

**Austral Spring Extratropical Southern Hemisphere
zonally assymmetric circulation**

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Abstract abstract

Keywords ·

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1 Introduction

introduction

Agregar párrafo que introduzca el problema del estudio de la circulación extratropical en SH, su variabilidad y sus cambios. Quizás algo también de los impactos. También algo habría que decir de la primavera, ya que solo nos concentramos en esa estación

The large-scale extratropical circulation in the Southern Hemisphere is strongly zonally symmetric, but its zonal departures are highly relevant for surface impacts and could be related to high-impact climate extremes. Zonal asymmetries of extratropical circulation in the Southern Hemisphere strongly modulate weather systems and regional climate through latitudinal transport of heat, humidity, and momentum (Trenberth, 1980).

One typical way of describing the zonally asymmetric circulation is by the amplitude and phase of zonal waves obtained by Fourier decomposition of geopotential height at each latitude (e.g. van Loon and Jenne, 1972; Trenberth, 1980; Turner et al, 2017). This approach suggests that zonal waves 1 and 3 explained most of the variance of the tropospheric extratropical Southern Hemisphere circulation (van Loon and Jenne (1972)). However, this methodology rely on the assumption that the circulation can be meaningfully understood in terms of zonal waves of constant amplitude along a latitude circle. This is not valid for meridionally propagating waves or zonal waves with localised amplitudes. In the case of the wave 3, for example, Trenberth and Mo (1985) observed that it played a role in blocking events, but this was mostly due to increased amplitude of a longitudinally localised wave train instead of an hemispheric-scale zonal wave 3.

Another approach to characterising the Southern Hemisphere circulation is by using Empirical Orthogonal Functions (EOF, also known as Principal Component Analysis). Within the EOF framework, the Southern Annular Mode (SAM) appears as the leading mode of variability of the tropospheric Southern Hemisphere circulation (Fogt and Marshall, 2020) followed by the two Pacific–South American Patterns (PSA) (Mo and Paegle, 2001). The SAM represents a relatively zonally symmetric pattern of alternating low pressures in polar latitude and a ring of high pressures in high latitudes with an embedded wave 3 pattern that is more prominent in the Pacific sector. The PSA1 and PSA2 describe the two out-of-phase sides of a meridionally propagating wave train that originates in the Eastern equatorial Pacific and travels towards the South Atlantic following a great-circle arch along the Antarctic Peninsula. These patterns are derived by applying EOF to temporal anomalies, but Raphael (2003) applied EOF methods specifically to zonal anomalies.

EOFs are more flexible than Fourier decomposition modes in the sense that they can capture oscillation patterns that cannot be characterised by purely sinusoidal waves with constant amplitude. Nonetheless, they are restricted to standing oscillation modes and could not represent properly propagating or phase-varying modes such as zonal waves. A single EOF can also represent a mixture of two or more physical modes. The inability of a single EOF to describe travelling waves is what forces the PSA pattern to be described by

two EOFs. Irving and Simmonds (2016) characterises the Pacific–South American Pattern in a Fourier framework. Being a meridionally propagating mode, the PSA cannot be correctly characterised by Fourier decomposition at each latitude circle, so they reprojected meridional wind fields so that the path of the PSA laid on the equator. On this new projection, they could identify the PSA using Fourier decomposition.

Finally, another, hybrid, methodology commonly used consist on identifying particular features of interest and creating indices using simple methods such as averages and differences. The Marshal SAM Index (Marshall, 2003), for example, tries to characterise the SAM by the average difference of sea level pressure between 40°S and 65°S, following Gong and Wang (1999). Raphael (2004) used a similar methodology to describe the wave 3 in the Southern Hemisphere. Instead of using Fourier to compute the amplitude and phase of the zonal wave, they averaged standardised geopotential height anomalies in three points representing the location of the ridges of the zonal wave 3 of the climatological mean. This is equivalent to an index of the amplitude of the zonal wave 3 that projects into the phase of the zonal wave 3 of the mean field. Similarly, Hobbs and Raphael (2010) propose that the zonally asymmetric circulation in the Southern Hemisphere can be described by the strength and location of two anticyclones located in the sub-Antarctic western hemisphere. These methods are grounded on other methods to identify the centers of action for the described phenomena and can be useful to characterise features that are not readily apparent with Fourier or EOF methods. The use of data of only specific regions or locations makes them suitable for easy computation and for extending into less quality data from the past, but also makes them not very robust and could not capture non-stationary behaviours of the patterns.

Falta un párrafo que deje más claro por qué es necesario considerar un enfoque alternativo y cuál va a ser el beneficio de ello. También agregar qué se estudiara conjuntamente la troposfera y la estratósfera

Falta el objetivo que justifica el uso de la metodología

In this paper we propose using complex Empirical Orthogonal Functions (Horel, 1984) as a robust extension of EOF analysis that is capable of describing rich structures with meridional and zonal propagation, and amplitude modulation such as the PSA. We apply this method to characterise the Spring-time zonally asymmetric circulation of the extratropical Southern Hemisphere.

In Section 2 we describe the methods. In Section ?? we describe the temporal variability and vertical coherence of the indices. In Section 3.1, we analyse the spatial patterns of each complex EOF. In Section 3.2 we study the spatial regressions with geopotential height and temperature. In Section 3.3, we analyse the relationship between cEOF1 and Ozone, and between EOF2 and the Southern Annular Mode and the PSA. In Section 3.4 we look for tropical forcings that explain the variability of each cEOF. Finally, in Section 3.5 we show the relationship between these modes of variability and precipitation in South America and Oceania.

2 Data and Methods

methods

2.1 Data

data

We used monthly geopotential height, air temperature, ozone mixing ratio, and Total Ozone Column (TOC) at 2.5° longitude by 2.5° latitude of horizontal resolution and 37 vertical isobaric levels from ERA5 (Hersbach et al, 2019) for the period 1979 to 2019. Most of our analysis was restricted to the post-satellite era to avoid any confounding factors arising from the incorporation of satellite observations, but we also used the preliminary back extension of ERA5 from 1950 to 1978 (Bell et al, 2020) to look at long-term trends. Streamfunction was derived from ERA5 vorticity at 200 hPa using the FORTRAN subroutine FISHPACK (Adams et al, 1999) and horizontal wave activity fluxes was computed following Plumb (1985). We used Sea Surface Temperature (SST) monthly fields from Extended Reconstructed Sea Surface Temperature (ERSST) v5 (Huang et al, 2017) and precipitation monthly data from the CPC Merged Analysis of Precipitation (Xie and Arkin, 1997), with a 2.5° resolution in latitude and longitude. This rainfall gridded dataset is based on information from different sources such as rain gauge observations, satellite inferred estimations and the NCEP-NCAR reanalysis, and it is available since 1979 to present.

2.2 Methods

methods-1

The study is restricted to the spring season, defined as the September-October-November (SON) trimester. We compute seasonal means for the different variables, averaging monthly values weighted by the number of days in each month. We use 200 hPa level to represent the high troposphere and 50 hPa to represent the lower stratosphere.

The amplitude of the zonal waves was defined through computing the Fourier transform of the spatial field at each latitude circle. We computed the amplitude and phase of the zonal wave 1 by averaging (area-weighted) variables (temperature, geopotential height, ozone mixing ratio and Total Ozone Column) between 75°S and 45°S for each SON and extracting the wave-1 component of the Fourier spectrum. We chose this latitude band because it is wide enough to capture most of the relevant anomalies.

