

Elijah Koukle Algo Hw 2

Merge Sort
1) STEP BY STEP to merge two sorted lists
list 1: [1, 2, 3, 6] list 2: [-3, 0, 6, 7] Sol: []

We compare the first element of both lists and add the smaller value to the sorted merged array.

L1: [1, 2, 3, 6] L2: [-3, 0, 6, 7] | Sol: [] 1 < -3

L1: [1, 2, 3, 6] L2: [0, 6, 7] | Sol: [-3] 1 > 0

L1: [1, 2, 3, 6] L2: [6, 7] | Sol: [-3, 0] 1 < 6

L1: [2, 3, 6] L2: [6, 7] | Sol: [-3, 0, 1] 2 < 6

L1: [3, 6] L2: [6, 7] | Sol: [-3, 0, 1, 2] 3 < 6

L1: [6] L2: [6, 7] | Sol: [-3, 0, 1, 2, 3] 6 < 6

L1: [] L2: [6, 7] | Sol: [-3, 0, 1, 2, 3, 6]

append rest of L2

→ Sol: [-3, 0, 1, 2, 3, 6, 6, 7]

2) Insertion Sort STEP BY STEP

list: [-21, 5, 7, -10, 61, 8, 3, 10]

i=1 -21 < 5 no shift

i=2 5 < 7 no shift

i=3 7 < -10 not true so swap. 5 < -10 swap. -21 < -10 stop.

i=4 7 < 61 no shift

i=5 61 < 8 not true so swap. 7 < 8 true so stop.

[-21, -10, 5, 7, 8, 61, 3, 10]

i=6 61 < 3 not true. it swaps all the way to index 2.

[-21, -10, 3, 5, 7, 8, 61, 10]

$i \Rightarrow 6 \leq 10$ not true so we swap once and stop

and stop
we end with $[-2, 10, 3, 5, 7, 8, 10, 6]$

3) quick sort

List: $[-5, 4, 2, 619, 11, 5, 620, -3]$ pivot $+ 3$

$[-5]$ done $\swarrow -3$ \swarrow (-3)

$$7-3$$

$[4, 2, 619, 11, 5, 620]$

$\angle 620$ 620 > 620

$$[4, 2, 619, 11, 5]$$

[]

⑤

$[4,2]$

57

75

[619, 11]

46

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[]

$[4]$

⑪

10

(619)

Sorted List $[-5, -3, 2, 4, 5, 11, 619, 620]$

4) Shell Sort Steps.

$$h = 8$$

List: [5, 10, 60, 0, -1, 34, 6, 10]

start with gap = $n/2$ (4 in this case)

pass 1: (0,4) (1,5) (2,6) (3,7)

$(0, 4) \rightarrow S > -1 \text{ swap} \rightarrow [-1, 10, 60, 0, 5, 34, 6, 10]$

(1,5) $\rightarrow 10 < 34$ keep

$(0, 5) \rightarrow 10 < 34$ keep
 $(3, 6) \rightarrow 60 > 6$ swap $\rightarrow [-1, 10, 6, 0, 5, 34, 60, 10]$

(3, 7) 0 < 10 keep

[1, 10, 6, 0, 5, 34, 60, 10]

(0, 2) (1, 3) (2, 4) (3, 5) (4, 6) (5, 7)

$$\text{gap} = n/4 = 2$$

(0, 2) $\rightarrow -1 < 6$ no swap

(1, 3) $\rightarrow 10 > 0$ swap $\rightarrow [-1, 0, 6, 10, 5, 34, 60, 10]$

(2, 4) $\rightarrow 6 > 5 \rightarrow$ swap $\rightarrow [-1, 0, 5, 10, 6, 34, 60, 10]$

(3, 5) $\rightarrow 0 < 34$ no swap

(4, 6) $\rightarrow 6 < 60$ no swap

(5, 7) $\rightarrow 34 > 10$ swap $\rightarrow [-1, 0, 5, 10, 6, 10, 60, 34]$

Gap = 1 ~~stands~~ normal insertion now

insert 6: $[-1, 0, 5, 6, 10, 10, 60, 34]$

insert 34: $[-1, 0, 5, 10, 10, 34, 60]$

5) Algorithm analysis

1) quick sort & merge sort. I think these are the fastest since it splits the list then goes through each element so its n and $\log n$. it is a divide and conquer algorithm

2) Shell sort. Since it's like insertion but you move in gaps and the numbers can jump I think it's faster than insertion

3) insertion, selection, bubble sort. These are all $O(n^2)$ I think which would make them all the slowest. since its two loops it's $n \times n = O(n^2)$