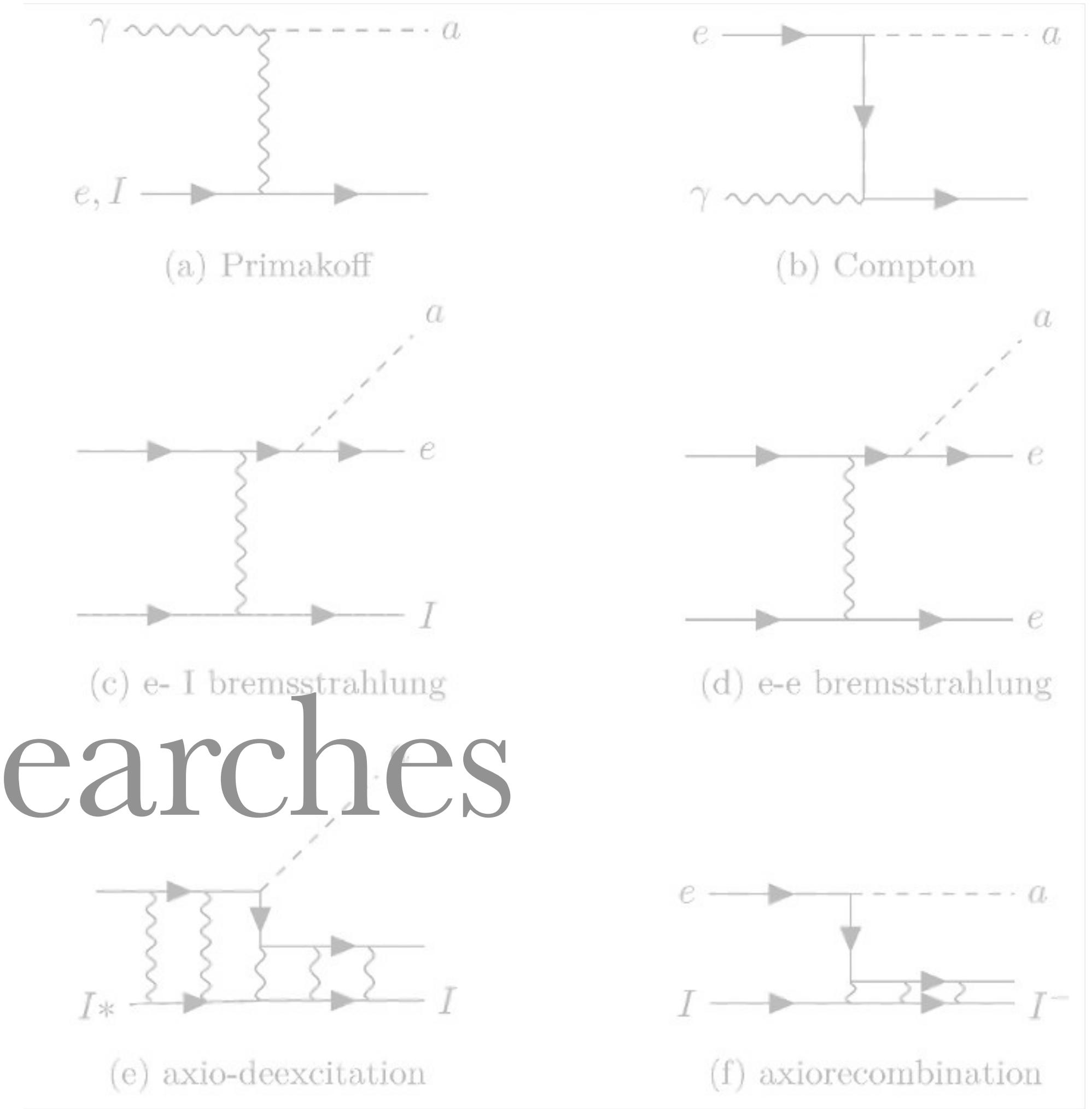


Lecture 3: ULD_M searches

Interactions with SM

Elisa G. M. Ferreira

Kavli IPMU & University of Sao Paulo



Outline

Lecture 1: Cosm. Signatures 1

Part I:

- Evidences
- ULDM models
- Observational signatures
- Gravitational Bounds

Part II:

Practice!

Notebook 1: linear

- Linear observational signature of ULDM: suppression of structures

Lecture 2: Cosm. Signatures 2

Part I:

- Cont. ULDM gravitational bounds
- Future of grav. observations

Part II:

Notebook 2: non-linear

- Consequences on small scales

Lecture 3: interac. with SM

- Cont. ULDM gravitational bounds

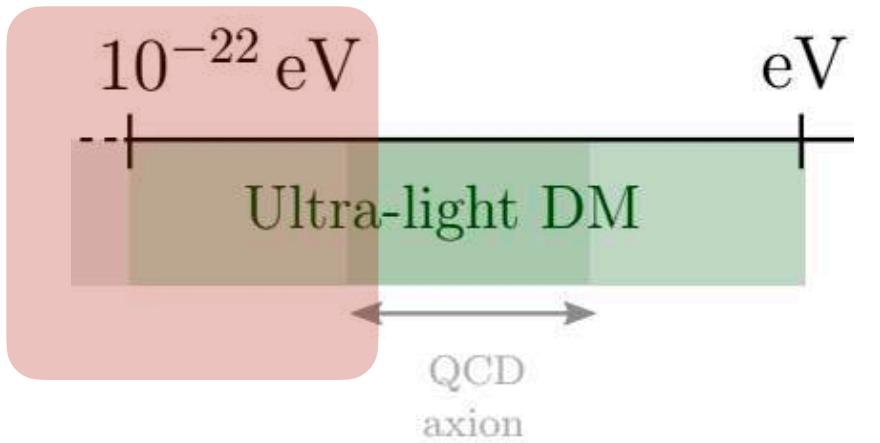
- DM Superfluid

- Interaction of ULDM with SM

- Axion/ALPs interaction in astrophysical systems
- Direct detection

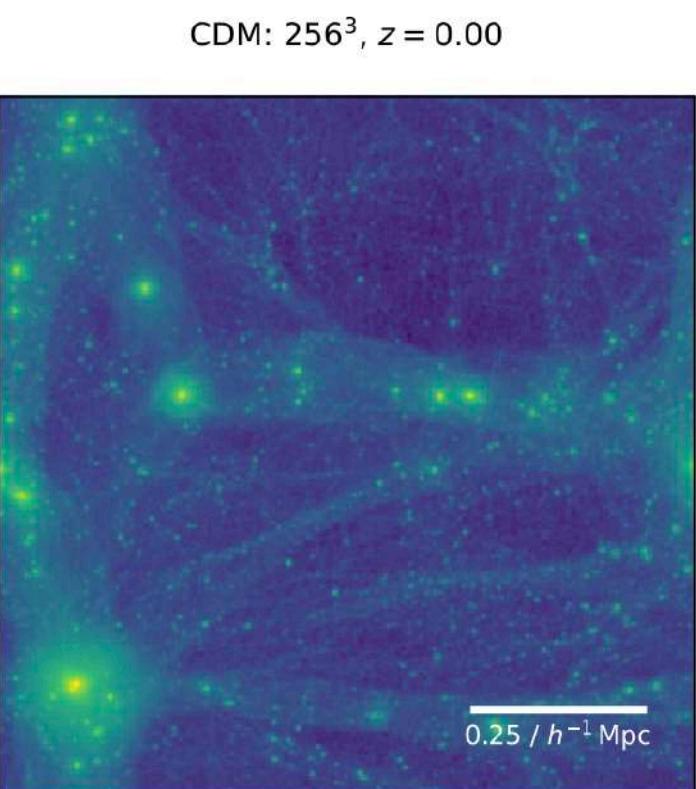
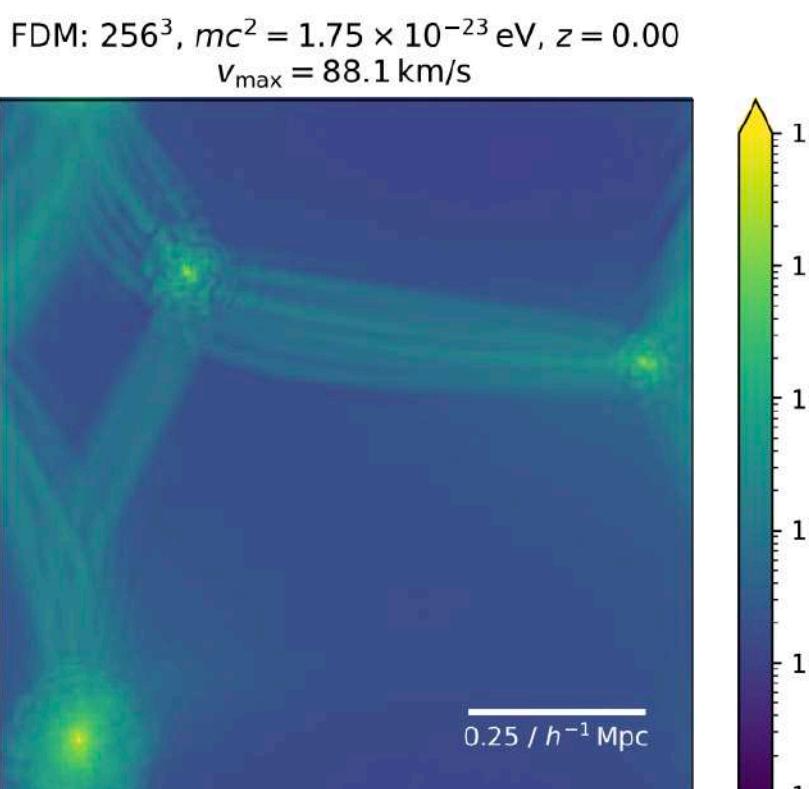
Phenomenology

RICH PHENOMENOLOGY ON SMALL SCALES



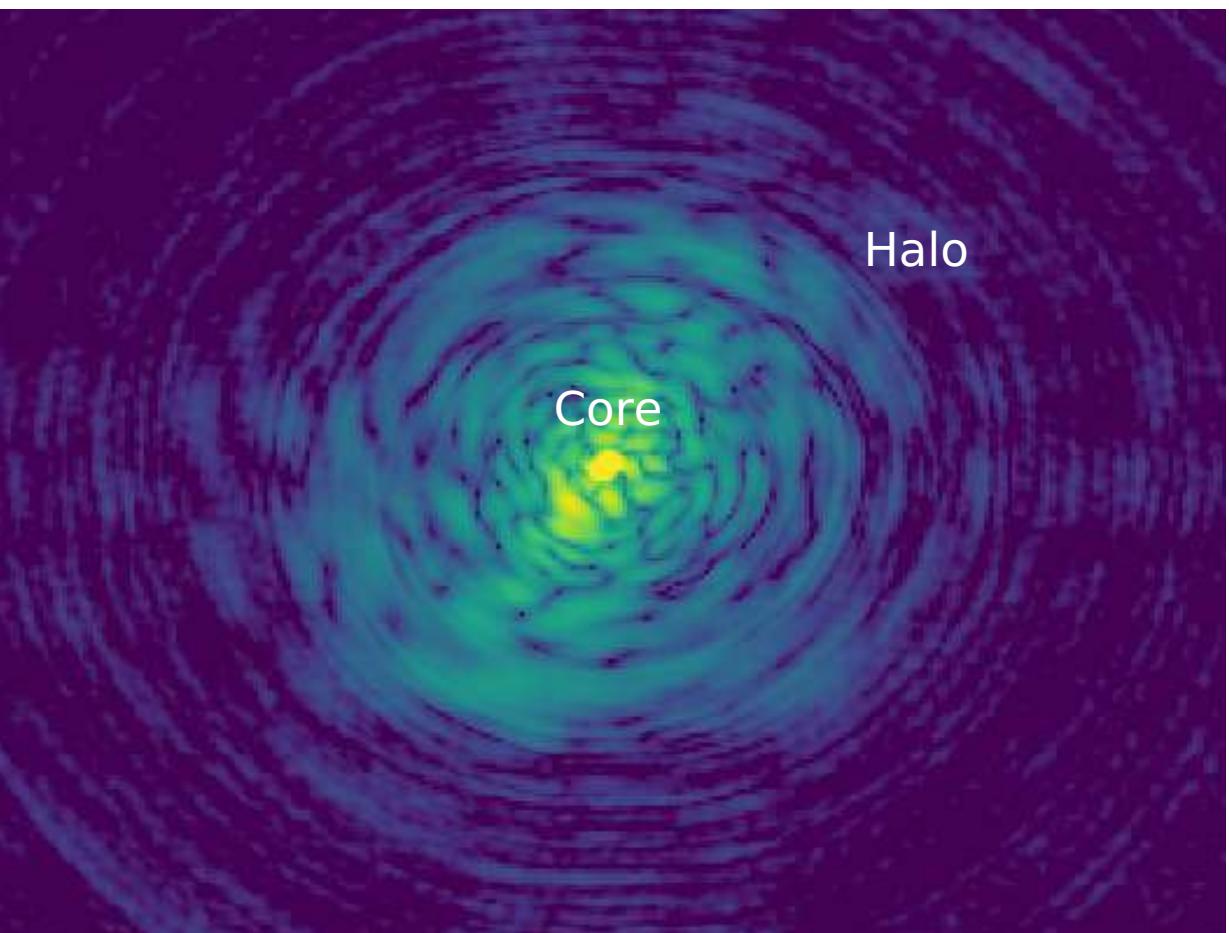
* Focus only in gravitational signatures

Suppression of small structures

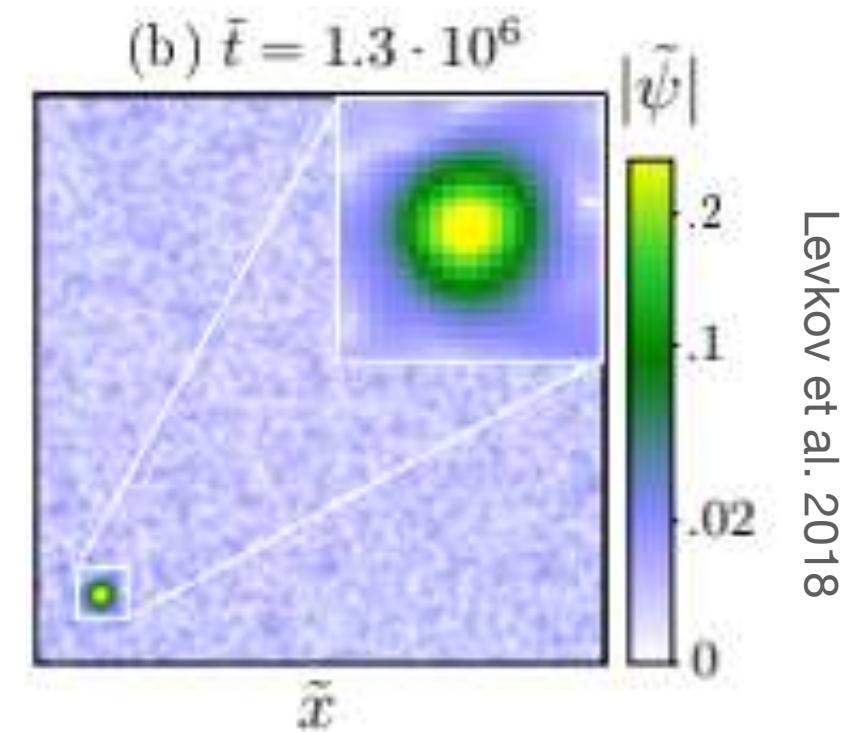


S. May et al. 2021

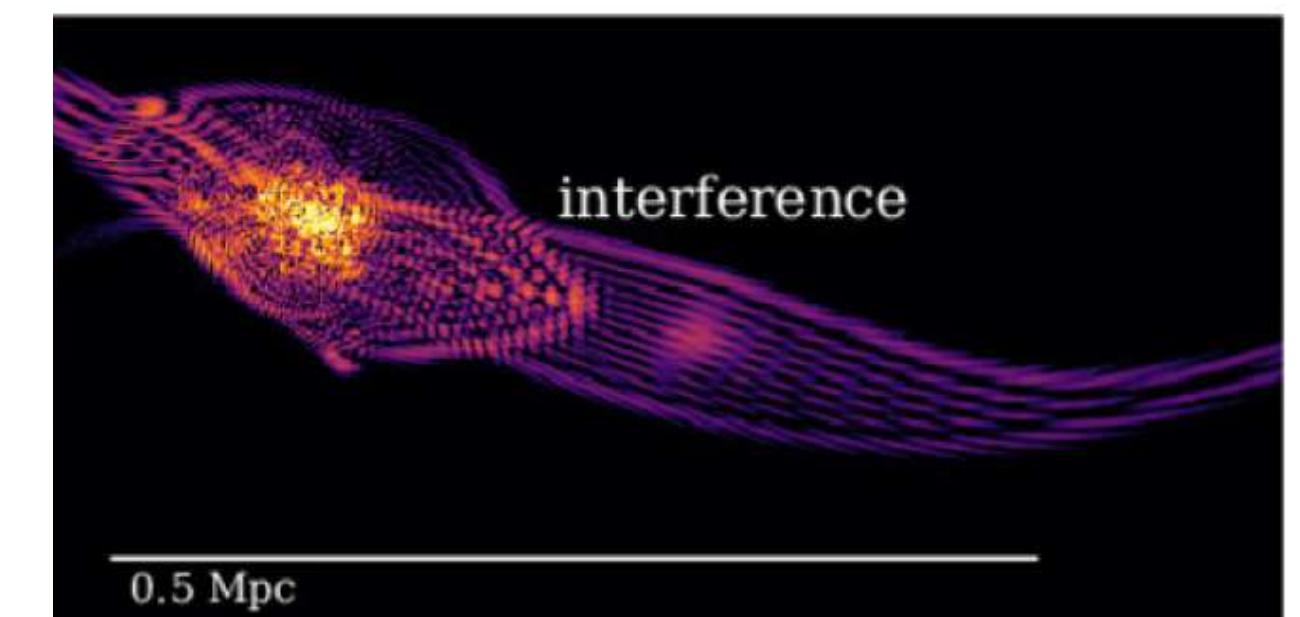
Formation of a solitonic core



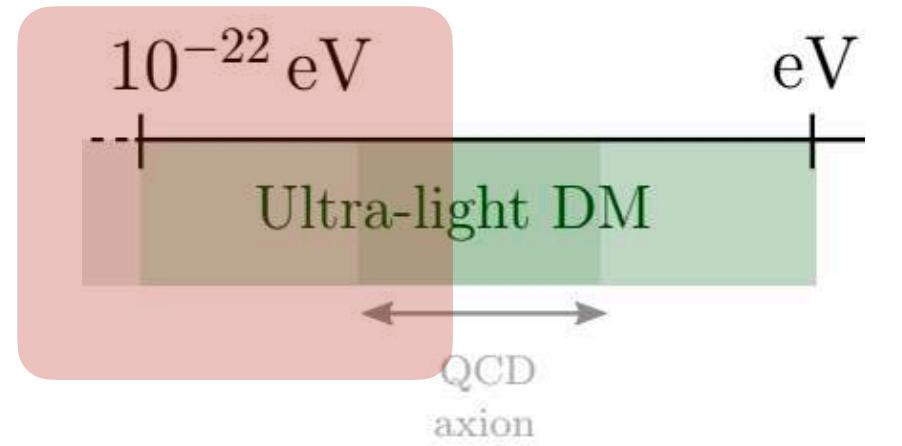
Dynamical effects



Wave interference



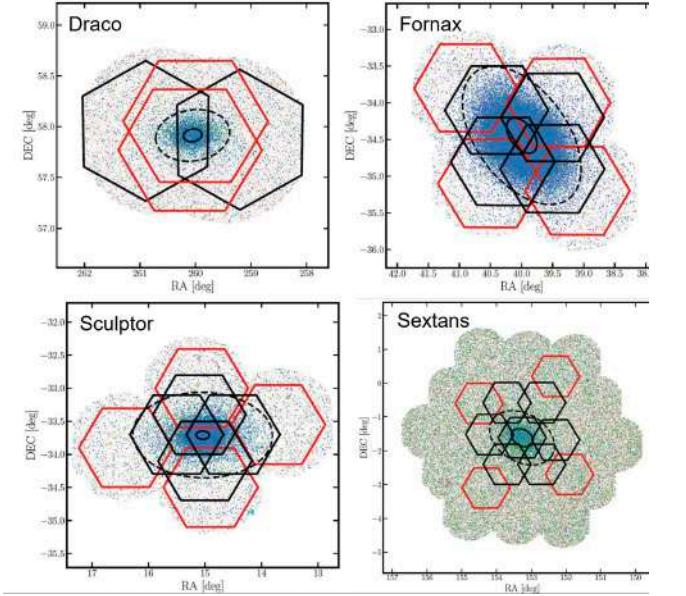
Observational implications and constraints



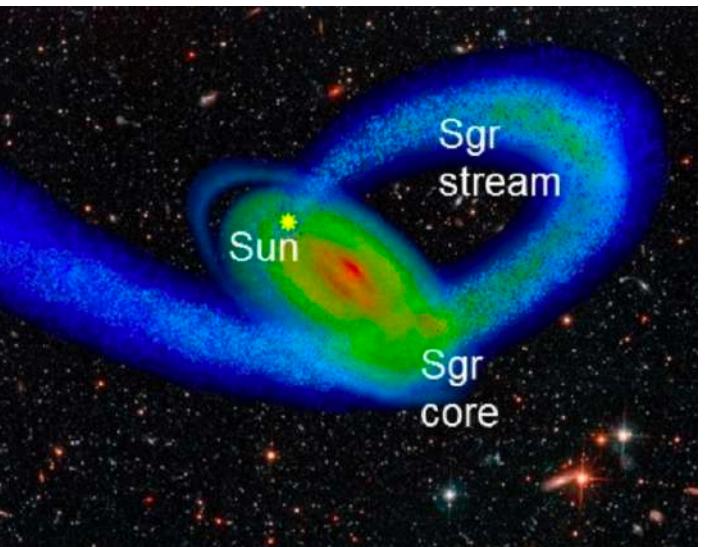
Galaxies



Dwarfs

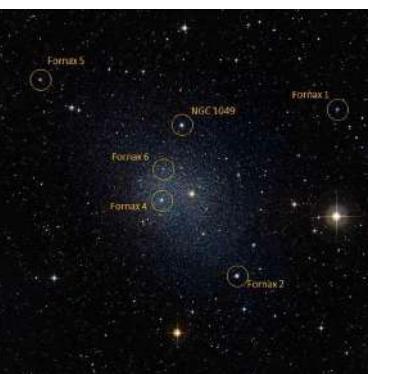


Stellar stream

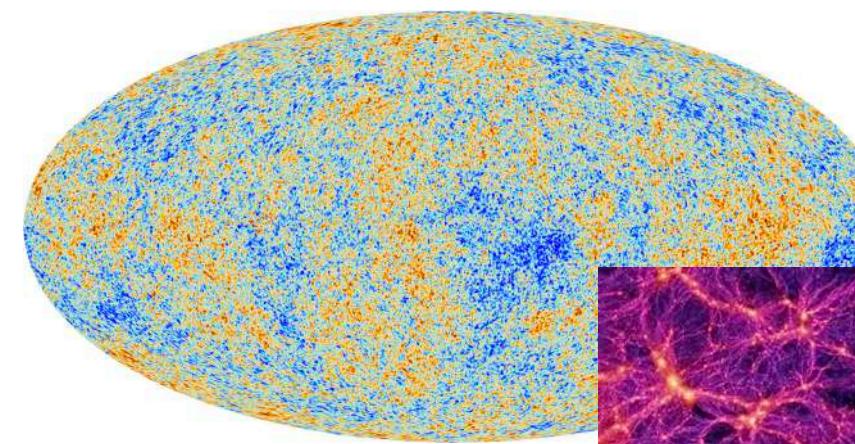


NASA and ESA

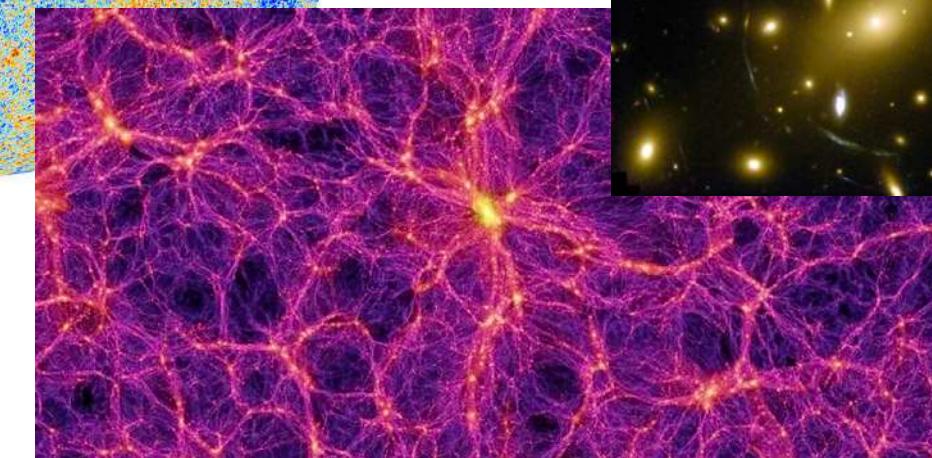
Globular clusters



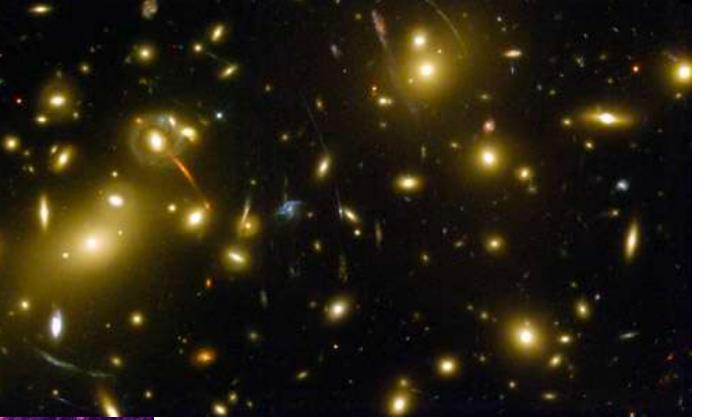
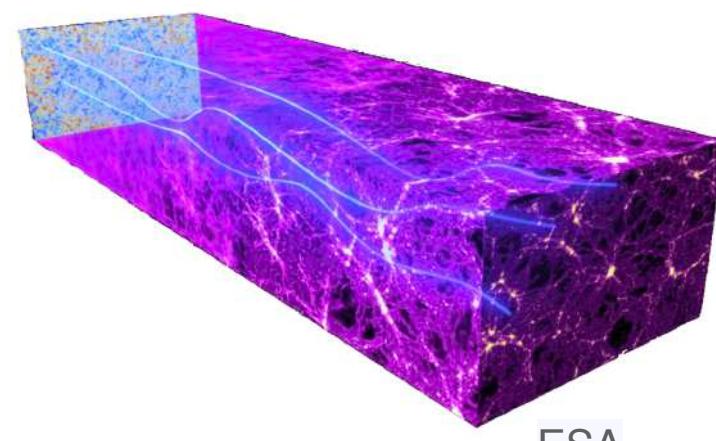
CMB+LSS



ESA and the Planck Collaboration

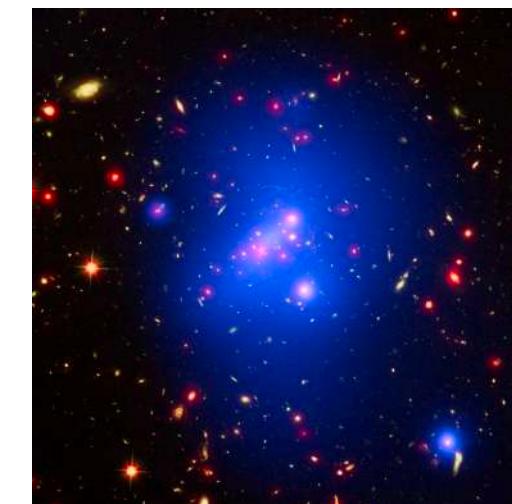


Springel & others / Virgo Consortium



NASA and ESA

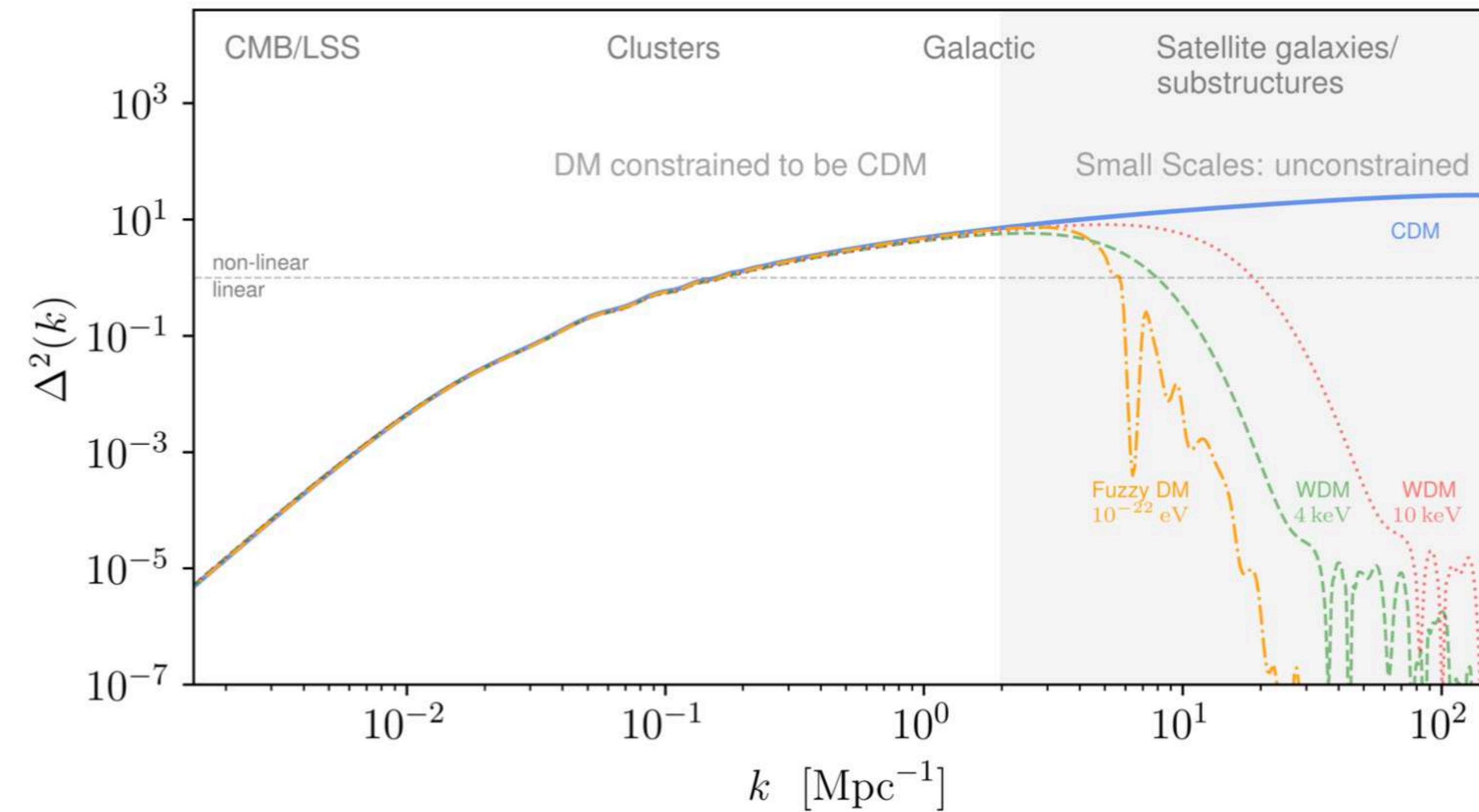
Clusters

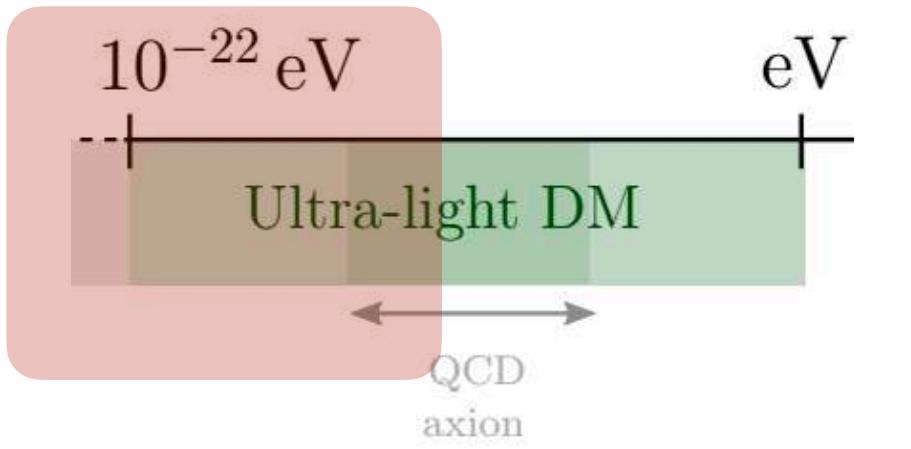


CC BY 4.0

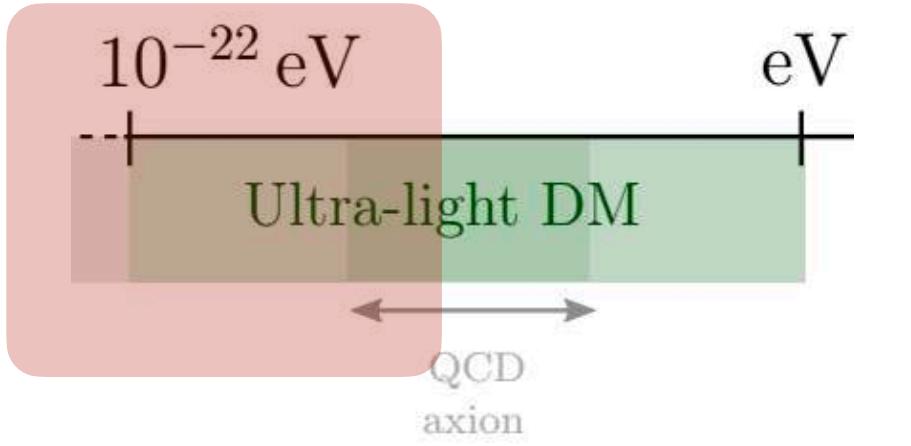
ESA

Power spectrum





Cont. Observational implications and constraints



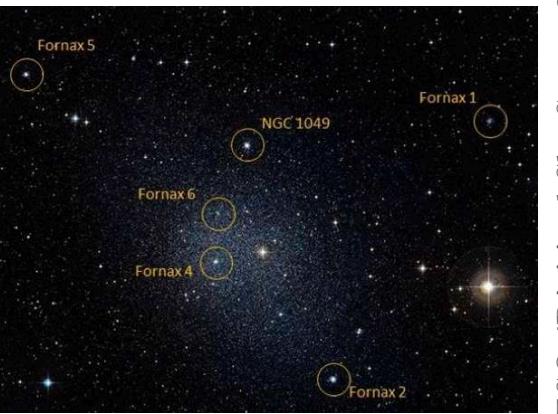
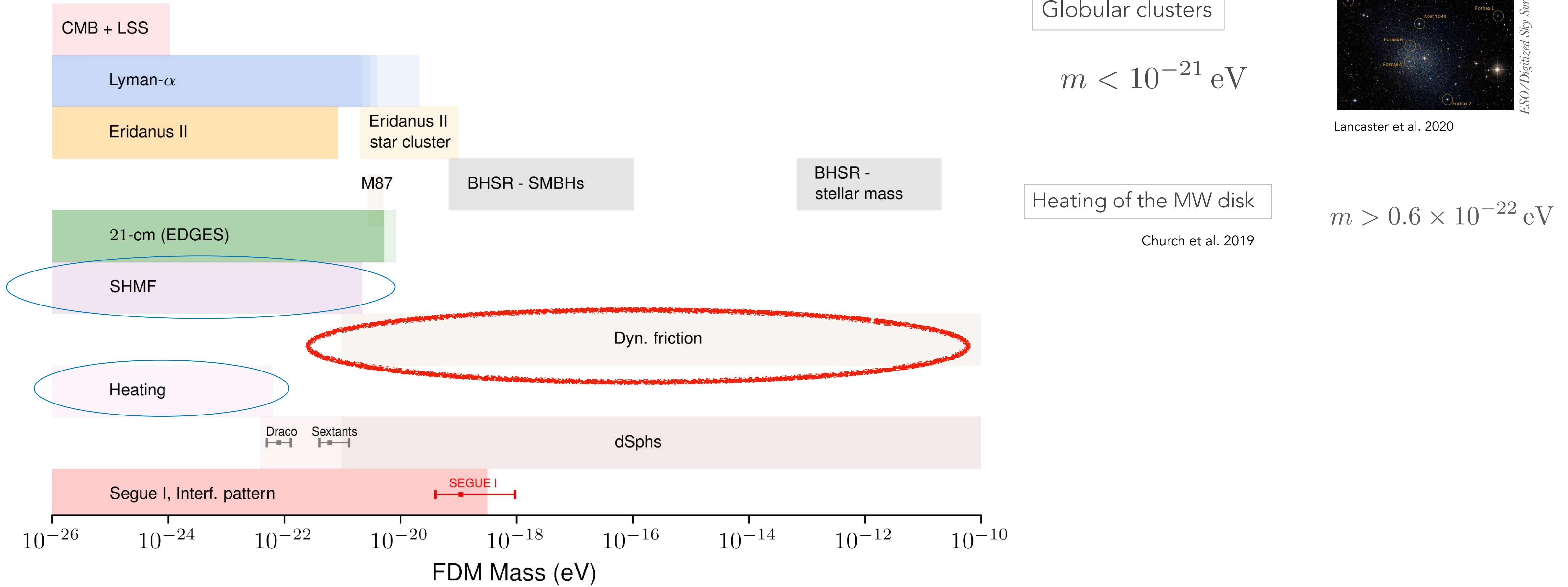
Observational implications and constraints

