Natural Language Processing with Deep Learning

Lecture 3 — Text classification 1: Log-linear models

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We focus on Trustworthy Human Language Technologies

www.trusthlt.org

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Feedback

Feedback

Motivation

Towards supervised machine learning on text data

Numerical representation of natural language text

Binary text classification

- Binary classification as a function
- Finding the best model's parameters

Thank you for your feedback!

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- Slow pace

Motivation

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What are we going to achieve

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Example task: Binary sentiment classification into positive and negative

Recall the IMDB dataset

We will learn a simple yet powerful supervised machine learning model

- Known as logistic regression, maximum entropy classifier
- In fact, it is a single-layer neural network
- An essential important building block of deep neural networks

Towards supervised machine learning on text data

Mathematical notation

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Scalars, vectors, matrices

Lowercase letters represent scalars: x, y, b

Bold lowercase letters represent vectors: $\boldsymbol{w}, \boldsymbol{x}, \boldsymbol{b}$

Bold uppercase letters represent matrices: $\boldsymbol{W}, \boldsymbol{X}$

Indexing

$[.]$ as the index operator of vectors and matrice

$\boldsymbol{b}_{[i]}$ is the i-th element of vector $\boldsymbol{b}$

$\boldsymbol{W}_{[i,j]}$ is the i-th row, j-th column of matrix $\boldsymbol{W}$

Notation

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Sequences

$\boldsymbol{x}_{1:n}$ is a sequence of vectors $\boldsymbol{x}_1, \ldots, \boldsymbol{x}_n$

$[\boldsymbol{v}_1; \boldsymbol{v}_2]$ is vector concatenation

Note! We use vectors as *row* vectors

$$\boldsymbol{x} \in \mathbb{R}^d$$

Example $d = 5$:

$$\boldsymbol{x} = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 \end{pmatrix}$$

which is simply a list (1-d array) of numbers $(1, 2, 3, 4, 5)$

Multiplication example

$$\boldsymbol{x} \in \mathbb{R}^{d_{in}} \qquad \boldsymbol{W} \in \mathbb{R}^{d_{in} \times d_{out}} \qquad \boldsymbol{b} \in \mathbb{R}^{d_{out}}$$

Example: $\boldsymbol{y} = \boldsymbol{x}\boldsymbol{W} + \boldsymbol{b}$**,** $d_{in} = 3$**,** $d_{out} = 2$

$$\begin{pmatrix} \boldsymbol{x}_{[1]} & \boldsymbol{x}_{[2]} & \boldsymbol{x}_{[3]} \end{pmatrix} \begin{pmatrix} \boldsymbol{W}_{[1,1]} & \boldsymbol{W}_{[1,2]} \\ \boldsymbol{W}_{[2,1]} & \boldsymbol{W}_{[2,2]} \\ \boldsymbol{W}_{[3,1]} & \boldsymbol{W}_{[3,2]} \end{pmatrix} + \begin{pmatrix} \boldsymbol{b}_{[1]} & \boldsymbol{b}_{[2]} \end{pmatrix} = \begin{pmatrix} \boldsymbol{y}_{[1]} & \boldsymbol{y}_{[2]} \end{pmatrix}$$

Mult. simplified with dot product $\boldsymbol{u} \cdot \boldsymbol{v} = \sum_i \boldsymbol{u}_{[i]} \boldsymbol{v}_{[i]}$

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Example: $\boldsymbol{y} = \boldsymbol{x}\boldsymbol{W} + \boldsymbol{b}$**,** $d_{in} = 3$**,** $d_{out} = 1$

$\boldsymbol{x} \in \mathbb{R}^{d_{in}}$ $\quad$ $\boldsymbol{W} \in \mathbb{R}^{d_{in} \times d_{out}}$ $\quad$ $\boldsymbol{b} \in \mathbb{R}^{d_{out}}$

$$\begin{pmatrix} \boldsymbol{x}_{[1]} & \boldsymbol{x}_{[2]} & \boldsymbol{x}_{[3]} \end{pmatrix} \begin{pmatrix} \boldsymbol{W}_{[1,1]} \\ \boldsymbol{W}_{[2,1]} \\ \boldsymbol{W}_{[3,1]} \end{pmatrix} + b = y$$