We computed the level-dependent Southern Annular Mode (SAM) index as the leading EOF of year-round monthly geopotential height anomalies south of 20°S at each level for the whole period (Baldwin and Thompson, 2009). We further split the SAM into its zonally symmetric and zonally asymmetric components (S-SAM and A-SAM indices respectively). These indices were obtained by projecting the zonally asymmetric and zonally symmetric part of the SAM spatial pattern onto monthly geopotential height fields, as proposed by Campitelli et al (2021). The Pacific South American patterns (PSA1 and PSA2) were calculated following Mo and Paegle (2001) as the third and fourth

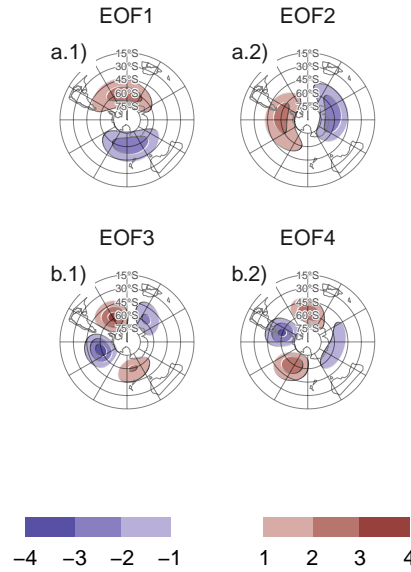


fig:eof-naive
 Fig. 1: Spatial patterns of the leading 4 EOFs of SON zonal anomalies of geopotential height at 50 hPa south of 20°S for the 1979 – 2019 period (arbitrary units).

leading EOF of seasonal mean anomalies for SH 500 hPa geopotential height combining all seasons.

Linear trends were computed by Ordinary Least Squares and the 95% confidence interval was computed assuming a t-distribution with the appropriate residual degrees of freedom (Wilks, 2011).

2.3 Complex Empirical Orthogonal Functions (cEOF)

In traditional EOF analysis zonal waves appear as pairs of EOFs, that could be degenerated representing similar patterns but shifted in phase (Horel, 1984). For instance, Figure 1 shows the leading 4 EOFs of SON geopotential height zonal anomalies at 50 hPa south of 20°S. It is clear that the first two EOFs represent the same zonal wave 1 pattern and the last two represent a same zonal wave pattern with shorter wavenumber and four centers of action shifted by 1/4 wavelength. A similar EOF structure can be seen in 200 hPa (not shown). Since each pair of EOFs seem to represent the same phase-varying structure, it would be desirable to combine them into a single index with amplitude and phase.

Complex Empirical Orthogonal Functions (cEOF) is a useful method to characterise zonal waves, considering phase-varying structures (Horel, 1984). This method involves computing EOF on the analytic representation of the original field. This representation is a complex field in which the real part is the

Table 1: ^{tab:corr-ceof-split}Coefficient of determination (R^2) of the absolute magnitude of complex EOFs between 200 hPa and 50 hPa computing EOF separately for each level. Background colour indicates the value of R^2 .

200 hPa	50 hPa		
	cEOF1	cEOF2	cEOF3
cEOF1	0.28	0.01	0.02
cEOF2	0.00	0.60	0.02
cEOF3	0.00	0.00	0.02

original variable and the imaginary part is the original data shifted by 90° at each spectral frequency – i.e. its Hilbert transform. The Hilbert transform is usually understood in terms of time-varying signal. However, in this work we apply the Hilbert transform to each latitude circle at each moment in time. Since each latitude circle is a periodic domain, this procedure does not suffer from edge effects.

The result of the cEOF methodology is a set of complex spatial patterns and complex time series. The real and imaginary part of each spatial pattern represent two phases wave-like spatial patterns that are in quadrature. The magnitude and argument of each complex time series represent the amplitude and phase of each zonal wave.

The cEOF methodology is applied to SON geopotential height zonal anomalies south of 20°S at 50 and 200 hPa, representing a stratospheric and upper tropospheric level respectively. Table 1 shows the coefficient of determination between time series of the amplitude of each complex EOF (cEOF) across levels. There's a high degree of correlation between the respective cEOF1 and cEOF2 at each level. The spatial patterns of the 50 hPa and 200 hPa cEOFs are also similar (not shown).

Both the spatial pattern similarity and the high temporal correlation of cEOFs computed at 50 hPa and 200 hPa suggest that these are, to a large extent, modes of joint variability. This motivates the decision of performing complex EOF jointly between levels. The computation of the cEOFs was carried out using data from both levels at the same time, therefore, each cEOF has a spatial component that depends on longitude, latitude and level, and a temporal component that depends only on time.

The phase of principal components is defined up to an additive constant. For real principal components, this constant can be either 0 or π , corresponding to a change in sign. For complex principal components, it can be any number between 0 and 2π (Horel, 1984). Since any choice is arbitrary and equally valid, we chose the phase of each cEOF so that the real and imaginary parts are aligned with meaningful phases in our analysis. This procedure does not create a spurious correlation, it only takes whatever relationship that already exist and aligns it with a specific phase.

For the first complex principal component, the phase was chosen so that the time series corresponding to the real part has the maximum correlation

with the zonal wave 1 of Total Ozone Column between 75°S and 45°S. This also nearly minimises the correlation with the imaginary part.

For the second complex principal component, the phase was chosen so that the coefficient of determination between the Oceanic Niño Index (Bamston et al, 1997) and the real part was minimized, which also nearly maximizes the correlation with the imaginary part.

While we compute these complex principal components using data from 1979 to 2019, we extended the complex time series back to the 1950 – 1978 period by projecting monthly geopotential height zonal anomalies standardised by level south of 20°S onto the corresponding spatial patterns.

We performed linear regressions to quantify the association between the cEOFs and other variables. For each cEOF, we create regression maps by computing fitting a multiple linear model involving both the real and the imaginary part. To obtain the linear coefficients of a variable X (geopotential, temperature, precipitation, etc...) with the Imaginary and Real parts of each cEOF we fit the equation

$$X(\lambda, \phi, t) = \alpha(\lambda, \phi) \text{Im}(\text{cEOF}) + \beta(\lambda, \phi) \text{Re}(\text{cEOF}) + X_0(\lambda, \phi) + \epsilon(\lambda, \phi, t)$$

where λ and ϕ are the longitude and latitude, t is the time, α and β are the linear regression coefficients, X_0 and ϵ are the constant and error terms respectively.

We evaluated statistical significance using a two-sided t-test and, in the case of regression maps, p-values were adjusted by controlling for the False Discovery Rate (Benjamini and Hochberg, 1995; Wilks, 2016) to avoid misleading results from the high number of regressions (Walker, 1914; Katz and Brown, 1991).

2.4 Computation procedures

computation-procedures

We performed all analysis in this paper using the R programming language (R Core Team, 2020), using data.table (Dowle and Srinivasan, 2020) and metR (Campitelli, 2020) packages. All graphics are made using ggplot2 (Wickham, 2009). We downloaded data from reanalysis using the ecmwfr package (Hufkens, 2020) and indices of the ENSO with the rsoi package (Albers and Campitelli, 2020). The paper was rendered using knitr and rmarkdown (Xie, 2015; Allaire et al, 2019).

3 Results

results

3.1 cEOF spatial patterns

spatial

To describe the variability of the circulation zonal anomalies, the spatial and temporal parts of the first two leading cEOFs of zonal anomalies of geopotential

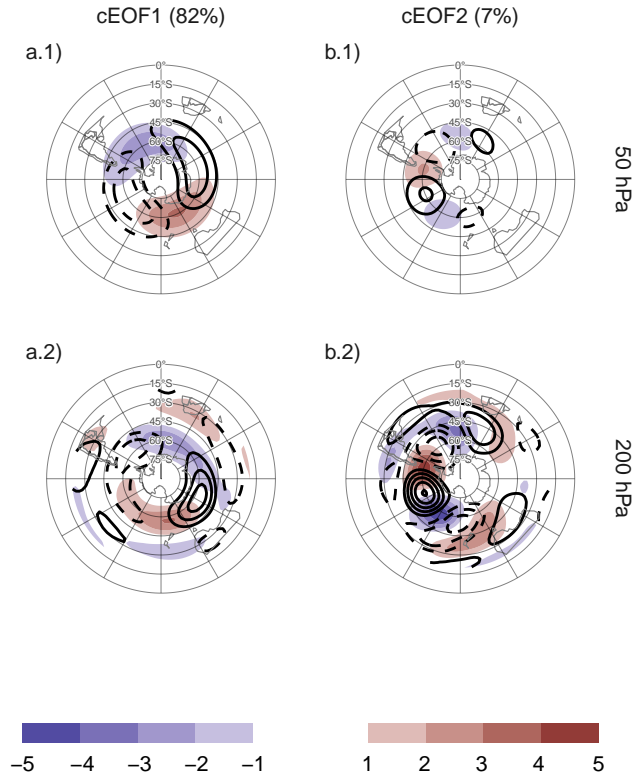


fig:ceofs-1
 Fig. 2: Spatial patterns for the two leading cEOFs of SON zonal anomalies of geopotential height at 50 hPa and 200 hPa for the 1979 – 2019 period. The shading (contours) corresponds to real (imaginary) part. Arbitrary units.

height at 50 hPa and 200 hPa, computed jointly at both levels, are shown in Figures 2 and @ref(fig:extended-series,). The first mode (cEOF1) explains 82% of the variance, while the second mode (cEOF2) explains a smaller fraction (7%). In the spatial patterns (Fig. 2), the real and the imaginary components are in quadrature by construction, so that each cEOF describe a single wave-like pattern whose amplitude and position (i.e. phase) is controlled by the magnitude and phase of the temporal cEOF. The wave patterns described by these cEOFs match the patterns seen in the traditional EOFs of Figure 1.

