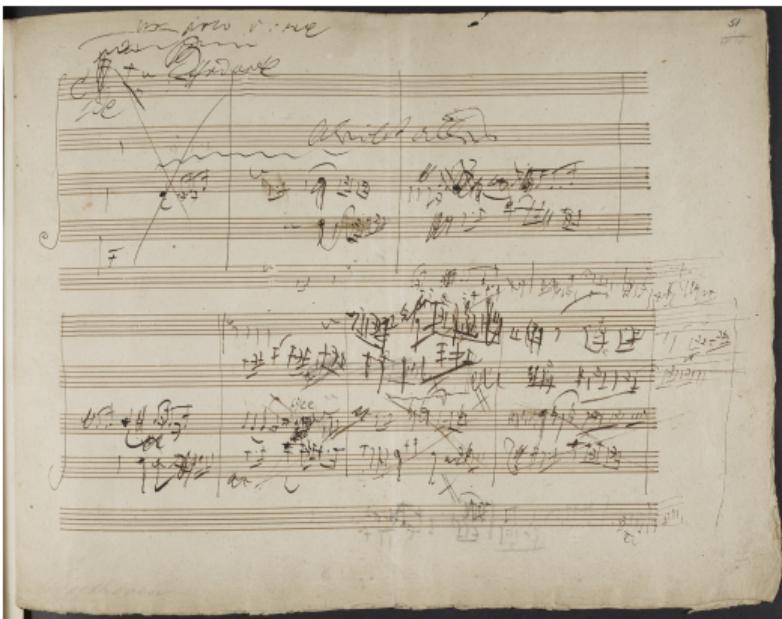


# Beethoven's late string quartets

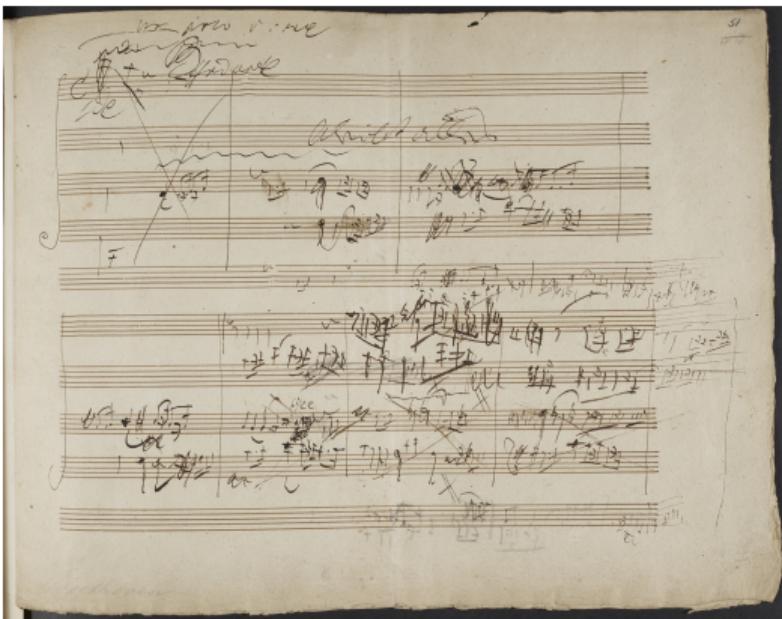
String Quartet No. 14 - Adagio ma non troppo e molto espressivo



[click here for video](#)

