Are planetary waves the same thing as quasi-stationary waves?

In the meteorological literature the analysis of the zonally asymmetric it is very common to analyse

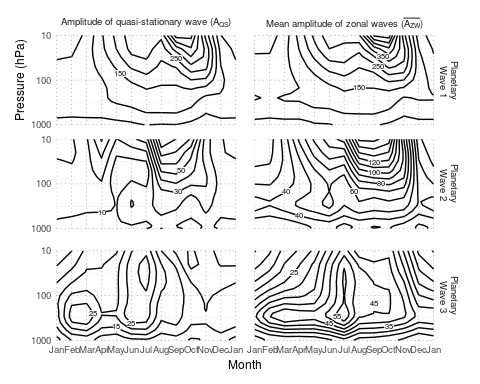
# Introduction

Many atmospheric variables have a strong dependence with latitude, thus it is often natural to decompose a generic variable () into a zonal mean component () and a deviation from it such that

The zonally asymmetric part can further be characterised by a fourier decomposition. These components are sometimes called “zonal waves” or “planetary waves”. The names “stationary waves” or “quasi-stationary waves”, on the other hand, are generally reserved to the zonal asymmetries of the time mean field (). However, these terms are sometimes used interchangeably in the literature (e.g. Rao, Fernandez, and Franchito 2004; Raphael 2004; Kravchenko et al. 2012; Irving and Simmonds 2015; Turner et al. 2017; Lastovicka, Krizan, and Kozubek 2018) which can lead to some confusion.

We define *zonal waves* (ZW) as the zonal asymmetries of each individual “instantaneous” field and *quasi-stationary waves* (QS) as the zonal asymmetries of the mean field. That means that given a set of atmospheric fields with observations, there are ZW fields and 1 QS field for each wave number. While these definitions depend on which are the “instantaneous field” in question (monthly, daily, sub daily, etc…) and the averaging time scale, they illustrate that ZW are properties of the *elements* of the set, while QS are properties of the set as a whole. This is an important distinction with theoretical and methodological implications that is not always appreciated in the literature.

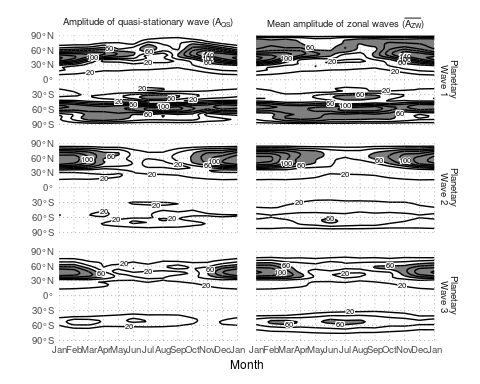
# Zonal waves and stationary waves



Seasonal cycle of amplitude of the geopotential planetary waves 1 to 3 at 60S computed as the amplitude of the mean wave () and as the mean amplitude of the monthly waves (). From monthly NCEP/NCAR Reanalysis, 1950 to 1998. The right column reproduces Figure 3 from .

To illustrate the distinction between ZW and QS, Figure shows the monthly seasonal cycle of amplitude of planetary waves at 60S using monthly fields from the NCEP/NCAR reanalysis (Kalnay et al. 1996) between 1950 and 1998. The left column () is computed by taking the amplitude of the average geopotential field for each month, level and wave number. The right column () reproduces Figure 3 from Rao, Fernandez, and Franchito (2004) and is computed by taking the average amplitude of the 49 individual ZW.

The resulting fields convey different information. First, is always greater or equal than . This is a mathematical necessity (*xx¿Deberia demostrar eso? Vale la pena una demostracion en un material suplementario?xx*) that explains Rao, Fernandez, and Franchito (2004)’s observation that their Wave 1 amplitude was greater than that reported by Hurrell, Loon, and Shea (1998). Secondly, they have different annual cycles and vertical structures. has a strong minimum in the low stratosphere during the austral autumn that is not apparent in . Similarly, the austral winter mid-tropospheric maximum is very well defined in but not so in . Thirdly, the relative importance between each wave number vary. fields show a preponderance of wave 2 over 3 in almost every level and month. However, the QS3 has greater amplitude than QS2 in the first half of the year. In contrast with wave-numbers 2 and 3, and QS1 fields are very similar.



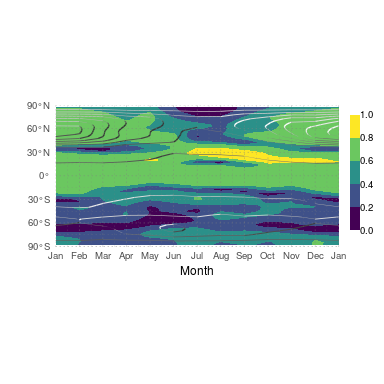
Seasonal cycle of amplitude of the geopotential planetary waves 2 at 300hPa computed as the amplitude of the mean wave () and as the mean amplitude of the monthly waves (). From monthly NCEP/NCAR Reanalysis, 1958 to 2017.