The first cEOF (Fig. 1 column a) is a hemispheric wave 1 pattern with maximum amplitude at high latitudes. At 50 hPa the Real cEOF1 has the maximum of the wave 1 at 150°E and at 200 hPa, the maximum is located at around 175°E indicating a westerly shift in phase. The second cEOF (Fig. 1 column b) shows also a zonal wave-like structure with maximum amplitude at high latitudes, but with shorter spatial scales. In particular, its dominant structure at both levels is a wave 3 but with larger amplitude in the pacific

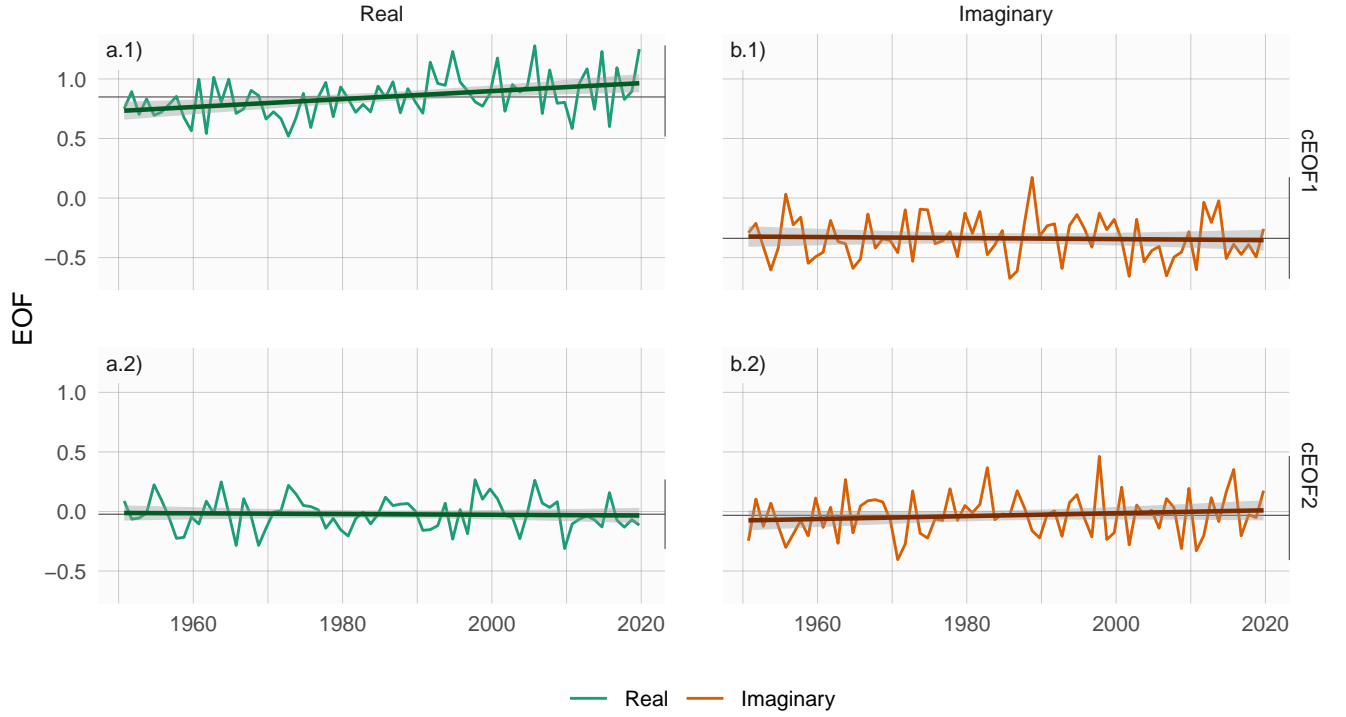


Fig. 3: Time series extended using ERA5 back extended preliminary edition (period 1950 – 1978) and ERA5 (period 1979 – 2019). Dark straight line is the OLS trend. Black horizontal and vertical line mark the mean value and range of each time series respectively.

fig:extended-series

sector. This modulated amplitude is especially apparent at 200 hPa. There is no apparent phase shift, suggesting a rather barotropic structure.

The temporal variability for both components of the cEOF1 have non zero mean (Fig. @ref(fig:extended-series,)). This is due to the fact that the geopotential fields that enter into the cEOFs algorithm are anomalies with respect to the zonal mean, not the time mean. As a consequence, the variability associated with the cEOF1 includes variability that projects onto the mean zonally anomalous field. There are no significant simultaneous correlation between the time series. Both cEOFs show year-to-year variability but show no evidence of decadal variability.

There is a significant upward trend in the real component of cEOF1 (Fig. 3a.1, $p\text{-value} < 0.001$) and no significant trend in any of the complex components of cEOF2. The positive trend in the real cEOF1 translates into a positive trend in cEOF1 magnitude, but not in the phase (not shown).

This long-term change indicates an increase in the magnitude of the high latitude zonal wave 1. A similar observation was made by Raphael (2003), who

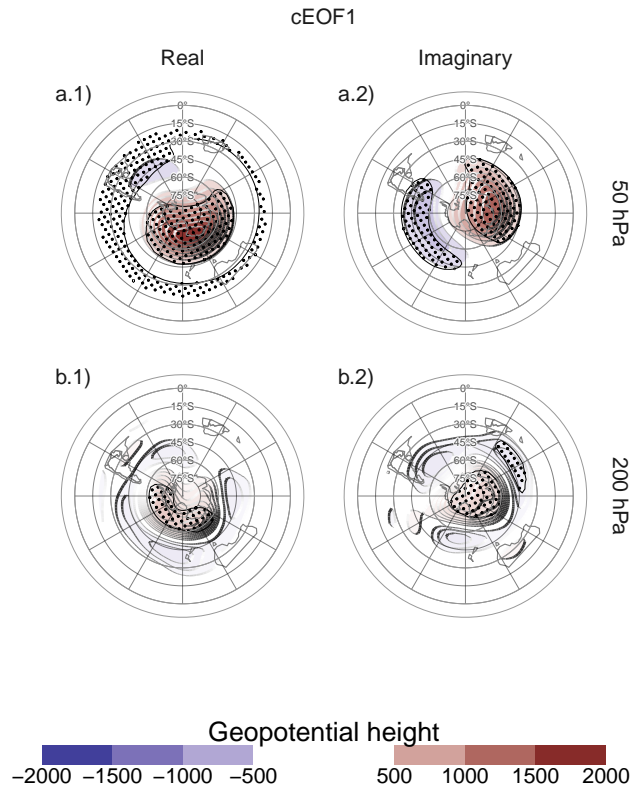


Fig. 4: Regression of SON geopotential height anomalies (meters) with the (column 1) real and (column 2) imaginary parts of the first cEOF for the 1979 – 2019 period at (row a) 50 hPa and (row b) 200 hPa. These coefficients come from multiple linear regression involving the real and imaginary parts. Areas marked with dots have p-values smaller than 0.05 adjusted for False Detection Rate.

detected a step after around 1975 in the leading EOF of August-September-October 500 hPa zonal geopotential height anomalies.