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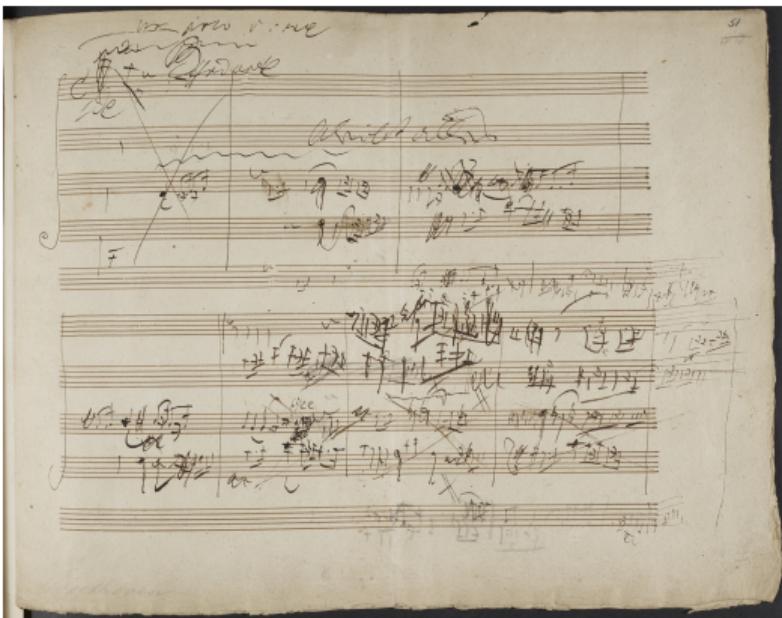


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“indecipherable, uncorrected horrors” – Spohr

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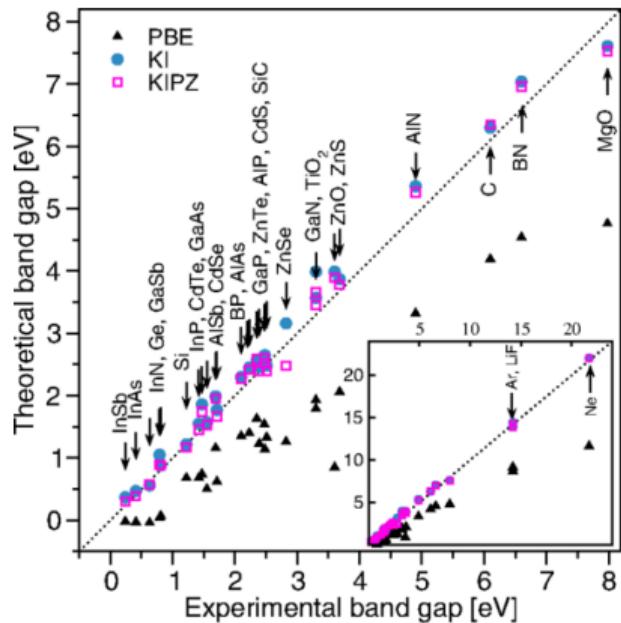
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“indecipherable, uncorrected horrors” – Spohr  
“After this, what is left for us to write?” – Schubert

# Towards black-box Koopmans band structures or: getting lost down a pseudopotential-generation rabbit hole



# Koopmans functionals give accurate band structures



Mean absolute error (eV) across prototypical semiconductors and insulators

	PBE	$G_0W_0$	KI	KIPZ	$QSG\tilde{W}$
$E_{gap}$	2.54	0.56	0.27	0.22	0.18
IP	1.09	0.39	0.19	0.21	0.49

# Koopmans functionals give accurate band structures

	PBE	$G_0W_0^1$	scGW <sup>2</sup>	KI@[PBE,MLWFs]	KIPZ@PBE	exp <sup>3</sup>
$E_g$	0.49	1.06	1.14	1.16	1.15	1.17
$\Gamma_{1v} \rightarrow \Gamma_{25'v}$	11.97	12.04		11.97	12.09	$12.5 \pm 0.6$
$X_{1v} \rightarrow \Gamma_{25'v}$	7.82			7.82		7.75
$X_{4v} \rightarrow \Gamma_{25'v}$	2.85	2.99		2.85	2.86	2.90
$L_{2'v} \rightarrow \Gamma_{25'v}$	9.63	9.79		9.63	9.74	$9.3 \pm 0.4$
$L_{1v} \rightarrow \Gamma_{25'v}$	6.98	7.18		6.98	7.04	$6.8 \pm 0.2$
$L_{3'v} \rightarrow \Gamma_{25'v}$	1.19	1.27		1.19		$1.2 \pm 0.2$
$\Gamma_{25'v} \rightarrow \Gamma_{15c}$	2.48	3.29		3.17	3.20	$3.35 \pm 0.01$
$\Gamma_{25'v} \rightarrow \Gamma_{2'c}$	3.28	4.02		3.95	3.95	$4.15 \pm 0.05$
$\Gamma_{25'v} \rightarrow X_{1c}$	0.62	1.38		1.28	1.31	1.13
$\Gamma_{25'v} \rightarrow L_{1c}$	1.45	2.21		2.12	2.13	$2.04 \pm 0.06$
$\Gamma_{25'v} \rightarrow L_{3c}$	3.24	4.18		3.91	3.94	$3.9 \pm 0.1$
MSE	0.35	0.02		0.01	0.03	
MAE	0.44	0.21		0.14	0.17	

