250	21114	149340
C3DPSO	Average	3324.04	<b>433.64</b>	<b>7598.76</b>	<b>551.72</b>	<b>21689.30</b>	<b>30374.30</b>
	Best	3323	427	7542	540	21296	29563
	Error (%)	<b>0.03</b>	<b>1.793</b>	<b>0.753</b>	<b>2.550</b>	<b>1.914</b>	<b>3.427</b>
	Suc (%)	<b>100</b>	60	74	36	84	82
	Time(ms)	267	<b>4060</b>	<b>4116</b>	<b>11594</b>	<b>23950</b>	<b>198551</b>
PSO-TS	Average	33.69	582.501	8100.105	588.712	-----	-----
	Error (%)	9.12	35.47	7.37	9.98	-----	-----
	Time(ms)	1000	30000	120000	60000	-----	-----
PSO-TS-2opt	Average	30.88	459.273	7938.041	564.523	-----	-----
	Error (%)	0	6.81	5.22	5.46	-----	-----
	Time(ms)	1000	30000	120000	60000	-----	-----
PSO-TS-CO	Average	33.94	500.231	8323.432	604.126	-----	-----
	Error (%)	10	16.34	10.33	12.86	-----	-----
	Time(ms)	1000	30000	120000	60000	-----	-----
PSO-TS-CO-2opt	Average	30.88	440.900	7704.242	560.712	-----	-----
	Error (%)	0	2.54	2.12	4.75	-----	-----
	Time(ms)	1000	30000	120000	60000	-----	-----
ACO	Average	3329.68	434.14	7694.92	560.72	21821.16	31057.02
	Best	3323	<b>426</b>	7542	543	21341	30083
	Error (%)	0.20	1.91	2.03	4.22	2.53	5.75
	Suc (%)	98	<b>66</b>	56	6	64	36
	Time(ms)	<b>107</b>	5765	5897	18229	41642	338981
Optimal		3323	426	7542	538	21282	29368
Limitation		3356	435	7693	549	21920	30836

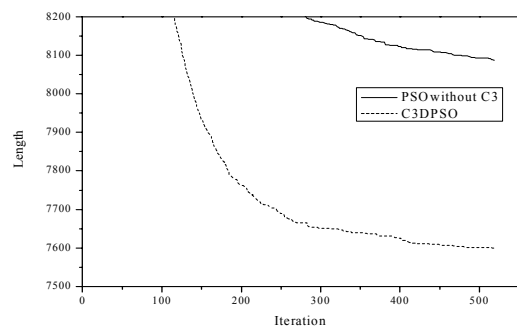


Fig. 6. Convergence of the algorithm in Benlin52

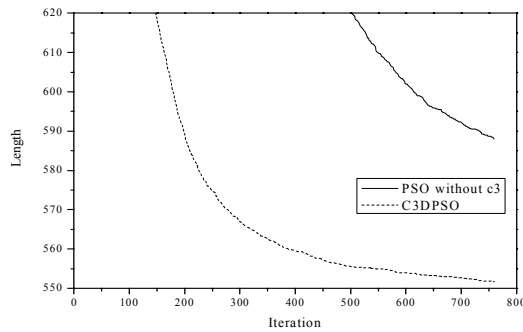


Fig. 7. Convergence of the algorithm in Eil76

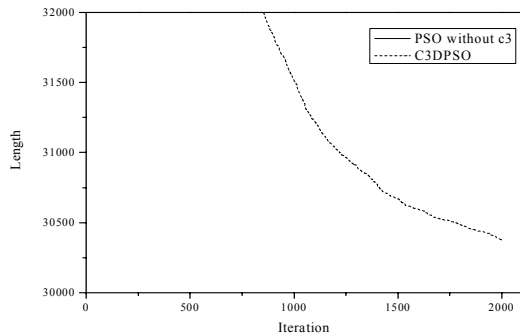


Fig. 8. Convergence of the algorithm in KroA200

## VI. CONCLUSION

In this paper, a novel discrete PSO called C3DPSO to approach TSP is proposed. It was proved that the algorithm is much more effective than previous work done by [14]~[17]. With mutation factor  $c_3$ , some new edges are brought into the solutions to keep balance between exploitation and exploration. Further work should focus on improving the algorithm, such as how to set effective parameters, and how to adjust the parameters dynamically, and so on.

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