3.2 cEOFs Regressions

The spatial patterns shown in Figure 2 are derived by removing the zonally symmetric circulation, so they might not include all the variability that is actually associated with the cEOF time series. To understand the full geopotential height field changes associated with each cEOF, we computed regression patterns of the full geopotential fields onto each cEOF.

Figure 4 shows regression maps of SON geopotential height anomalies upon cEOF1. At 50 hPa (Figure 4 row a), both the Real and Imaginary cEOF1

are associated with planetary wave 1 patterns, that are 90° off phase. Their phases coincide with the ones shown in Figure 2a.1, with the positive centre of the real cEOF1 located towards the dateline, and the one of the Imaginary cEOF1 located over Eastern Antarctica. However, the Real cEOF1 pattern is substantially altered by the zonally symmetric circulation. Instead of a clear wave 1 pattern, the regression pattern can be better describes as a monopole with its centre displaced from the South Pole.

The regression patterns at 200 hPa (Figure 4 row b) are similarly influenced by the zonally symmetric circulation. It is only possible to distinguish partially the wave 1 pattern in relation with the real cEOF1 (Figure 4b.1). The imaginary cEOF1 shows a much more zonally symmetrical pattern resembling the negative SAM phase.

With the exception of the imaginary cEOF1, it is clear that these patterns are very different than the fully zonally asymmetric versions (Fig. 2), particularly at 200 hPa. Moreover, only in the stratosphere these patterns actually show a distinguishable wave 1 pattern shifted in phase by 90° , suggesting that using the cEOF method is artificially generating a wave structure at 200hPa. Therefore, the magnitude and phase of the cEOF1 are associated with the magnitude and phase of a zonal wave only in the stratosphere. While in the troposphere, they are associated with slightly off-centre monopoles.

Figure 5 shows the regression pattern of geopotential height anomalies upon the cEOF2. Unlike for cEOF1, in this case the regression patterns are similar to the fully zonally asymmetric patterns from Figure 2. Although there are some differences (particularly in 50 hPa), the wave trains identified before are well characterised and patterns associated with the real cEOF2 are 90° out of phase with those associated with the imaginary cEOF2. Zonal wave 3 dominates all fields, but only in the western hemisphere, over the Pacific and Atlantic Oceans. cEOF2 then represents a equivalent barotropic wave train that is very similar to the the Pacific South American Patterns (Mo and Paegle, 2001). Comparing the location of the positive anomaly near 90° W in column b of Figure 5 with Figures 1.a and b from Mo and Paegle (2001), the real cEOF2 can roughly be identified with PSA2, while the imaginary cEOF2 resembles PSA1.

3.3 cEOFs relationship with other variables

other-variables

3.3.1 SAM

sam

To explore the relationship between SAM and the modes described from the cEOF, we compute the coefficient of determination between the cEOFs time-series and the three SAM indices (SAM, A-SAM and S-SAM) at each vertical level (Fig. 6). The SAM index is moderately correlated with the Real cEOF1 in all levels, and with the Imaginary cEOF1 and Imaginary cEOF2 in the troposphere. It is not correlated with the Real cEOF2 at any level.

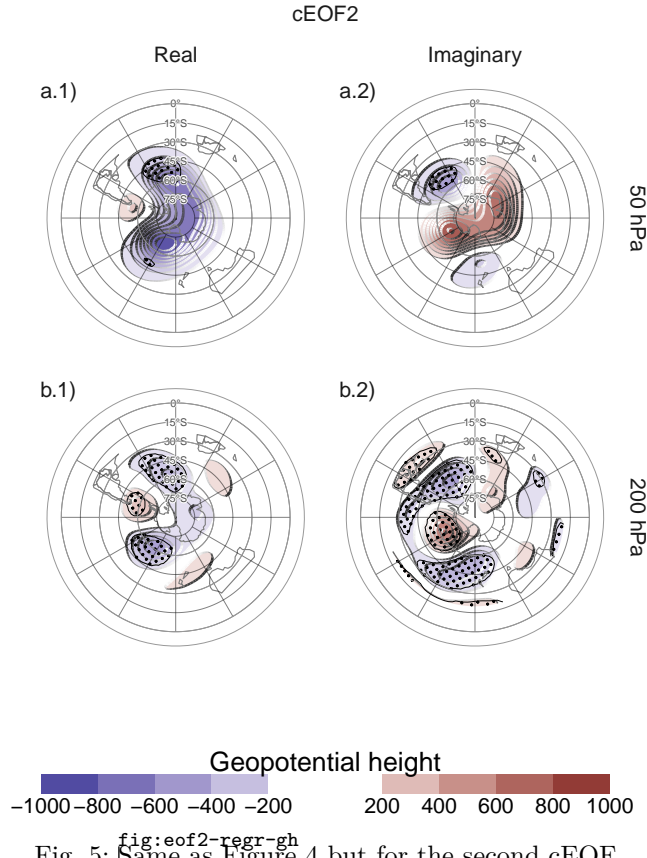


Fig. 5: Same as Figure 4 but for the second cEOF.

The relationship between the tropospheric SAM and cEOF1 is explained entirely by the zonally symmetric component of the SAM as shown by the low and statistically non-significant correlations between the A-SAM and either the Real or Imaginary cEOF1 and the high correlation with the S-SAM below 100 hPa. In the stratosphere, the Real cEOF1 is correlated with both A-SAM and S-SAM, while the Imaginary cEOF1 is highly correlated only with the A-SAM. These correlations are consistent with the regression patterns of geopotential height in Figure 4.

In the case of cEOF2, the moderate correlation between SAM and Imaginary cEOF2 becomes extremely high only when the zonally asymmetric variability of the SAM is considered. The Imaginary cEOF2 and the A-SAM share up to 92% of their variance, reached at 225 hPa (Figure 6.b2). Such extremely high correlation between the asymmetric SAM and the Imaginary cEOF2 suggests that these might be different ways of characterising the same phenomenon.

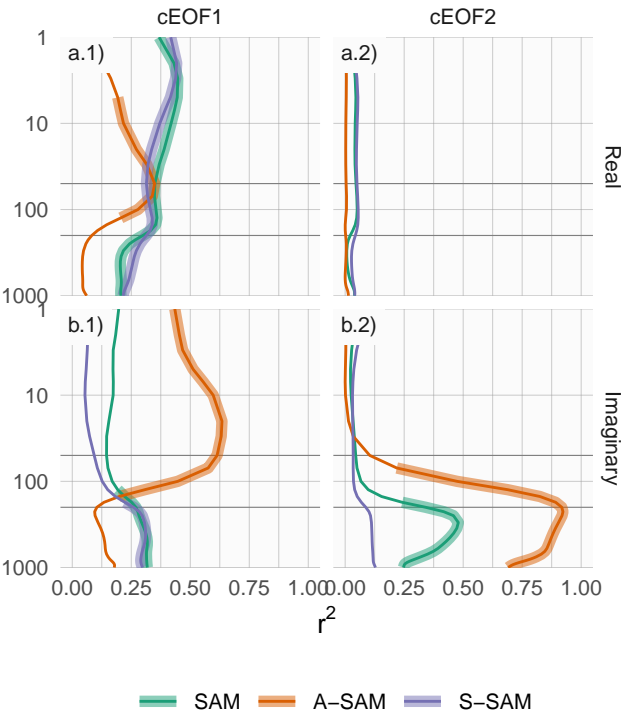


Fig. 6: Coefficient of determination between the real and imaginary part of each cEOF and the SAM, Asymmetric SAM (A-SAM) and Symmetric SAM (S-SAM) indices computed at each level according to Campitelli et al (2021). Thick lines represent estimates with p -value < 0.01 corrected for False Detection Rate (Benjamini and Hochberg, 1995).