Dynamical effects

Observational implications and constraints

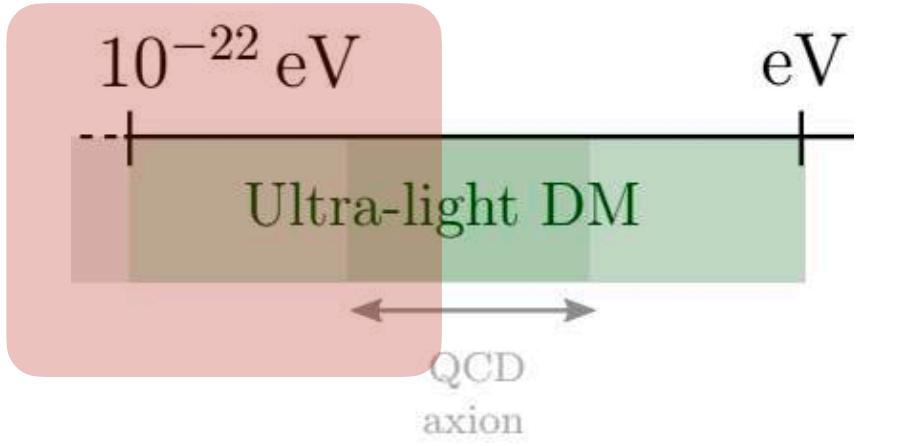
Fuzzy Dark Matter - bounds on the mass

Dynamical effects



ESO/Digitized Sky Survey 2

Lancaster et al. 2020

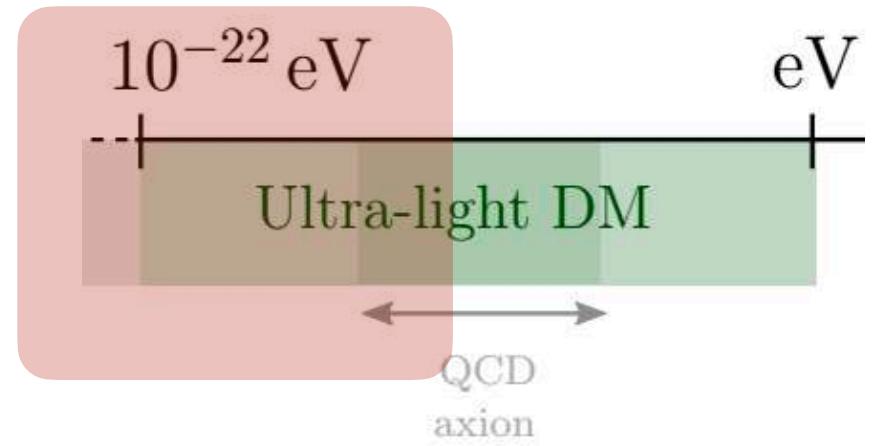


Observational implications and constraints

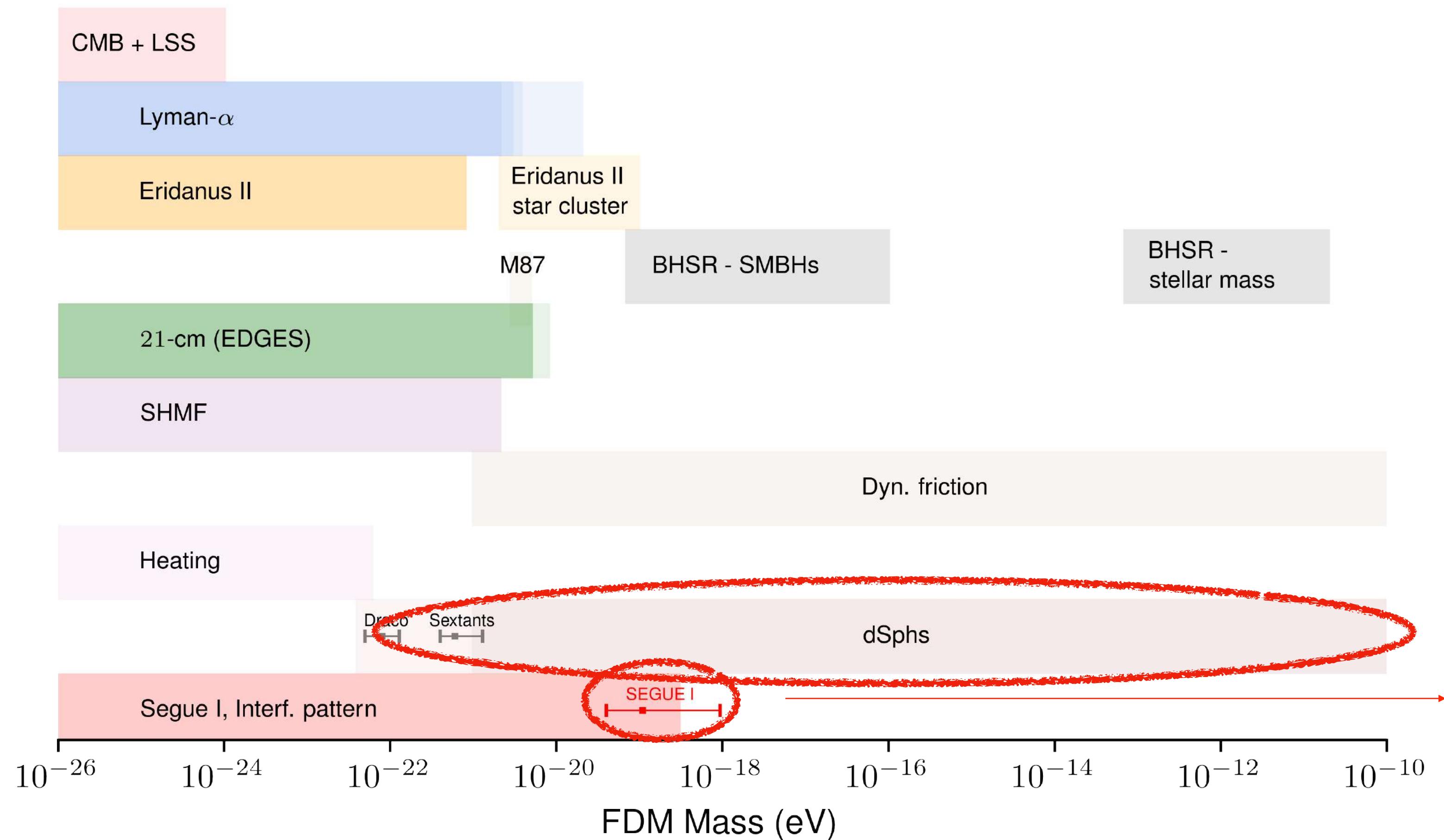
Core in the interior of galaxies

Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass

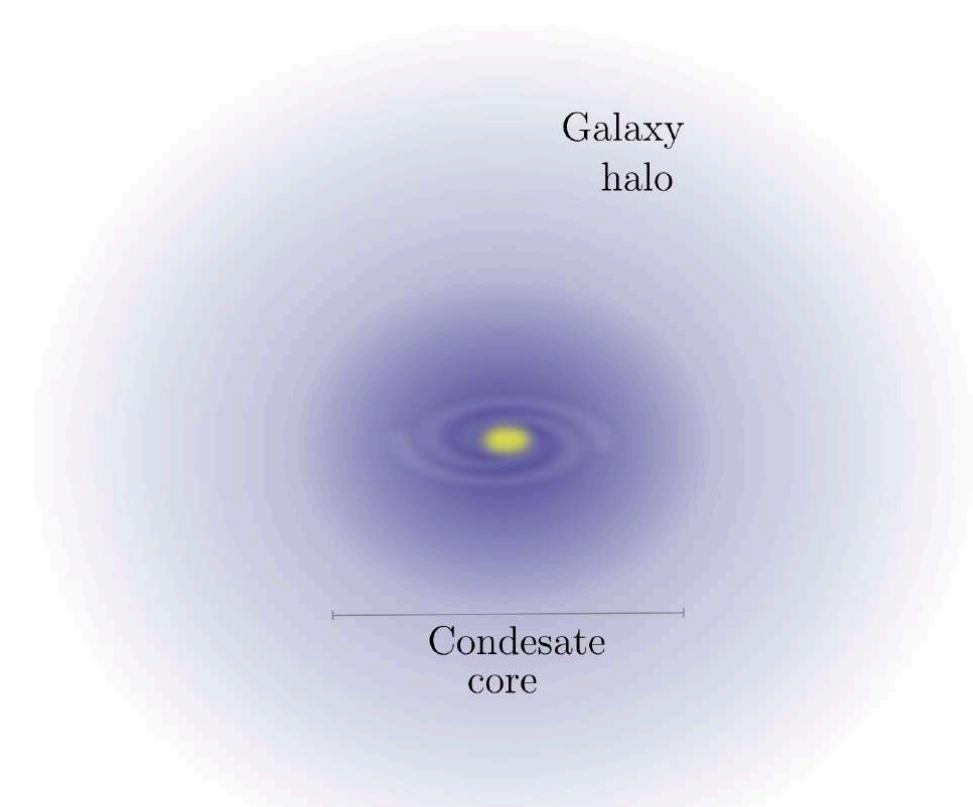


Presence of a core



Presence of a core

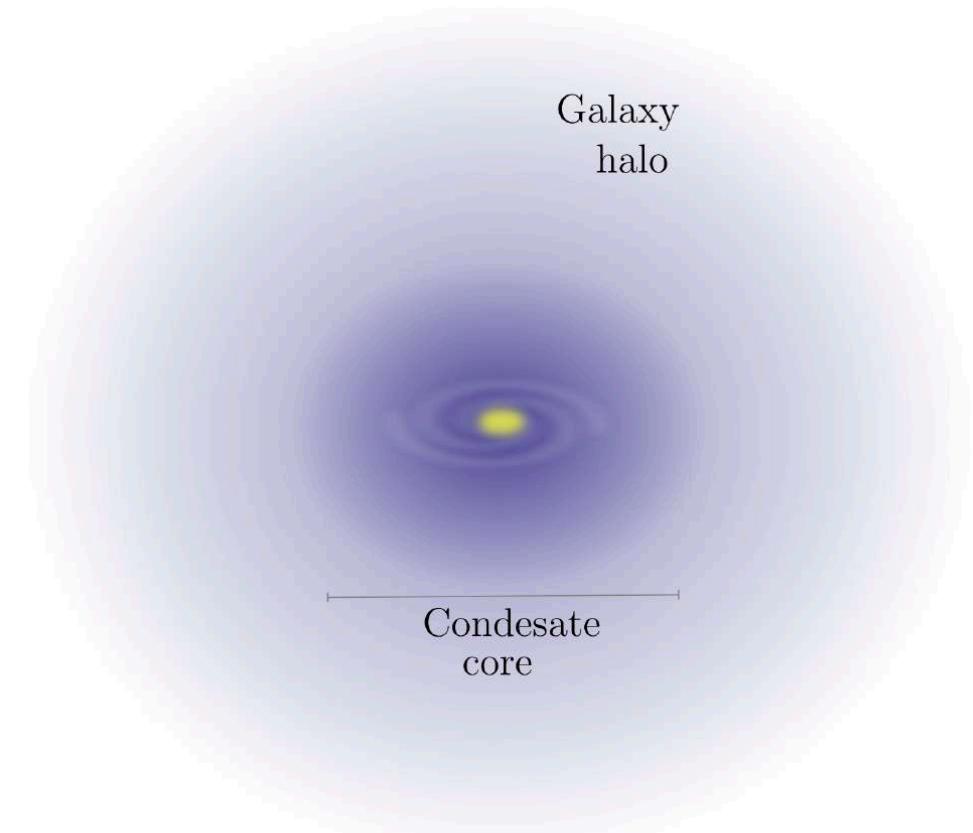
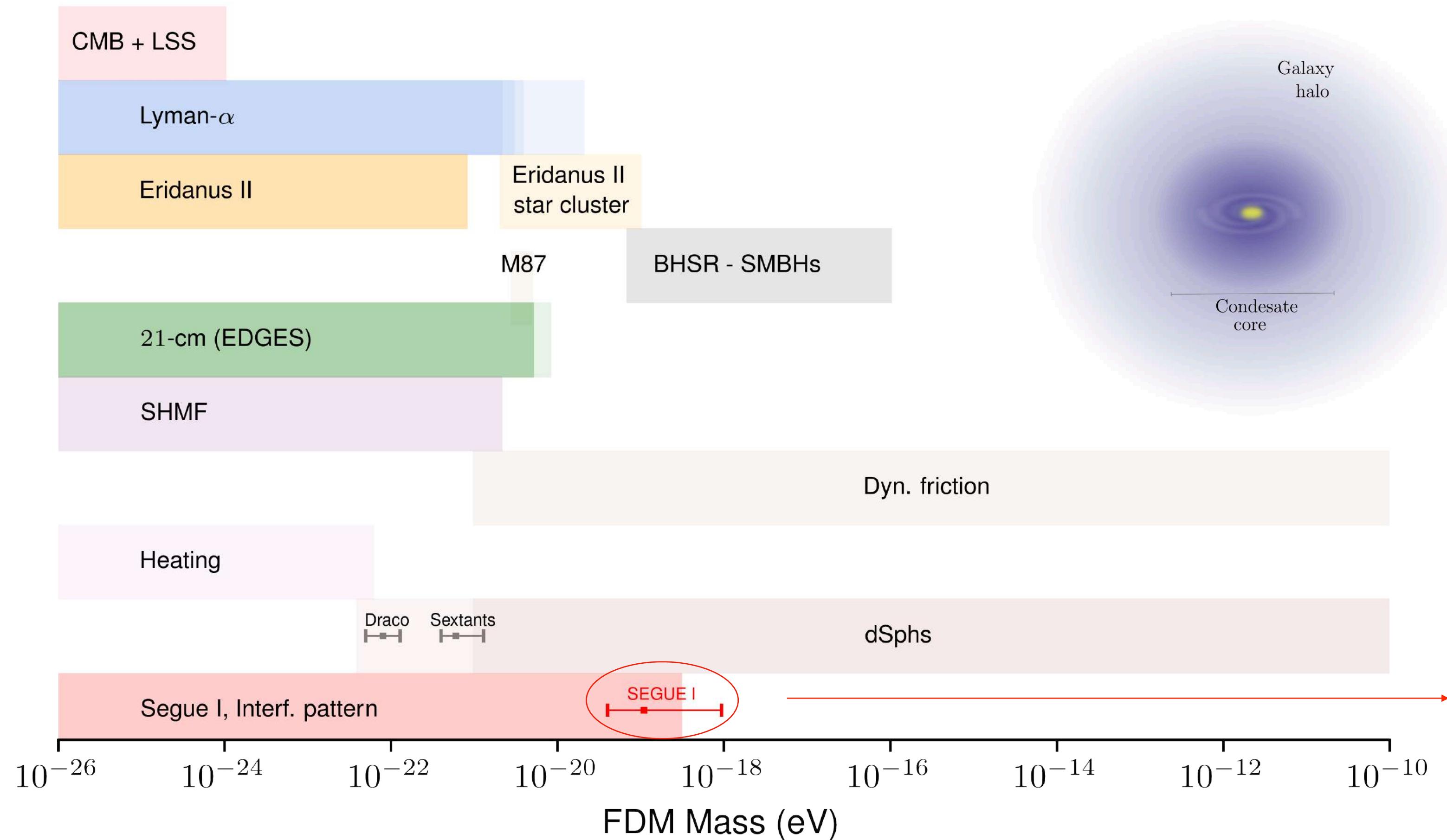
DWARF GALAXIES



Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass

Presence of a core



DWARFS

Ultra faint dwarfs

FDM SIMULATIONS

$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \simeq \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_\epsilon \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_\epsilon \end{cases}$$

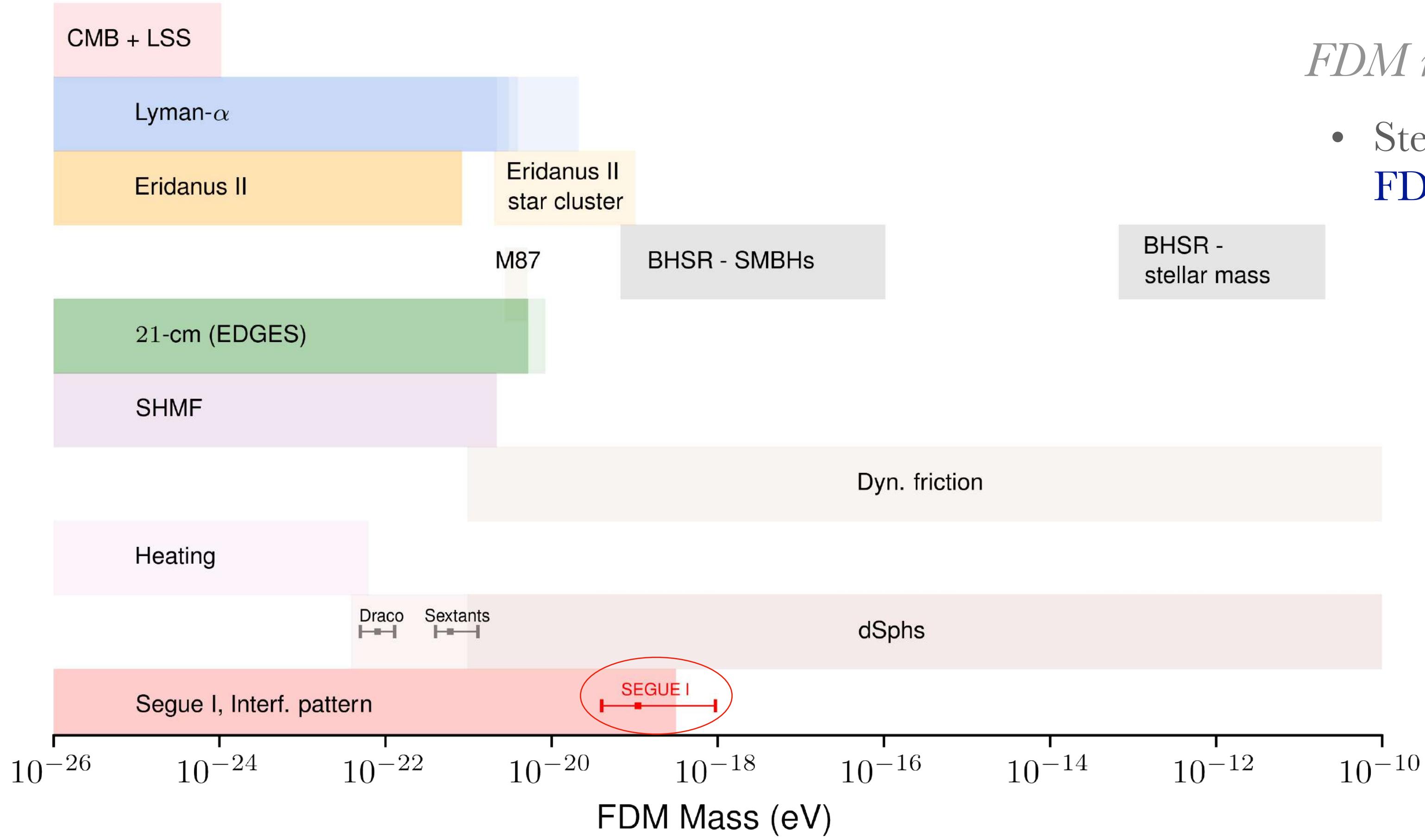
“Narrowing the mass range of Fuzzy Dark Matter with Ultra-faint Dwarfs”, J. Chan, E.F., K. Hayashi, 2021.

Ultra-light Dark Matter

Fuzzy Dark Matter - bounds on the mass

Ultra faint dwarfs

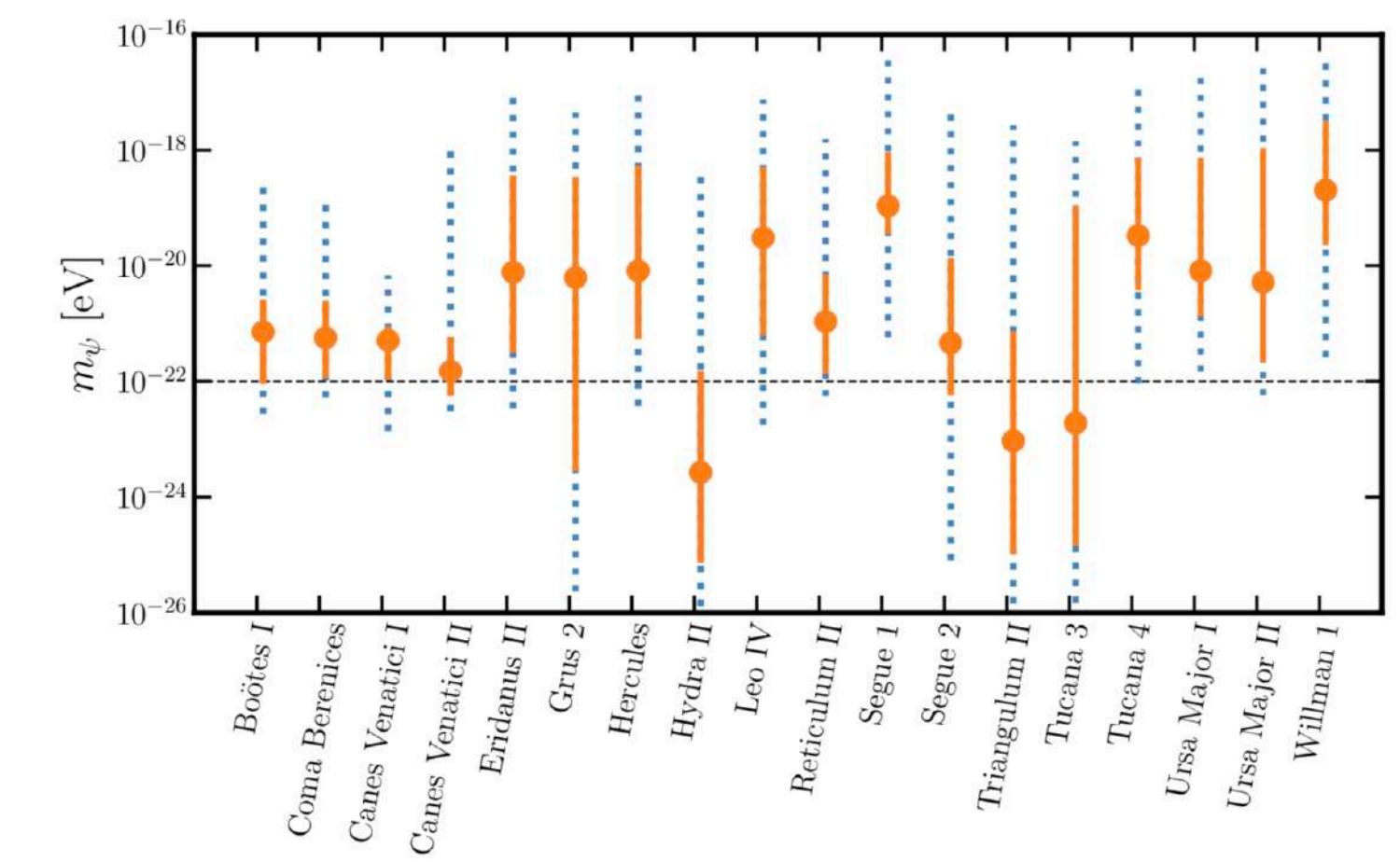
Hayashi, E.F.Chan, 2021.



FDM mass from Ultra-faint dwarfs

- Stellar kinematic data from 18 UFDs to fit the **FDM profile from simulations**

$$m_{\text{FDM}}^{(\text{Seg1})} = 1.1_{-0.7}^{+8.3} \times 10^{-19} \text{ eV}$$

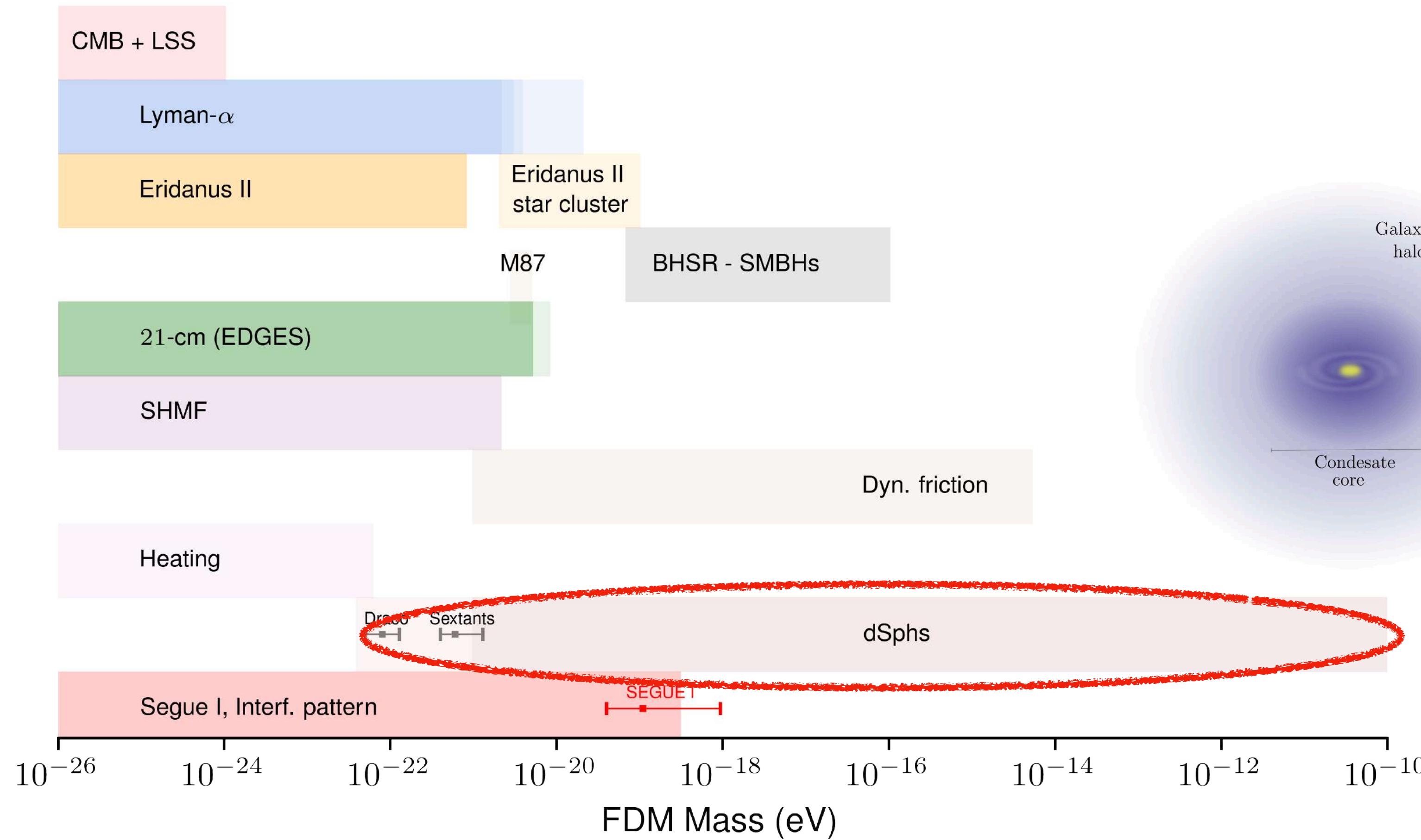


Preference for higher mass

Observational implications and constraints

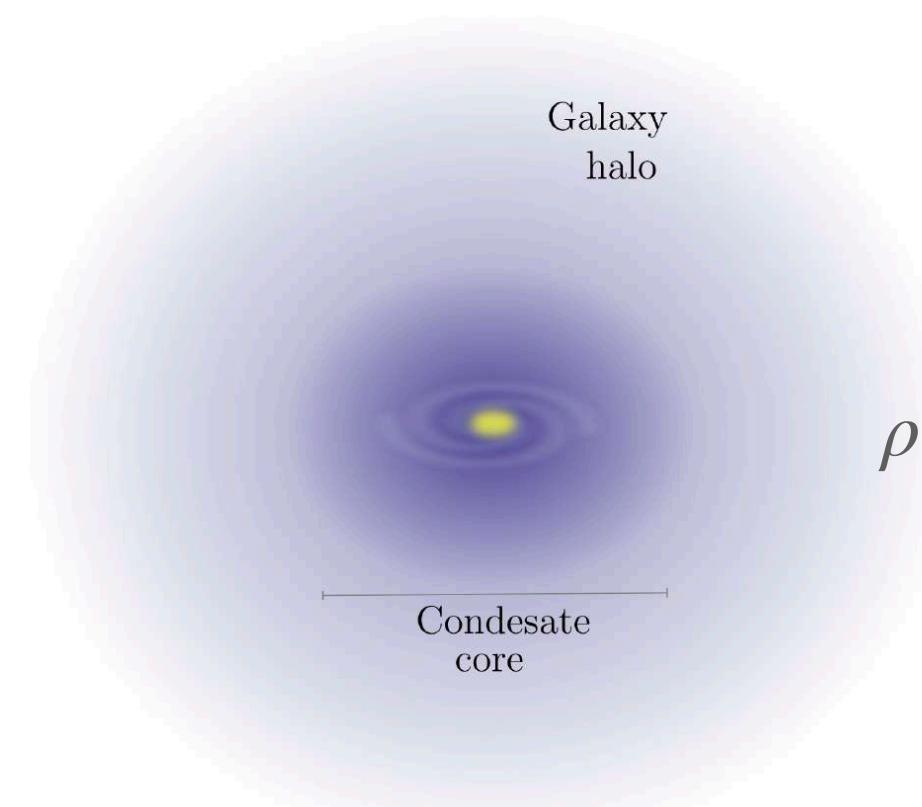
Fuzzy Dark Matter - bounds on the mass

Presence of a core



DWARFS

Dwarf Spheroidals (dSphs)