<sup>1</sup> M. Shishkin et al. *Phys. Rev. Lett.* 99.24 (2007), 246403 for  $E_g$  and M. S. Hybertsen et al. *Phys. Rev. B* 34.8 (1986), 5390 for the transitions;

<sup>2</sup> M. Shishkin et al. *Phys. Rev. B* 75.23 (2007), 235102.

<sup>3</sup> O. Madelung. *Semiconductors*. 3rd ed. Berlin: Springer-Verlag, 2004.

# Features of Koopmans functionals

$$E_{\text{Koopmans}}[\rho, \{f_i\}, \{\alpha_i\}] = E_{DFT}[\rho] + \sum_i \alpha_i \left( - \int_0^{f_i} \varepsilon_i(f) df + f_i \eta_i \right)$$

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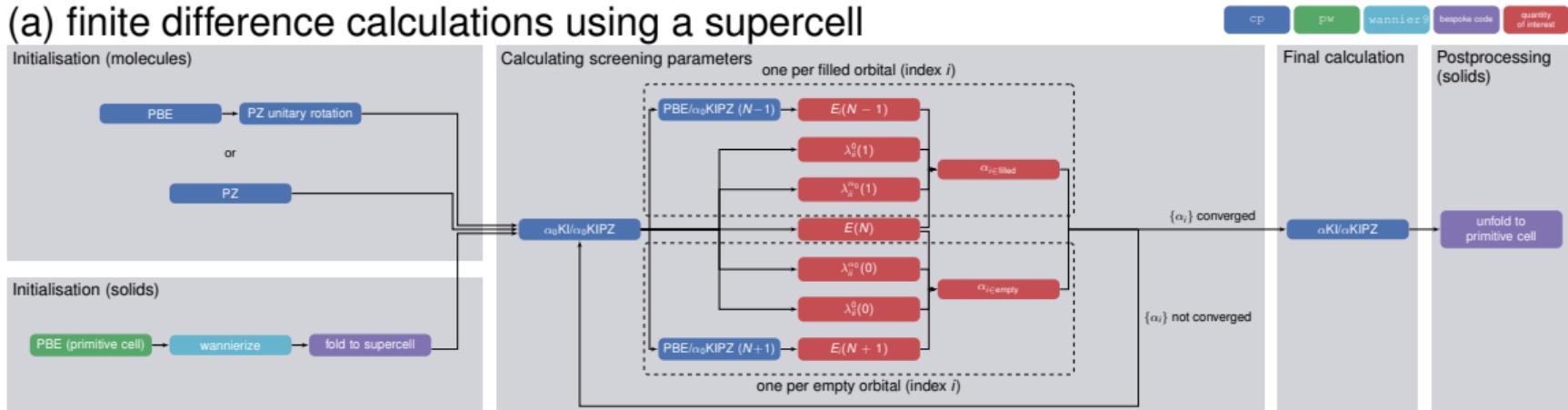
In order to evaluate this functional, one must...