Table 2: Correlations between the Real and Imaginary parts of cEOF2 and the PSA1 and PSA2 modes computed as the second and third EOFs of seasonal geopotential height anomalies (following Mo and Paegle, 2001) for the 1979 – 2019 period. 95% confidence intervals in parenthesis. Background colour indicates the value of correlation.

PC	cEOF2	
	Real	Imaginary
PSA1	-0.32 (CI: -0.57 – -0.015)	-0.82 (CI: -0.9 – -0.69)
PSA2	0.81 (CI: 0.67 – 0.9)	-0.062 (CI: -0.36 – 0.25)

3.3.2 PSA

The relationship between PSAs and the modes described from the cEOFs is also studied. Table 2 shows the correlations between the two PSA indices and the timeseries for Real and Imaginary phase of cEOF2. As anticipated by Fig-

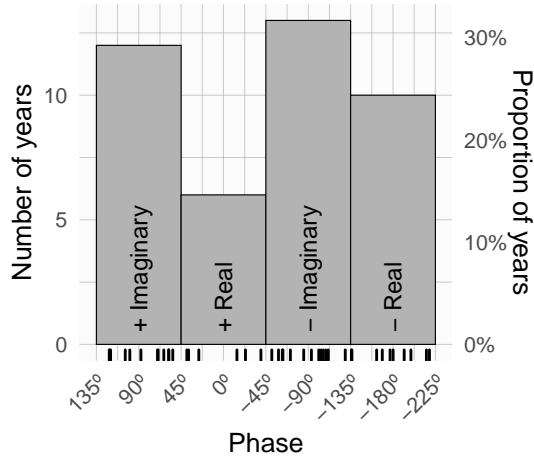


Fig. 7: Histogram of phase distribution of cEOF2 for the 1979 – 2019 period. Bins are centred at 90° , 0° , -90° , -180° with a binwidth of 90° . The small vertical lines near the horizontal axis mark the observations.

ure 5, there is a strong correlation between PSA1 and Imaginary cEOF2, and between PSA2 and Real cEOF2. Conversely, there is no relationship between PSA1 and Real cEOF2, and between PSA2 and Imaginary cEOF2. As a result, cEOF2 represents well both the spatial structure and temporal evolution of the PSA modes, as well as it is possible to make a rather clean association between its two phases and the two PSA modes. So, It could be concluded that the same particular rotation of cEOF2 that maximises the association between cEOF2 parts and PSA modes, is the one which maximises the relationship between ENSO and Imaginary cEOF2.

The reason the conventional EOF analysis arrives at the same separation than our particular cEOF rotation is probably the fact that not all phases are equally frequent. To visualize that, Figure 7 shows an histogram that counts the number of SON years in which the cEOF2 was close to each of the four particular phases (positive/negative Real/Imaginary), with the observations for each season marked as rugs on the horizontal axis. For instance, years with cEOF2 phase within 45° of 0° are nearest the “positive Real” phase. About two thirds of time cEOF2 has a phase similar to either the negative or positive Imaginary phase. It could be seen that Imaginary phase is the most common phase and It is also the direction that has the maximum relationship with ENSO. Therefore, the Imaginary cEOF2 explains more variance than the Real cEOF2 and conventional EOF analysis will tend to separate the two.

The result obtained here is similar to the one obtained by Irving and Simmonds (2016). From their Fourier decomposition of reprojected meridional wind fields *¿En qué región?*, they show that the phase distribution is bimodal and isolate the PSA pattern from the rest of the PSA-like variability by select-

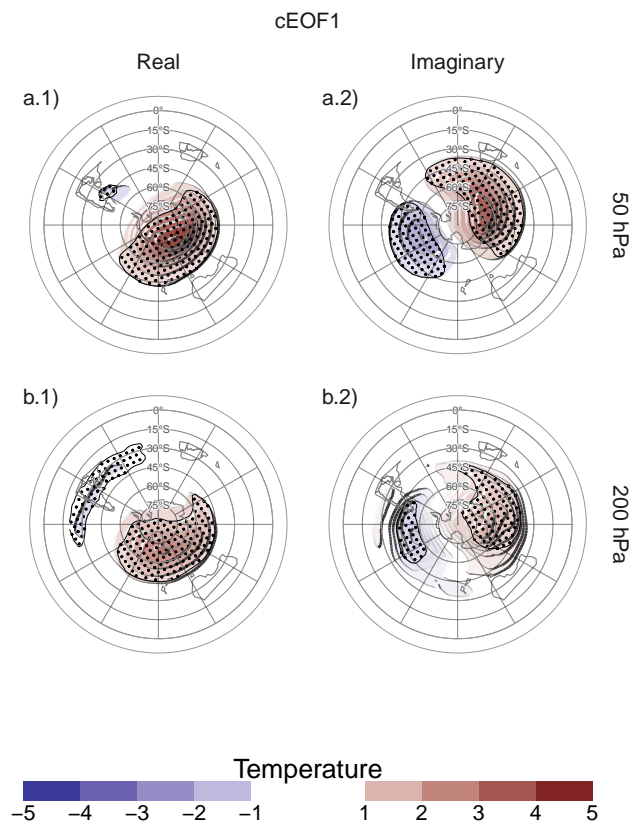


Fig. 8: Same as Figure 4 but for air temperature.

ing events that are near the peaks of the distribution (compare our Figure 7 with their Figure 6).

The advantage of our method is that it is much simpler to implement, it provides magnitude and phase naturally, and it facilitates the description of this mode as a propagating wave instead of as standing oscillation. As a consequence, the cEOF2 offers an alternative way of representing the PSA which has several advantages over using the second and third EOFs.

3.3.3 Temperature and Ozone

The relation between cEOFs and temperature was also evaluated. Figure 8 shows regression patterns of air temperature at 50hPa and 200hPa onto cEOF1. In both levels, the Real cEOF1 is associated with positive monopole over the South Pole with its centre moved slightly towards 150°E (Fig. 8 column 1). On the other hand, the regression maps on the Imaginary cEOF1 show a more clear wave 1 pattern with its maximum around 60°E. The distribution

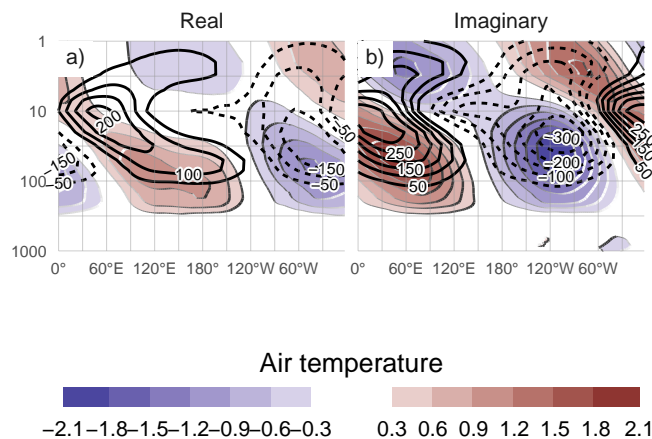


Fig. 9: Regression of SON anomalies of mean air temperature (shaded, Kelvin) and ozone mixing ratio (contours, negative contours with dashed lines, labels in parts per billion by mass) averaged between 75°S and 45°S with the (a) real and (b) imaginary parts of the first cEOF for the 1979 – 2019 period.

of temperature regression coefficients at 50 hPa and at 200 hPa mirror the geopotential height regression maps at 50 hPa (Fig. 4).

Figure 9 shows the vertical distribution of the regression coefficients on cEOF1 from zonal anomalies of air temperature and zonal anomalies of ozone mixing ratio averaged between 75°S and 45°S. *Deberias aclarar qué significa la terminología que estas utilizando. Lo puedes hacer en los métodos y ya queda para todo el texto.* Temperature zonal anomalies associated with cEOF1 show a clear wave 1 pattern for both real and imaginary components throughout the atmosphere above 250 hPa with a change in sign above 10 hPa. Following hydrostatic balance, this is the level in which the geopotential anomaly have maximum amplitude (not shown).

