

Elijah Kontole Algo Hw 2

### Merge Sort

- 1) Step by step to merge two sorted lists  
list 1: [1, 2, 3, 6] list 2: [-3, 0, 4, 7] Sol: []

We compare the first element of both lists and add the smaller value to the sorted merged array.

- [1: [1, 2, 3, 6] L2: [-3, 0, 4, 7] | Sol: [] ] > -3  
L1: [1, 2, 3, 6] L2: [0, 4, 7] | Sol: [-3 ] ] > 0  
L1: [1, 2, 3, 6] L2: [4, 7] | Sol: [-3, 0 ] ] > 6  
L1: [2, 6] L2: [4, 7] | Sol: [-3, 0, 1 ] ] > 6  
L1: [3, 6] L2: [4, 7] | Sol: [-3, 0, 1, 2 ] ] > 6  
L1: [6] L2: [4, 7] | Sol: [-3, 0, 1, 2, 3 ] ] > 6  
L1: [] L2: [4, 7] | Sol: [-3, 0, 1, 2, 3, 6 ] ]  
Append rest of L2  
 $\rightarrow$  Sol: [-3, 0, 1, 2, 3, 6, 7]

### 2) insertion sort step by step

- list: [-21, 5, 7, -10, 61, 8, 3, 10]  
i=1 -21 < 5 no shift ↪ [-21, -10, 5, 7, 61, 8, 3, 10]  
i=2 5 < 7 no shift ↪ [-21, -10, 5, 7, 61, 8, 3, 10]  
i=3 7 < 61 not true so swap. 5 < -10 swap. -21 < -10 stop. ↪  
i=4 7 < 8 not true so swap. 7 < 8 true so stop.  
i=5 61 < 8 not true so swap. [-21, -10, 5, 7, 8, 61, 3, 10]  
i=6 61 < 3 not true. it swaps all the way to index 2. ↪ [-21, -10, 3, 5, 7, 8, 61, 10]

$i \Rightarrow 6 < 10$  not true so we swap once  
and stop  
we end with  $[-2, 10, 3, 5, 7, 8, 10, 6]$

### 3) Quick Sort

List:  $[-5, 4, 2, 619, 11, 5, 620, -3]$  pivot 3

$\begin{array}{c} -3 \\ [-5] \end{array}$  done

$> -3$

$[4, 2, 619, 11, 5, 620]$

$\begin{array}{c} 620 \\ < 620 \end{array}$

$> 620$   
 $[ ]$

$[4, 2, 619, 11, 5]$

$\begin{array}{c} 5 \\ [4, 2] \end{array}$

$> 5$   
 $[619, 11]$

$\begin{array}{c} 2 \\ [ ] \end{array}$

$\begin{array}{c} 11 \\ [619] \end{array}$

$\begin{array}{c} 11 \\ [ ] \end{array}$

Sorted List  $[-5, -3, 2, 4, 5, 11, 619, 620]$

### 4) Shell Sort Steps.

$n = 8$

List:  $[5, 10, 60, 0, -1, 34, 6, 10]$

start with gap =  $n/2$  ( $4$  in this case)

Pass 1:  $(0, 4) (1, 5) (2, 6) (3, 7)$

$(0, 4) \rightarrow 5 > -1$  swap  $\rightarrow [-1, 10, 60, 0, 5, 34, 6, 10]$

$(1, 5) \rightarrow 10 < 34$  keep

$(2, 6) \rightarrow 60 > 6$  swap  $\rightarrow [-1, 10, 6, 0, 5, 34, 60, 10]$

$(3, 7) \quad 0 < 10$  keep

$[1, 10, 6, 0, 5, 34, 60, 10]$   
 $(0, 2) (1, 3) (2, 4) (3, 5) (4, 6) (5, 7)$

$$\text{Gap} = n/4 = 2$$

$(0, 2) \rightarrow 1 < 6$  no swap

$(1, 3) \rightarrow 10 > 0$  swap  $\rightarrow [1, 0, 6, 10, 5, 34, 60, 10]$

$(2, 4) \rightarrow 6 > 5 \rightarrow$  swap  $\rightarrow [-1, 0, 5, 10, 6, 34, 60, 10]$

$(3, 5) \rightarrow 0 < 34$  no swap

$(4, 6) \rightarrow 6 < 60$  no swap

$(5, 7) \rightarrow 34 > 10$  swap  $\rightarrow [-1, 0, 5, 10, 6, 10, 60, 34]$

Gap = 1 standard insertion now

insert 6:  $[-1, 0, 5, 6, 10, 10, 60, 34]$

insert 34:  $-1, 0, 5, 10, 10, 34, 60$

## 5) Algorithm analysis

1) quick sort & merge sort. I think  
these are the fastest since it splits  
the list then goes through each element  
so its  $n$  and  $\log n$ . It is a divide  
and conquer algorithm

2) Shell sort. Since it's like insertion but  
you move in gaps and the numbers can  
jump. I think it's faster than insertion

3) insertion, selection, bubble sort. These are all  
 $O(n^2)$  I think which would make them  
all the slowest. Since its two loops  
it's  $n \cdot n = O(n^2)$