These differences are related to the degree of stationarity of zonal waves and are location-dependent. Figure show the same variables that Figure but in an horizontal section at 300hPa. The contrast between the northern and southern hemispheres is not only evident in the amplitude of the planetary waves, but also in the comparison between and . Specially for wave-numbers 2 and 3, and fields are very similar in the north but they have significant differences in the south.

## Stationarity

Another important consequence of the distinction between and is that the quotient between the two can be used as a measure of stationarity. As an analogy with the constancy of the wind (Singer 1967), planetary wave stationarity can be estimated as

It can be shown that for completely stationary waves and that for completely non-stationary waves (where is the sample size).



Seasonal cycle of stationarity of the 300hPa geopotential QS2 computed using Equation (shaded) and (contours). From monthly NCEP/NCAR Reanalysis, 1958 to 2017.

As an example, Figure shows for QS2 computed using Equation . The southern hemisphere clearly shows a lower degree of QS2 stationarity than the northern hemisphere or the tropics. In the northern mid latitudes there is a seasonal cycle of stationarity that follows the seasonal cycle of (Figure ) with maximum values in boreal summer and minimum in the boreal winter. In the southern hemisphere there is no clear annual cycle and at 60S stationarity and appear to be anticorrelated.

can equivalently be defined as the mean projection of the ZW onto the climatological QS divided by the mean ZW amplitude (*xx de nuevo, esto podría demostrarse en un material suplementario xx*). This definition allows one to construct a time series of by computing a running mean.

While is used –sometimes as (Singer 1967)– in the meteorological literature in the context of wind steadiness, to our knowledge this is the first time it has been applied to the study of atmospheric waves. Furthermore, its statistical properties are not well studied. One problem with , is that its estimation from a finite sample has a positive bias that is inversely proportional to the population stationarity, but its convergence properties are not explored.

## QS activity

Defining quasi-stationary waves as a property of the a climatology of set of atmospheric fields, precludes, in principle, the possibility of quantifying a QS metric that applies to instantaneous fields. It would seem impossible to, for example, construct an time series of QS activity that could be use as a basis for correlations with other variables, compositions or for use in other methodologies. But there are ways of solving this issue.

One possibility to characterise individual fields by their degree of similarity with the climatological QS. Yuan and Li (2008) use Principal Component Analysis on the meridional wind field; the spatial pattern of the leading mode is very similar to the QS3 so a time series can be obtained by projecting each instantaneous field to it. The index produced by Raphael (2004) for the QS3 is similar. While not expressly a measure of similarity, it is sensitive to wave 3 patterns with phase close to the stationary phase and is almost identical to the projection of monthly ZW3 onto the climatological QS3 (with correlation = 0.98)(*xx esto también puede ir al material suplementario, junto con una figura? xx*).

Another way of constructing a time series is to exploit the time scale dependence of QS. By applying a running mean with a suitable window before computing wave amplitudes, one obtains the QS wave amplitude of that window. This is the methodology applied by Wolf et al. (2018) who performed a 15 day low pass filter before computing wave envelopes. Each data time represented, then, the mean field of the set of fields covered the 15 day window an thus waves computed from it are actually QS waves for each of those sets. (*xx no estoy seguro que se entienda bien xx*)

# Conclusions

The fact that zonal waves (ZW) and quasi-stationary waves (QS) are two distinct but related phenomena has both practical and theoretical implications.

First, researchers should be aware of which phenomena they want to study and use the appropriate methods. The mean amplitude of the ZW could be appropriate to study the vertical propagation of Rossby waves, for example. But ZW amplitude could lead to misleading results if used as the basis of local impacts studies because they are probably more influenced by phase effects. For clarity and reproducibility, we encourage researchers in the field to describe if they are using the mean amplitude of the individual waves or the amplitude of the mean wave.

Secondly, comparison between results should also be made having this issues in mind. For instance, Irving and Simmonds (2015) compare their planetary wave activity index with Raphael (2004)’s wave 3 index and conclude that the later cannot account for events with waves far removed from their climatological position. However, by understanding it as an index of QS3 similitude, this limitation becomes a feature, not a bug.

Since planetary waves are generally more stationary in the northern hemisphere, these issues are more critical for studies of the southern hemisphere.

Thirdly, the explorations of both ZW and QS can lead to novel levels of analysis. Here, we showed it can be used to define a metric of stationarity of quasi-stationary waves, but other applications are also possible. Smith and Kushner (2012) used the phase relationship between ZW1 and QS1 to show that linear interference between the QS1 and ZW1 was related to vertical wave activity transport at the tropopause.

*xx me falta un final acá xx*

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