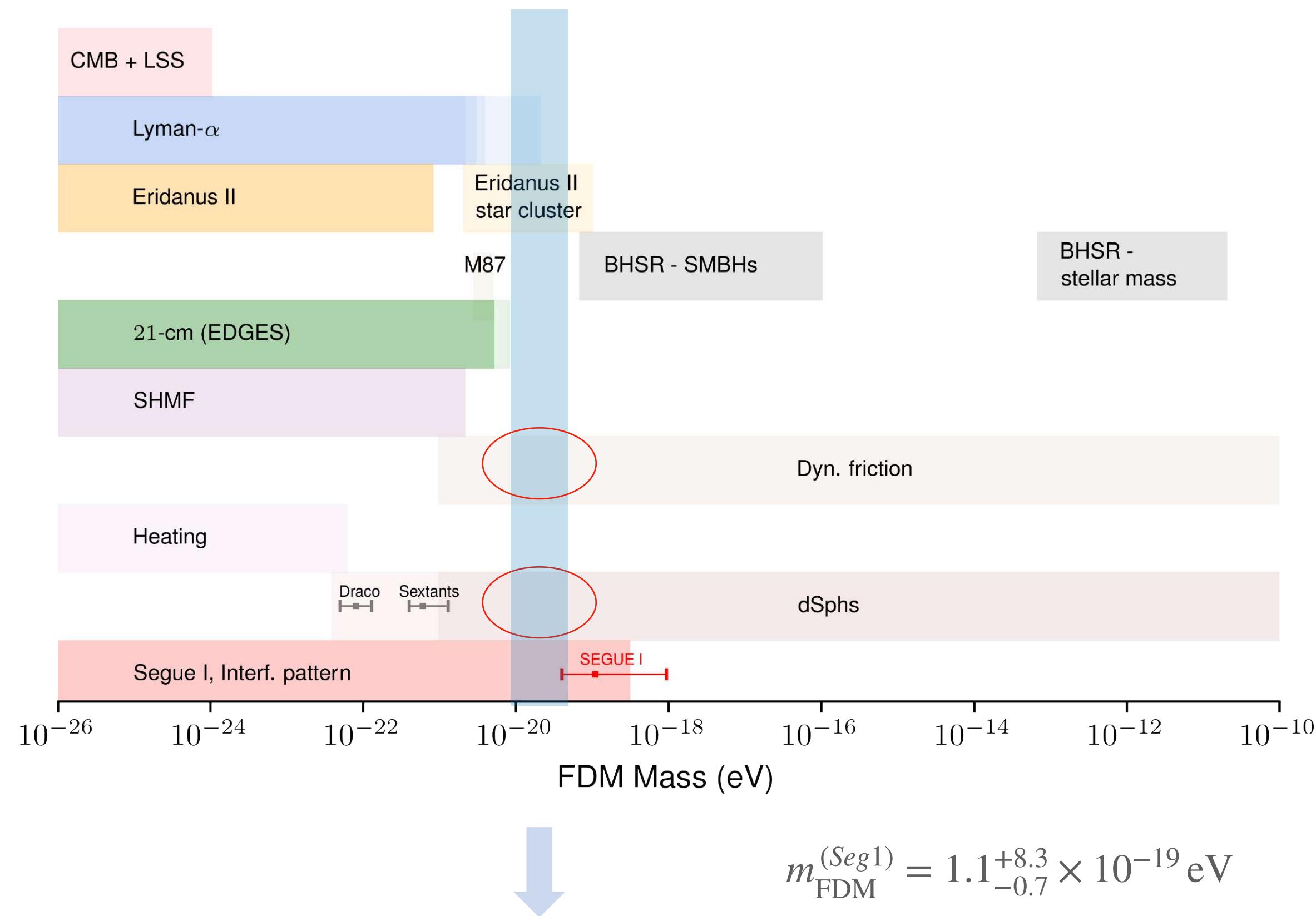
FDM SIMULATIONS

$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \simeq \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_c \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_c \end{cases}$$

Fornax - Sculptor

$$m < 0.8 \times 10^{-22} \text{ eV}$$

Constraints on the mass



Incompatibility between all bounds and the dSphs
(Fornax and Sculptor) bounds

Possible reasons for this incompatibility:

- *Influence of baryons*: baryonic processes can change the density structure of their halo - we are not probing the intrinsic DM profile.
- *Universality of the core profile*: FDM soliton profile might be too simplistic, could change for different systems (might also depend on baryons)
- *Core-mass relation*: might need to be better understood. \neq relation in \neq simulations
- *Challenge for the FDM model*

FDM - Core-halo mass relation

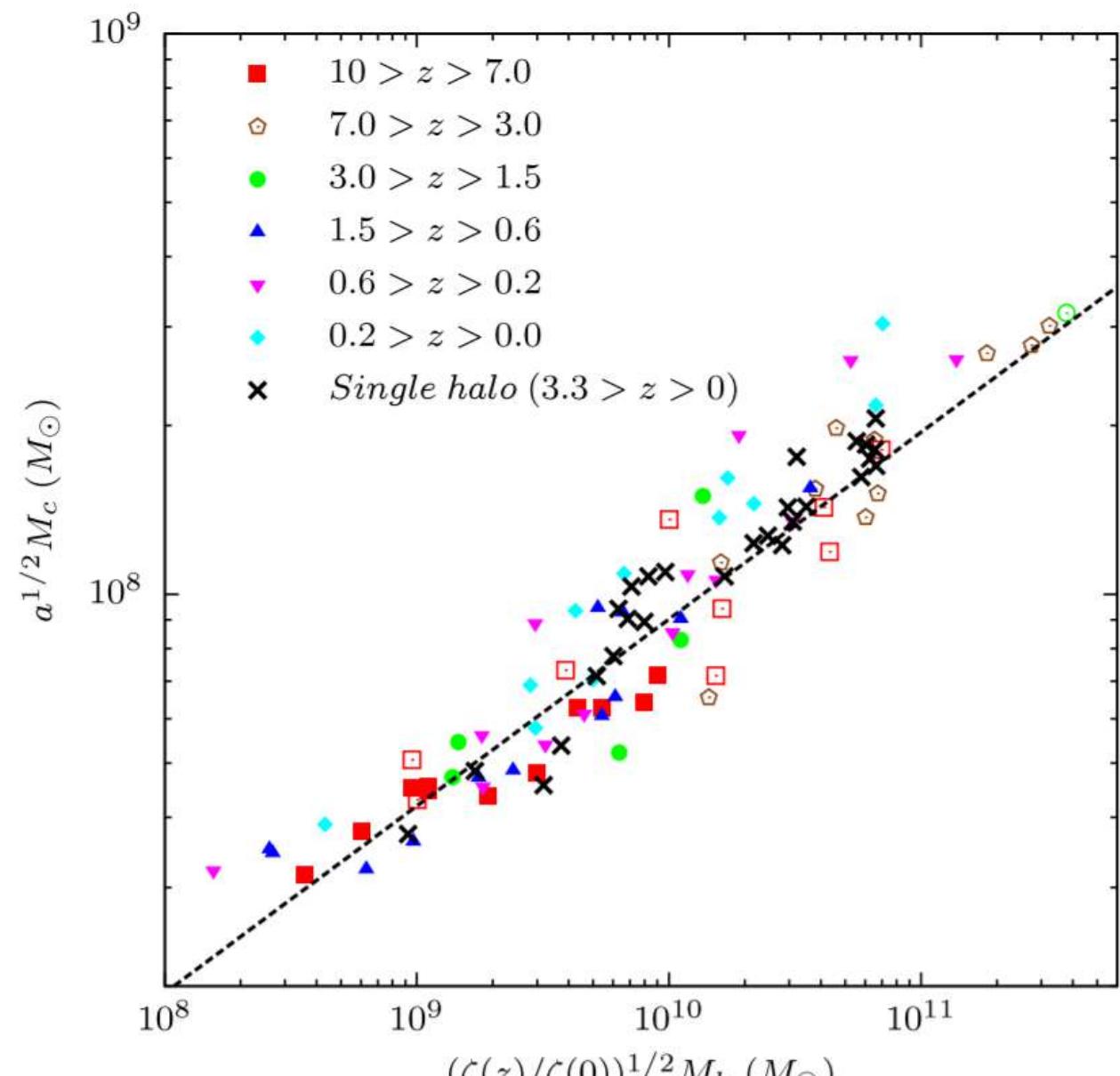
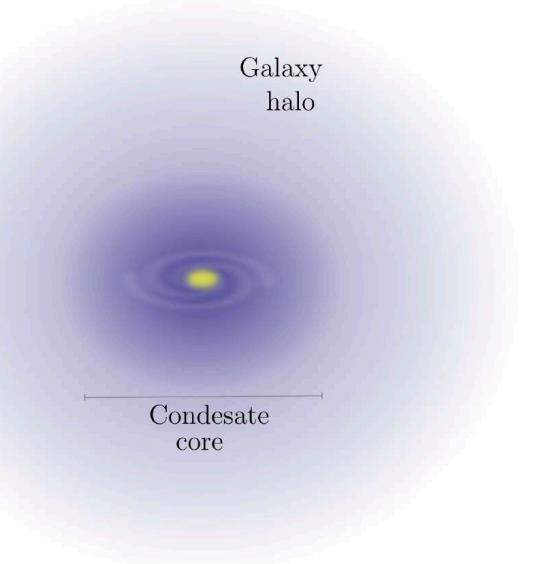
J. Chan et al. 2021

We want to study how the core relates to the halo mass - might be one part this puzzle

$$\rho_c \simeq \frac{1.9 \times 10^{-2}}{[1 + 0.091(r/R_{1/2,c})^2]^8} \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-2} \left(\frac{r_c}{\text{kpc}} \right)^{-4} M_\odot \text{ pc}^{-3},$$

?

M_h



Schive et al. 2014

Schive et al 2014

$$M_c \propto M_h^{1/3}$$

Velocity dispersion tracing

$$\sigma_c \sim \sigma_h$$

Mocz et al 2017

$$M_c \propto M_h^{5/9}$$

Energy tracing

$$M_c \sigma_c^2 \sim M_h \sigma_h^2$$

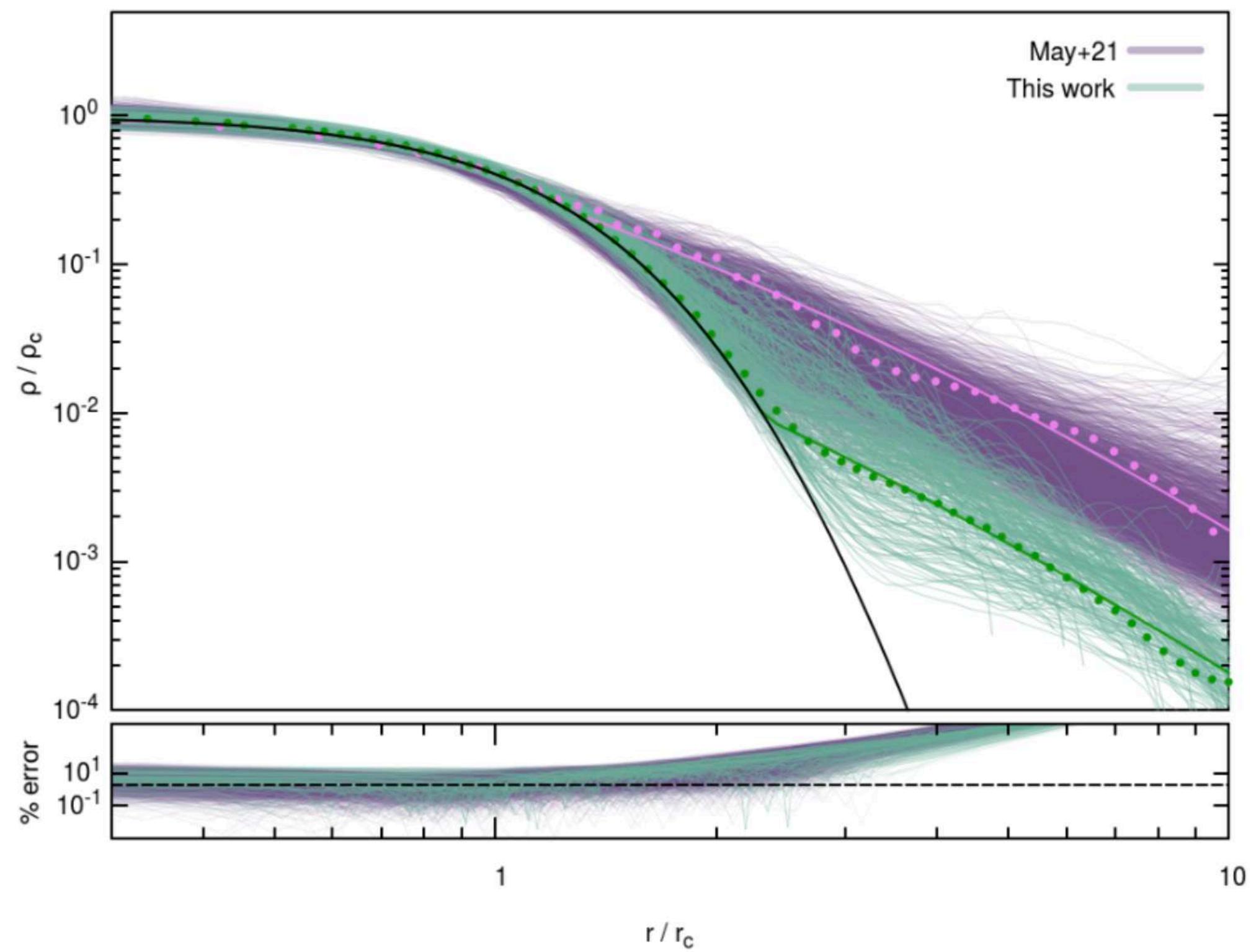
Velmatt et al 2018, Nori et al 2020, Nima et al 2020

= Schive

\neq Schive

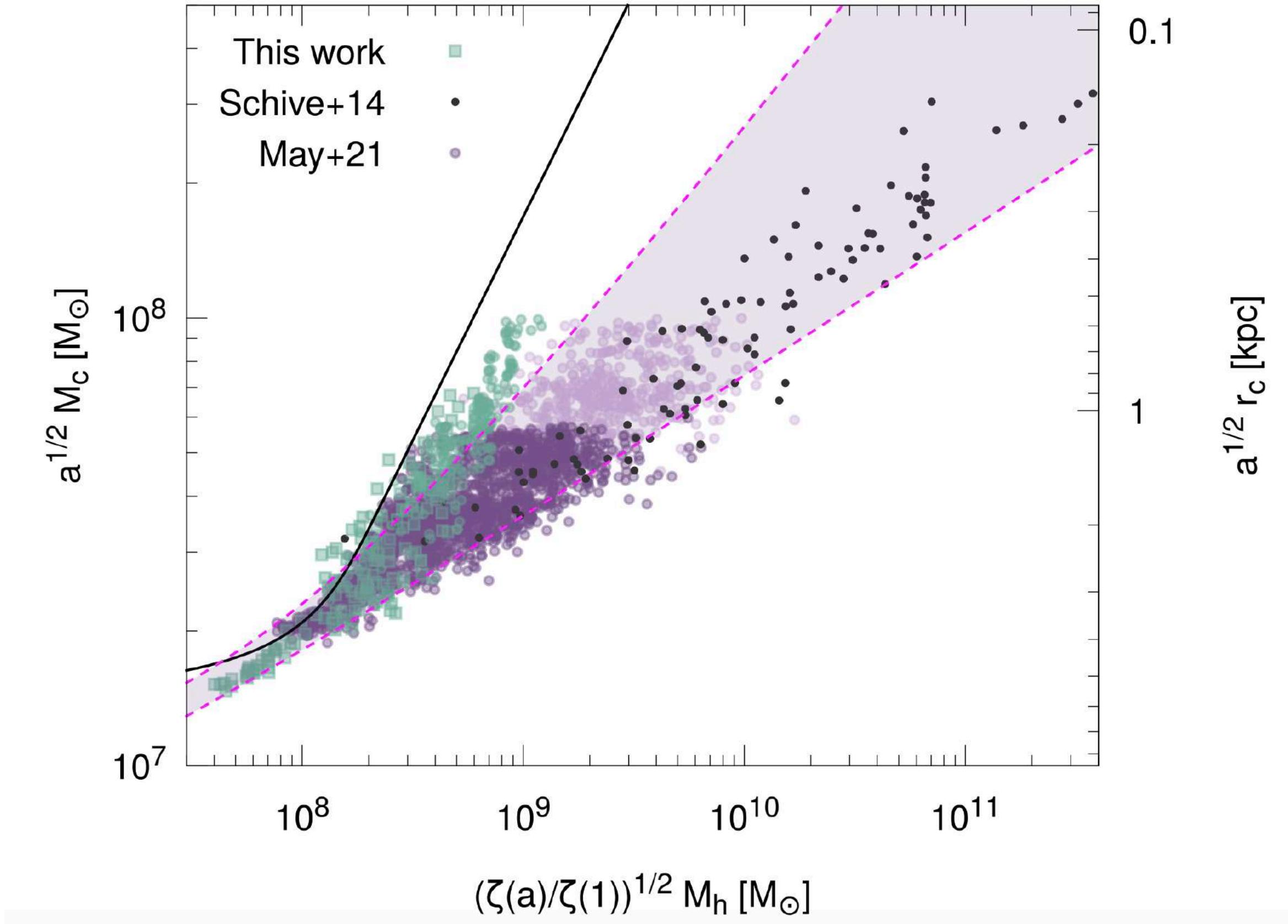
FDM - Core-halo mass relation

J. Chan, EF, S. May, K. Hayashi, M. Chiba 2021



Well fitted by:

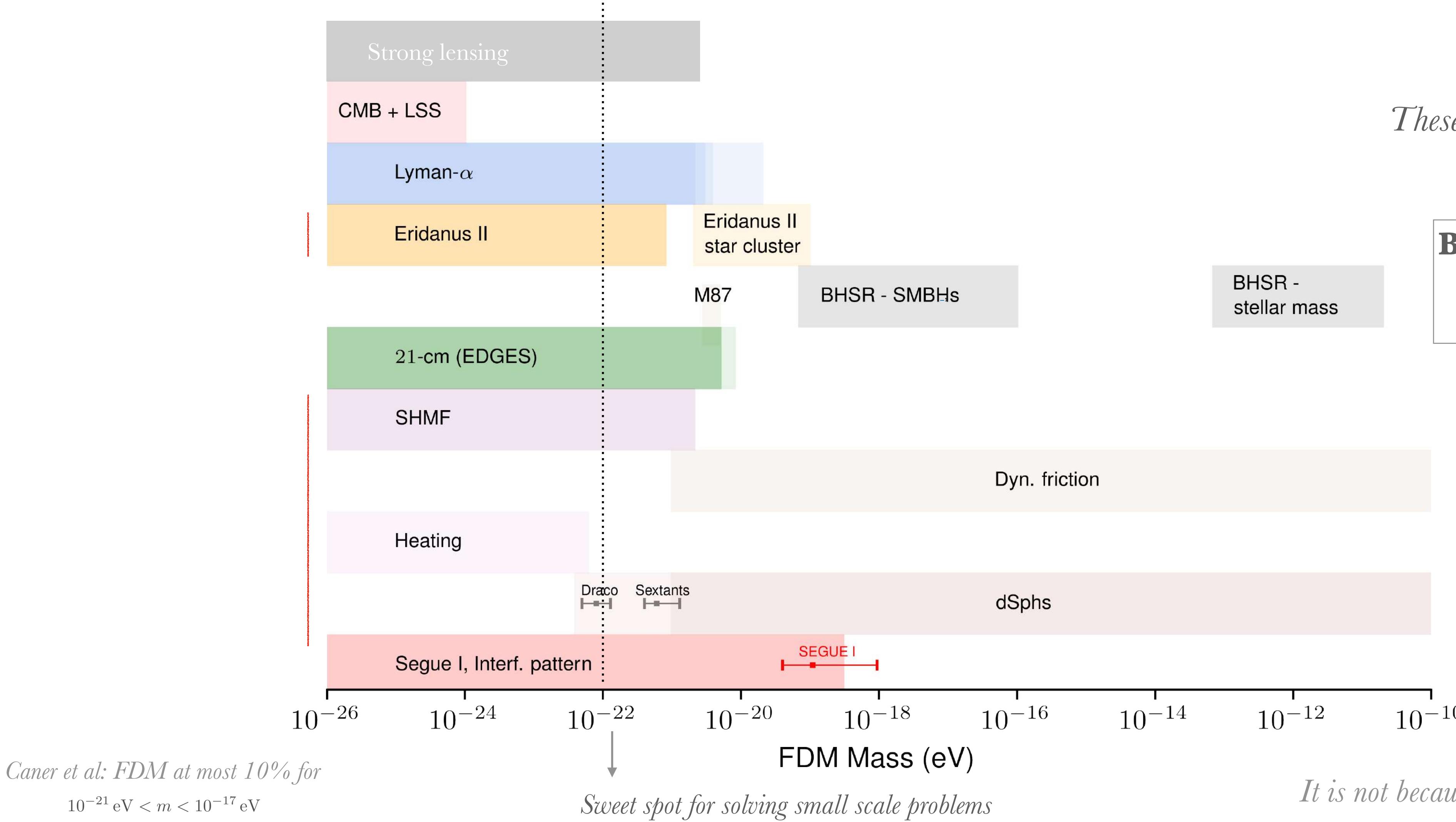
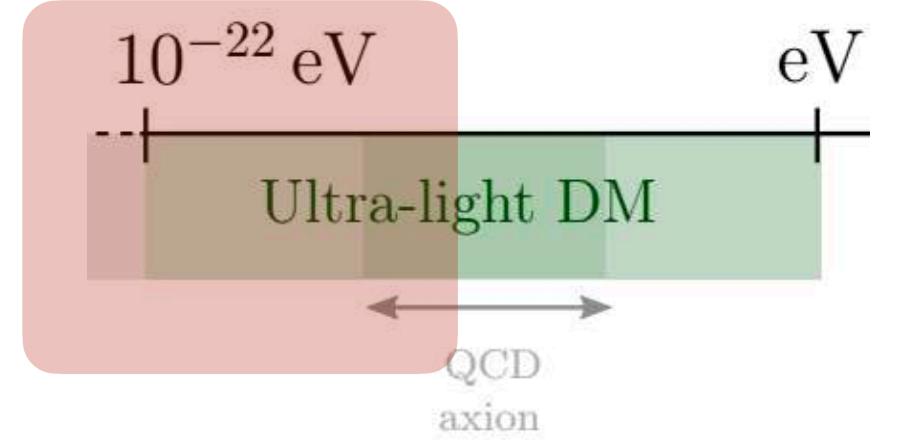
$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \simeq \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_\epsilon \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_\epsilon \end{cases}$$



Steeper slope → Smaller core → Smaller mass

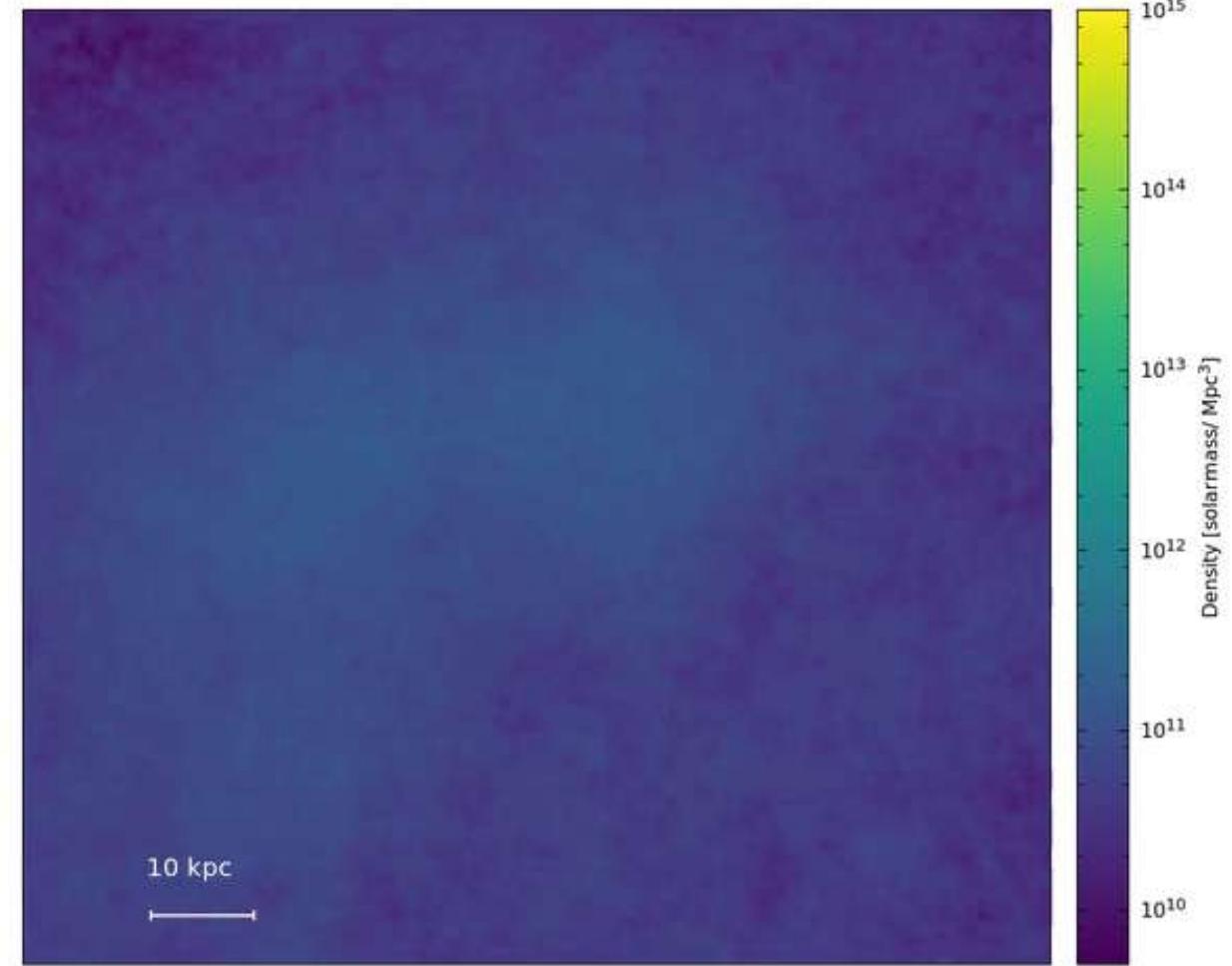
Current status

Fuzzy Dark Matter - bounds on the mass



New observables/new probes

Interference pattern



Simulation by Jowett Chan

$\mathcal{O}(1)$ fluctuations in density $\longrightarrow \sim \lambda_{dB}$

PROBES:

- Strong lensing
- Stellar streams
- Heating

} Gravitational
probes

ONGOING

- Characterizing the interference patterns using full simulations
- Strong lensing
- Stellar streams

In collaboration with Jowett Chan and Simon May

In collaboration with: Devon Powel, Simona Vegetti, Simon White

In collaboration with: Sten Delos and Fabian Schmidt

Previous studies:

Strong lensing:

J. Chan, H.Schive, S.g Wong, T. Chiueh, T. Broadhurst, 2020
A. Laroche, Daniel Gilman, X. Li, J. Bovy, X. Du, 2022

Stellar streams:

Neal Dalal, Jo Bovy Lam Hui, Xinyu Li, 2020

Sub-galactic power spectrum:

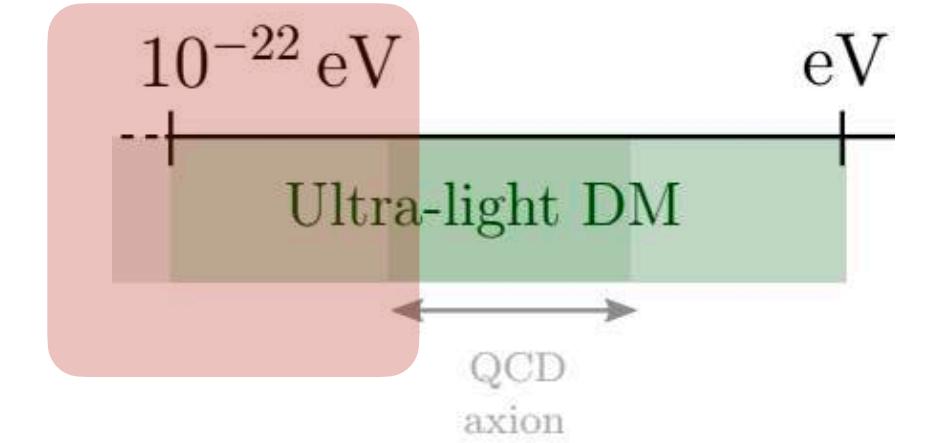
Hezaveh et al. (2016)

Sub-galactic power spectrum

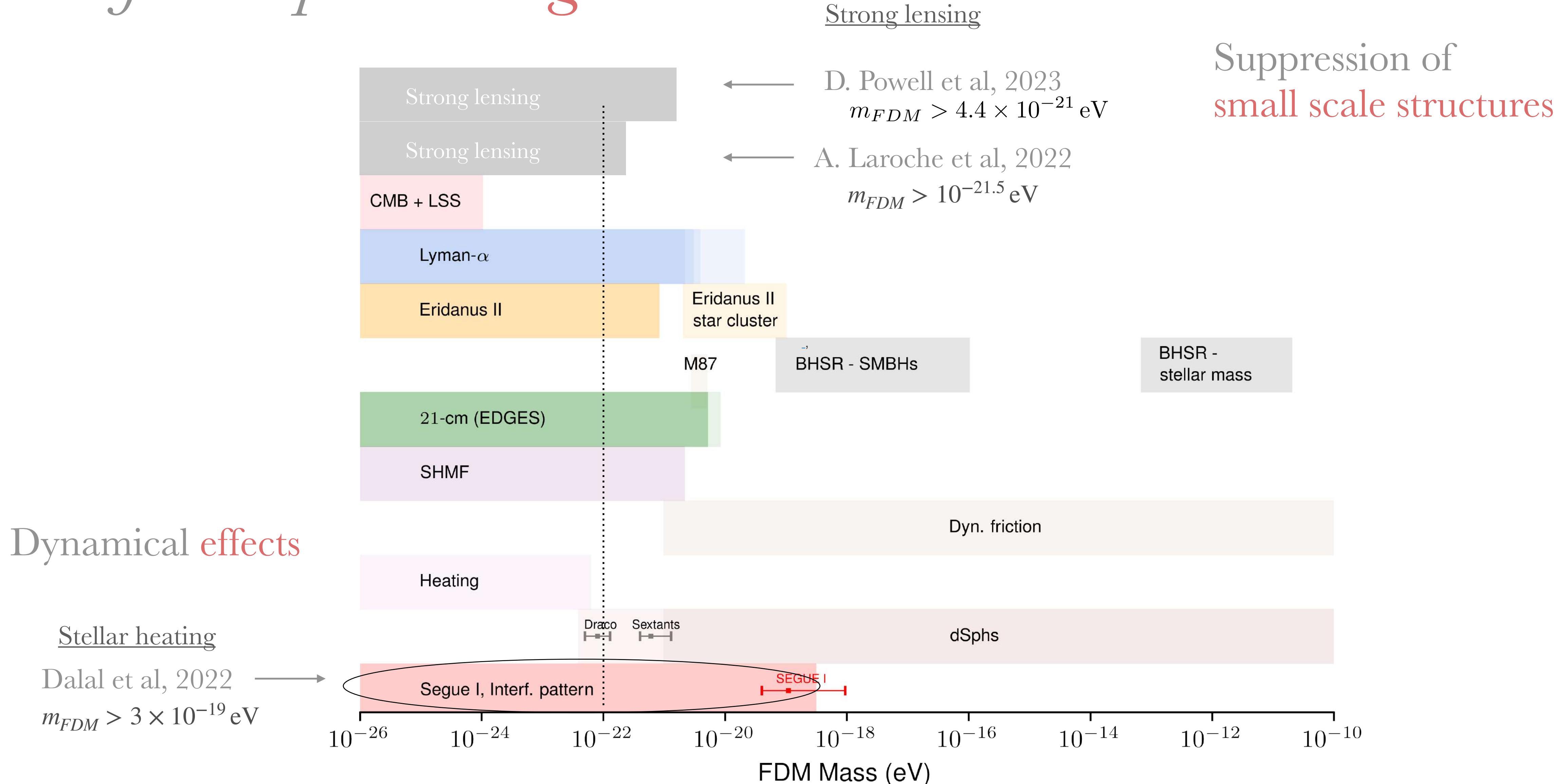
Kawai, Oguri (2021)