Equivalent dot product: $y = \boldsymbol{x} \cdot \boldsymbol{w} + b$**,** $d_{in} = 3$**,** $d_{out} = 1$

$\boldsymbol{x} \in \mathbb{R}^{d_{in}}$ $\quad$ $\boldsymbol{w} \in \mathbb{R}^{d_{out}}$ $\quad$ $b \in \mathbb{R}$

$$\begin{pmatrix} \boldsymbol{x}_{[1]} & \boldsymbol{x}_{[2]} & \boldsymbol{x}_{[3]} \end{pmatrix} \cdot \begin{pmatrix} \boldsymbol{w}_{[1]} & \boldsymbol{w}_{[2]} & \boldsymbol{w}_{[3]} \end{pmatrix} + b = y$$

Towards supervised classification setup

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We often restrict ourselves to search over specific families of functions, e.g., the space of all linear functions with d_{in} inputs and d_{out} outputs

- By restricting to a specific hypothesis class, we are injecting the learner with **inductive bias** (a set of assumptions about the form of the desired solution)

High-dimensional linear functions

Function $f(\boldsymbol{x}) : \mathbb{R}^{d_{in}} \rightarrow \mathbb{R}^{d_{out}}$

$$f(\boldsymbol{x}) \text{ or } f(\boldsymbol{x}; \underbrace{\boldsymbol{W}, \boldsymbol{b}}) = \boldsymbol{x}\boldsymbol{W} + \boldsymbol{b}$$

Explicit parameters

where $\boldsymbol{x} \in \mathbb{R}^{d_{in}}$ $\quad \boldsymbol{W} \in \mathbb{R}^{d_{in} \times d_{out}}$ $\quad \boldsymbol{b} \in \mathbb{R}^{d_{out}}$

Vector $\boldsymbol{x}$ is the **input**, matrix $\boldsymbol{W}$ and vector $\boldsymbol{b}$ are the **parameters** — typically denoted $\Theta = \boldsymbol{W}, \boldsymbol{b}$

Goal of learning

Set the values of the parameters $\boldsymbol{W}$ and $\boldsymbol{b}$ such that the function behaves as intended on a collection of input values $\boldsymbol{x}_{1:k} = \boldsymbol{x}_1, \ldots, \boldsymbol{x}_k$ and the corresponding desired outputs $\boldsymbol{y}_{1:k} = \boldsymbol{y}_1, \ldots, \boldsymbol{y}_k$

Binary classification

Function $f(\boldsymbol{x}) : \mathbb{R}^{d_{in}} \rightarrow \mathbb{R}$

$$f(\boldsymbol{x}) \text{ or } f(\boldsymbol{x}; \underbrace{\boldsymbol{w}, \boldsymbol{b}}_{\text{Explicit parameters}}) = \boldsymbol{x} \cdot \boldsymbol{w} + b$$

However, for binary text classification

- Our input is in the form of a natural language text
- Our labels are two categories, e.g., positive and negative

Let's start with the labels

Very easy: Just arbitrarily map the categories into 0 and 1 (e.g., negative = 0, positive = 1)

Numerical representation of natural language text

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Goal: Transform text into a fixed-size vector of real numbers

What's our setup:

$$f(\boldsymbol{x}) : \mathbb{R}^{d_{in}} \rightarrow \mathbb{R} \qquad f(\boldsymbol{x}) = \boldsymbol{x} \cdot \boldsymbol{w} + b$$

What we need:

$$\boldsymbol{x} \in \mathbb{R}^{d_{in}}$$

What we have:

One of my favorite movies ever,The Shawshank Redemption is a modern day classic as it tells the story of two inmates who become friends and find solace over the years in which this movie takes place.Based on a Stephen King novel, ...

What is a “word”?