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- calculate the screening parameters  $\{\alpha_i\}$
- construct and diagonalize the Hamiltonian



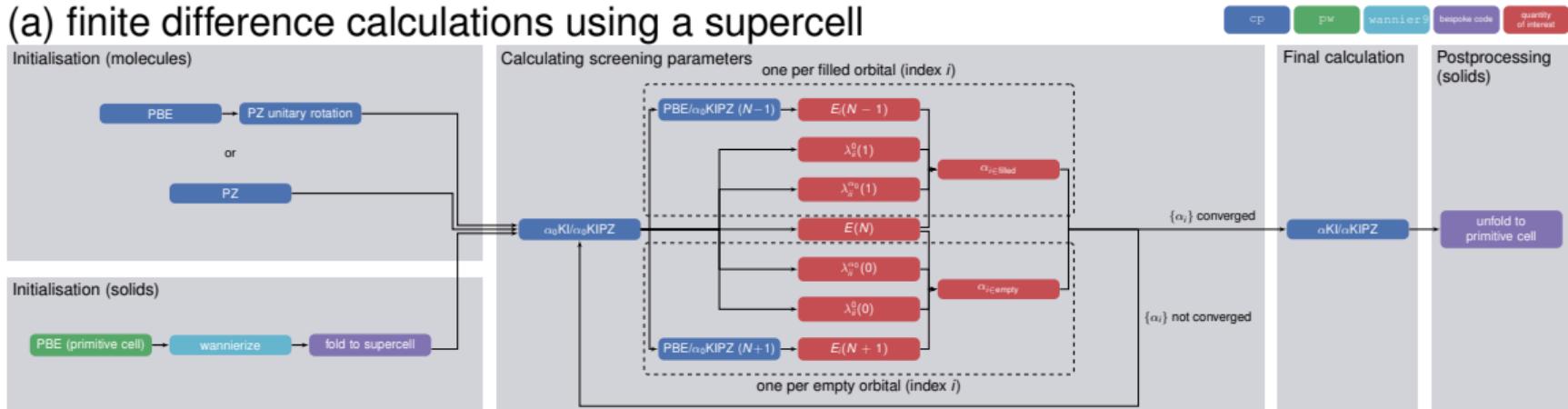
# Workflows

## (a) finite difference calculations using a supercell

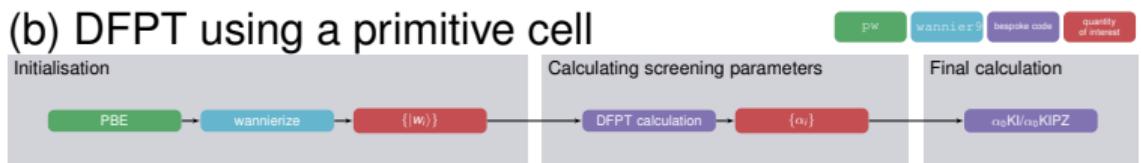


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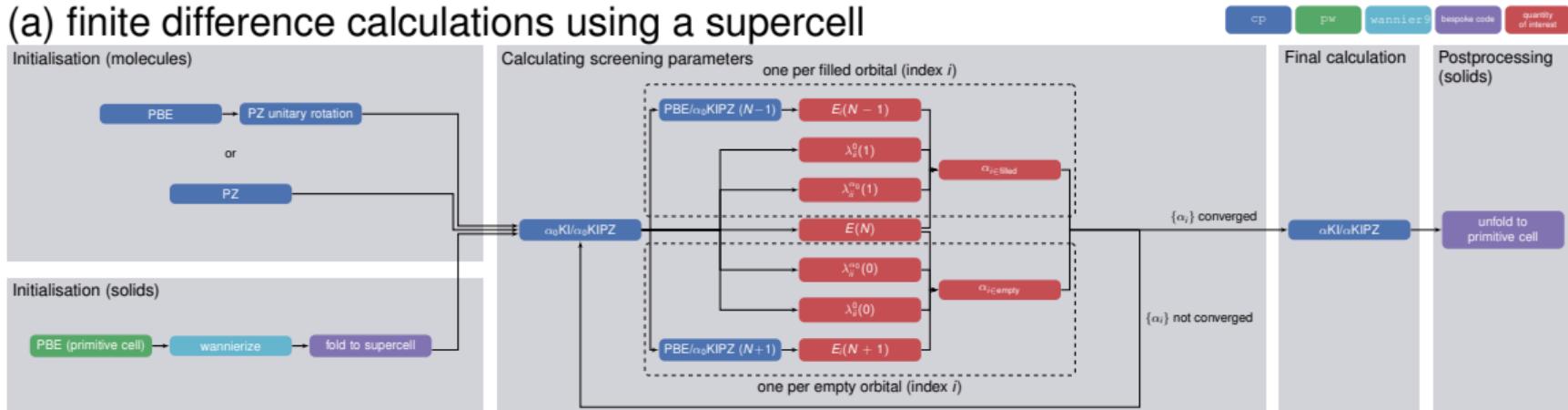