Dwarfs

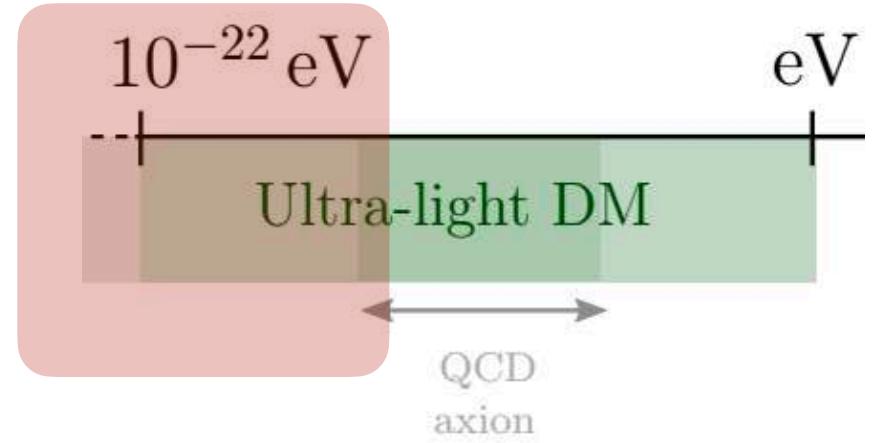
N. Dalal, A. Kravtsov, 2022



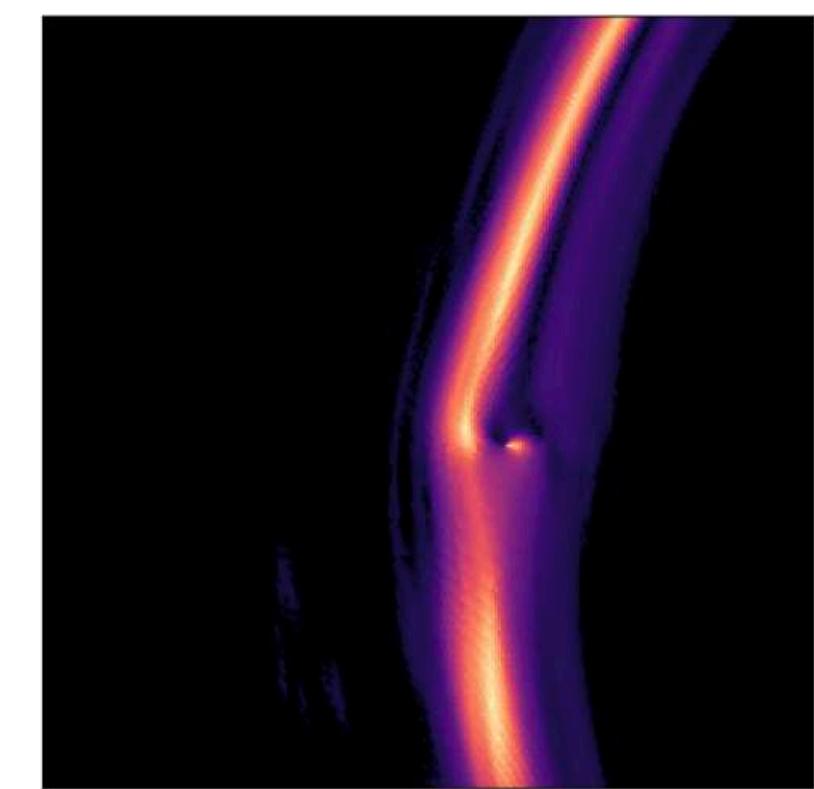
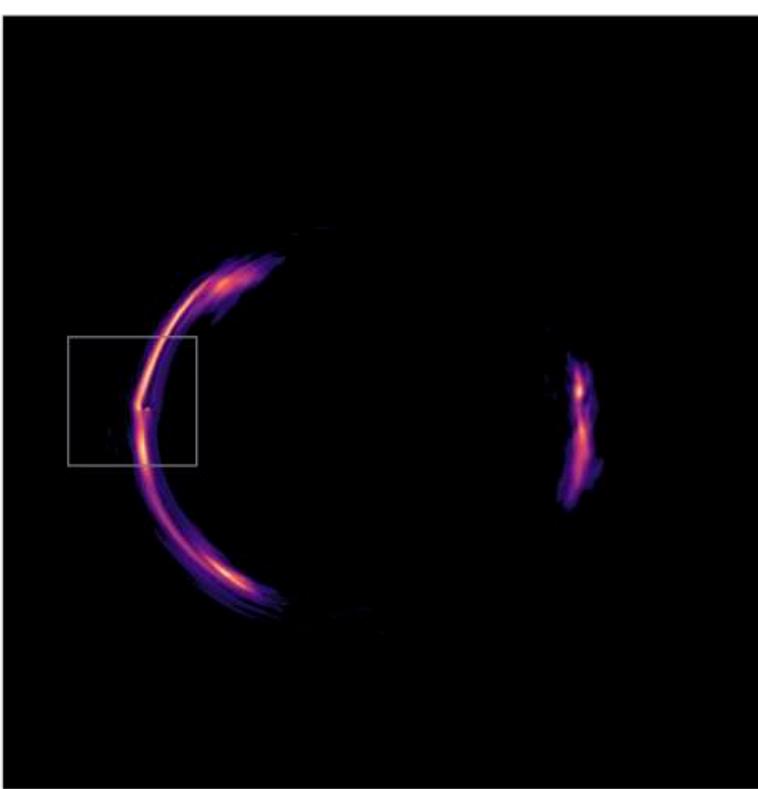
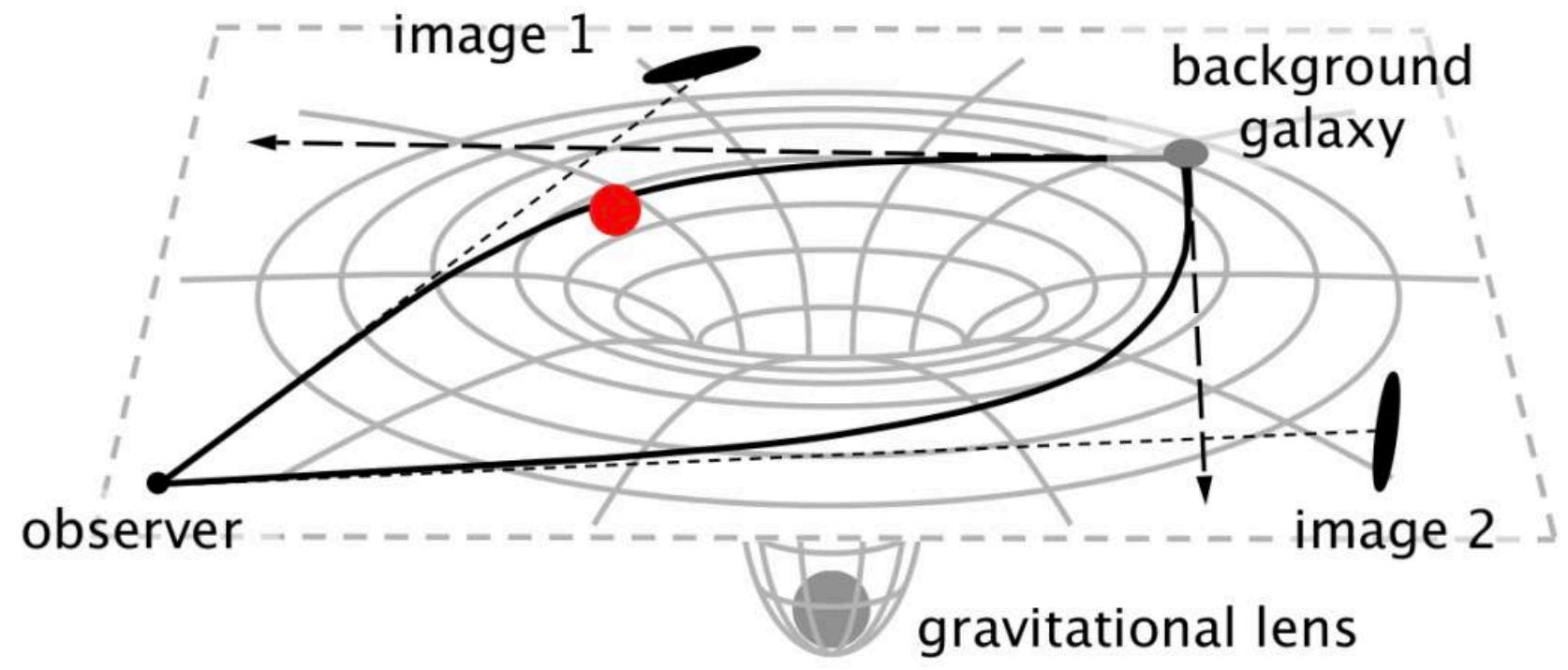
Interference patterns - granules



Strong *lensing*



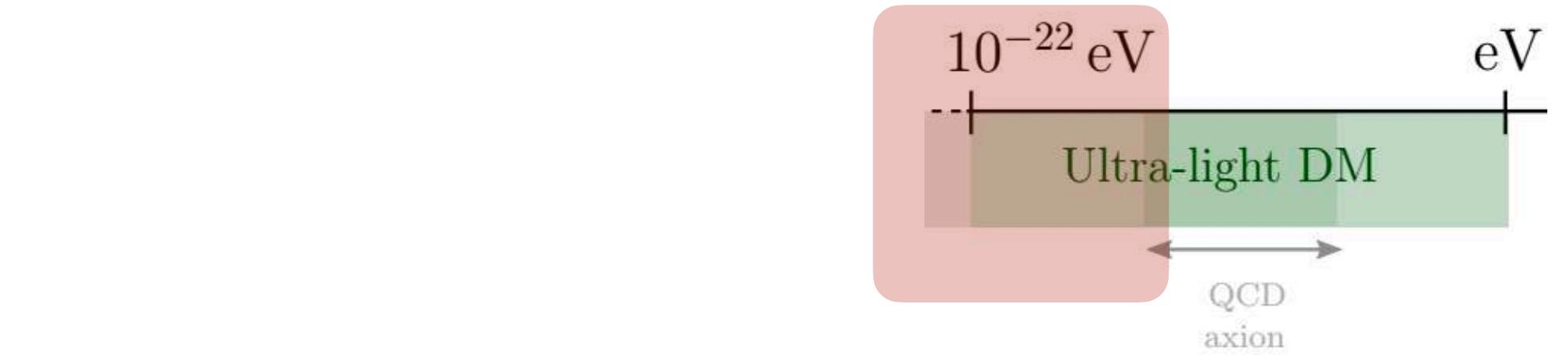
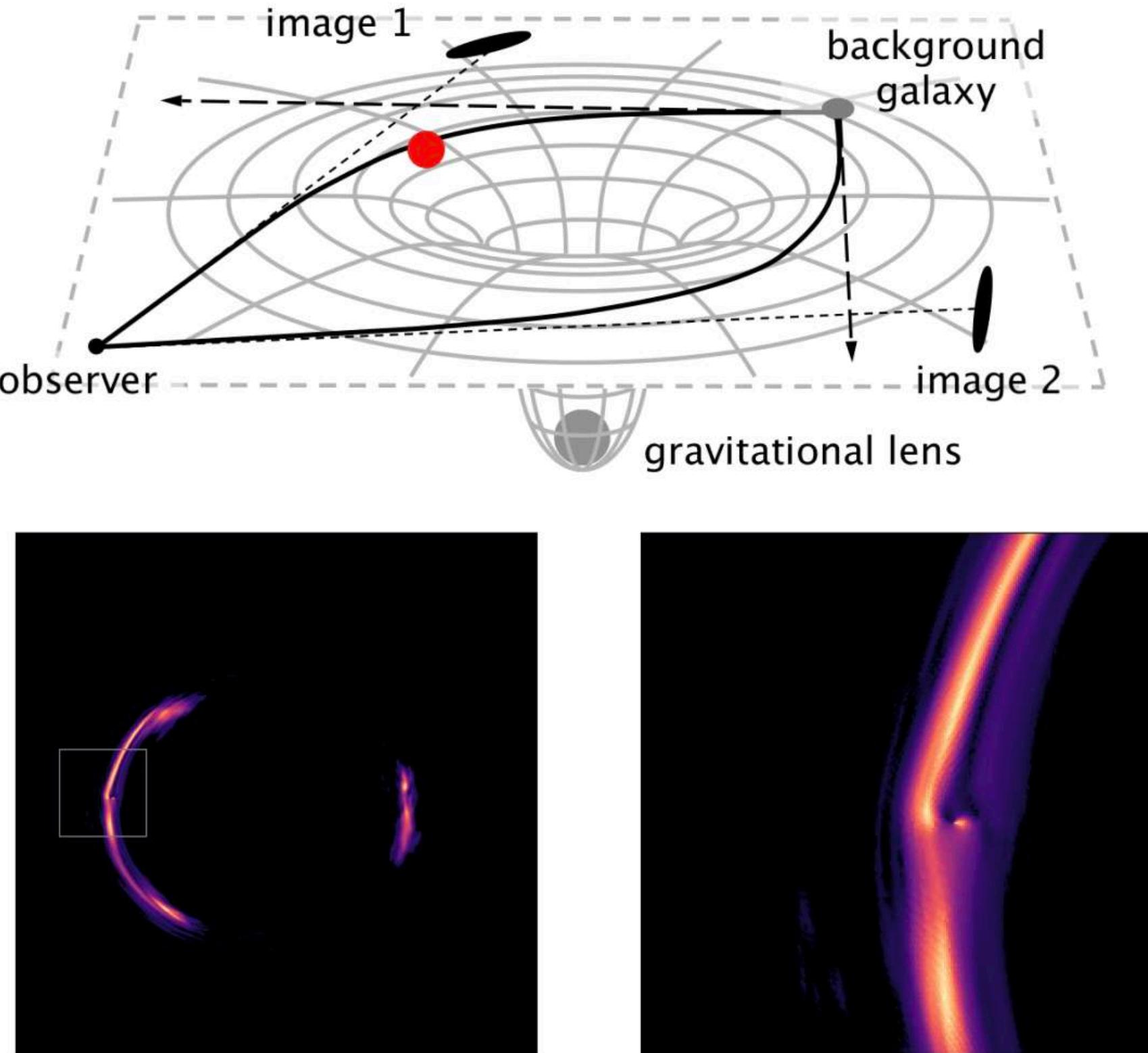
Low mass perturber with lensing



- Strong lensing: powerful probe of substructure
- Sensitivity is limited by angular **angular resolution**
- Roughly speaking, the resolution must be better than the scale radius of the perturber

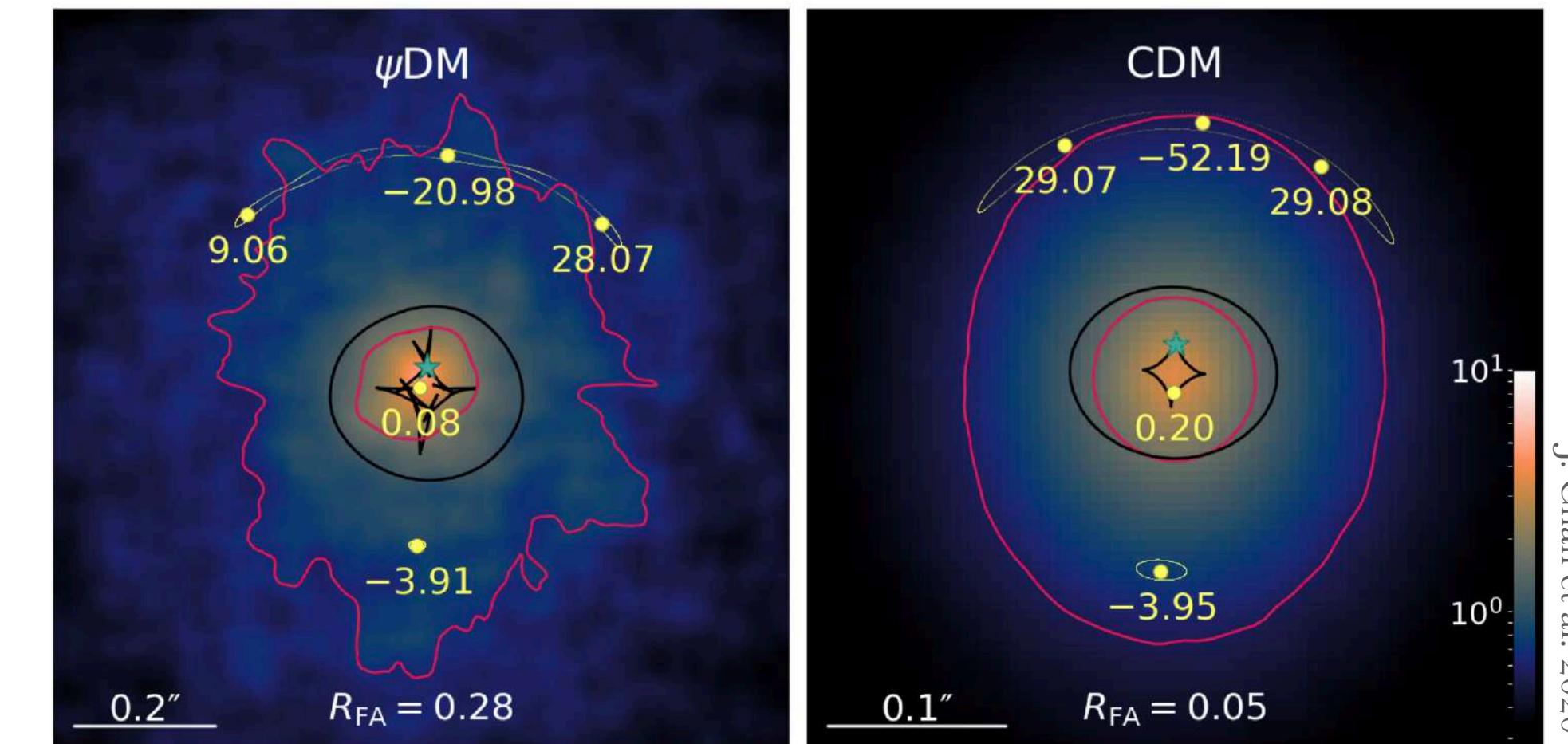
Strong *lensing*

Low mass perturber with lensing



Presence of granules

Surface densities overlaid with sources and quad images for fuzzy and smooth lenses



J. Chan et al. 2020

Fuzzy lens: fluctuating tangencial critical curve; flux ratio anomalies also sizable.

Previous works:

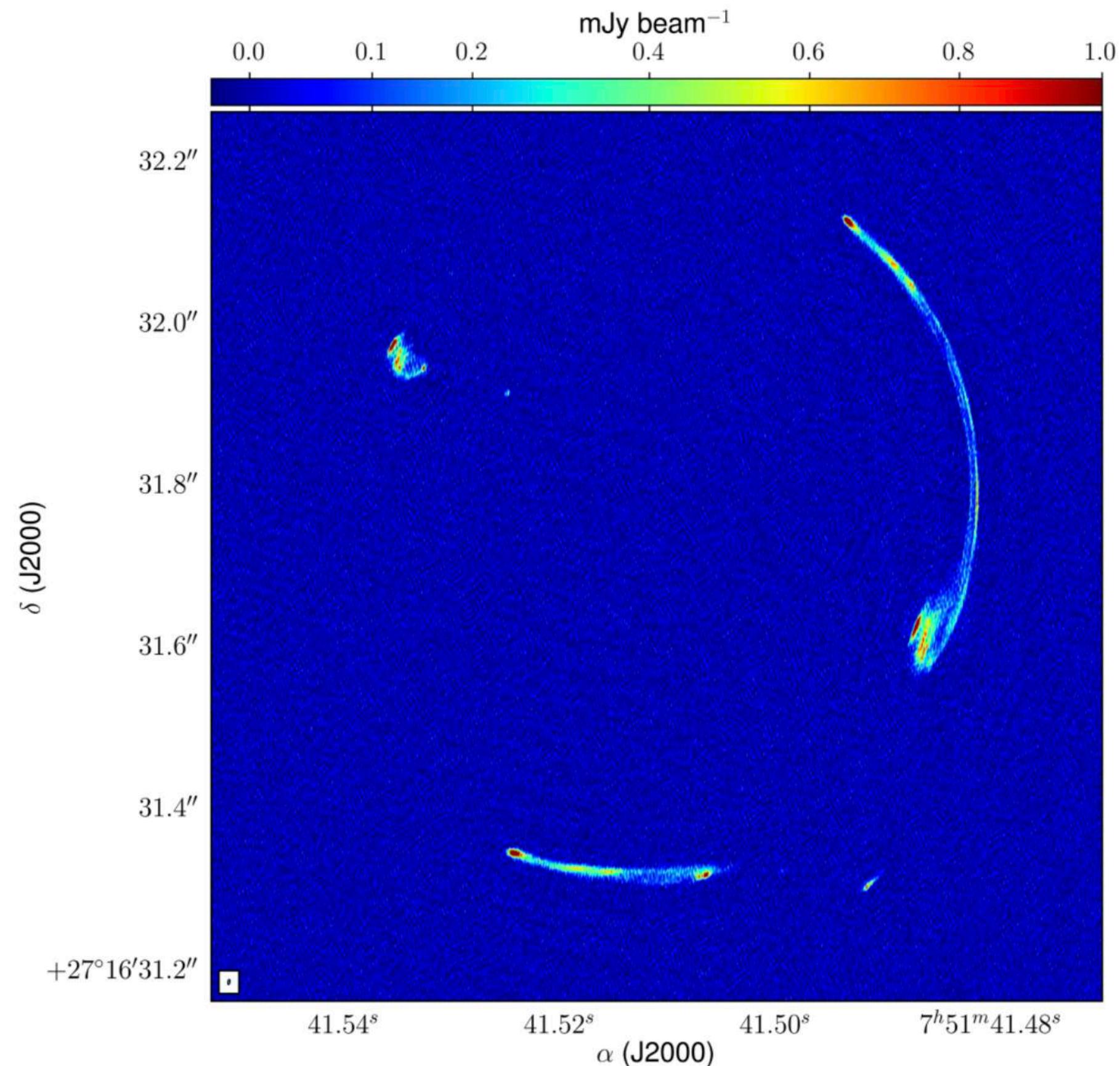
- J. Chan, H.Schive, S.g Wong, T. Chiueh, T. Broadhurst, 2020
- A. Laroche, Daniel Gilman, X. Li, J. Bovy, X. Du, 2022

Strong *lensing*

A lensed radio jet at milli-arcsecond resolution II: Constraints on fuzzy dark matter from an extended gravitational arc

D. Powell, S. Vegetti, J.P. McKean, S. White, EF, S. May, C. Spingola

MG J0751+2716



- Lensed radio jet, observed with global VLBI
- First image of a lensed radio jet!
- Source structure allows us to “image” the lens surface density
- Extended lensed radio arcs and the milli-arcsecond resolution provide direct sensitivity to the presence of **FDM granules** in the halo of the lens galaxy

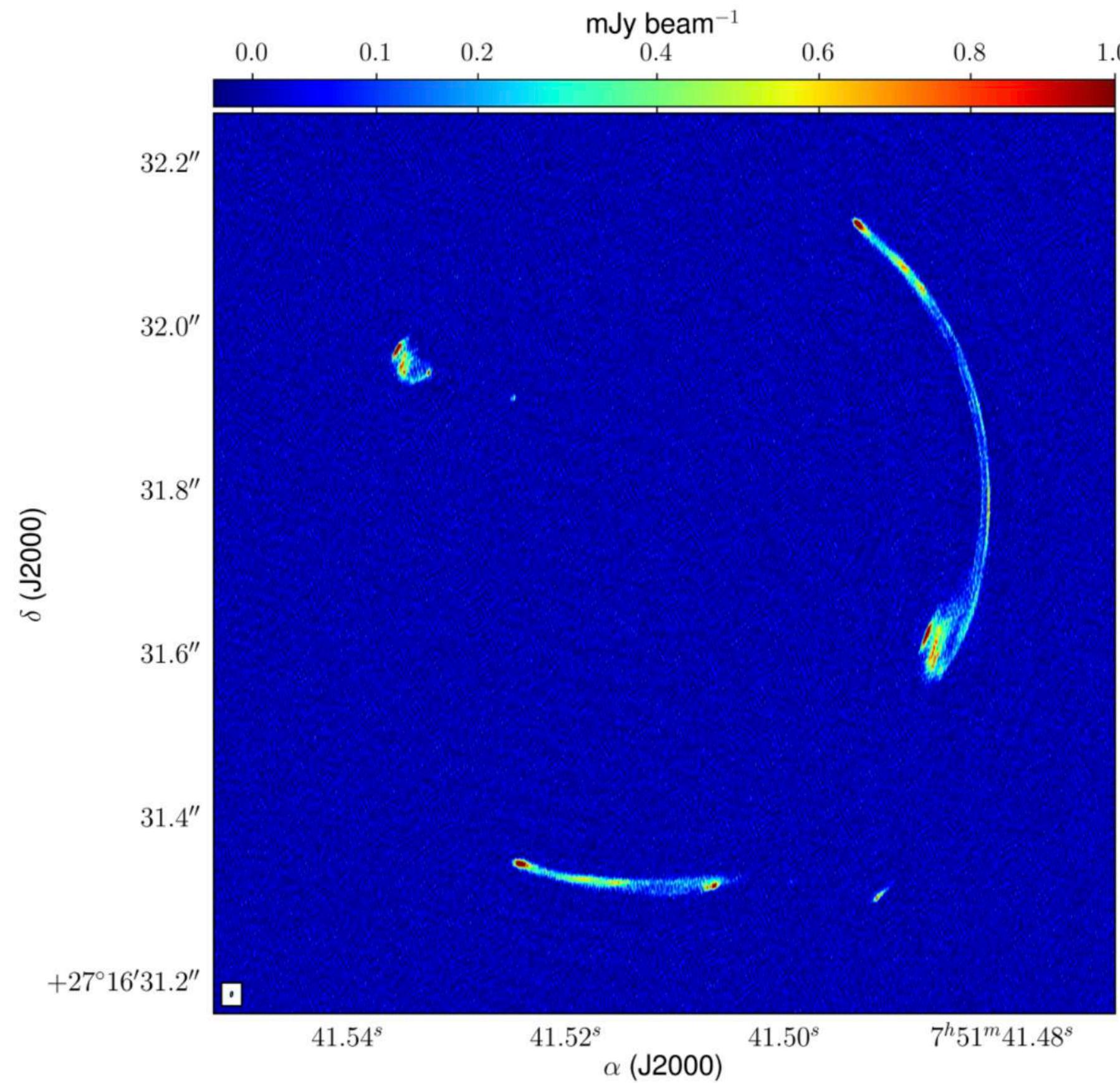
Data taken at 1.6 GHz using global very long baseline interferometry (VLBI) with an angular resolution, measured as the full width at half maximum (FWHM) of the main lobe of the dirty beam response, of 5.5×1.8 mas 2

Strong *lensing*

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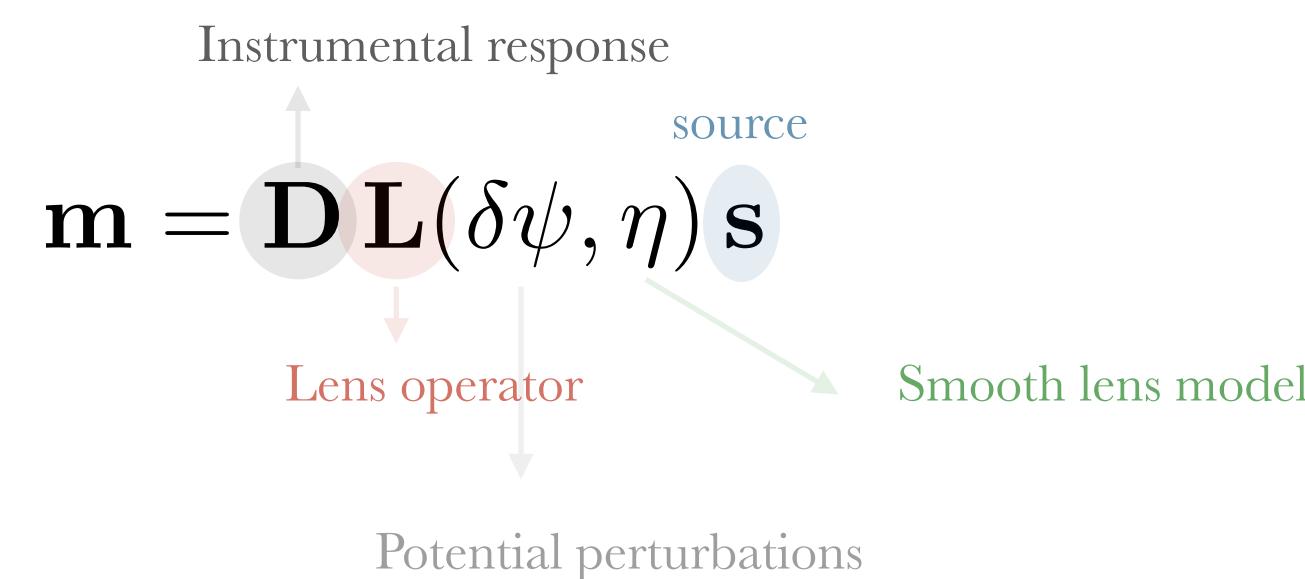
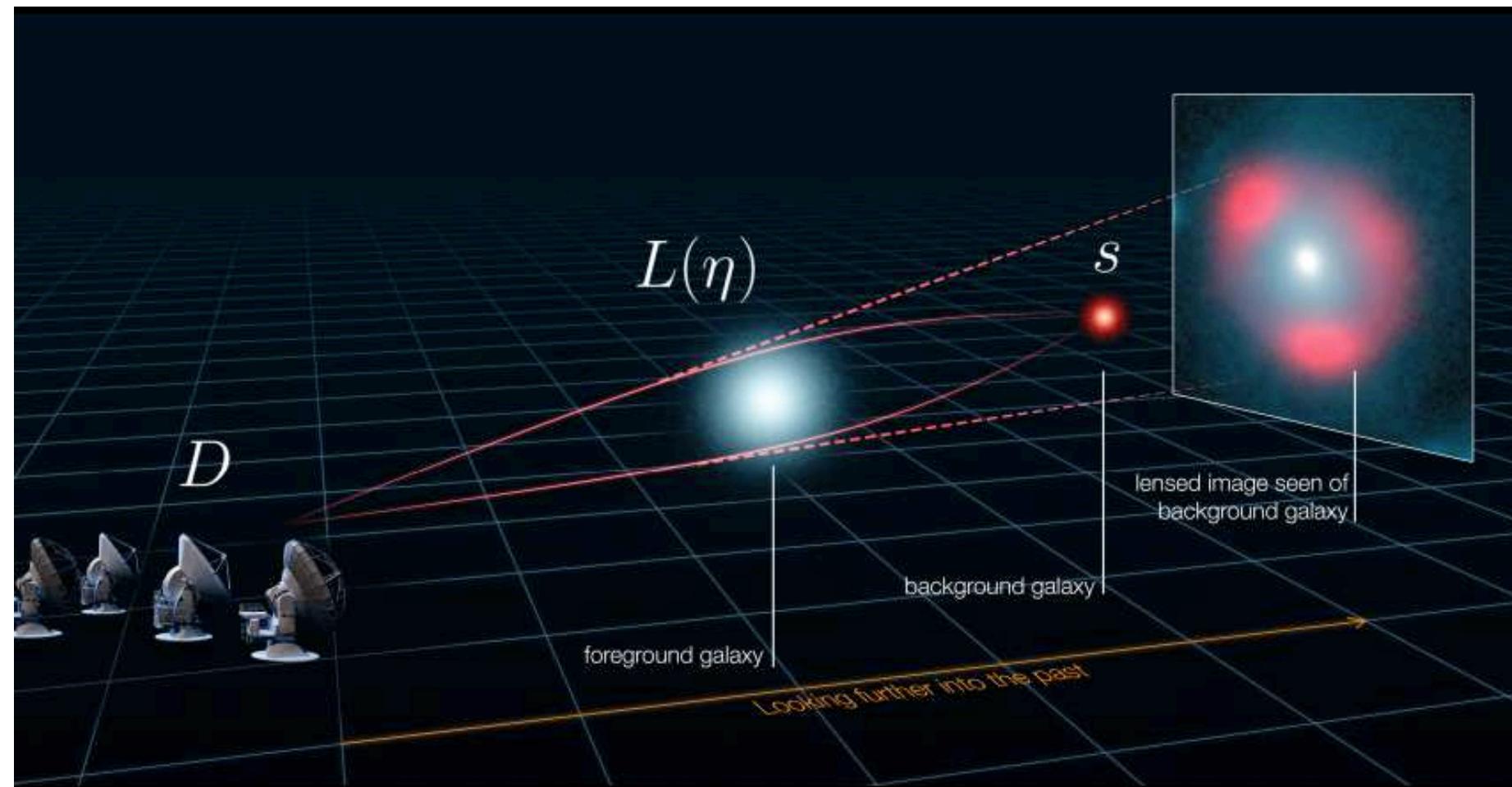
Bayesian approach to jointly inferring the lens mass model and source surface brightness distribution

Strong *lensing*

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D. Powell, S. Vegetti, J.P. McKean, S. White, EF, S. May, C. Springola

Forward modeling



$$\delta\psi(m_{fdm}, f_{dm}, \sigma_v)$$

Smooth lensing model: from *Powell et al 2022*

FDM granules:

Model by Chan et al 2020: statistics of spatially-varying surface mass density fluctuations, given the density profile of the dark matter, as well as some basic assumptions on the behavior of scalar fields in a potential well

$\delta\psi(m_{fdm}, f_{dm}, \sigma_v)$ (perturbation of the lensing potential)
fluctuations in the projected surface mass density written as perturbations in the lensing convergence due to the presence of the **granules**:

$$\langle \delta\kappa^2 \rangle = \frac{\lambda_{db}}{2\sqrt{\pi}\Sigma_c^2} \int_{los} \rho_{DM}^2 dl$$

↓

We wish to infer a posterior distribution on the dark matter particle mass $\mathcal{P}(m_{fdm})$

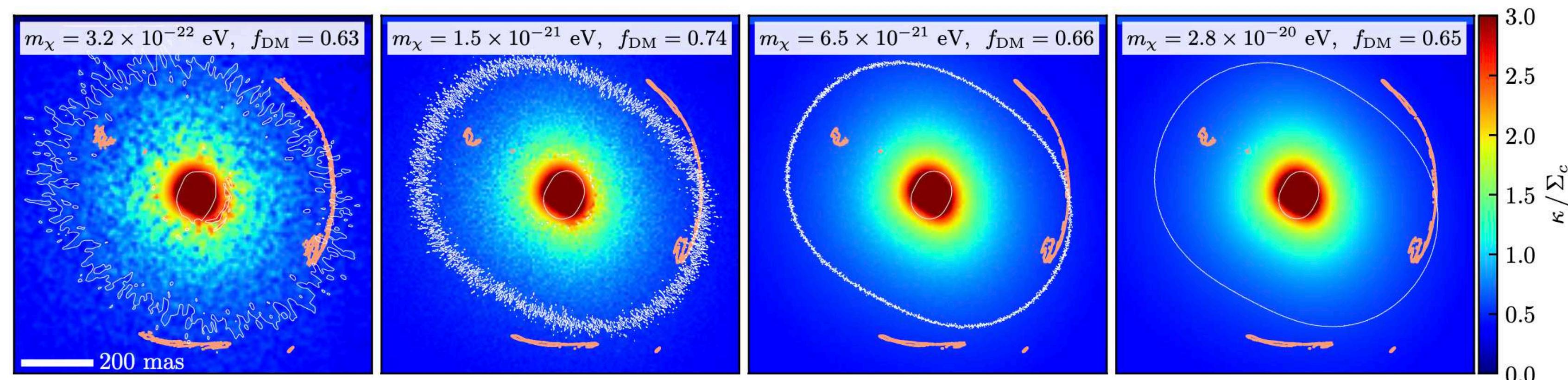
We compute likelihoods for 10^4 sample FDM lens realizations with m_{fdm} drawn from the log-uniform prior range $\log(m_{fdm}/\text{eV}) \in [-21.5, -19.0]$.