The maximum ozone anomalies are co-located with the minimum temperature anomalies above 10 hPa and with the maximum temperature anomalies below 10 hPa (Fig. 9)). Therefore, the ozone zonal wave 1 is anticorrelated with the temperature zonal wave 1 in the upper stratosphere, and directly correlated in the upper stratosphere. This change in phase is observed in ozone anomalies forced by planetary waves that reach the stratosphere. In the photochemically-dominated upper stratosphere, cold temperatures inhibit the destruction of ozone, and the advectively-dominated lower stratosphere, ozone anomalies are 90° out of phase with horizontal and vertical transport, which is 90° out of phase with temperature anomalies (Hartmann and Garcia, 1979; Wirth, 1993; Smith, 1995).

The regression maps of cEOF1 with fields of Total Ozone Column (TOC) (Fig. 10) show zonal wave 1 patterns in TOC associated with both phases of cEOF1. Climatologically, the springtime Ozone minimum is located off the South Pole and towards the Weddell Sea (Grytsai, 2011). Thus, the Real

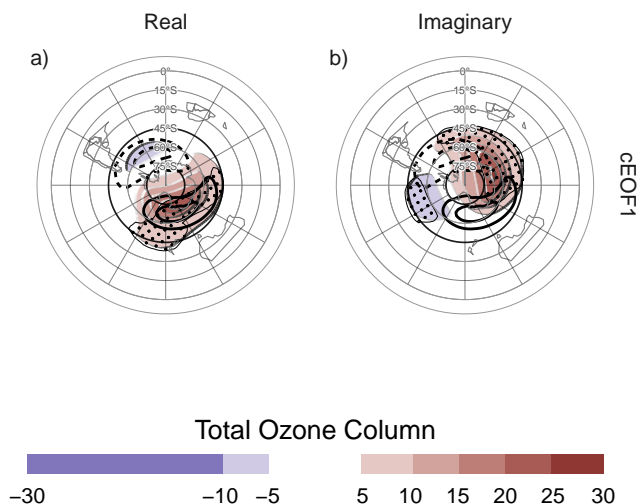


Fig. 10: Regression of SON mean Total Ozone Column anomalies (shaded, Dobson Units) with the (a) real and (b) imaginary parts of the first cEOF for the 1979 – 2019 period. On contours, the mean zonal anomaly of Total Ozone Column (negative contours in dashed lines, Dobson Units). Areas marked with dots have p-values smaller than 0.05 adjusted for False Detection Rate.

cEOF1 regression pattern (Figure 10a) coincides with the climatological position of the ozone hole while the one for the Imaginary cEOF1 is shifted by 90° .

There is a close spatial relationship between amplitudes and phases of the cEOF1 and TOC planetary wave 1 between 75°S and 45°S . The correlation between the amplitude of both indices is 0.77 (CI: 0.61 – 0.87) the overall correlation between the zonal wave 1 of ozone and cEOF1 (computed as the mean cosine of the difference in phase) is 0.87 (CI: 0.77 – 0.93). As expected from the location of regressions in Figure 10, the Real cEOF1 drives the relationship of amplitudes and the Imaginary cEOF1 drives the relationship of phases between the timeseries (not shown).

3.4 Tropical sources

The connections between cEOFs and Tropical sources is also assessed. Figure 11 shows the regression maps of Sea Surface Temperatures (SST) and Streamfunction at 200 hPa respectively upon cEOF2. The Imaginary cEOF2 is associated with strong positive SST anomalies on the Central Pacific and negative anomalies over an area across the North of Australia and New Zealand, the South Pacific Convergence Zone (SPCZ) (Figure 11.a2). This pattern is almost canonically positive ENSO (Bamston et al, 1997) and indeed, the correlation between the Imaginary cEOF2 and the Oceanic Niño Index (Bamston

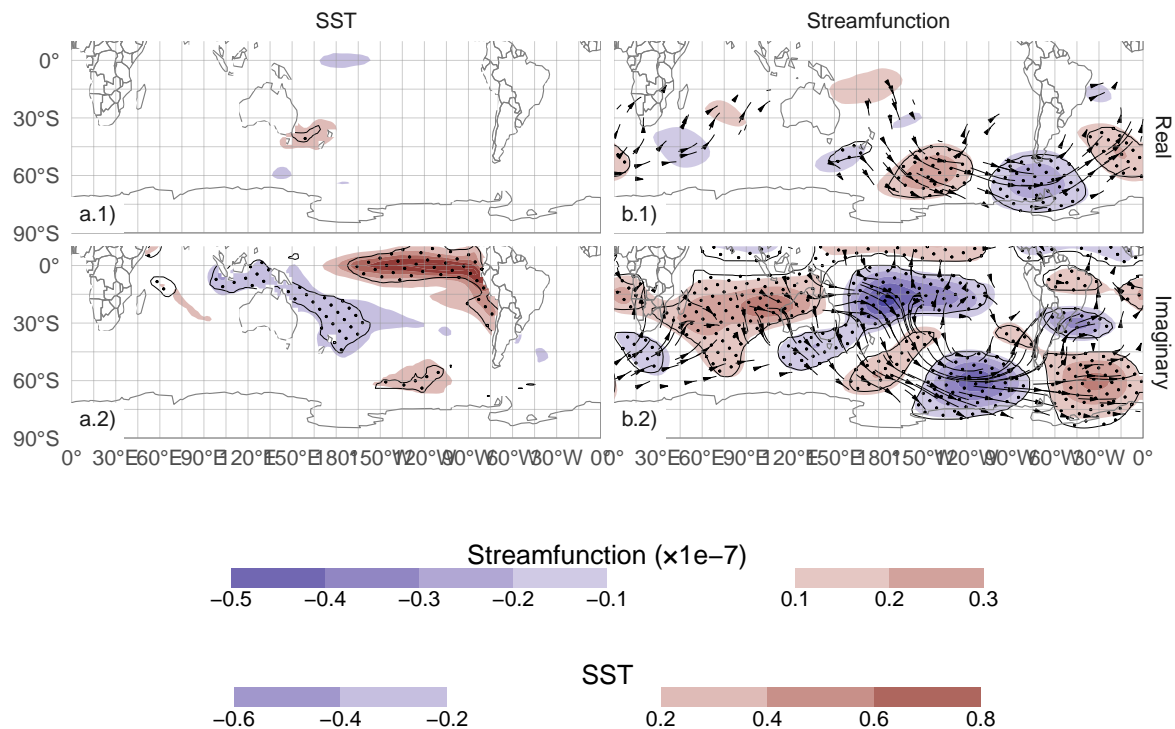


Fig. 11: Regression maps of cEOF2 with SST (column a) and streamfunction zonal anomalies (shaded) with their corresponding activity wave flux (vectors) (column b). Areas marked with dots have p-values smaller than 0.01 adjusted for FDR.

fig:sst-psi-2

et al, 1997) is very high 0.76 (CI: 0.59 – 0.87). Besides, the Imaginary cEOF2 is associated with strong wave-like streamfunction anomalies emanating from the tropics (Figure 11.b2). This is consistent with the effect of ENSO on the extratropics: SST anomalies initiate anomalous convection that excites Rossby waves that propagate meridionally towards higher latitudes (Mo, 2000).

Revisa los labels de la colorbar para la figura 13. Además ojo que solamente sirven para la columna a, faltan los correspondientes a la streamfunction y el vector de referencia para wave flux

Since the Real cEOF2 represents just a different phase of the same wave train, it would be expected to show a similar forcing pattern to the Imaginary cEOF with a slight translation of its location. However, Figure 11.a1 and b1 show that the Real cEOF2 is not associated either with any significant SST nor streamfunction anomalies in the tropics. The correlation between the Real cEOF2 and ENSO is also not significant (0.00025 (CI: -0.31 – 0.31)). This lack of tropical signal suggests different natures of the different phases of the Real cEOF2 wave train, which has the maximum amplitudes in the surroundings of southern South America.