## (b) DFPT using a primitive cell

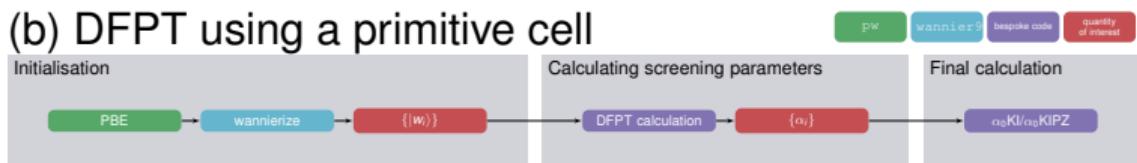


# Workflows

## (a) finite difference calculations using a supercell



## (b) DFPT using a primitive cell



All implemented in Koopmans

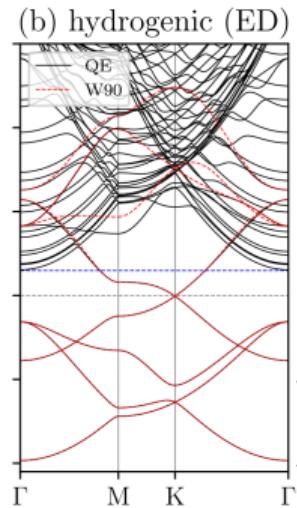
# Workflows

What still stands in our way? Take the example of silicon:

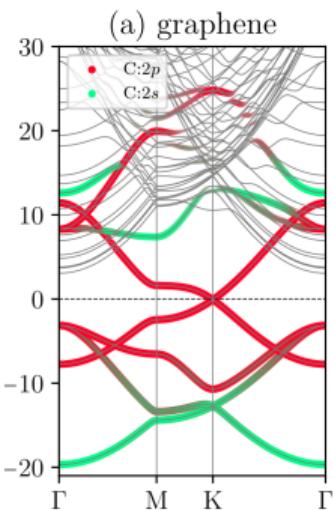
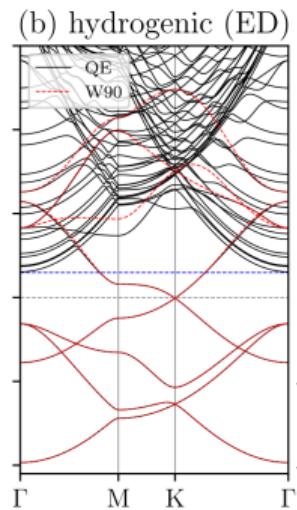
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                      [{"fsite": [0.25, 0.25, 0.25], "ang_mtm": "sp3"}]]],  
        "dis_froz_max": 10.6,  
        "dis_win_max": 16.9}}}}
```

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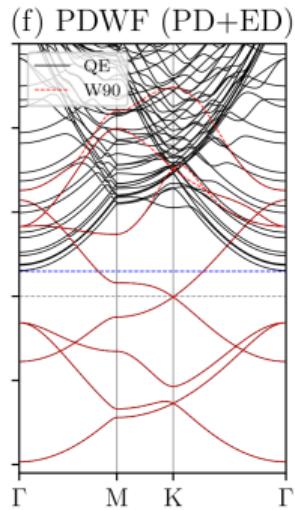
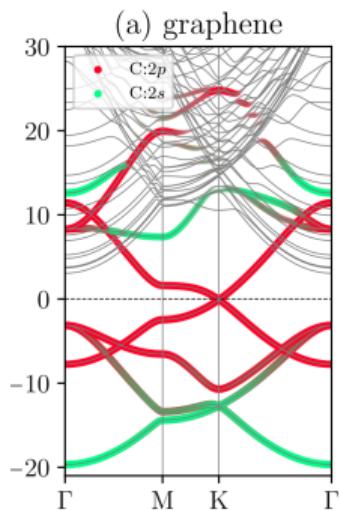
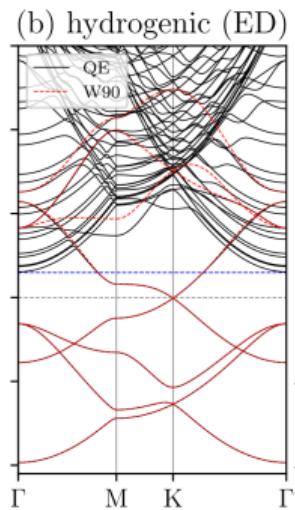


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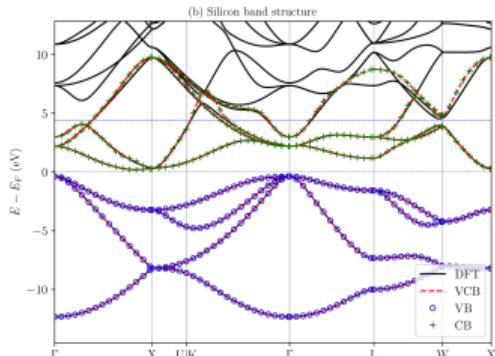


# Automating Wannierization

One very manual step: Wannierization. Can we automate this?



We separate target manifolds via parallel transport to obtain separate occupied and empty manifolds



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- we use them to calculate projectability
- they serve as our initial guesses for the Wannier functions

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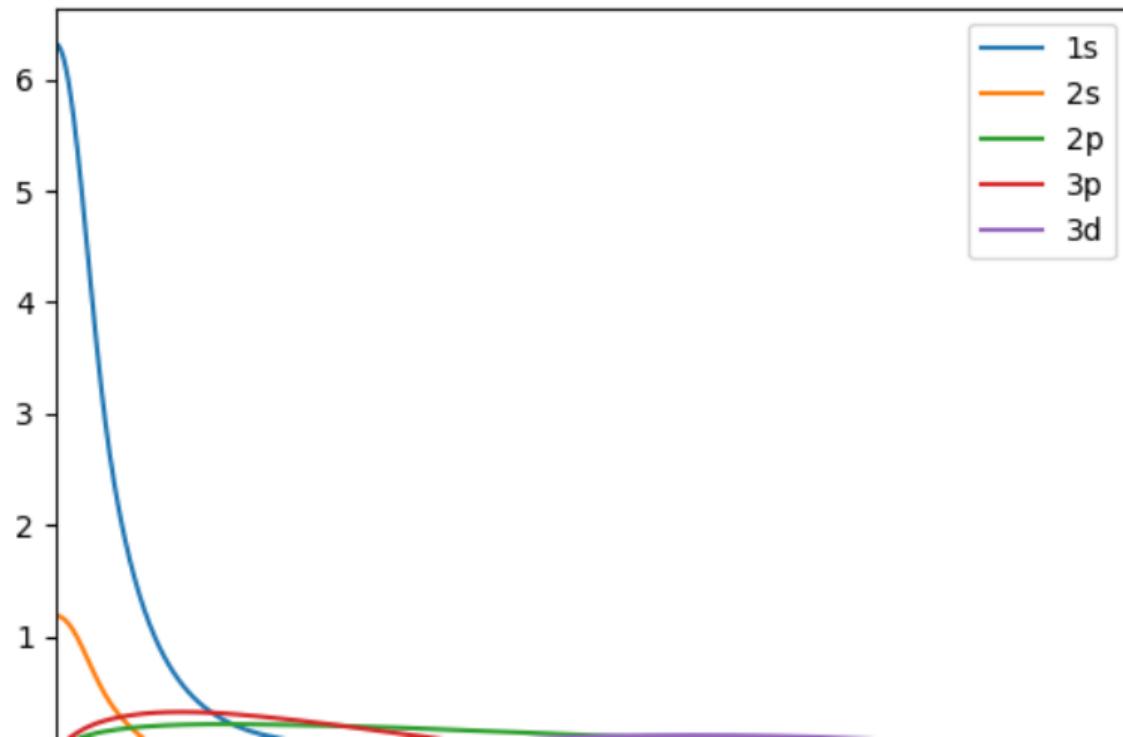
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If we want more Wannier functions, we're gonna need ~~a bigger boat~~ more PAOs...

# Automating Wannierization

Existing strategy: use the PAOs provided by OpenMX



The screenshot shows a GitHub browser interface for the `upf-tools` repository. The URL in the address bar is `github.com/elinscott/upf-tools/blob/main/README.md`. The left sidebar lists various files in the repository, with `README.md` being the active tab, indicated by a blue selection bar at the bottom.

The main content area displays the `upf-tools / README.md` page. At the top, there's a commit card for a minor patch by `elinscott` titled "Minor patch to update README (#2)". Below the commit card is a preview section showing the first few lines of the README:

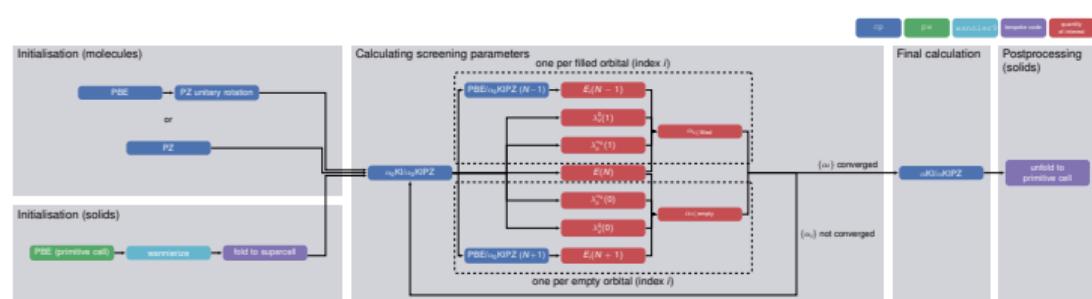
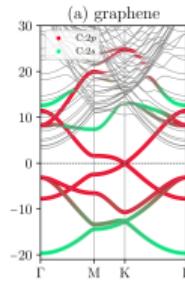