Strong *lensing*

A lensed radio jet at milli-arcsecond resolution II: Constraints on fuzzy dark matter from an extended gravitational arc

D. Powell, S. Vegetti, J.P. McKean, S. White, EF, S. May, C. Springola

Example convergence maps with corresponding MAP surface mass density maps (κ , in units of the critical density Σc) reconstruction for 4 random realizations of MG J0751+2716 in an FDM cosmology - the model lensed images in orange contours



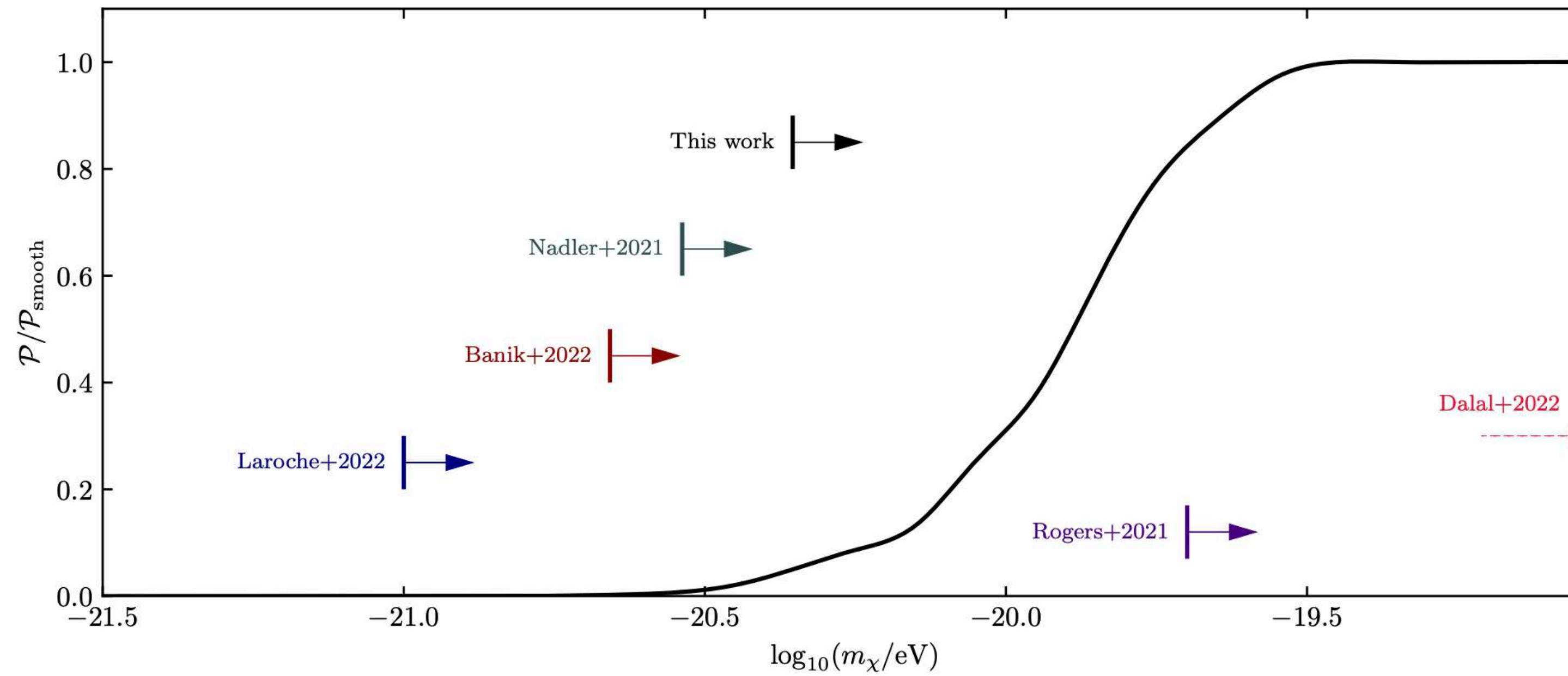
The lensing effect of the FDM granules is apparent: The critical curves wiggle back and forth across the lensed arcs, which would require the presence of multiple images of the same region of the source along the arc.

Strong lensing

A lensed radio jet at milli-arcsecond resolution II: Constraints on fuzzy dark matter from an extended gravitational arc

D. Powell, S. Vegetti, J.P. McKean, S. White, EF, S. May, C. Springola

Results quoted in terms of posterior odds ratio (POR) between FDM with a particle mass m_{fdm} and the smooth model, $\mathcal{P}/\mathcal{P}_{\text{smooth}}$



Fuzzy dark matter
(Single spin-0 particle)

$$m_{\text{fdm}} > 4.4 \times 10^{-21} \text{ eV}$$

Vector fuzzy dark matter
(spin-1 particle)
OR 3 same mass FDM

$$m_{\text{vdm}} > 1.4 \times 10^{-21} \text{ eV}$$

Spin-2 FDM

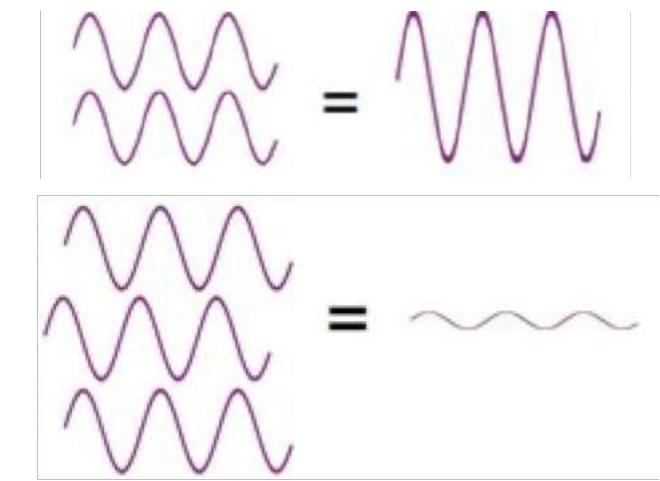
$$m_{\text{spin-2}} > 8.8 \times 10^{-22} \text{ eV}$$

Vector, higher spin or multicomponent FDM

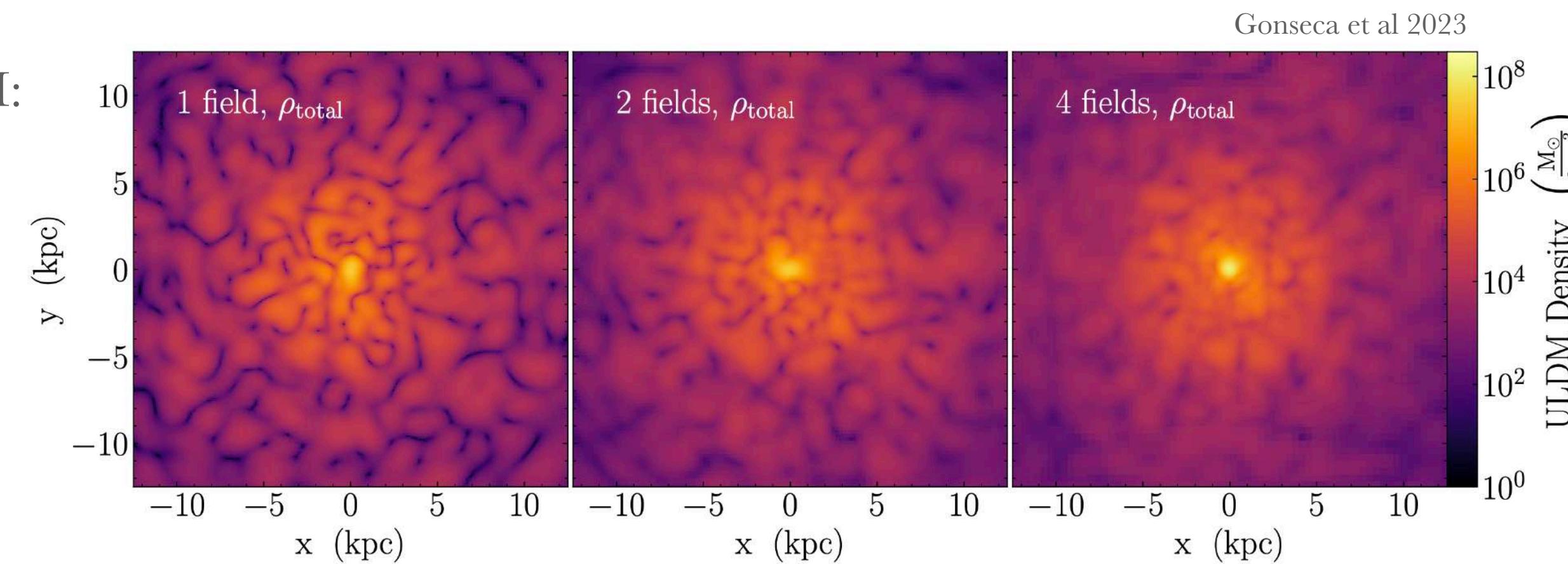
ULDM or ULA are a coherent wave - same frequency and constant phase difference

Multiple coherent waves

Interference patterns



For ULDM:



Gonseca et al 2023

Multiple FDM or VFDM (or higher spin s FDM)
attenuates the granule amplitude by

$$\frac{[\delta\rho/\rho]_{\text{nfdm},s}}{[\delta\rho/\rho]_{\text{fdm}}} \propto \frac{1}{\sqrt{(2s+1)}} = \frac{1}{\sqrt{N}}$$

(Amin et al 2022)

Expectation for lensing:

$$\langle \delta\kappa^2 \rangle = \frac{\lambda_{dB}}{2\sqrt{\pi}\Sigma_c^2} \int \rho_{\text{DM}}^2 dl$$



$$m_{\text{nfdm},s} = \frac{m_{\text{fdm}}}{N} = \frac{m_{\text{fdm}}}{2s+1}$$

Vector (and higher-spin) FDM Amin et al 2022
(Vector FDM = 3 x same mass FDM (spin 0))

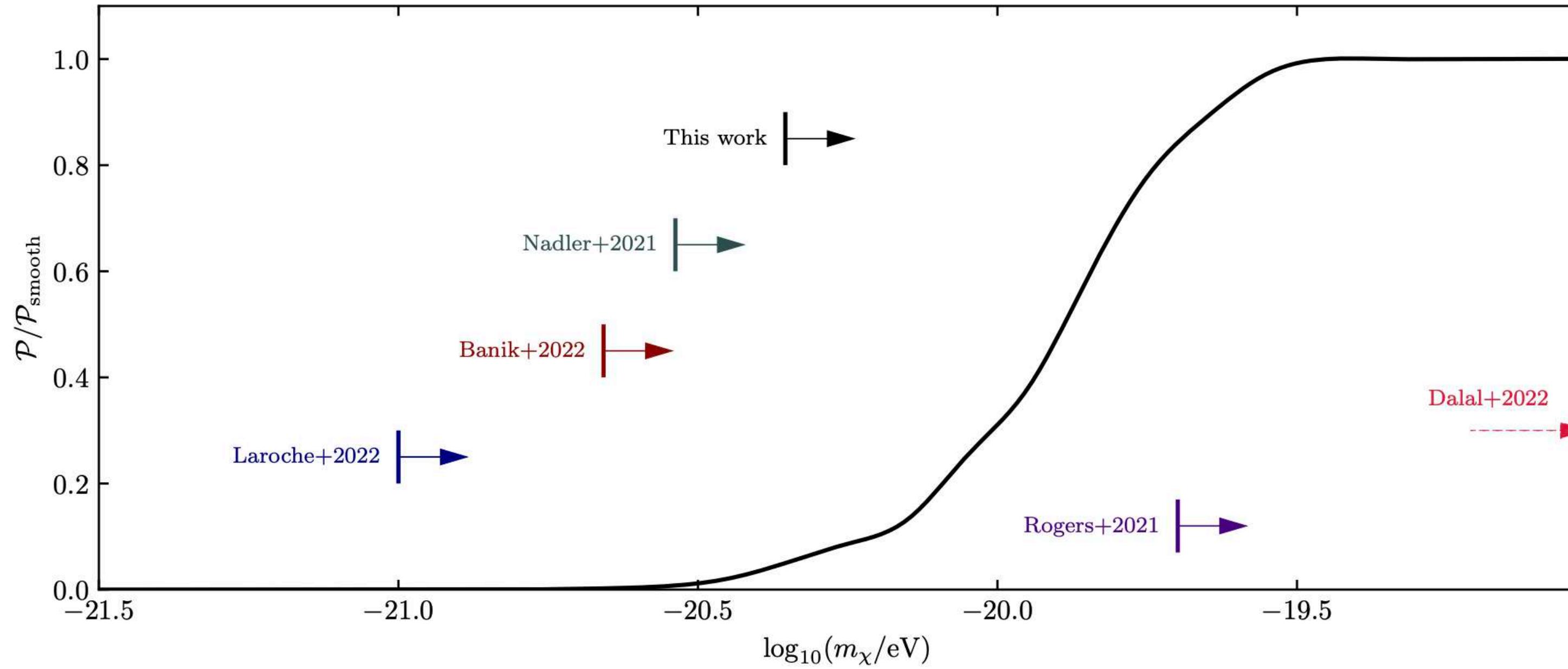
Multicomponent FDM Gonseca et al 2023

Detailed simulations and analysis in the future!

Strong lensing

A lensed radio jet at milli-arcsecond resolution II: Constraints on fuzzy dark matter from an extended gravitational arc

D. Powell, S. Vegetti, J.P. McKean, S. White, EF, S. May, C. Springola



Fuzzy dark matter
(Single spin-0 particle)

$$m_{\text{fdm}} > 4.4 \times 10^{-21} \text{ eV}$$

Vector fuzzy dark matter
(spin-1 particle)
OR 3 same mass FDM

$$m_{\text{vdm}} > 1.4 \times 10^{-21} \text{ eV}$$

Spin-2 FDM

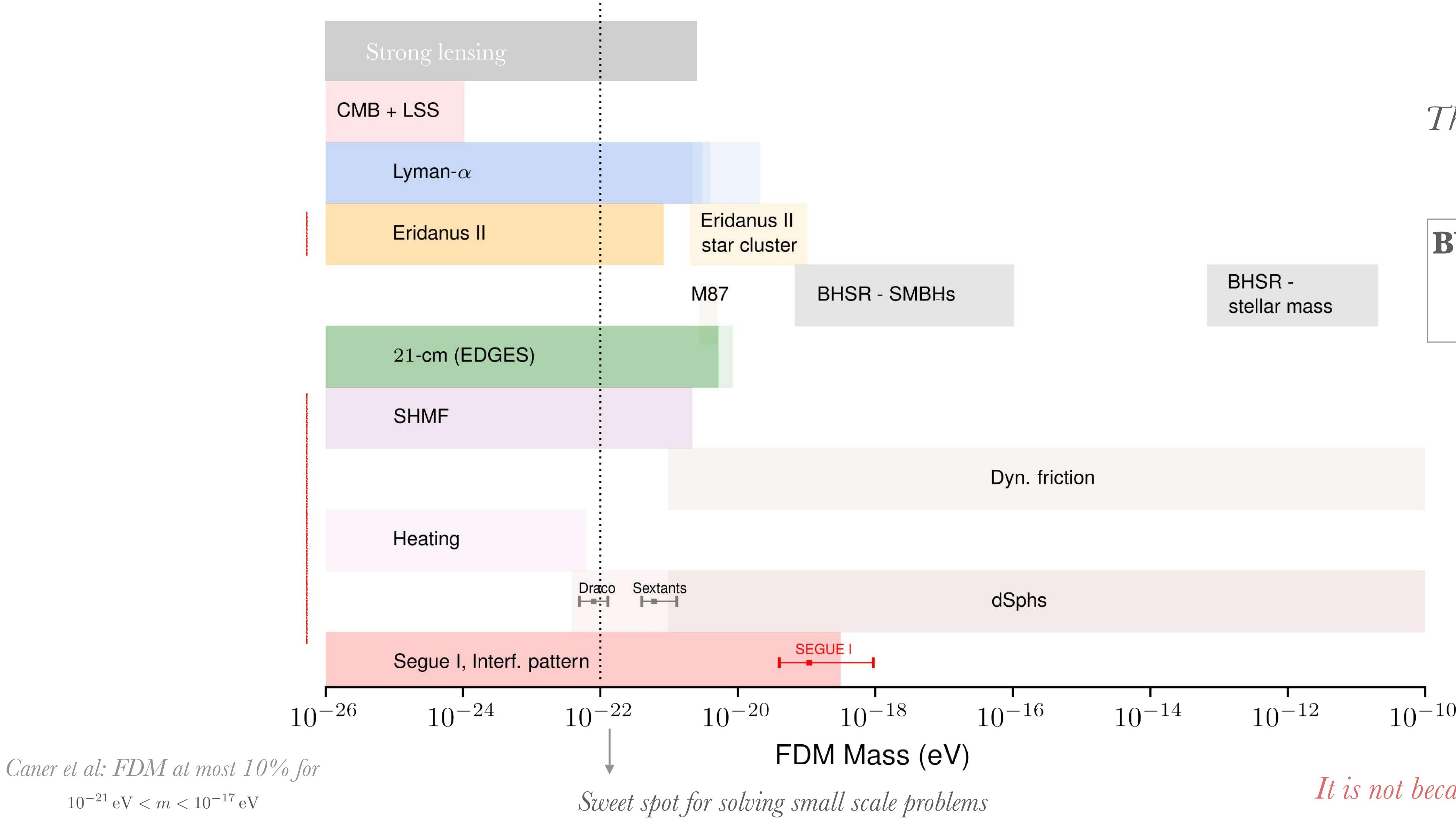
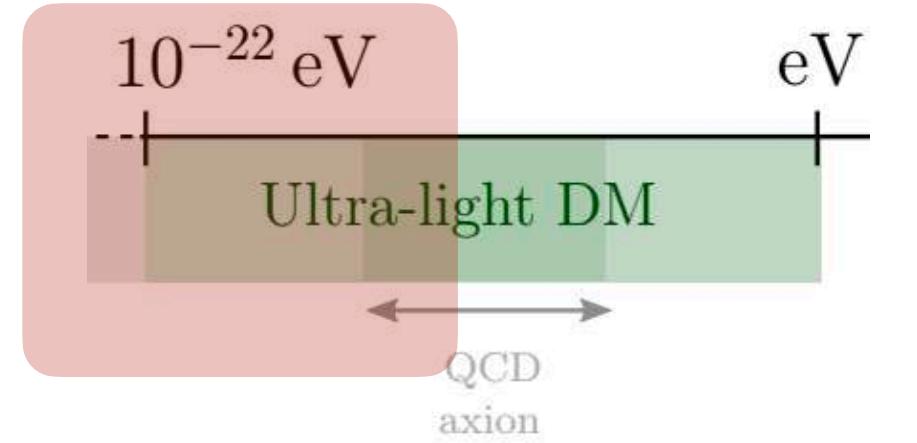
$$m_{\text{spin-2}} > 8.8 \times 10^{-22} \text{ eV}$$

Milli-arcsecond angular resolution of VLBI, **competitive constraints** on dark matter models can be inferred using a **single** strong gravitational lens observation

More lenses in the future!

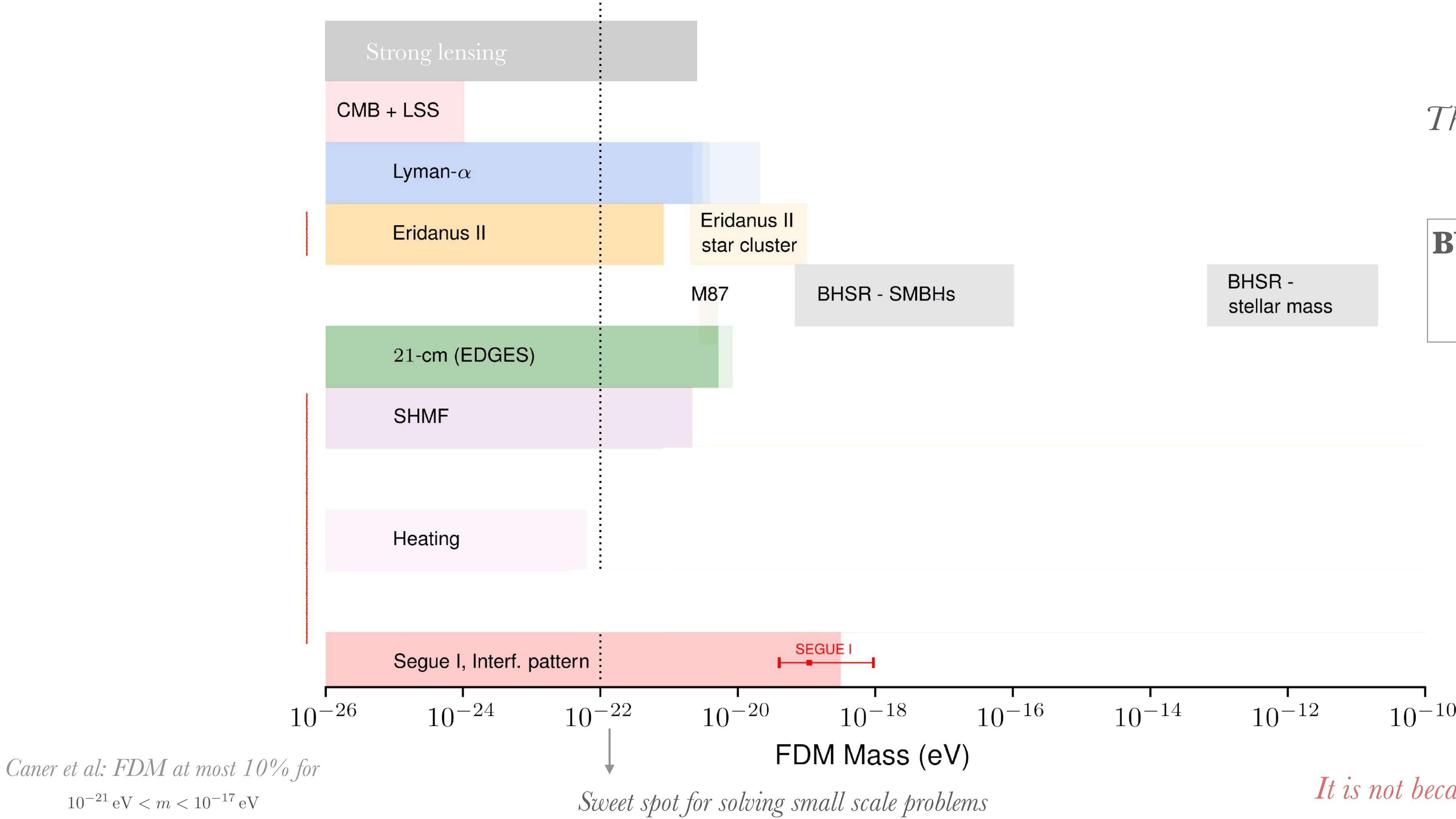
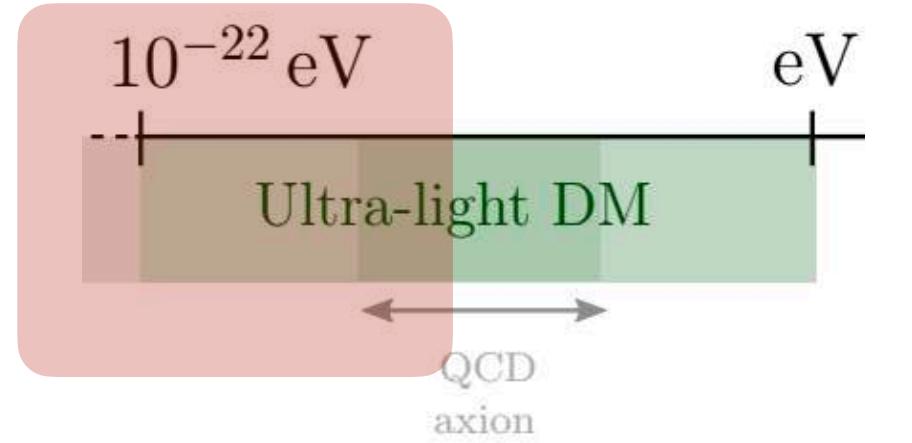
Current status

Fuzzy Dark Matter - bounds on the mass



Current status

Fuzzy Dark Matter - bounds on the mass



These models can be constrained

BUT: - systematic effects!!
- dynamics of FDM not fully understood.

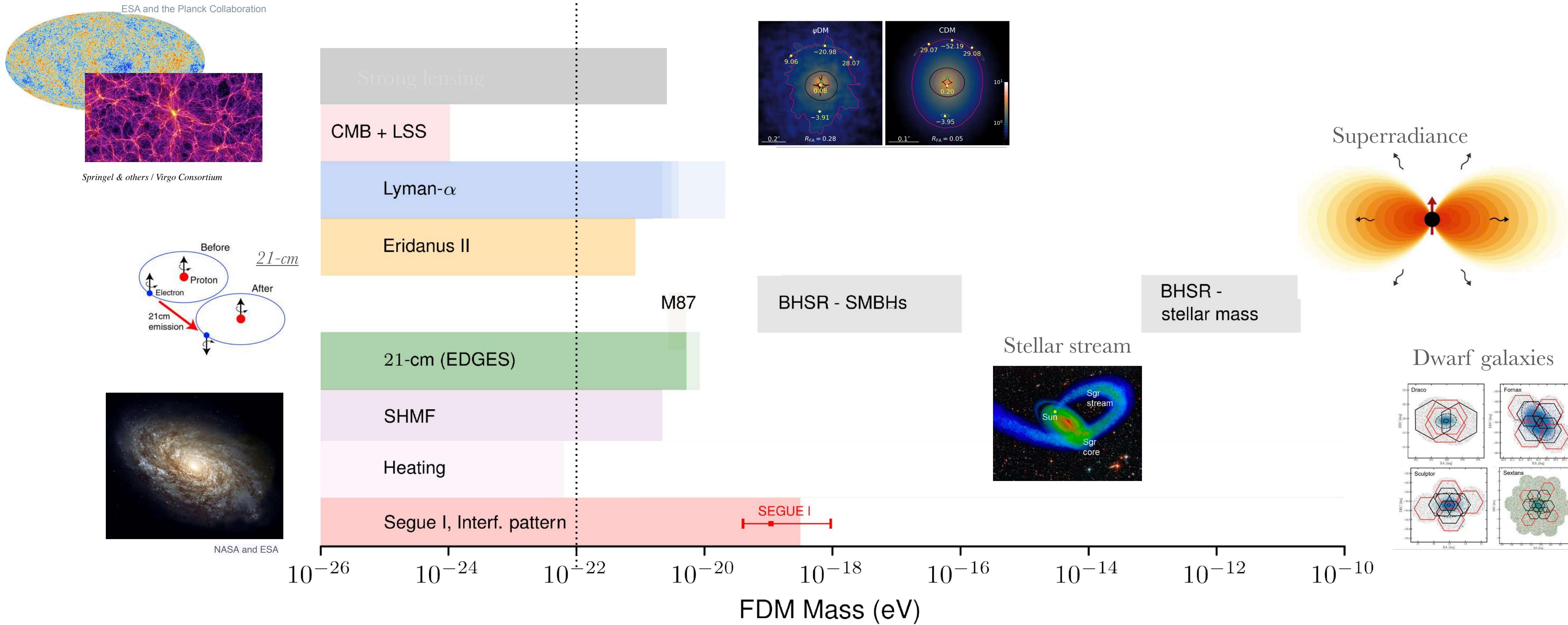
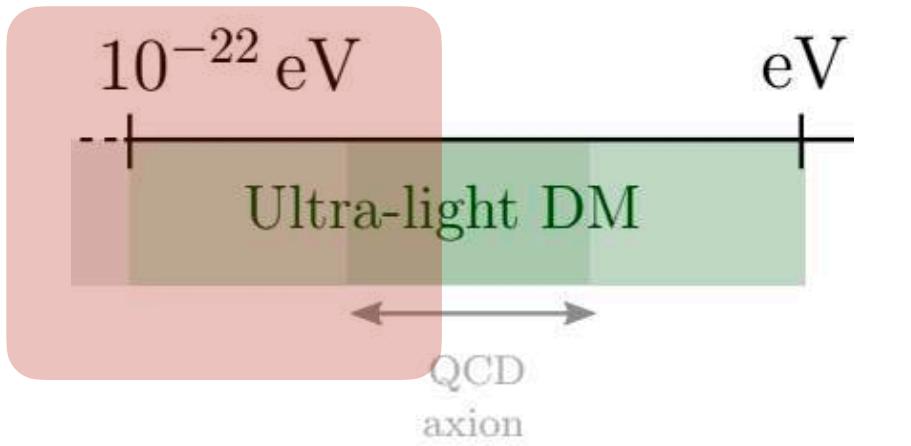
Some bounds are *incompatible!*

- Need:
- Observations
 - Improve sims
 - New observables
 - New probes

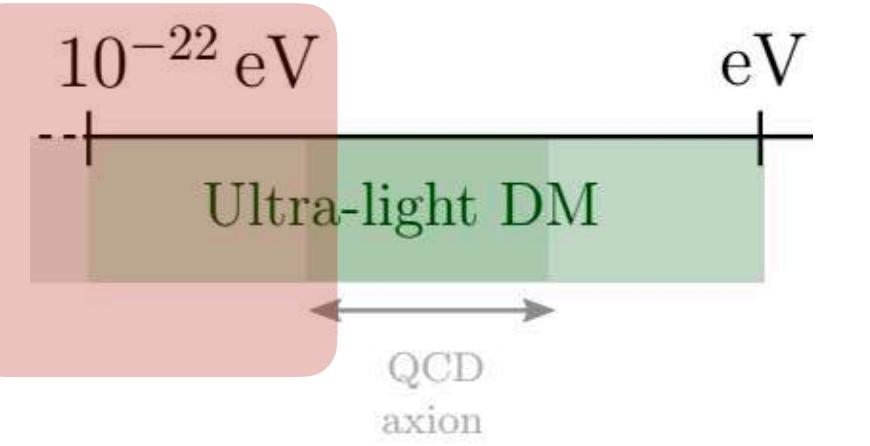
It is not because a bound is here that is correct!

Current status

Fuzzy Dark Matter - bounds on the mass



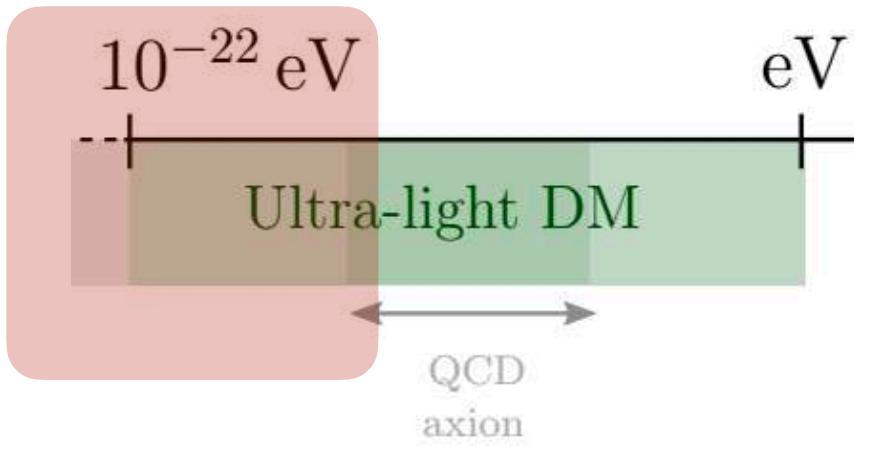
Fuzzy Dark Matter



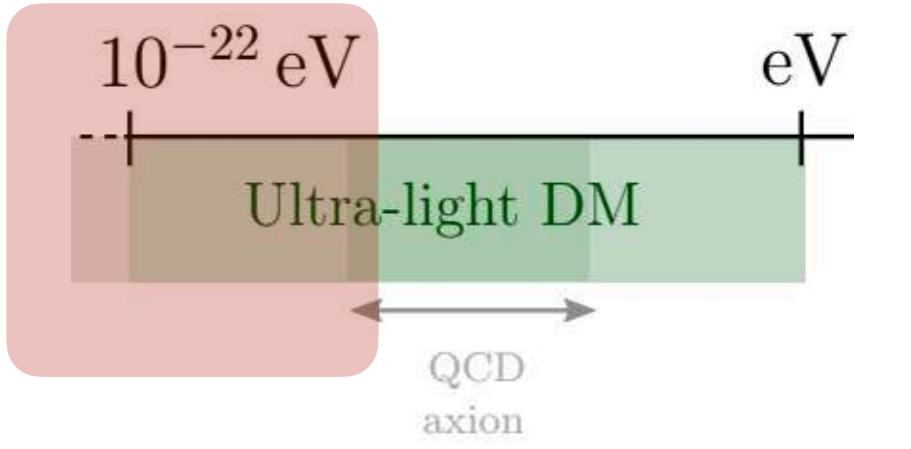
Open questions:

- Condensation?
- Quantum mechanical?
- Vortice description
- Baryons influence
- ...