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Y. Goldberg (2017). ***Neural Network Methods for Natural Language Processing.*** Morgan & Claypool

A matter of debate among linguists, answer not always clear

Very simplistic definition: words are sequences of letters separated by whitespace

But: `dog`, `dog?`, `dog.`, and `dog)` would be different words

Better: words separated by whitespace or punctuation

A process called **tokenization** splits text into tokens based on whitespace and punctuation

- English: the job of the tokenizer is quite simple
- Hebrew, Arabic: sometimes without whitespace
- Chinese: no whitespaces at all

Tokens

Symbols `cat` and `Cat` have the same meaning, but are they the same word?

Something like `New York`, is it two words, or one?

- We distinguish between words and tokens
- We refer to the output of a tokenizer as a token, and to the meaning-bearing units as words

Keep in mind

We use the term **word** very loosely, and take it to be interchangeable with **token**.

In reality, the story is more complex than that.

Vocabulary

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We build a fix-sized static **vocabulary** (e.g., by tokenizing training data)

- Typical sizes: 20,000 – 100,000 words

Each word has a unique fixed index

$$V = \left(\text{a}_1 \quad \text{abandon}_2 \quad \ldots \quad \text{cat}_{852} \quad \ldots \quad \text{zone}_{2,999} \quad \text{zoo}_{3,000}\right)$$

(Averaged) Bag-of-words

$$\boldsymbol{x} = \frac{1}{|D|} \sum_{i=1}^{|D|} \boldsymbol{x}^{D_{[i]}}$$

$D_{[i]}$ – word in doc D at position i, $\boldsymbol{x}^{D_{[i]}}$ – one-hot vector

Example: a cat sat → a, `cat`, `sat`

$$V = \begin{pmatrix} \text{a}_1 & \text{abandon}_2 & \dots & \text{cat}_{852} & \dots & \text{zone}_{2,999} & \text{zoo}_{3,000} \end{pmatrix}$$

$$\text{a} = \boldsymbol{x}^{D_{[1]}} = \begin{pmatrix} 1_1 & 0_2 & 0_3 & \dots & 0_{2,999} & 0_{3,000} \end{pmatrix}$$

$$\text{cat} = \boldsymbol{x}^{D_{[2]}} = \begin{pmatrix} 0_1 & \dots & 1_{852} & \dots & 0_{2,999} & 0_{3,000} \end{pmatrix}$$

$$\text{sat} = \boldsymbol{x}^{D_{[3]}} = \begin{pmatrix} 0_1 & \dots & 1_{2,179} & \dots & 0_{2,999} & 0_{3,000} \end{pmatrix}$$

Averaged bag-of-words example: $x \in \mathbb{R}^{3,000}$

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Example: a cat sat → a, cat, sat

$$\text{a} = \boldsymbol{x}^{D_{[1]}} = \begin{pmatrix} 1_1 & 0_2 & 0_3 & \dots & 0_{2,999} & 0_{3,000} \end{pmatrix}$$

$$\text{cat} = \boldsymbol{x}^{D_{[2]}} = \begin{pmatrix} 0_1 & \dots & 1_{852} & \dots & 0_{2,999} & 0_{3,000} \end{pmatrix}$$

$$\text{sat} = \boldsymbol{x}^{D_{[3]}} = \begin{pmatrix} 0_1 & \dots & 1_{2,179} & \dots & 0_{2,999} & 0_{3,000} \end{pmatrix}$$

$$\boldsymbol{x} = \frac{1}{|D|} \sum_{i=1}^{|D|} \boldsymbol{x}^{D_{[i]}}$$

$$= \begin{pmatrix} 0.33_1 & 0_2 & \dots & 0_{851} & 0.33_{852} & 0_{853} & \dots & 0.33_{2,179} & \dots & 0_{3,000} \end{pmatrix}$$

Out-of-vocabulary (UNK) tokens

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P. Koehn (2020). ***Neural Machine Translation.*** (not freely available). Cambridge University Press

Words in a language are very unevenly distributed (Zipf's law)

- There is always a large 'tail' of rare words

When building the vocabulary, use the most frequent words, all others represented by an unknown token (UNK or 00V)

Example vocabulary, most common 3,000 words and UNK

$$V = \left(\text{a}_1 \quad \text{abandon}_2 \quad \ldots \quad \text{zone}_{2,999} \quad \text{zoo}_{3,000} \quad \text{UNK}_{3,001}\right)$$

- In machine translation, how to translate the UNK word?