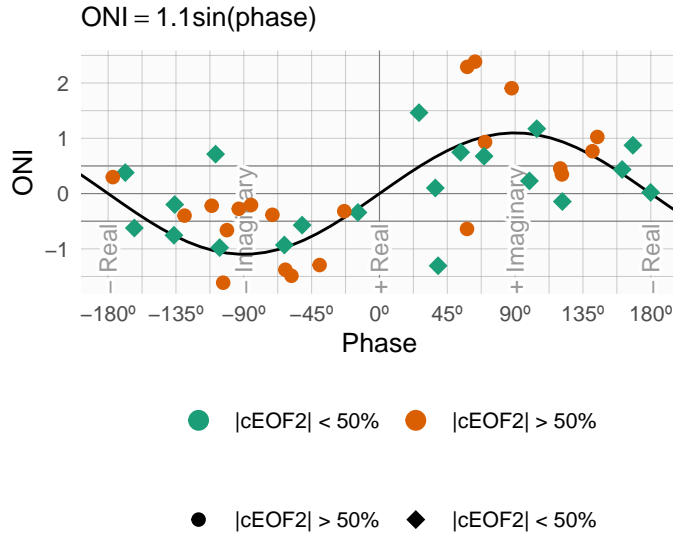


fig:enso-phase
 Fig. 12: ONI plotted against cEOF2 phase for the 1979 – 2019 period. Years with magnitude of cEOF2 greater or smaller than the 50th percentile are shown as orange circles and green diamonds respectively. Black line is the fit $ONI \sim \sin(\text{phase})$ computed by weighted OLS using the magnitude of the cEOF2 as weights.

To better explore the relationship between tropical forcing and phase of the cEOF2, Figure 12 shows the ONI index against the cEOF2 phase for each SON trimester between 1979 and 2019, highlighting years in which the magnitude of cEOF2 is above the median. In years with positive ONI, the phase of the cEOF2 is mostly around $+90^\circ$ (corresponding with positive imaginary part) and vice versa. In years with near neutral ENSO, the phase of the cEOF2 is much more variable. The black line in Figure 12 is a sinusoidal fit of the relationship between ONI and cEOF2 phase. The r^2 corresponding to the fit is 0.56, with p-value < 0.001 , indicating a quasi-sinusoidal relation between these two variables.

Furthermore, Figure 12 suggest that higher amplitude cEOF2 years tend to coincide with stronger ENSO years. The correlation between the absolute magnitude of the ONI and the magnitude of the cEOF2 is 0.45 (CI: 0.17 – 0.67). This relationship, however, appears to be driven only by the three years with strongest ENSO events in the period (2015, 1997, and 1982) which also coincide with the three years with strongest cEOF2 magnitude. If those years are removed, the correlation becomes non-significant (0.047 (CI: -0.28 – 0.36)). Furthermore, even when using all the datapoints, the Spearman correlation –which is robust to outliers– is also non-significant (0.2, p-value= 0.21). Therefore, the relationship between the magnitude of the cEOF2 train wave and ONI remains uncertain.

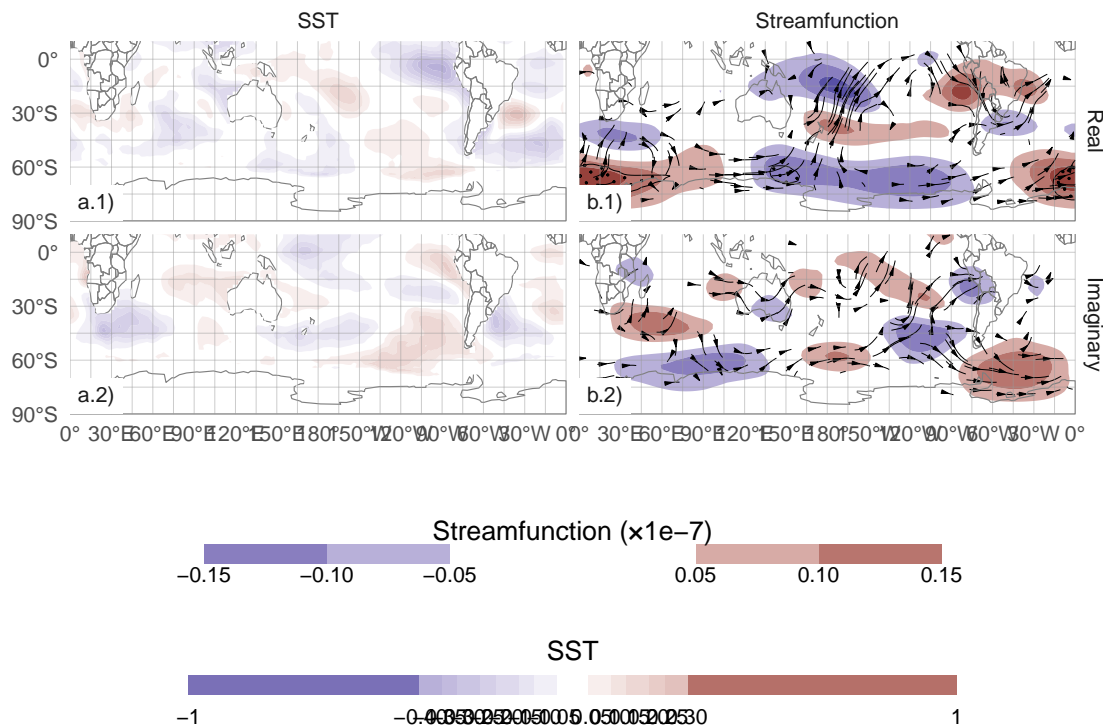


Fig. 13: Same as Figure 11 but for cEOF1.

fig:sst-psi-1

It could be concluded that the wave train represented by cEOF2 can be both part of the internal variability of the extratropical atmosphere or forced by tropical SSTs. In the former case, the wave train has little phase preference. However, when cEOF2 is excited by tropical SST variability, it tends to remain locked to the imaginary phase. This explains the relative overabundance of years with cEOF2 near positive and negative imaginary phase in Figure 7.

Figure 13 shows SST and streamfunction regression maps for cEOF1. Unlike the cEOF2 case, there is no significant pattern of SST anomalies associated with either the Real or Imaginary cEOF1. Consistently, streamfunction anomalies do not show any tropical influence. Instead of that, the real and imaginary CEOF1 are associated with zonally wave activity fluxes in the extra-tropics around 60°S, except for an equatorward flow from the coast of Antarctica around 150°E in the real component.

3.5 Precipitation

precipitation

The influence of cEOFs variability in continental rainfall of extra-tropical Southern Hemisphere is also explored. We focus on South America and Oceania sectors because there are no relevant signals in southern Africa (not shown).

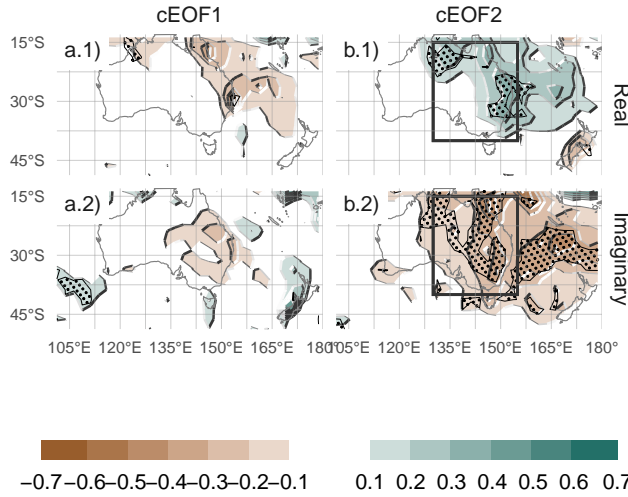


fig:pp-oceania
 Fig. 14: Regression of SON mean precipitation anomalies in Oceania (mm per day, shaded) and (column a) cEOF1 the (row 1) Imaginary and (column 1) Real phase. For the 1979 – 2019. Areas marked with dots have p-values smaller than 0.05 adjusted for False Detection Rate.

The precipitation anomalies in Oceania associated with cEOF1 are weak and not statistically significant (Figure 14 column a) whereas EFO2 is associated with large and widespread anomalies. The Real cEOF2 is associated with positive seasonal anomalies in Northern and Eastern Australia, and negative ones over New Zealand, while precipitation anomalies associated with Imaginary cEOF2 are negative over all Eastern Australia. Again, these negative anomalies are similar to the springtime precipitation anomalies observed in relation with the Asymmetric SAM (Campitelli et al, 2021) and ENSO (Cai et al, 2011).