Role of baryons

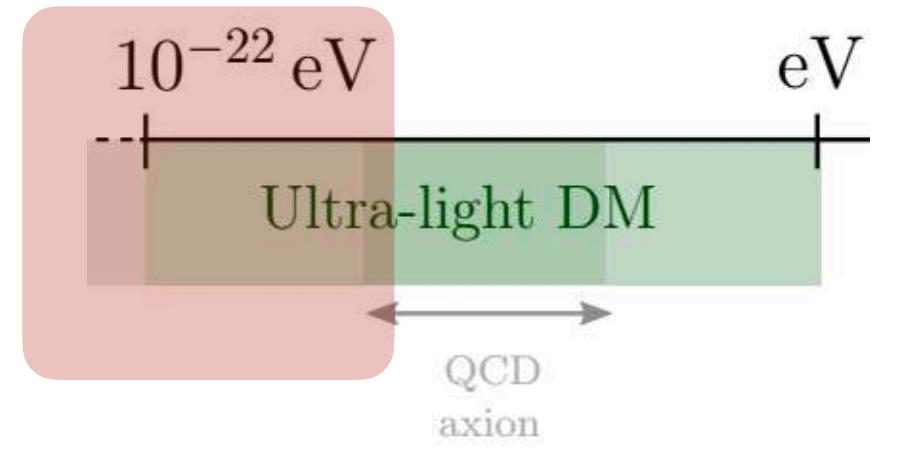


Role of baryons

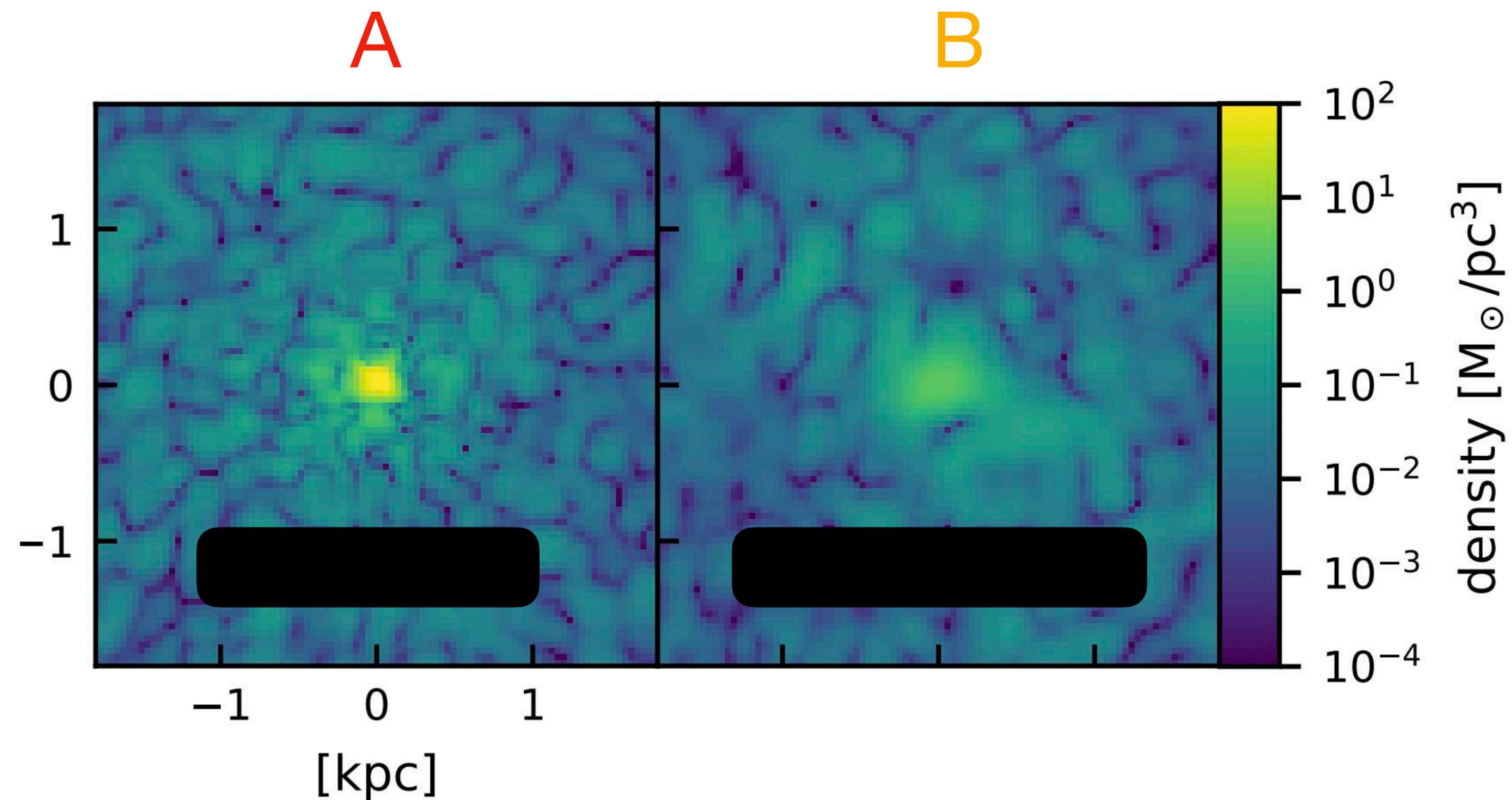


Quiz time!!

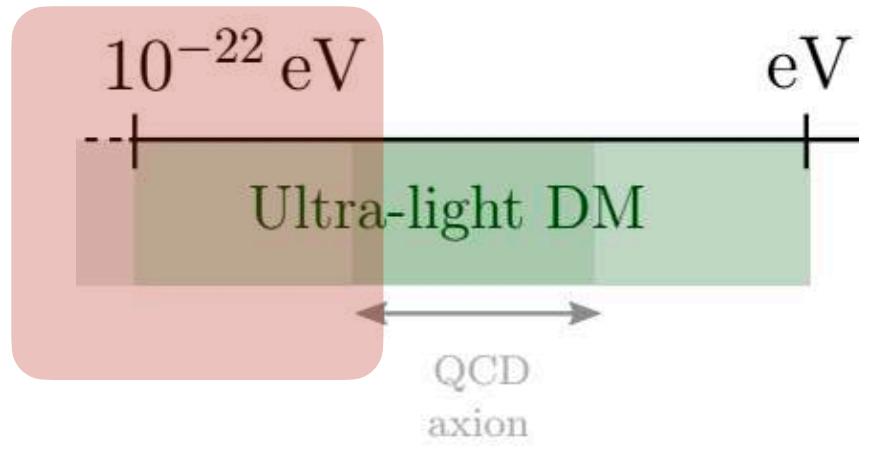
Role of baryons



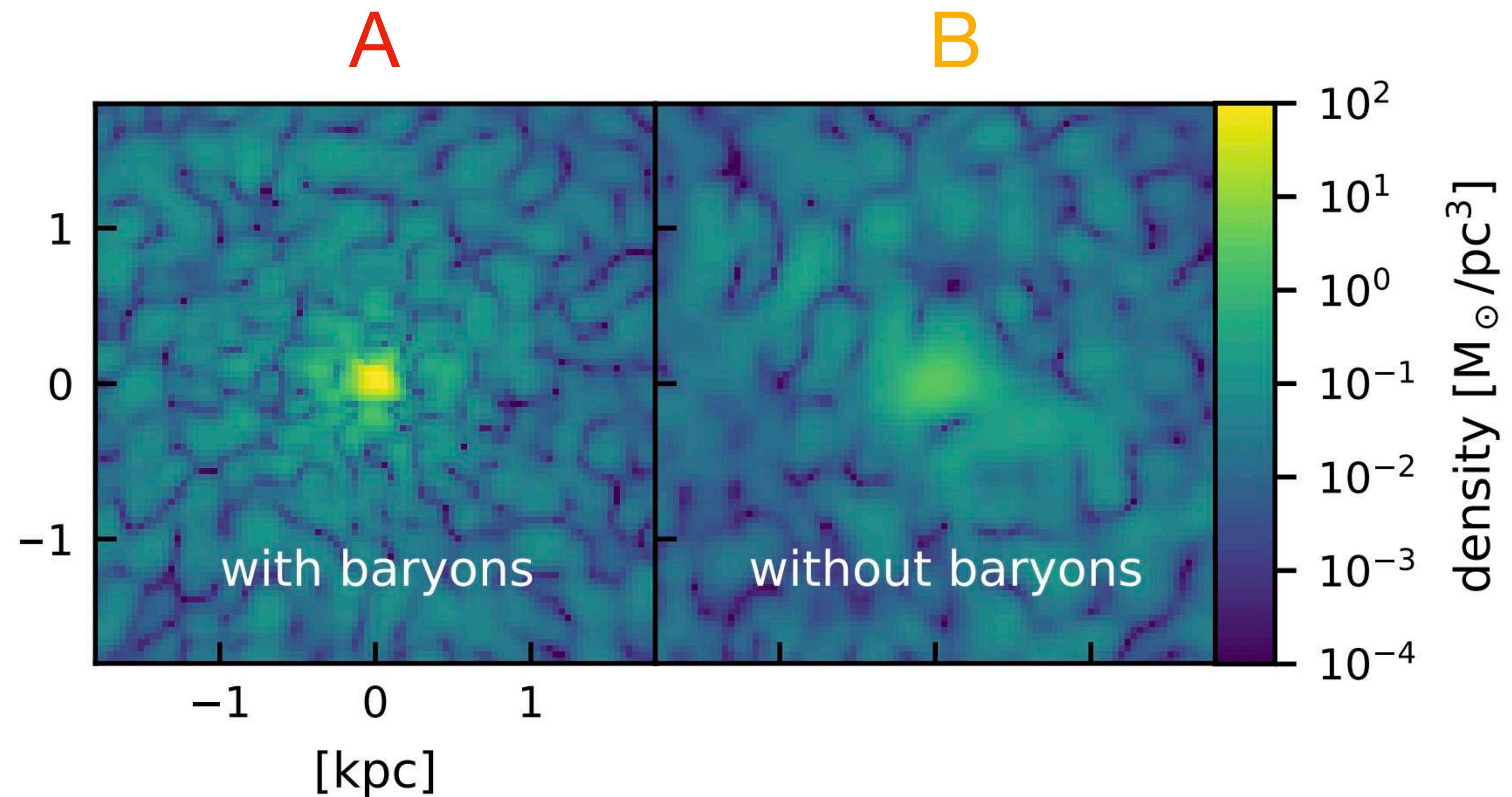
From those two images, which one do you think has the influence of baryons?



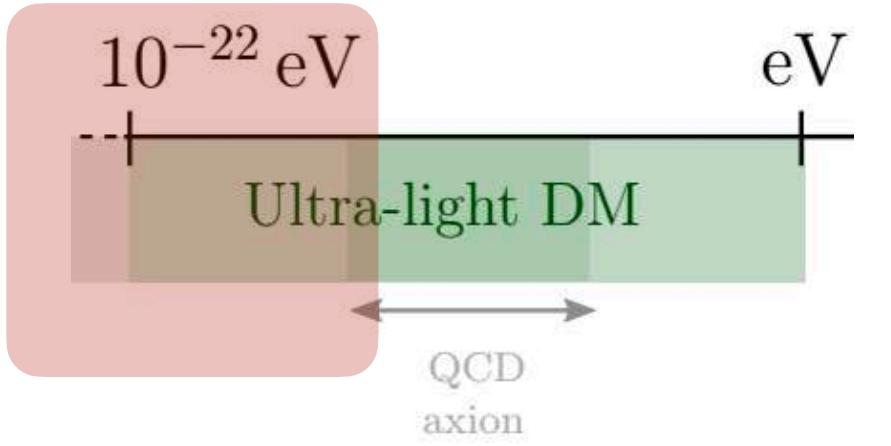
Role of baryons



From those two images, which one do you think has the influence of baryons?



Role of baryons



How baryons influence the behavior of ULDM?

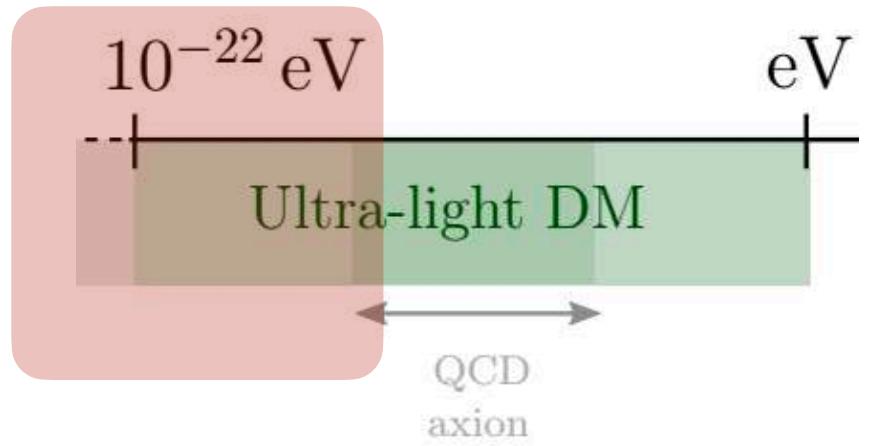
A) Enhance the small scale structures

C) Suppress small scale structure

B) Eject matter from galaxies

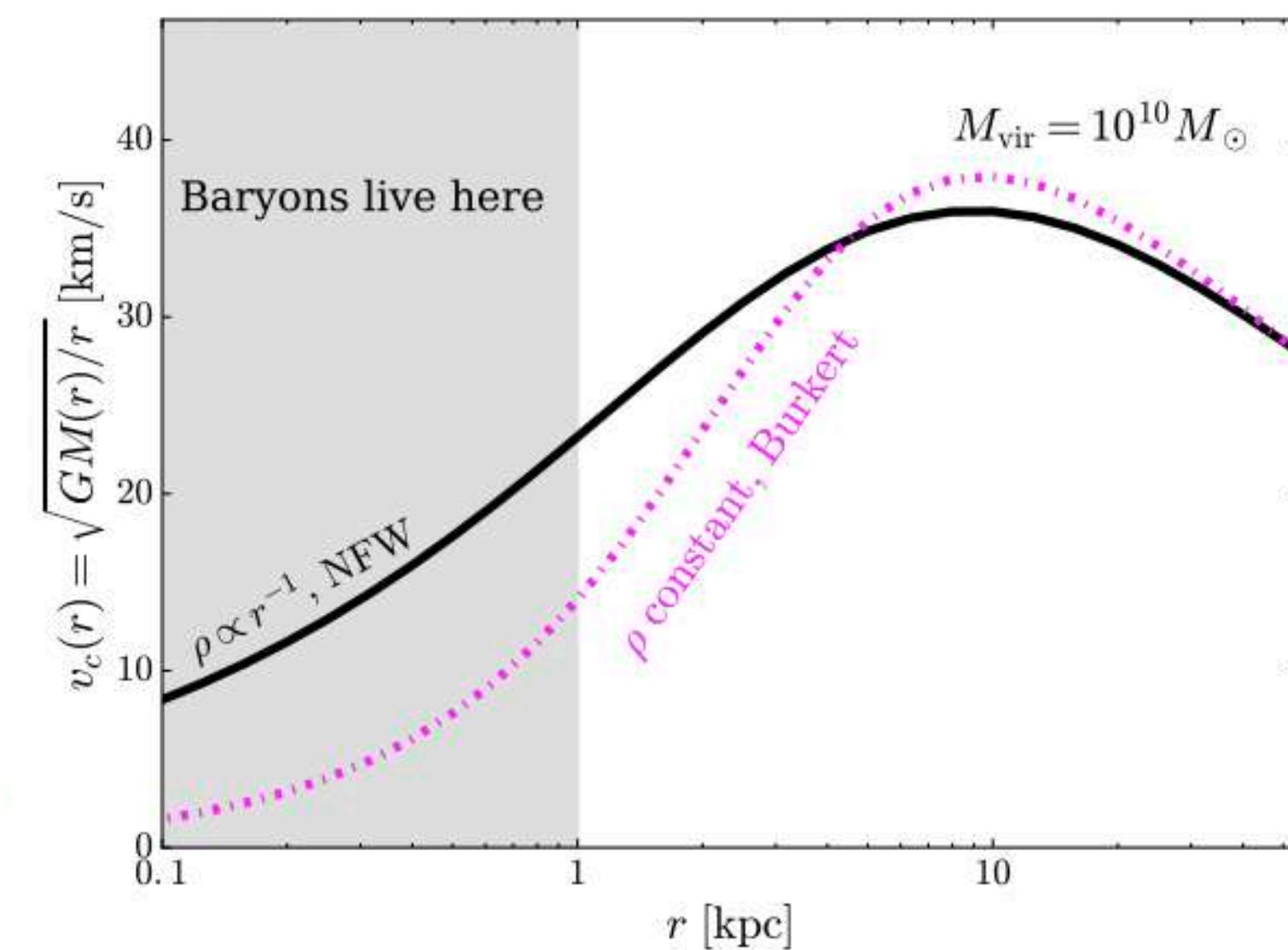
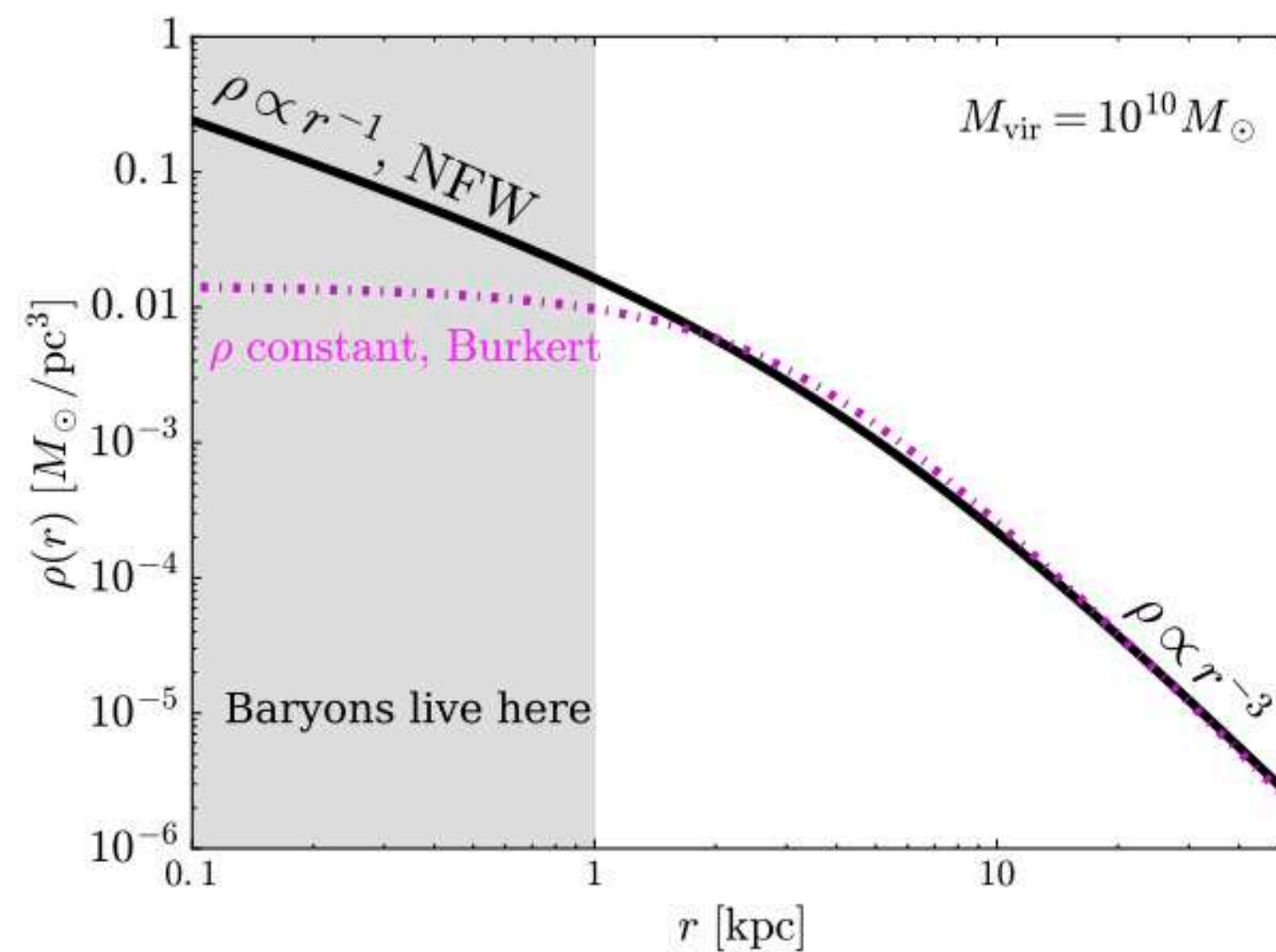
D) All of the above

Role of baryons

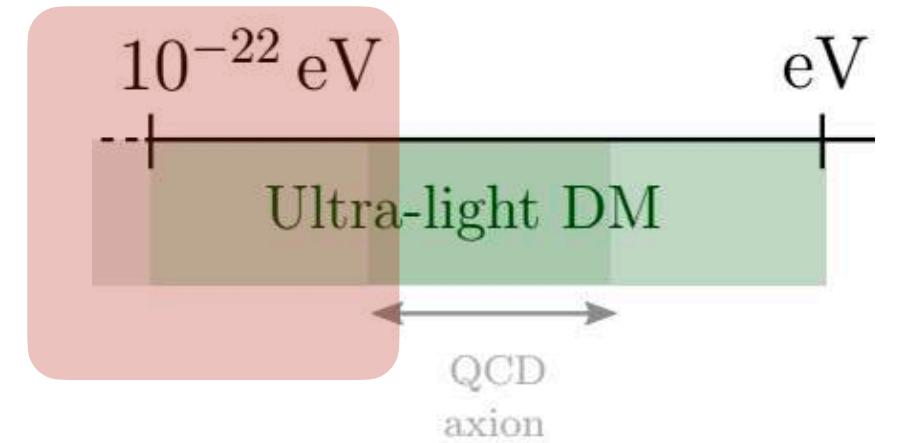


Core

Baryonic feedback

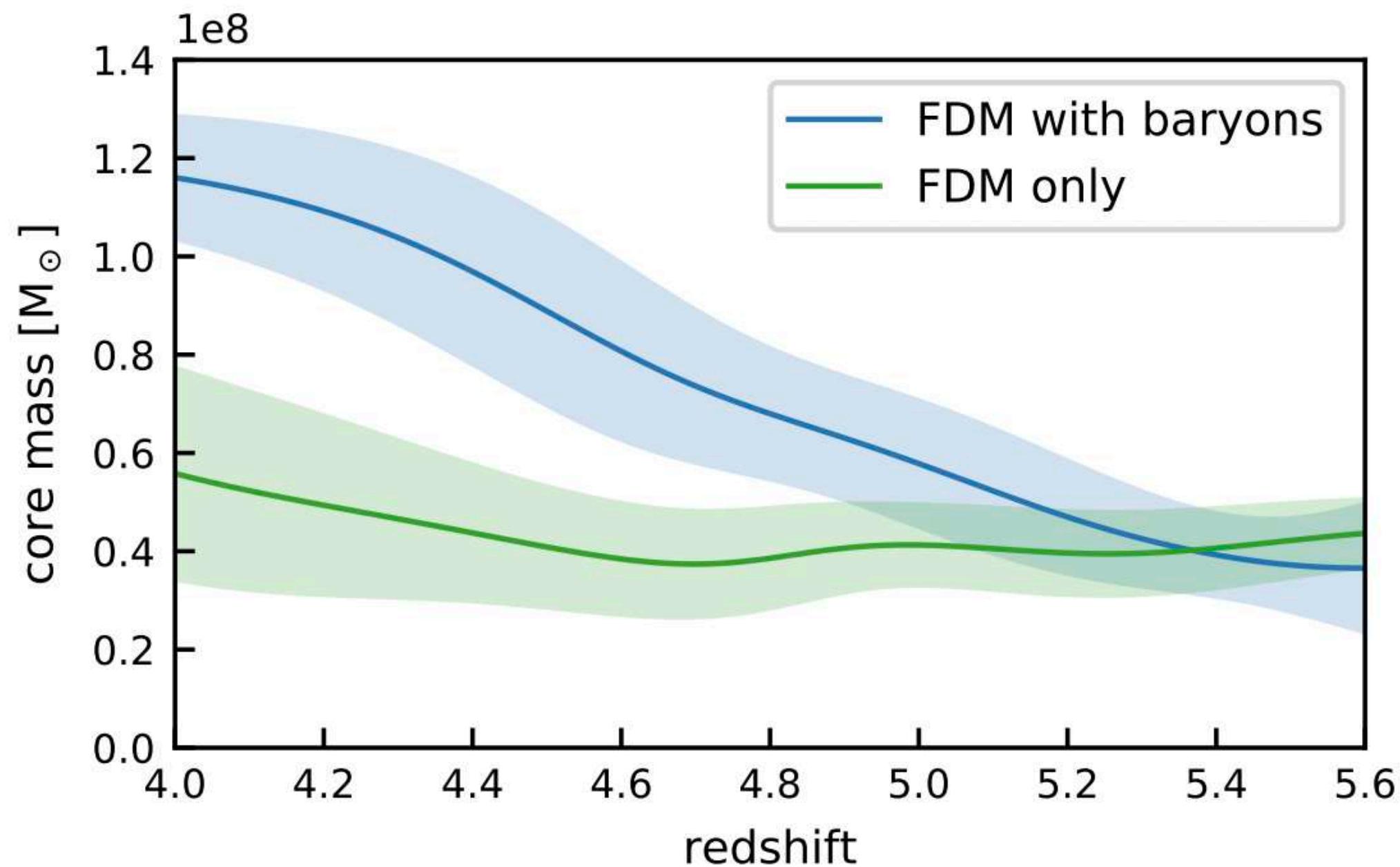


Role of baryons



Core

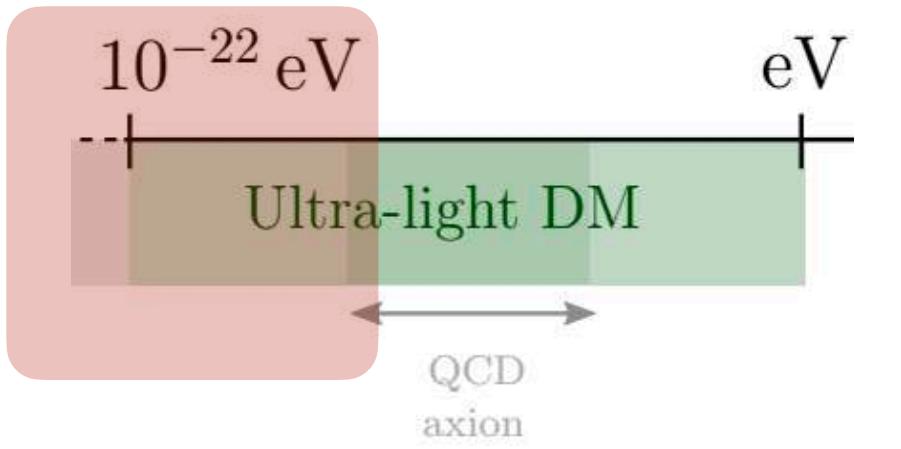
Adding baryons: increase in the gravitational potential in the interior of the halo



More massive and larger core than without baryons

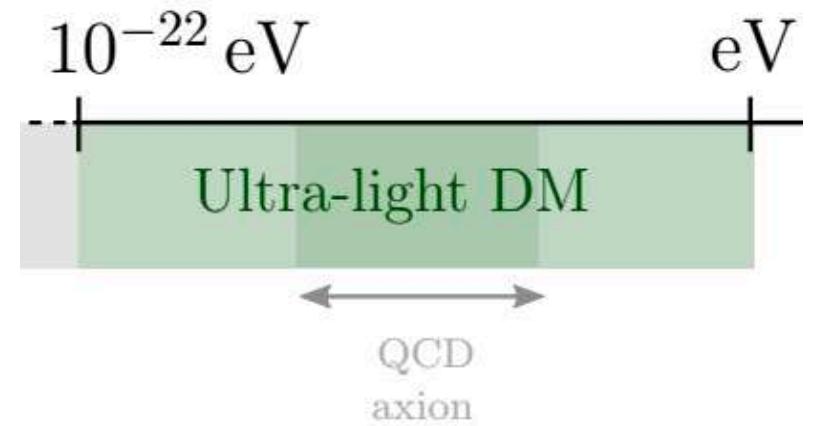
Role of baryons

Interference pattern



Observational implications and constraints

Bounds on the mass and other parameters



Self interacting FDM

DM Superfluid

m

g

$\mathcal{L} = P(X)$

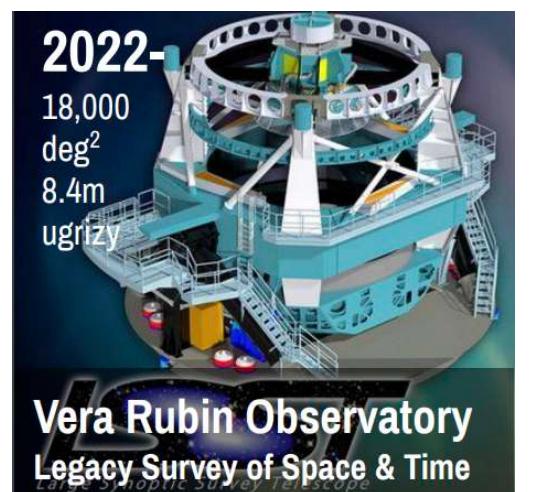
Still highly unconstrained

* Check: Lasha Berezhiani et al (2020)

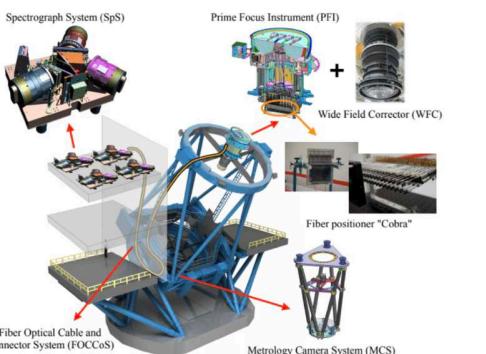
Future - signals in cosmology

Observations

Photometric and spectroscopic surveys



Prime Focus Spectrograph (PFS)



CMB

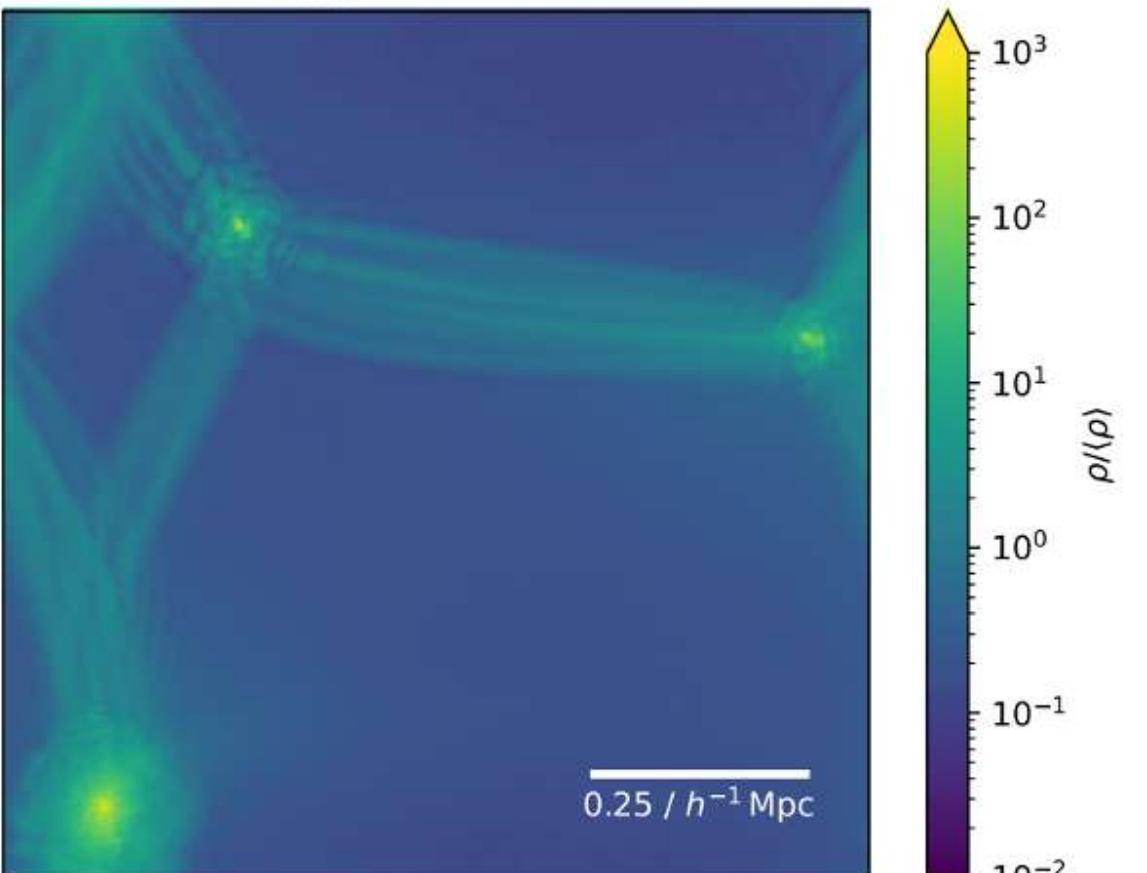


21cm



Simulations

FDM: 256^3 , $mc^2 = 1.75 \times 10^{-23}$ eV, $z = 0.00$
 $v_{\max} = 88.1$ km/s