Subword units: Byte-pair encoding

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1. The words in the corpus are split into characters (marking original spaces with a special space character) — this is the initial vocabulary V
2. The most frequent pair of characters is merged and added to V
3. Repeat 2 for a fixed given number of times
4. Each of these steps increases V by one, beyond the original inventory of single characters

When done over large corpora with multiple languages and writing systems, BPE prevents OOV!

Byte-pair encoding example on a toy corpus (part 1)

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```
t h i s _ f a t _ c a t _ w i t h _ t h e _
h a t _ i s _ i n _ t h e _ c a v e _ o f _
t h e _ t h i n _ b a t
```

Most frequent: `t h` (6 times), merge into a single token

```
th i s _ f a t _ c a t _ w i th _ th e _ h a
t _ i s _ i n _ th e _ c a v e _ o f _ th e
_ th i n _ b a t
```

Most frequent: `a t` (4 times), merge into a single token

```
th i s _ f at _ c at _ w i th _ th e _ h at
_ i s _ i n _ th e _ c a v e _ o f _ th e _
th i n _ b at
```

Byte-pair encoding example on a toy corpus (part 2)

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th i s _ f at _ c at _ w i th _ th e _ h at _ i s _ i n _ th e _ c a v e _ o f _ th e _ th i n _ b at

At the end of this process, the most frequent words will emerge as single tokens, while rare words consist of still unmerged subwords

Most frequent: th e (3 times), merge into a single token

th i s _ f at _ c at _ w i th _ the _ h at _ i s _ i n _ the _ c a v e _ o f _ the _ th i n _ b at

$V =$

{t, h, i, s, _, f, a, c, w, e, n, v, o, f, b, th, at, the}

SentencePiece: A variant of byte pair encoding

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Byte-pair example. Word splits indicated with @@.

```
[the] [relationship] [between] [Obama]
[and] [Net@@] [any@@] [ahu] [is] [not]
[exactly] [friendly] [.]
```

SentencePiece escapes the whitespace with _ and tokenizes the input into an arbitrary subword sequence

SentencePiece example of "Hello world."