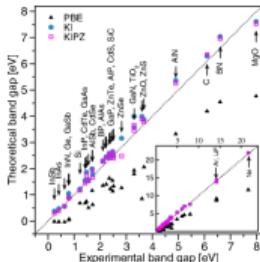
```
upf-tools
Tests passing pypi v0.1.1 python 3.8 | 3.9 | 3.10 | 3.11 license MIT docs passing codecov 79% Cookiecutter snekpack
code style black Contributor Covenant 2.1
```

The README text starts with "Tools for handling `.upf` (Unified Pseudopotential Format) files". Below this, there's a "Getting Started" section with a yellow lightbulb icon and the text "from upf\_tools import UPFDict psp = UPFDict.from\_upf('/path/to/file.upf')". A note below explains that `UPFDict` is a lightweight class that behaves like a dictionary with added functionalities.

At the bottom, there's a "Command Line Interface" section with the note: "The `upf_tools` command line tool is automatically installed. It can be used from the shell with the `--help`" command.

- Most of the infrastructure was from the cookiecutter I used (see my July 2022 GM)
- Publish your code! `upf-tools` was discovered by Marnik and is now used in AiIDA
- Also have unmerged tools for `oncvpsp` input and output files as well as Junfeng's custom `.dat` projector files (perhaps `oncvpsp-tools`) Need to decide on the right home for these...

# Take home messages



- Koopmans functionals yield band structures with comparable accuracy to state-of-the-art GW
- the release of koopmans means non-experts can now use Koopmans functionals in their own research
- work is ongoing to automate the Wannierization bottleneck

# Acknowledgements



Nicola Marzari



Nicola Colonna



Riccardo De Gennaro

Junfeng Qiao



**Swiss National  
Science Foundation**

**MARVEL**  
The logo for MARVEL consists of four red hexagons arranged in a horizontal row, with the second and third hexagons partially overlapping.

NATIONAL CENTRE OF COMPETENCE IN RESEARCH

slides available at  [github/elinscott-talks](https://github.com/elinscott-talks) and on the THEOS wiki