To better understand the relationship between precipitation anomalies over Eastern Australia and the cEOF2, Figure 15 plots precipitation anomalies averaged over Eastern Australia (box in Figure 14) as a function of cEOF2 phase. The black line shows a sinusoidal fit, whose coefficients are fitted by weighted least squares using the magnitude of the EFO2 as weight. The r^2 corresponding to the fit is 0.41 (p-value < 0.001). There is a strong relationship between the phase of the cEOF2 and precipitation anomalies in Eastern Australia, but the Real and Imaginary phases we chose are not exactly aligned with the direction that maximises this relationship. To perform a more in-depth analysis of the relationship between this pattern and precipitation in this region, it would be recommended to align one of the axis (either the Real or the Imaginary) to the phase that maximises the described relationship.

Figure 16 shows regression maps of seasonal precipitation with each cEOF in South America. cEOF1 is associated with slight decreases in precipitation in Southern Brazil and Paraguay, although these are not statistically significant

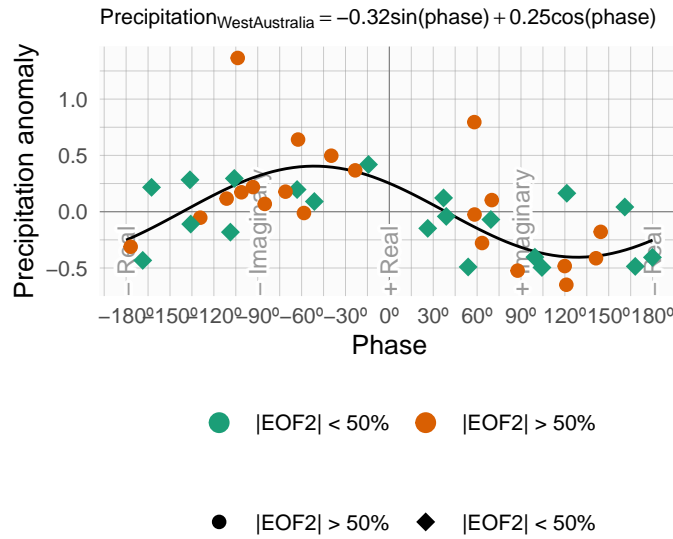


Fig. 15: Same as Figure 12 but for precipitation anomalies averaged between 130°E and 155°E and 40°S and 15°S (box shown in Figure 14 column b) in $\frac{\text{mm}}{\text{day}}$. Black line is the fit precipitation $\sim \sin(\text{phase}) + \cos(\text{phase})$ computed by weighted OLS using the magnitude of the cEOF2 as weights.

(Fig. 16 column a). The strongest precipitation regression coefficients are the ones associated with the Imaginary cEOF2. The positive regression coefficients on Southeastern South America (SESA) and Central Chile, and negative ones over South Atlantic Convergence Zone is a well-known springtime precipitation signature of ENSO (Cai et al, 2020) and it is also similar to the precipitation anomalies associated with the A-SAM (Campitelli et al, 2021). This is not surprising considering the close relationship between the ONI, the A-SAM index and the Imaginary cEOF2 shown previously, but further consolidates the identification of this mode with the PSA pattern. On the other hand, the Real cEOF2 is associated with negative precipitation anomalies in a smaller area of SESA. Resembling the relationship between ONI and the phase of cEOF2 (Fig. 12), there is a cEOF2 phase dependence of the precipitation anomalies in SESA (not shown). These variables could be related with a significant sinusoidal fit that has a coefficient of determination of 0.27 (p-value = 0.0022).

4 Conclusions

conclusions

Al igual que en la introducción, te falta establecer más claro el objetivo, después iría lo que escribiste.

We studied the two leading modes of co-variability of September-October-November tropospheric and stratospheric zonal anomalies by applying complex Empirical Orthogonal Functions.

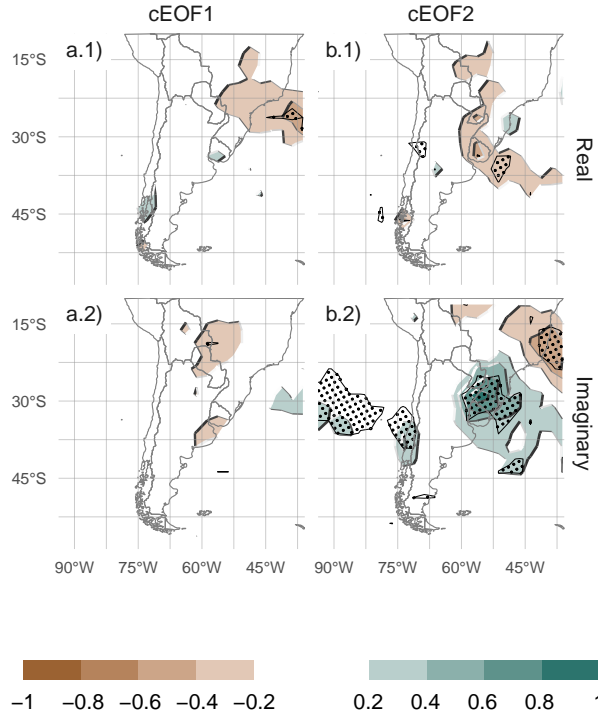


fig:pp-america
Fig. 16: As Figure 16 but for South America

The first complex EOF represents the variability of the zonal wave 1 in the stratosphere, but represents a more zonally symmetric monopole in the troposphere. There is a statistically positive trend in the magnitude of this cEOF, which is consistent with previous studies which showed secular changes in springtime wave-1-like patterns (e.g. Raphael, 2003). This mode is closely related to anomalies in Total Ozone Column.

The second complex EOF represents a wave-3 pattern with maximum magnitude in the Pacific sector. Essentially, it is an alternate representation of the PSA1 and PSA2 patterns (Mo and Paegle, 2001). We show that the Imaginary cEOF2 can be identified with the PSA1 and the Real cEOF2 with the PSA2. This cEOF prefers a phase aligned with the Imaginary cEOF2. This is because when ENSO is active, it forces the cEOF2 to be in the Imaginary phase. When ENSO is neutral, the cEOF2 is still active, but with no particular preferred phase. This mirrors the results of Cai and Watterson (2002), who showed that the CSIRO Model can create PSA-like variability even in the absence of ENSO forcing (with a climatological run), but the variability of one of the PSA modes was enhanced when adding the ENSO signal. The magnitude of the cEOF2 appears not to be related to the magnitude of ENSO, except for the three strongest ENSO events in the period which coincide with the three strongest cEOF2 years.

We further show that the Imaginary cEOF2 is closely related to the Southern Annular Mode in the troposphere. In fact, it has a closer resemblance of the zonally asymmetric portion of the SAM.

This raises the possibility that the asymmetric component of the SAM is actually a statistical contamination of the PSA mode.

Precipitation anomalies in South America associated with the Imaginary cEOF2 show a clear ENSO-like impact, with positive anomalies in South-Eastern South America, negative anomalies in Southern Brazil and positive anomalies in central Chile. Precipitation anomalies associated with the Real cEOF2 are low and not statistically significant, showing that the Imaginary phase is optimally aligned with the direction of maximum precipitation impacts.

On the other hand, over Australia, both the Real and Imaginary phase are associated with significant precipitation anomalies, and we further show that the direction of maximum impact is not aligned with our chosen rotation of cEOF2. However, this underscores the benefit of using complex EOF, since it would be trivial to rotate it.

Debería cerrarse con algún párrafo que diga qué tiene de bueno trabajar con esta metodología y qué permitiría hacer a futuro (se puede poner que sería deseable extenderlo a otras estaciones, etc.)

Code availability

code-availability

A version-controlled repository of the code used to create this analysis, including the code used to download the data can be found at <https://github.com/eliocamp/shceof>.

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