```
[Hello] [_wor] [ld] [.]
```

Lossless tokenization — all the information to reproduce the normalized text is preserved

T. Kudo and J. Richardson (2018). **"SentencePiece: A simple and language independent subword tokenizer and detokenizer for Neural Text Processing".** In: *Proceedings of the 2018 Conference on Empirical Methods in Natural Language Processing: System Demonstrations.* Brussels, Belgium: Association for Computational Linguistics, pp. 66–71

Recap: Transform text into a fixed-size vector of real numbers

What's our setup:

$$f(\boldsymbol{x}) : \mathbb{R}^{d_{in}} \rightarrow \mathbb{R} \qquad f(\boldsymbol{x}) = \boldsymbol{x} \cdot \boldsymbol{w} + b$$

What we need:

$$\boldsymbol{x} \in \mathbb{R}^{d_{in}}$$

What we have:

One of my favorite movies ever,The Shawshank Redemption is a modern day classic ...

Simple solution:

- Bag-of-words (tokenized), $d_{in} = |V|$

Binary text classification

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Binary text classification

Binary classification as a function

Linear function and its derivatives

We have this linear function

$$f(\boldsymbol{x}) : \mathbb{R}^{d_{in}} \rightarrow \mathbb{R} \qquad f(\boldsymbol{x}) = \boldsymbol{x} \cdot \boldsymbol{w} + b = \boldsymbol{x}_{[1]}\boldsymbol{w}_{[1]} + \ldots + \boldsymbol{x}_{[d_{in}]}\boldsymbol{w}_{[d_{in}]} + b$$

Derivatives wrt. parameters w and b

$$\frac{\mathrm{d}f}{\mathrm{d}\boldsymbol{w}_{[i]}} = \boldsymbol{x}_{[i]} \qquad \frac{\mathrm{d}f}{\mathrm{d}b} = 1$$

Non-linear mapping to $[0, 1]$

We have this linear function

$$f(\boldsymbol{x}) : \mathbb{R}^{d_{in}} \rightarrow \mathbb{R} \qquad f(\boldsymbol{x}) = \boldsymbol{x} \cdot \boldsymbol{w} + b$$

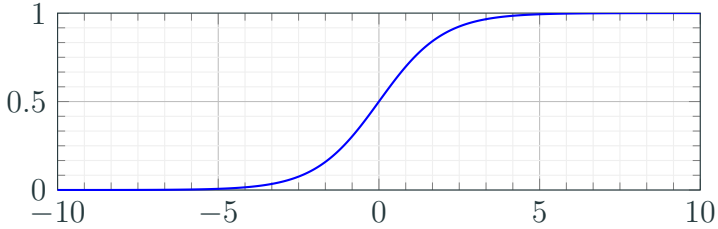
which has an unbounded range $(-\infty, +\infty)$

However, each example's label is $y \in \{0, 1\}$

Sigmoid (logistic) function

Sigmoid function $\sigma(t) : \mathbb{R} \to \mathbb{R}$

$$\sigma(t) = \frac{\exp(t)}{\exp(t)+1} = \frac{1}{1+\exp(-t)}$$



Symmetric function, range of $\sigma(t) \in [0, 1]$,

Sigmoid $\sigma(t) = \frac{1}{1+\exp(-t)}$

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Derivative of sigmoid wrt. its input

$$\begin{aligned}\frac{\mathrm{d}\sigma}{\mathrm{d}t} &= \frac{\exp(t)\cdot(1+\exp(t)) - \exp(t)\cdot\exp(t)}{(1+\exp(t))^2} \\ &= \dots \\ &= \sigma(t)\cdot(1-\sigma(t))\end{aligned}$$

Our binary text classification function

Linear function through sigmoid — log-linear model

$$\hat{y} = \sigma(f(\boldsymbol{x})) = \frac{1}{1 + \exp(-(\boldsymbol{x} \cdot \boldsymbol{w} + b))}$$

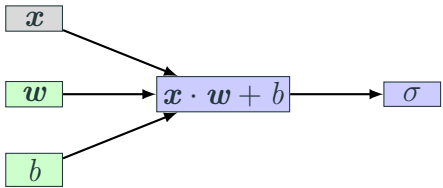

Figure 1: Computational graph; green circles are trainable parameters, gray are inputs

Decision rule of log-linear model

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Log-linear model $\hat{y} = \sigma(f(\boldsymbol{x})) = \frac{1}{1+\exp(-(\boldsymbol{x}\cdot\boldsymbol{w}+b))}$

- Prediction = 1 if $\hat{y} > 0.5$
- Prediction = 0 if $\hat{y} < 0.5$

Natural interpretation: Conditional probability of prediction = 1 given the input $\boldsymbol{x}$

$$\sigma(f(\boldsymbol{x})) = \Pr(\text{prediction} = 1|\boldsymbol{x})$$
$$1 - \sigma(f(\boldsymbol{x})) = \Pr(\text{prediction} = 0|\boldsymbol{x})$$

Binary text classification

Finding the best model's parameters

The loss function

Loss function: Quantifies the loss suffered when predicting $\hat{y}$ while the true label is y for a single example. In binary classification:

$$L(\hat{y}, y) : \mathbb{R}^2 \rightarrow \mathbb{R}$$