New observables

New probes

Substructures

- strong lensing
- stellar streams

Small scale information from PS
- substructure convergence PS

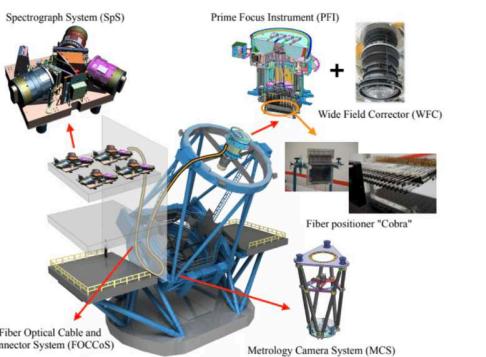
Future - signals in cosmology

Observations



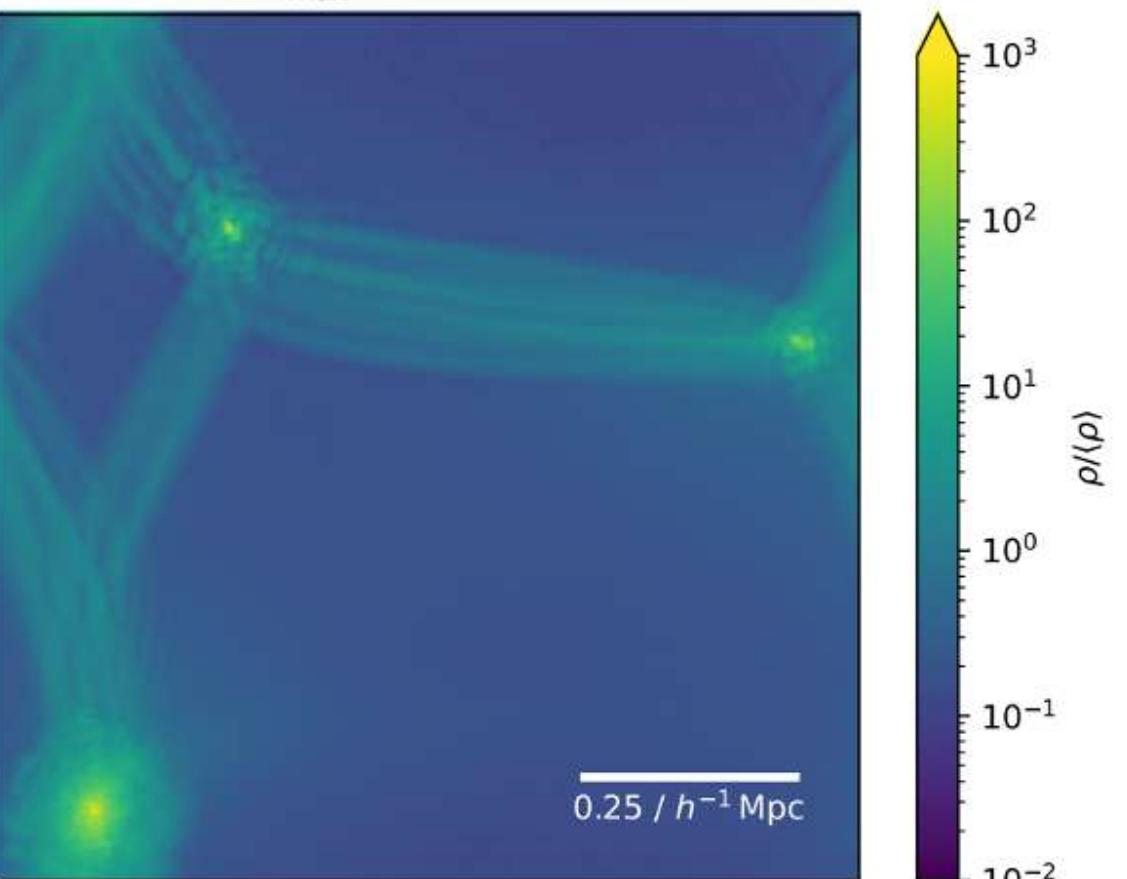
Photometric and spectroscopic surveys

Prime Focus Spectrograph (PFS)



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New observables

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21cm



New probes

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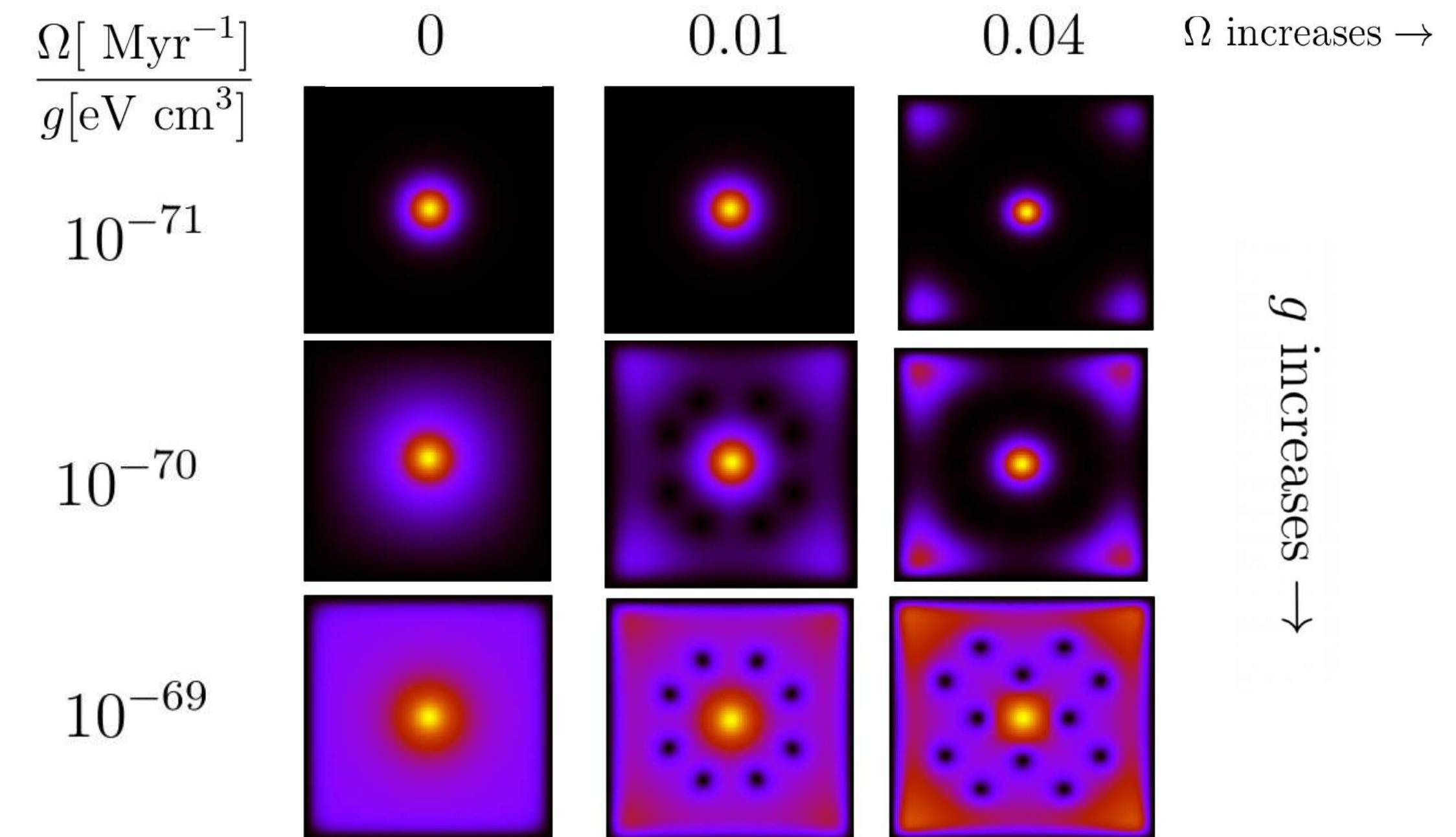
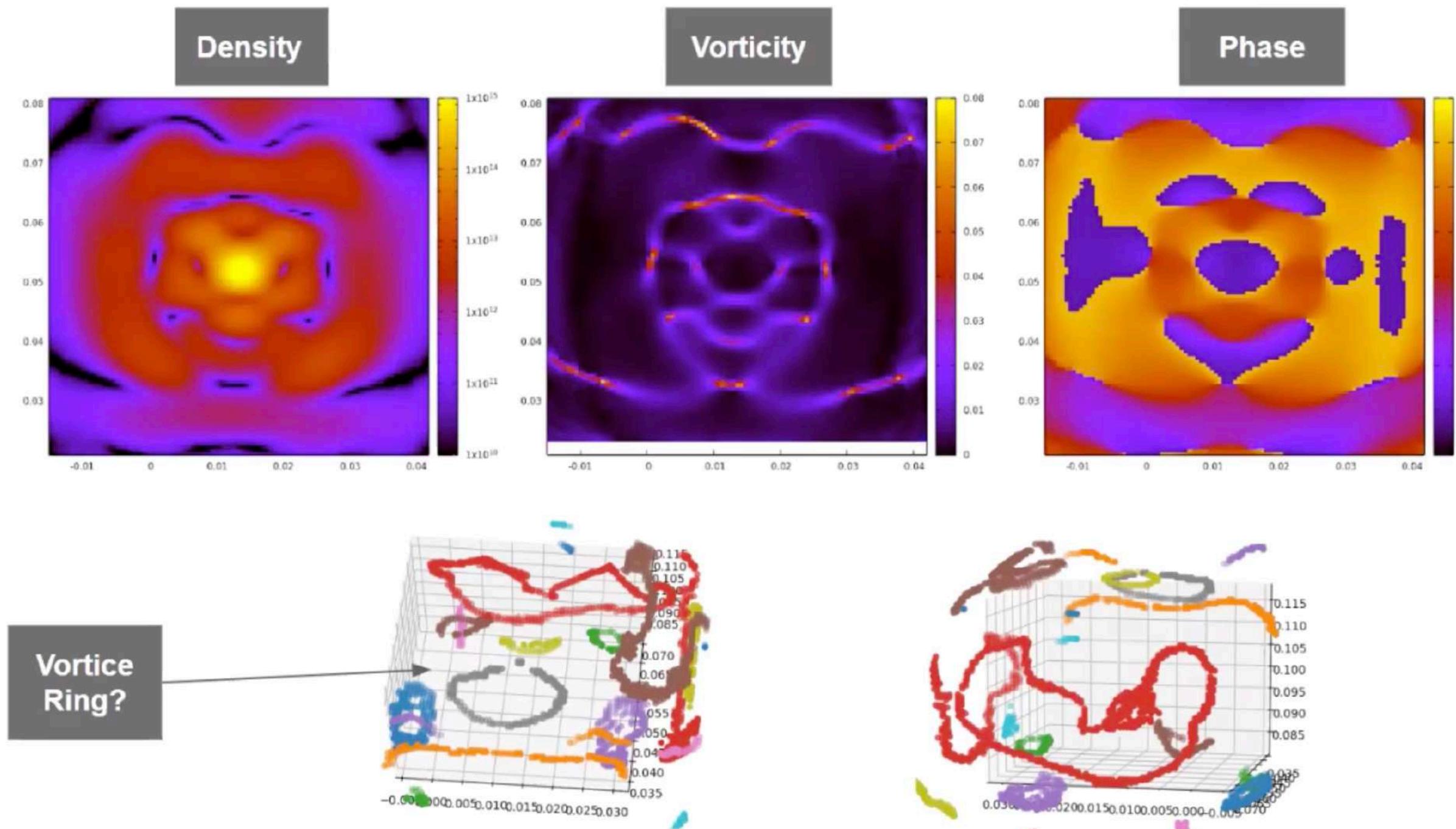
What is the predicted **size** and abundance of vortices in the halo?
Are they **observable**?
Strong lensing? Stellar streams?
Can they be formed in the filaments?

New observables

Vortices

PRELIMINARY

Fuzzy DM



Improve theoretical understanding of these DM vortices

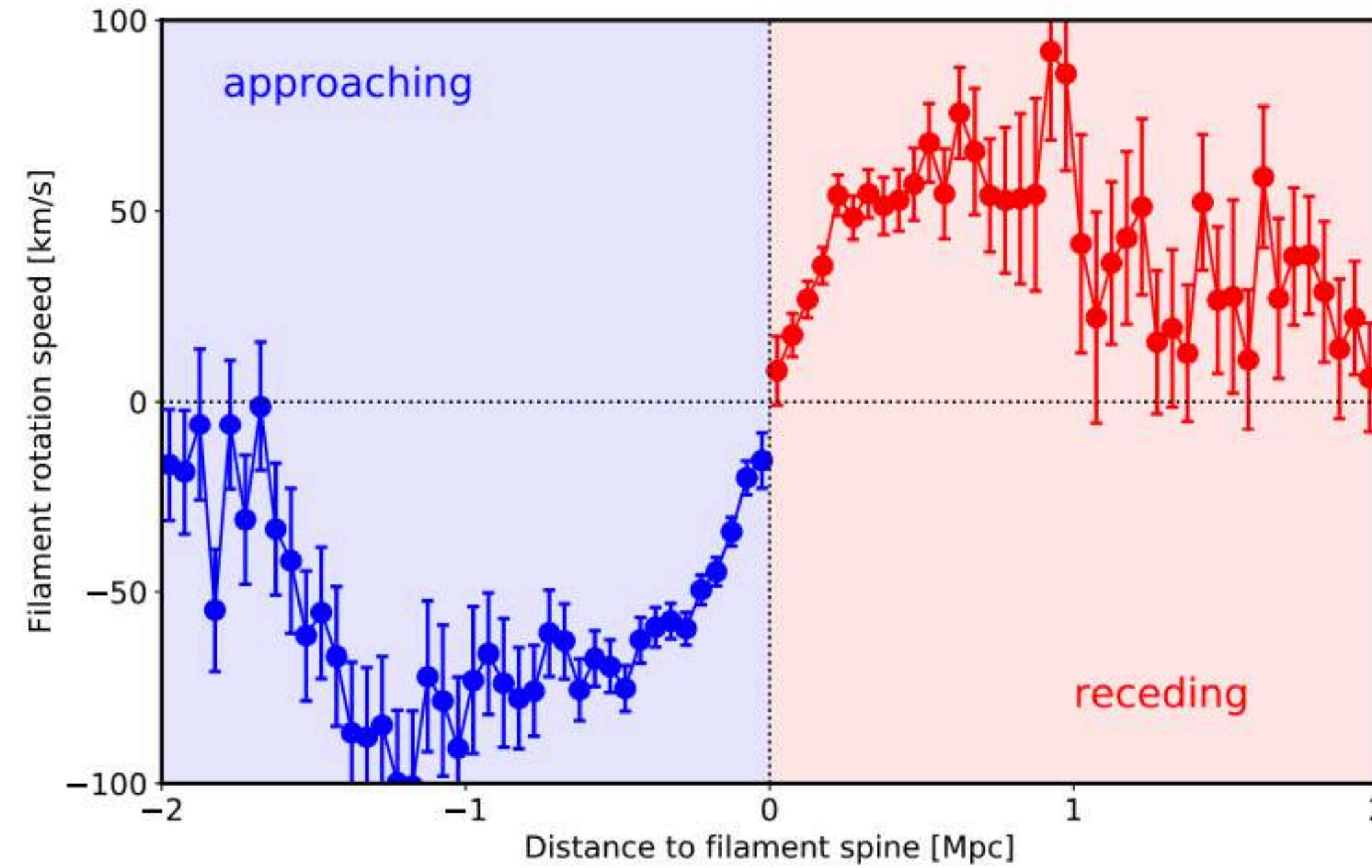
In collaboration with P. Bittar



In collaboration with Jowett Chan

Rotation of filaments: vortices

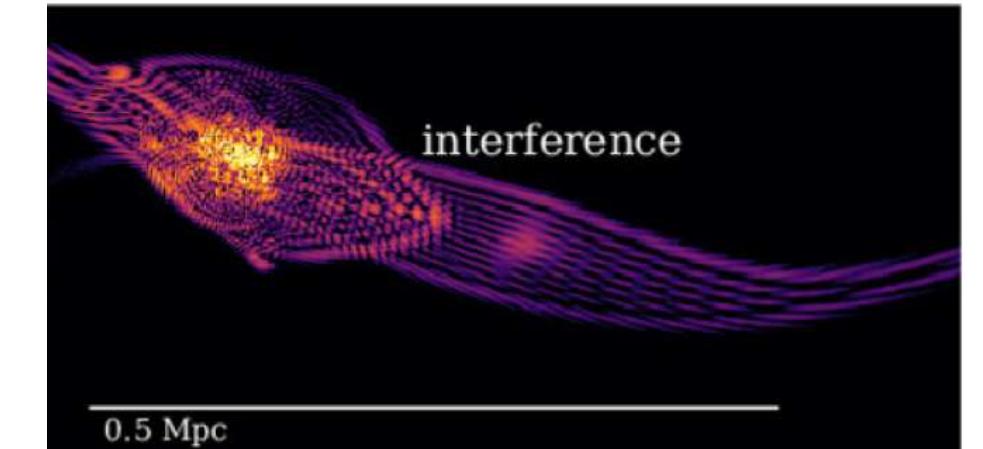
Peng Wang, Noam I. Libeskind, Elmo Tempel, Xi Kang, Quan Guo, "Possible observational evidence that cosmic filaments spin" (2021)



- Stacking thousands of filaments and examining the velocity of galaxies perpendicular to the filament's axis (via their red and blue shift)
- Found that filaments display motion consistent with rotation → largest objects known to have angular momentum

Rotation of filaments: vortices

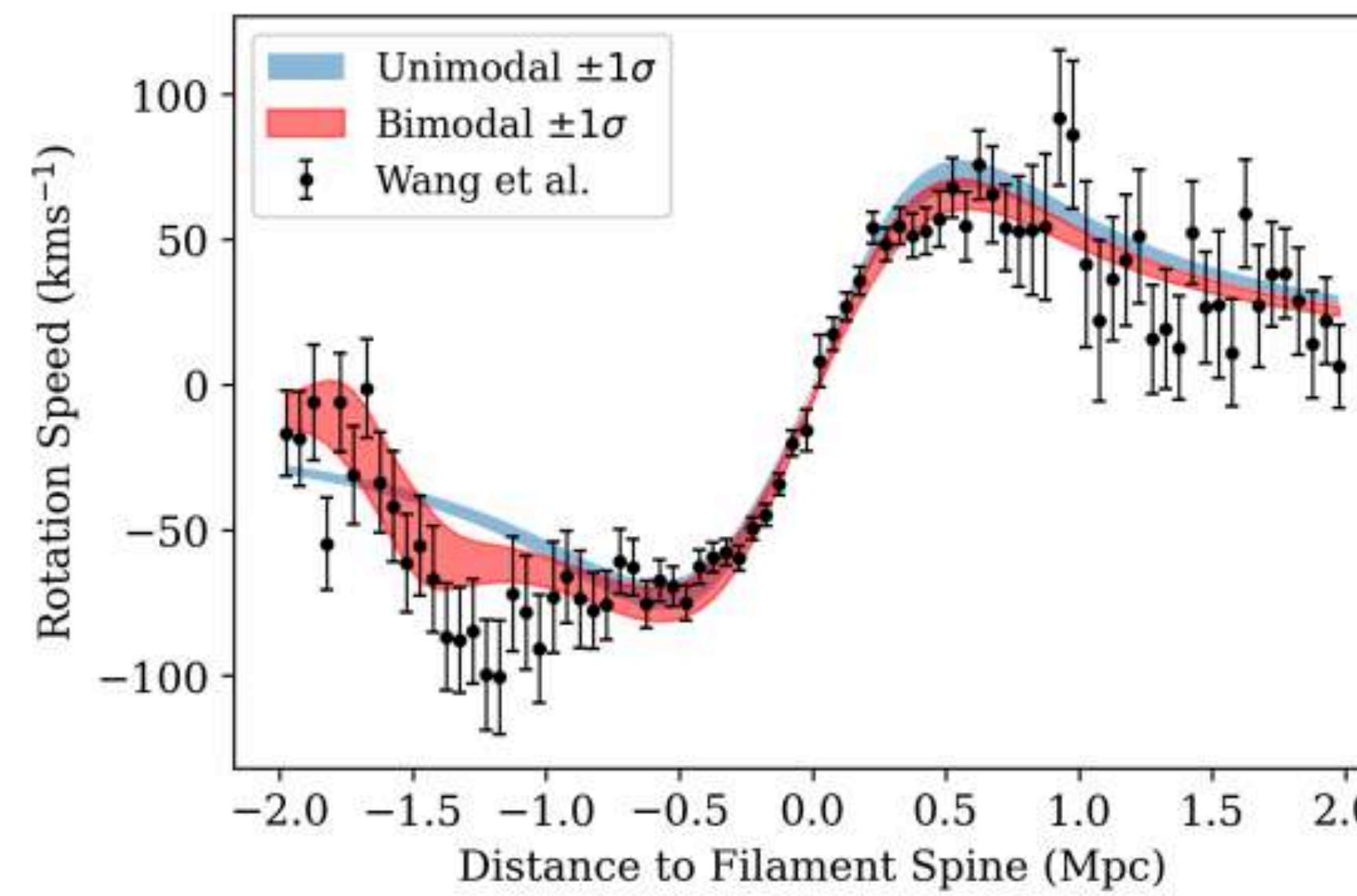
- Not clear that we can get spinning cosmic filaments in LCDM
 - Seems to be difficult to theoretically explain the acquisition of angular momentum on megaparsec scales
 - Some simulations seem to be finding spinning cosmic filaments



Mocz et al. 2017

Stephon Alexander, Christian Capanelli, Elisa G. M. Ferreira, and Evan McDonough, "Cosmic Filament Spin from Dark Matter Vortices" (2021)

- Suggest that a collection of (ULDM) vortices enclosed in a cylindrical volume aligned with the axis of a filament are able to generate rotations at the Mpc scale and reproduce the result of Wang et al (2021)



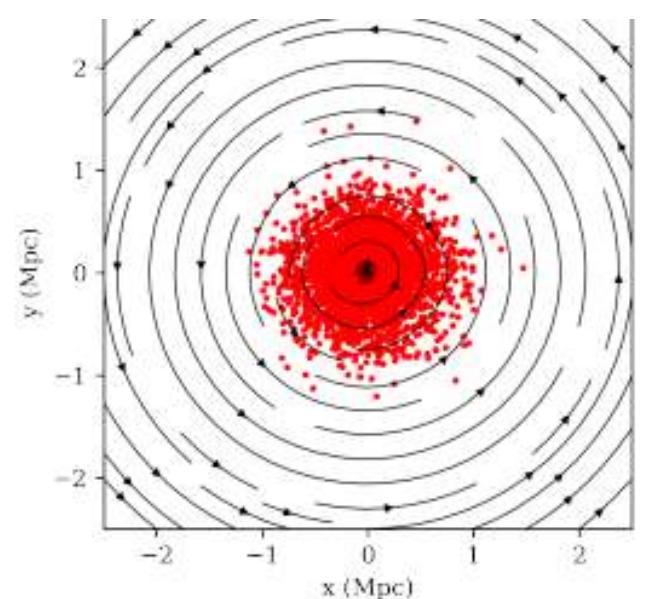
$$R = 0.51^{+0.02}_{-0.02} \text{ Mpc}$$

$$\frac{N_V}{m} = 2.9^{+0.2}_{-0.2} \times 10^{25} \text{ eV}^{-1}.$$

For example, for a $m \sim 10^{-22} \text{ eV} \longrightarrow N_V \sim 3000$

Compatible with:

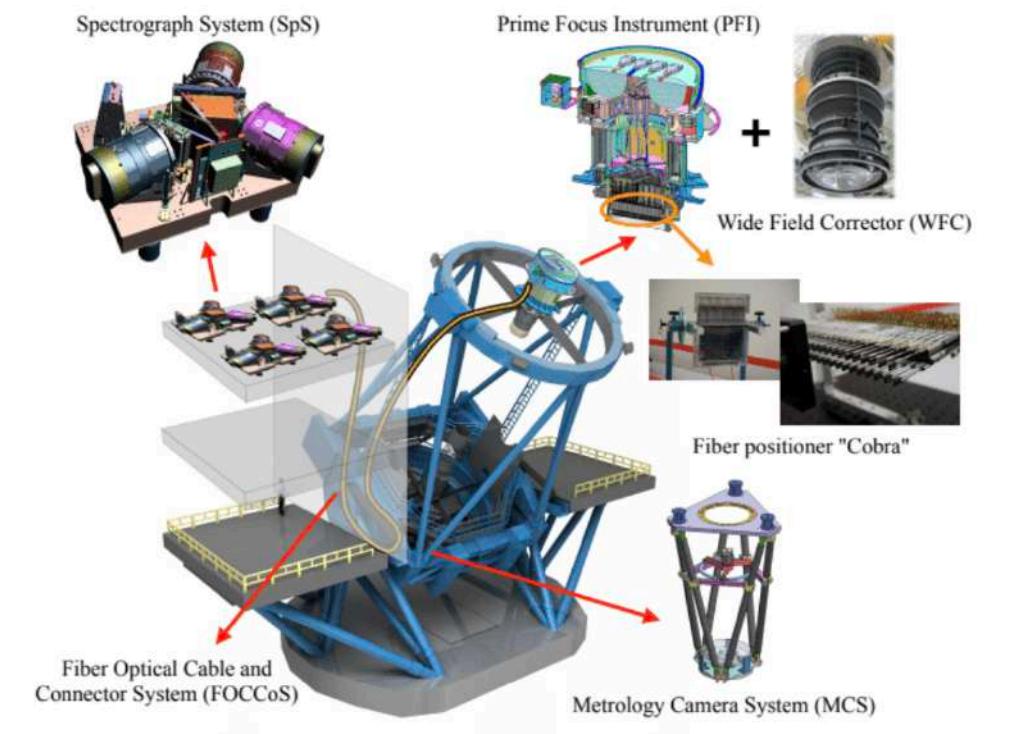
- in regions where the density vanishes (Hui et al 2020, Lague et al 2020)
- Transfer of angular momentum (Berezhiani, 2015)



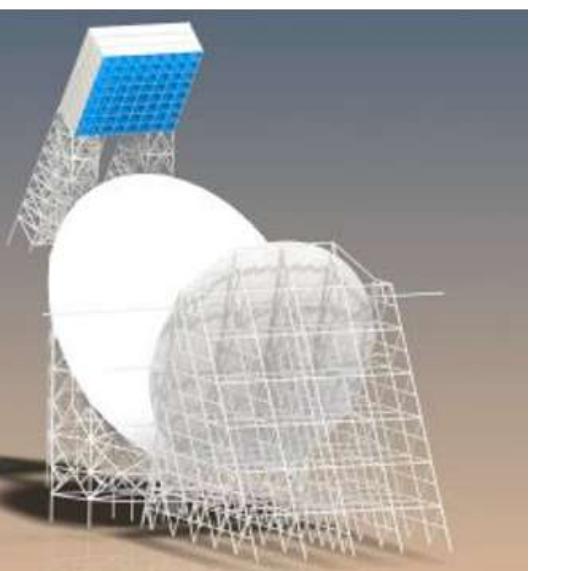
Future

Observations

Prime Focus Spectrograph (PFS)



BINGO telescope

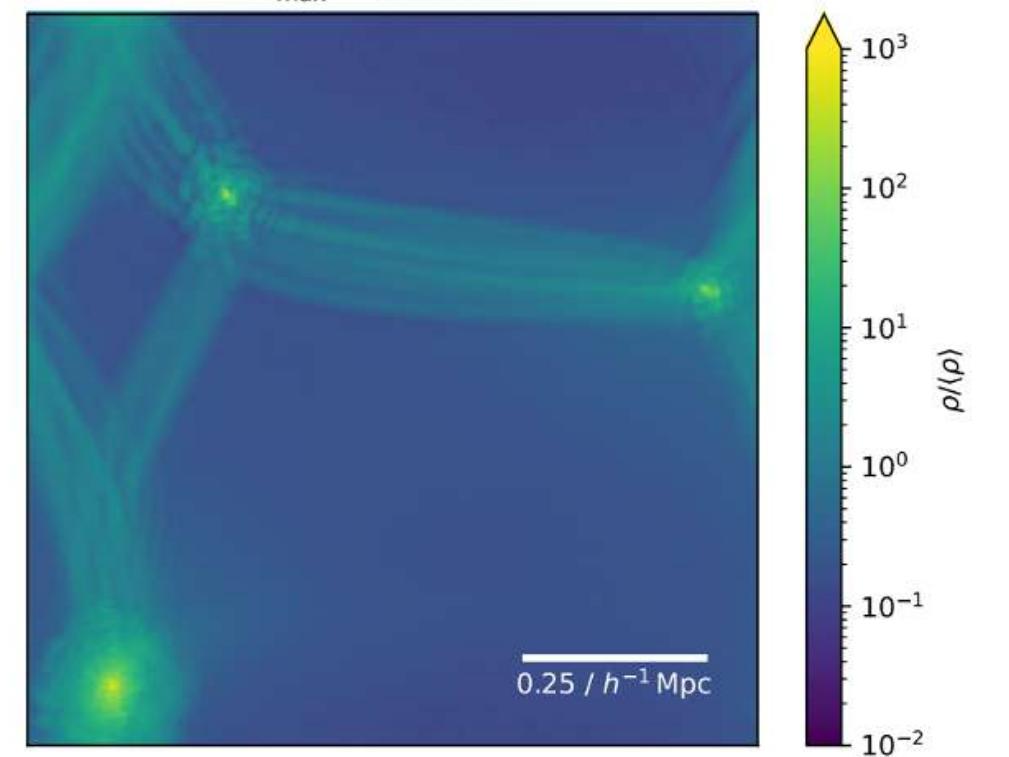


Vera Rubin observatory (LSST)



Simulations

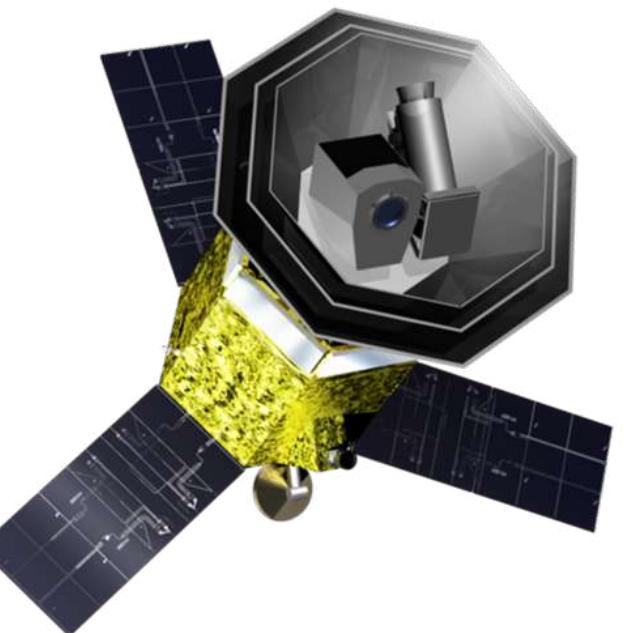
FDM: 256^3 , $mc^2 = 1.75 \times 10^{-23}$ eV, $z = 0.00$
 $v_{\max} = 88.1$ km/s