Given a labeled training set $(\boldsymbol{x}_{1:n}, \boldsymbol{y}_{1:n})$, a per-instance loss function L and a parameterized function $f(\boldsymbol{x}; \Theta)$ we define the corpus-wide loss with respect to the parameters Θ as the average loss over all training examples

$$\mathcal{L}(\Theta) = \frac{1}{n} \sum_{i=1}^{n} L(f(\boldsymbol{x}_i; \Theta), y_i)$$

Training as optimization

$$\mathcal{L}(\Theta) = \frac{1}{n}\sum_{i=1}^{n} L(f(\boldsymbol{x}_i;\Theta), y_i)$$

The training examples are fixed, and the values of the parameters determine the loss

The goal of the training algorithm is to set the values of the parameters Θ, such that the value of $\mathcal{L}$ is minimized

$$\hat{\Theta} = \underset{\Theta}{\operatorname{argmin}}\, \mathcal{L}(\Theta) = \underset{\Theta}{\operatorname{argmin}}\, \frac{1}{n}\sum_{i=1}^{n} L(f(\boldsymbol{x}_i;\Theta), y_i)$$

Binary cross-entropy loss (logistic loss)

$$L_{\text{logistic}} = -y \log \hat{y} - (1 - y) \log(1 - \hat{y})$$

Partial derivative wrt. input $\hat{y}$

$$\frac{\mathrm{d}L_{\text{Logistic}}}{\mathrm{d}\hat{y}} = -\left(\frac{y}{\hat{y}} - \frac{1 - y}{1 - \hat{y}}\right) = -\frac{y - \hat{y}}{\hat{y}(1 - \hat{y})}$$

Full computational graph

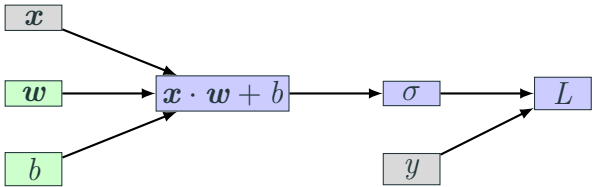

Figure 2: Computational graph; green nodes are trainable parameters, gray are constant inputs

How can we minimize this function?

- Recall Lecture 2: (a) Gradient descent and (b) backpropagation

(Online) Stochastic Gradient Descent

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1: **function** SGD($f(\boldsymbol{x}; \Theta)$, $(\boldsymbol{x}_1, \ldots, \boldsymbol{x}_n)$, $(\boldsymbol{y}_1, \ldots, \boldsymbol{y}_n)$, L)
2: **while** stopping criteria not met **do**
3: Sample a training example $\boldsymbol{x}_i, \boldsymbol{y}_i$
4: Compute the loss $L(f(\boldsymbol{x}_i; \Theta), \boldsymbol{y}_i)$
5: $\hat{\boldsymbol{g}} \leftarrow$ gradient of $L(f(\boldsymbol{x}_i; \Theta), \boldsymbol{y}_i)$ wrt. Θ
6: $\Theta \leftarrow \Theta - \eta_t \hat{\boldsymbol{g}}$
7: **return** Θ

Loss in line 4 is based on a **single training example** $\rightarrow$ a rough estimate of the corpus loss $\mathcal{L}$ we aim to minimize

The noise in the loss computation may result in inaccurate gradients

Minibatch Stochastic Gradient Descent

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function MBSGD($f(\boldsymbol{x};\Theta)$, $(\boldsymbol{x}_1,\ldots,\boldsymbol{x}_n)$, $(\boldsymbol{y}_1,\ldots,\boldsymbol{y}_n)$, L)
    while stopping criteria not met **do**
        Sample m examples $\{(\boldsymbol{x}_1,\boldsymbol{y}_1),\ldots(\boldsymbol{x}_m,\boldsymbol{y}_m)\}$
        $\hat{\boldsymbol{g}} \leftarrow 0$
        for $i = 1$ to m **do**
            Compute the loss $L(f(\boldsymbol{x}_i;\Theta),\boldsymbol{y}_i)$
            $\hat{\boldsymbol{g}} \leftarrow \hat{\boldsymbol{g}}$ + gradient of $\frac{1}{m}L(f(\boldsymbol{x}_i;\Theta),\boldsymbol{y}_i)$ wrt. Θ
        $\Theta \leftarrow \Theta - \eta_t\hat{\boldsymbol{g}}$
    return Θ

Properties of Minibatch Stochastic Gradient Descent

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The minibatch size can vary in size from $m = 1$ to $m = n$

Higher values provide better estimates of the corpus-wide gradients, while smaller values allow more updates and in turn faster convergence

Lines 6+7: May be easily parallelized

Recap

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Take aways

- Tokenization is tricky
- Simplest representation of text as bag-of-word features
- Binary classification as a linear function of words and a sigmoid
- Binary cross-entropy (logistic) loss
- Training as minimizing the loss using minibatch SGD and backpropagation

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