CMB-S4



LiteBIRD

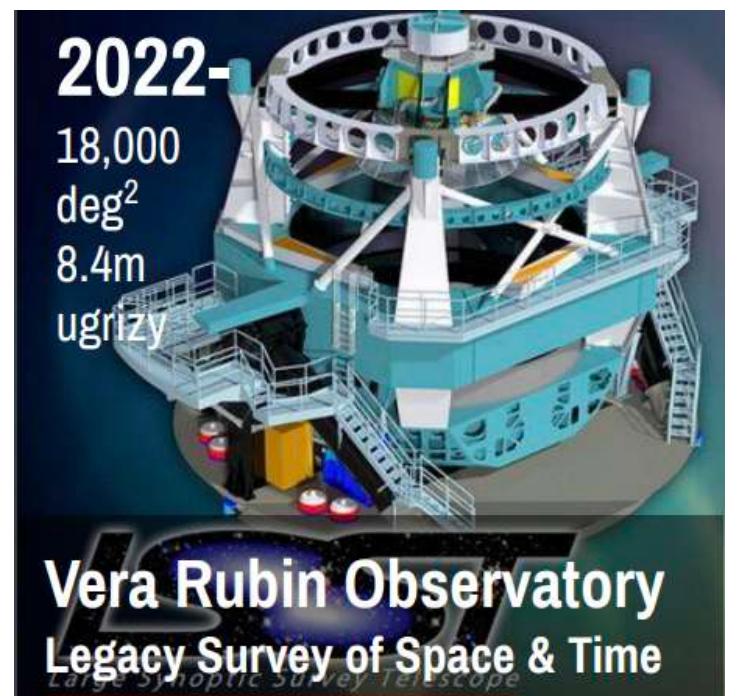


New probes

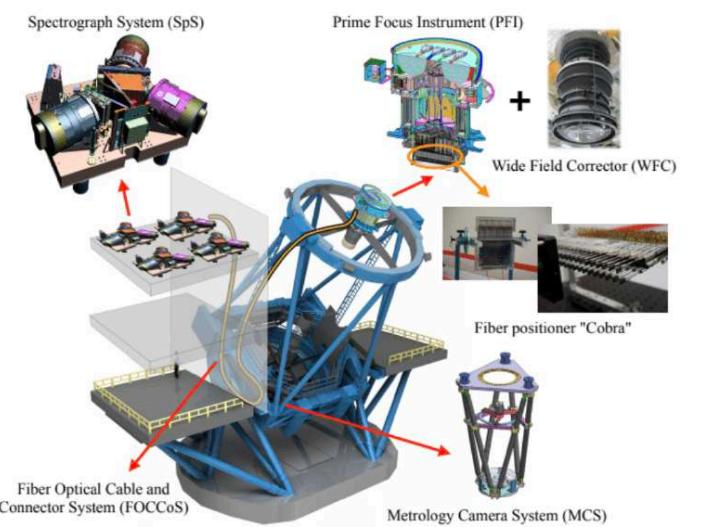
Future - signals in cosmology

Observations

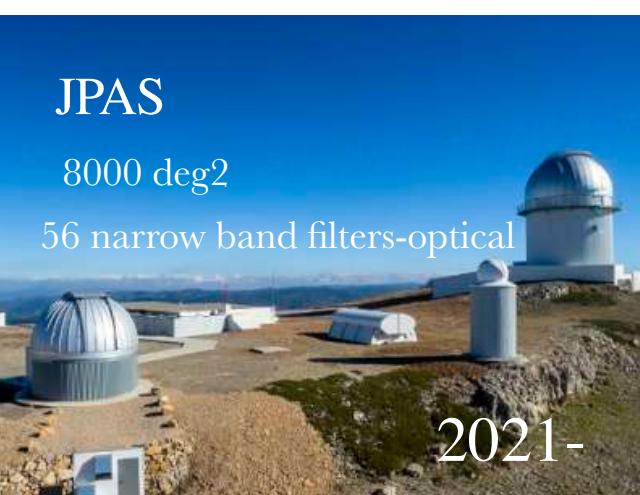
Photometric and spectroscopic surveys



Prime Focus Spectrograph (PFS)



21cm



GWs



CMB



CMB-S4
Next Generation CMB Experiment



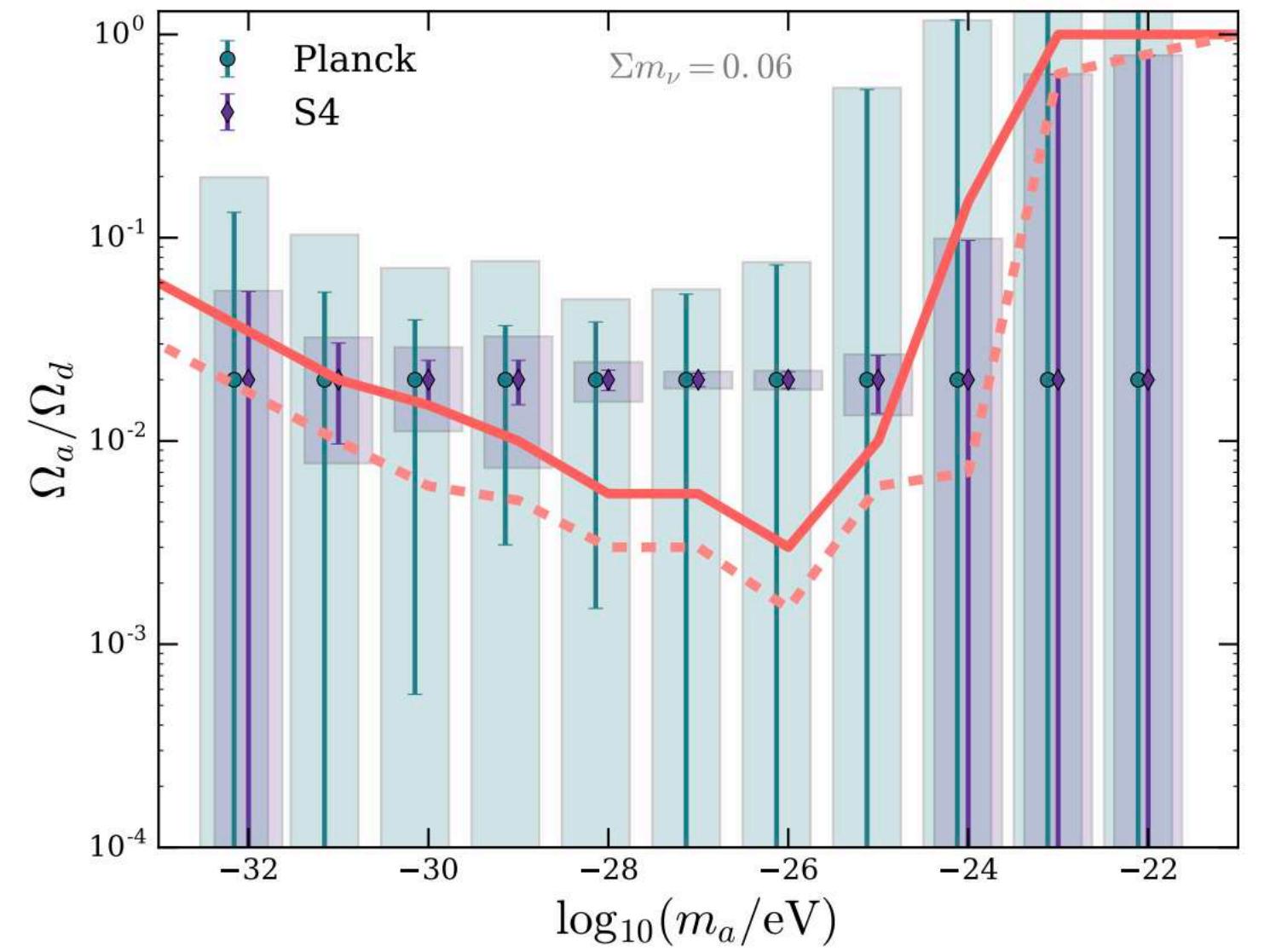
Modified from Jia Liu

Future - Cosmic Microwave Background

TESTING ULTRA LIGHT DM CMB

CMB - S4

Constraints on Ω_a/Ω_d



Hlozek et al., 2016

Significantly improve constraints on the composition of the dark sector!

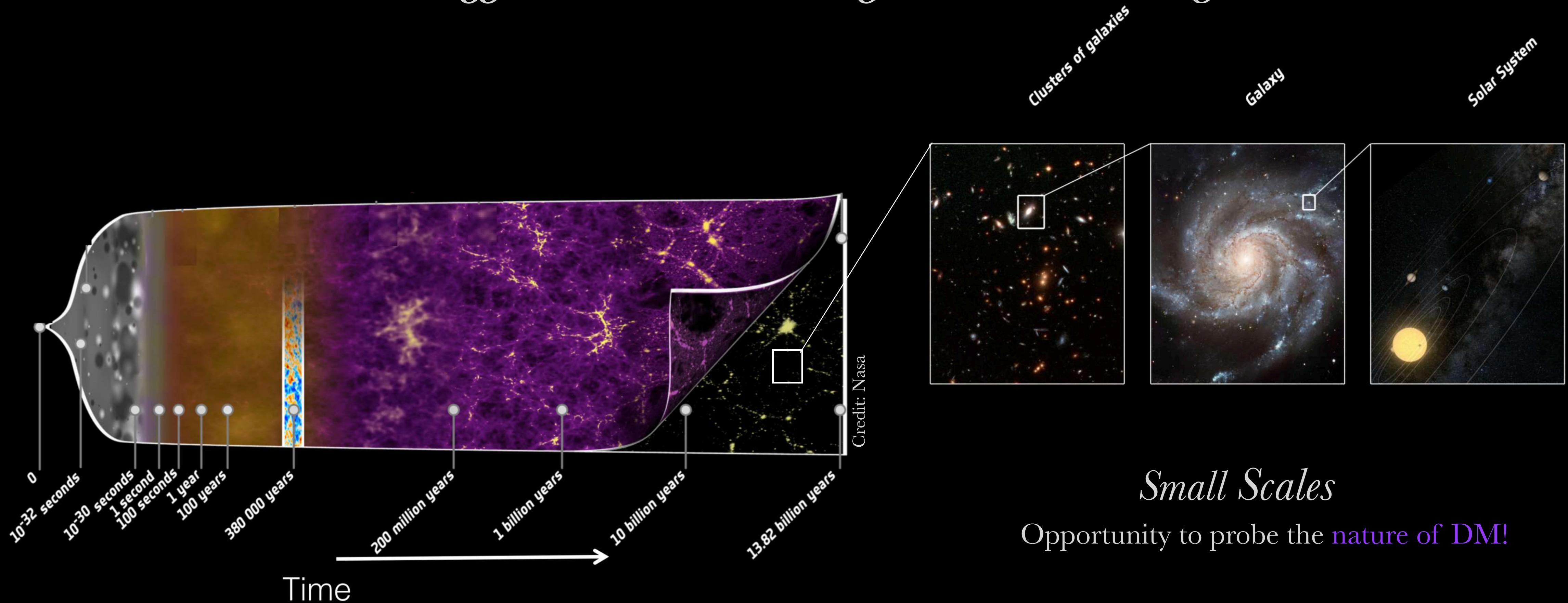
Constraints on the *optical depth* $\tau(r_{\text{rec}})$

Constraint the ULDM mass

Kinematic Sunyaev-Zel'dovich effect: sensitive to the duration of the reionization

- *LiteBIRD*
- *Advances ACTPol*
- *CMB-S4*

*Small scales can offer some **hints** of the nature of DM*



Small Scales

Opportunity to probe the **nature of DM!**

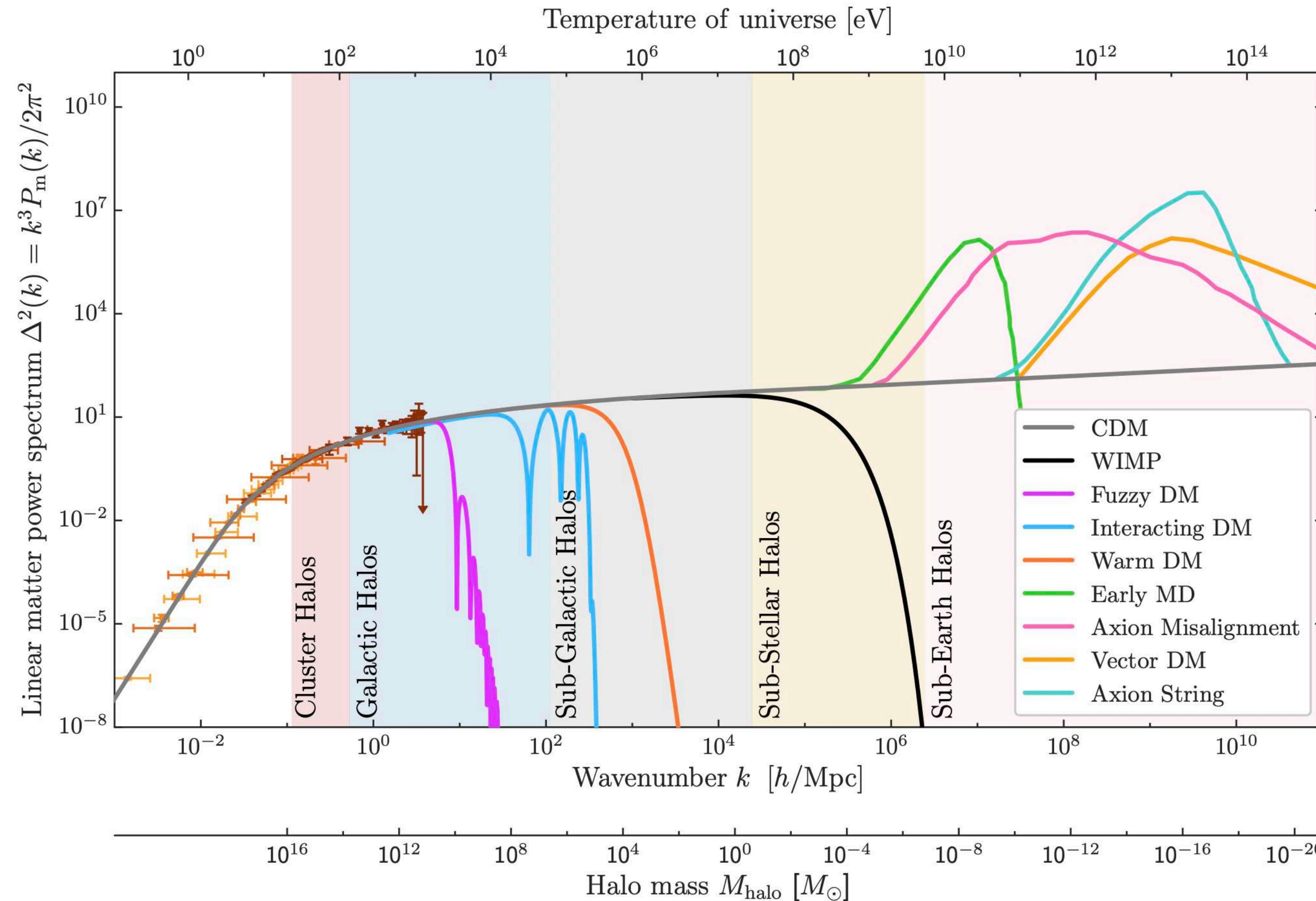
Astrophysical
Observables



DM
Distribution

Nature of DM
Microphysics
Particle physics

*Small scales can offer some **hints** of the nature of DM*



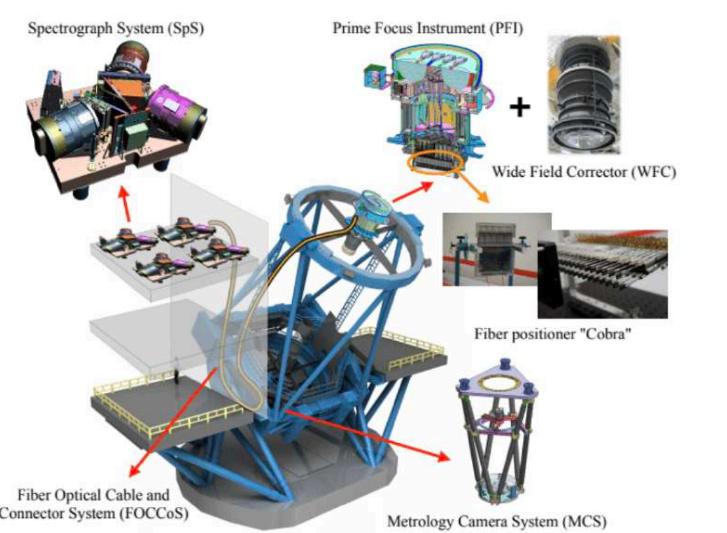
Future - signals in cosmology

Observations

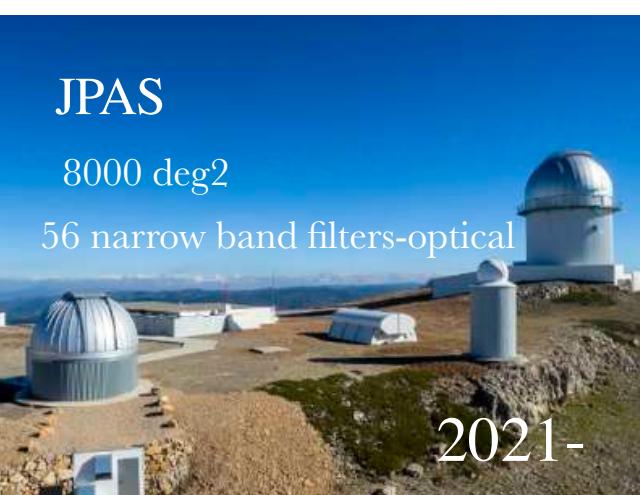
Photometric and spectroscopic surveys



Prime Focus Spectrograph (PFS)



21cm



GWs



CMB



Modified from Jia Liu

PFS (*Prime Focus Spectrograph*)

PFS is going to be exquisite to measure the properties of DM

GOAL

PFS: spectroscopy part of *SuMIRe project*

DM with PFS → synergy between science goals

Galaxy archeology

- Nature of DM (dSphs)
- Structure of MW dark halo
- Streams
- Stellar kinematics and chemical abundances – MW & M31

Cosmology

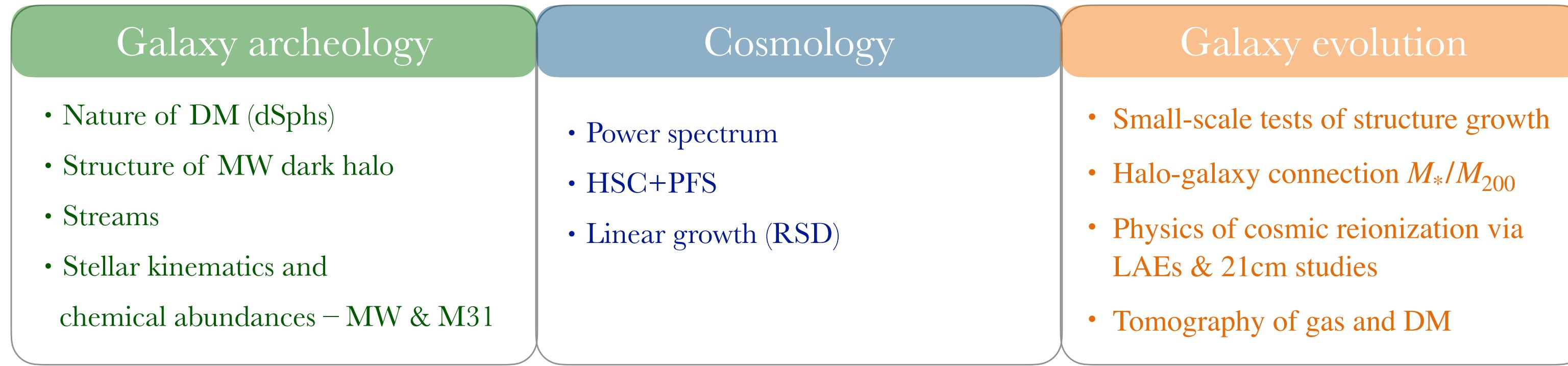
- Power spectrum
- HSC+PFS
- Linear growth (RSD)

Galaxy evolution

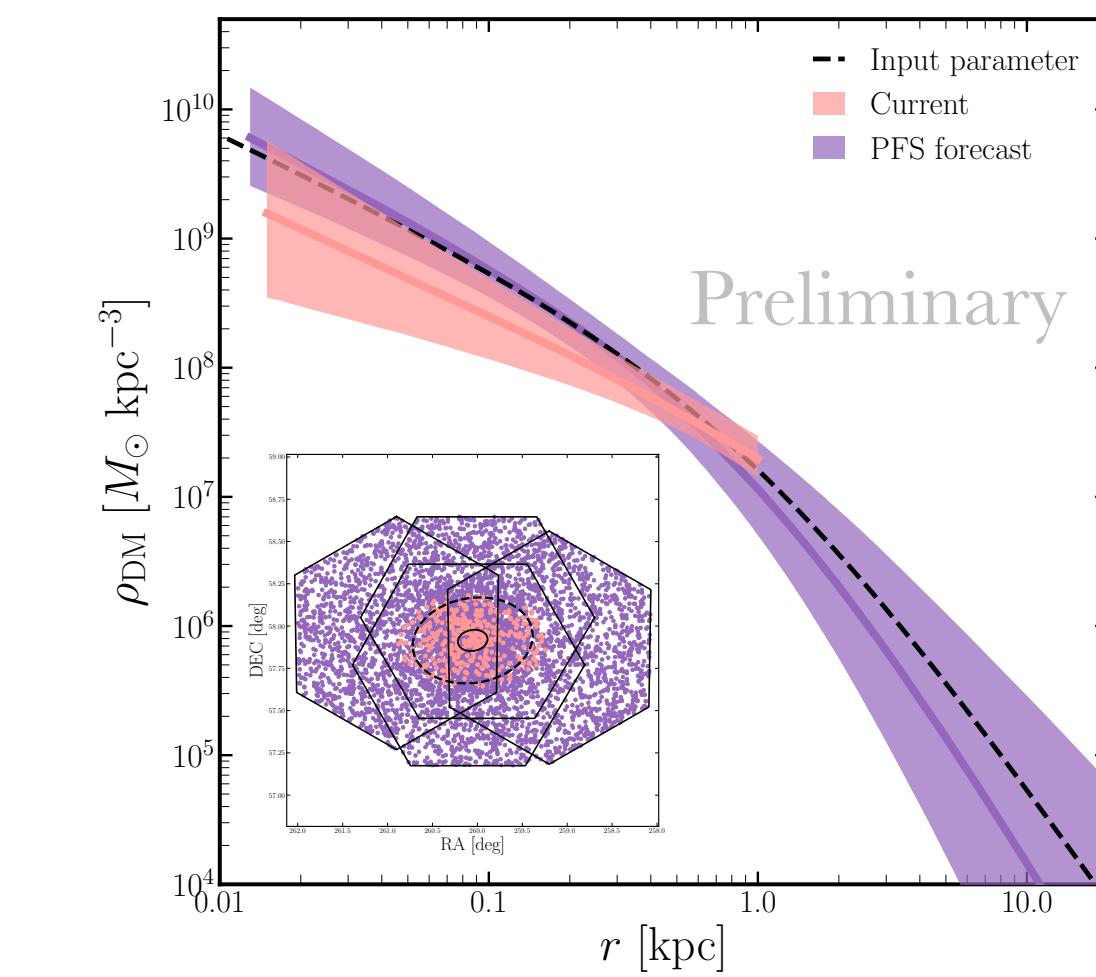
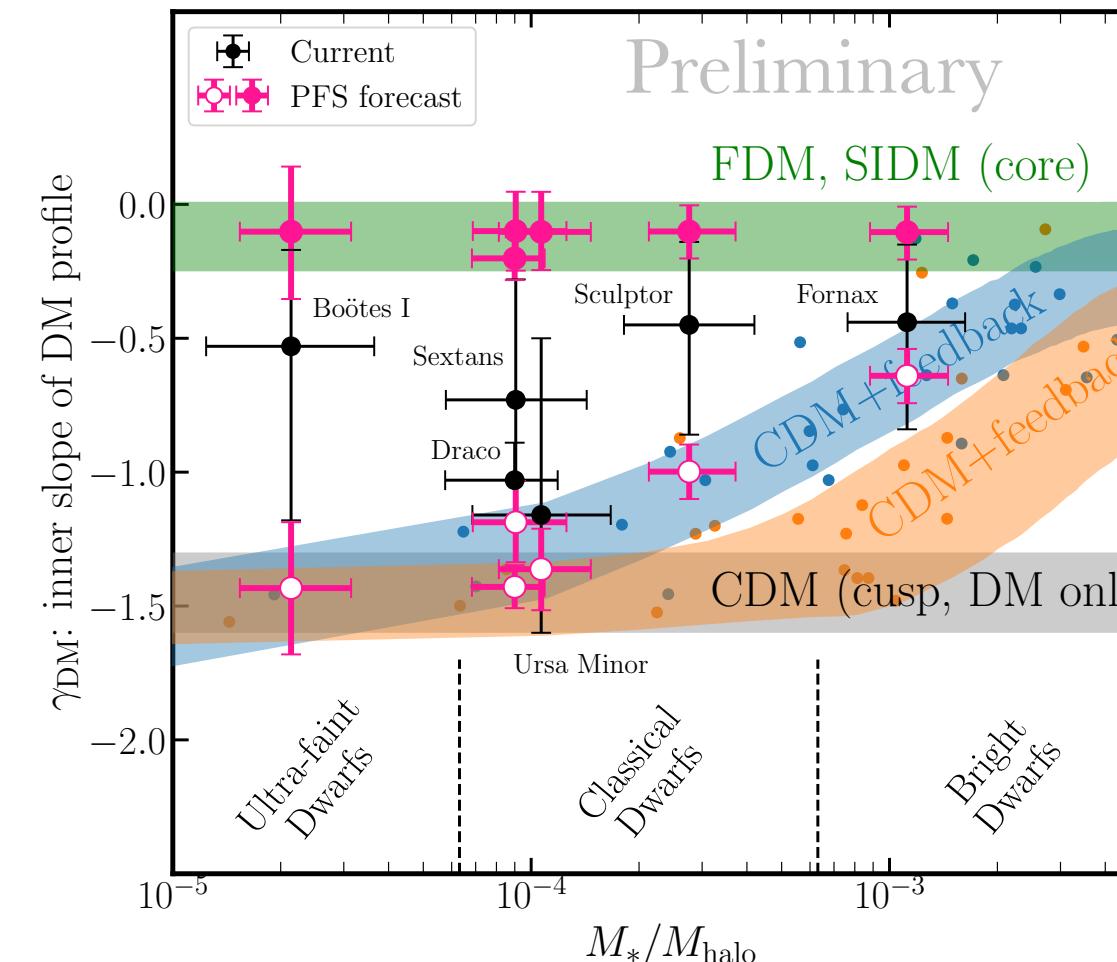
- Small-scale tests of structure growth
- Halo-galaxy connection M_*/M_{200}
- Physics of cosmic reionization via LAEs & 21cm studies
- Tomography of gas and DM

Wide & deep survey of MW dwarf galaxies w. Subaru/PFS

DM with PFS



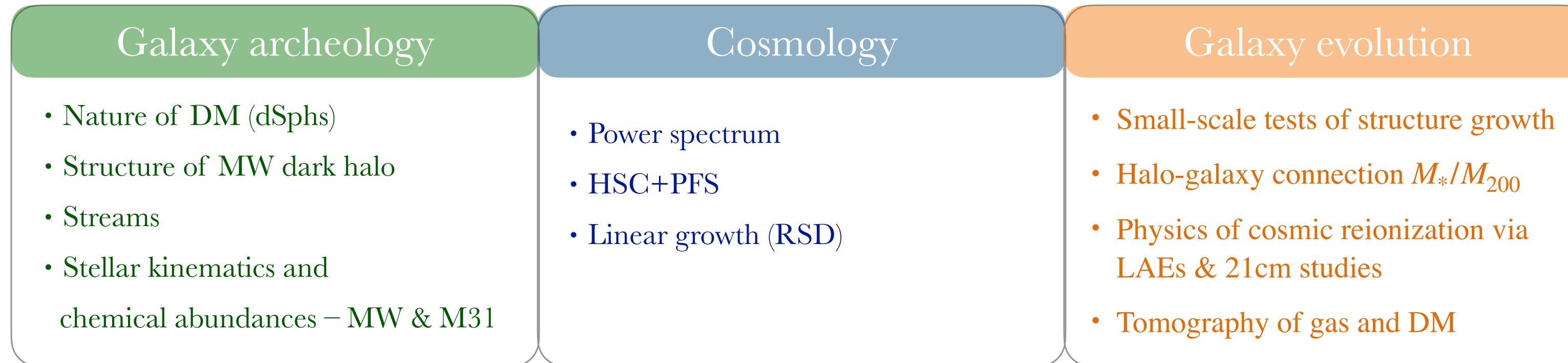
- Science with dwarf galaxies
- Core:
 - Presence of a core or not (slope)
 - Size of the core
 - Profile
 - Inner density
 - Transition radius
- FDM
 - Abundance data to understand the role of baryons in each system
- SIDM
- ULA
- Beyond the core
 - Granules: heating of stars (dwarfs)
 - Angular momentum
 - Stellar streams
- ...



Kohei Hayashi' and Masashi Chibas talk

Figures by Kohei Hayashi

DM with PFS

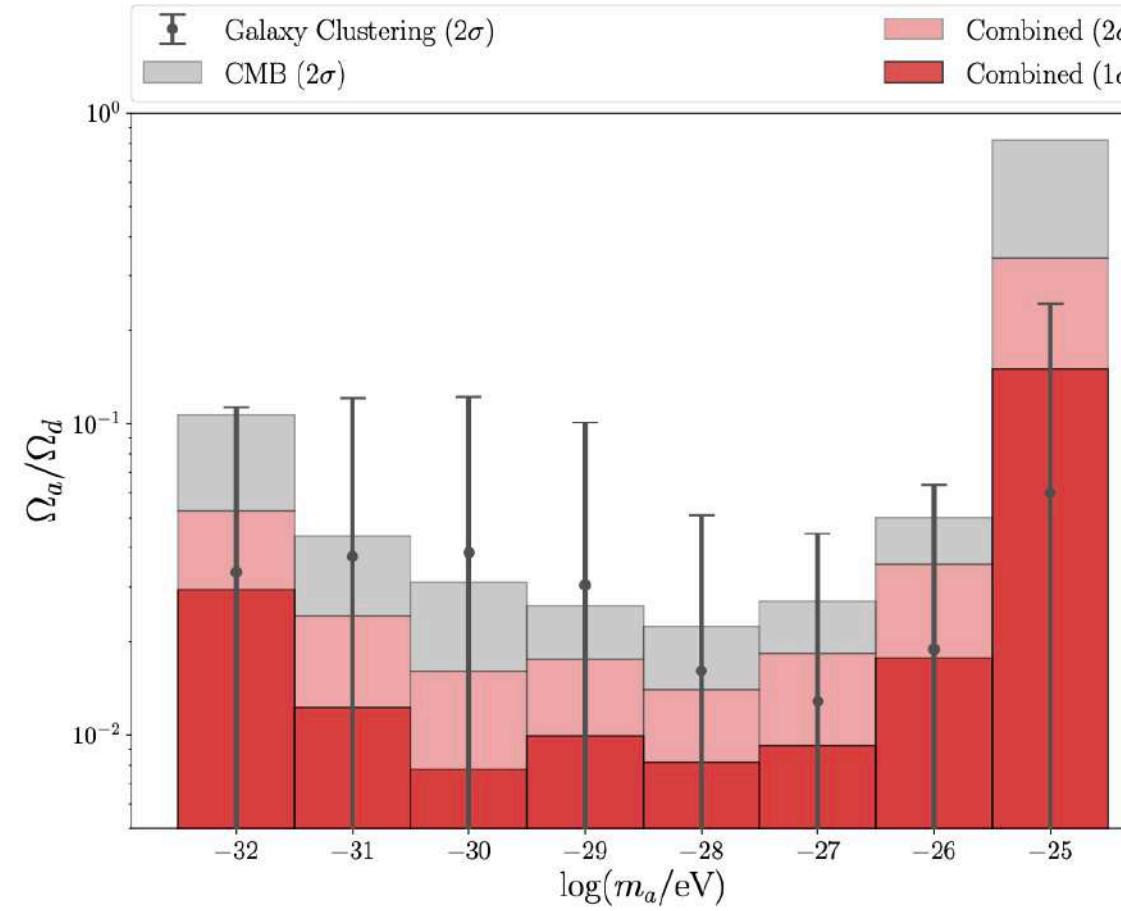


- Science with dwarf galaxies
 - Core:
 - Presence of a core or not (slope)
 - Size of the core
 - Profile
 - Inner density
 - Transition radius
 - Abundance data to understand the role of baryons in each system
- Beyond the core
 - Granules: heating of stars (dwarfs)
 - Angular momentum
 - Stellar streams

FDM

SIDM

ULIA



Lague et al 2021

The small-scale Ly-a forest power spectrum

ULIA

Halo mass function

FDM

WDM

SIDM

Constraints on the *optical depth*:

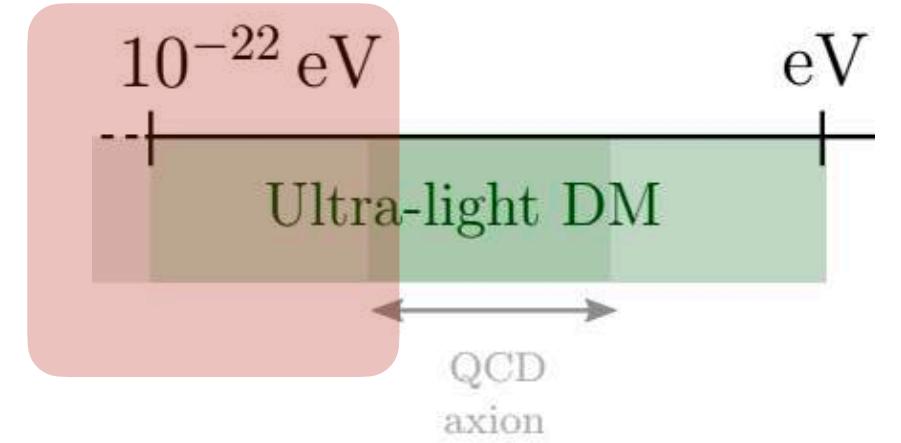
Constraint the ULDM mass

Kinematic Sunyaev-Zel'dovich effect: sensitive to the duration of the reionization

...

Properties of DM

Ultra-light Dark Matter -classes



3 classes:

Fuzzy DM (FDM)

- Gravitationally bounded ultra-light scalar field model
- Condensation under gravity (BEC)

m

DOFs

Self Interacting FDM (SIFDM)

- Presence of (weakly) self-interaction
- Condensation under gravity + SI (superfluid)

$m \quad g$

DM Superfluid

- Forms a superfluid in galaxies
- MOND behaviour interior of galaxies

Axion and ALP (axion like particles)

$$i\dot{\psi} = \left(-\frac{1}{2m} \nabla^2 + \frac{g}{8m^2} |\psi|^2 - m\Phi \right) \psi$$

$$\mathcal{L} = P(X)$$

→ Connection with condensed matter and particle physics!

“*Ultra-light dark matter*”, **E.Ferreira**, 2020. The Astronomy and Astrophysics Review.

Superfluid Dark Matter



MakeAGIF.com



What we don't know about dark matter

- Gold
- Pressureless
- Dark
- Collisionless

CDM on large scales



How cold it is?

Cluster on all scales?

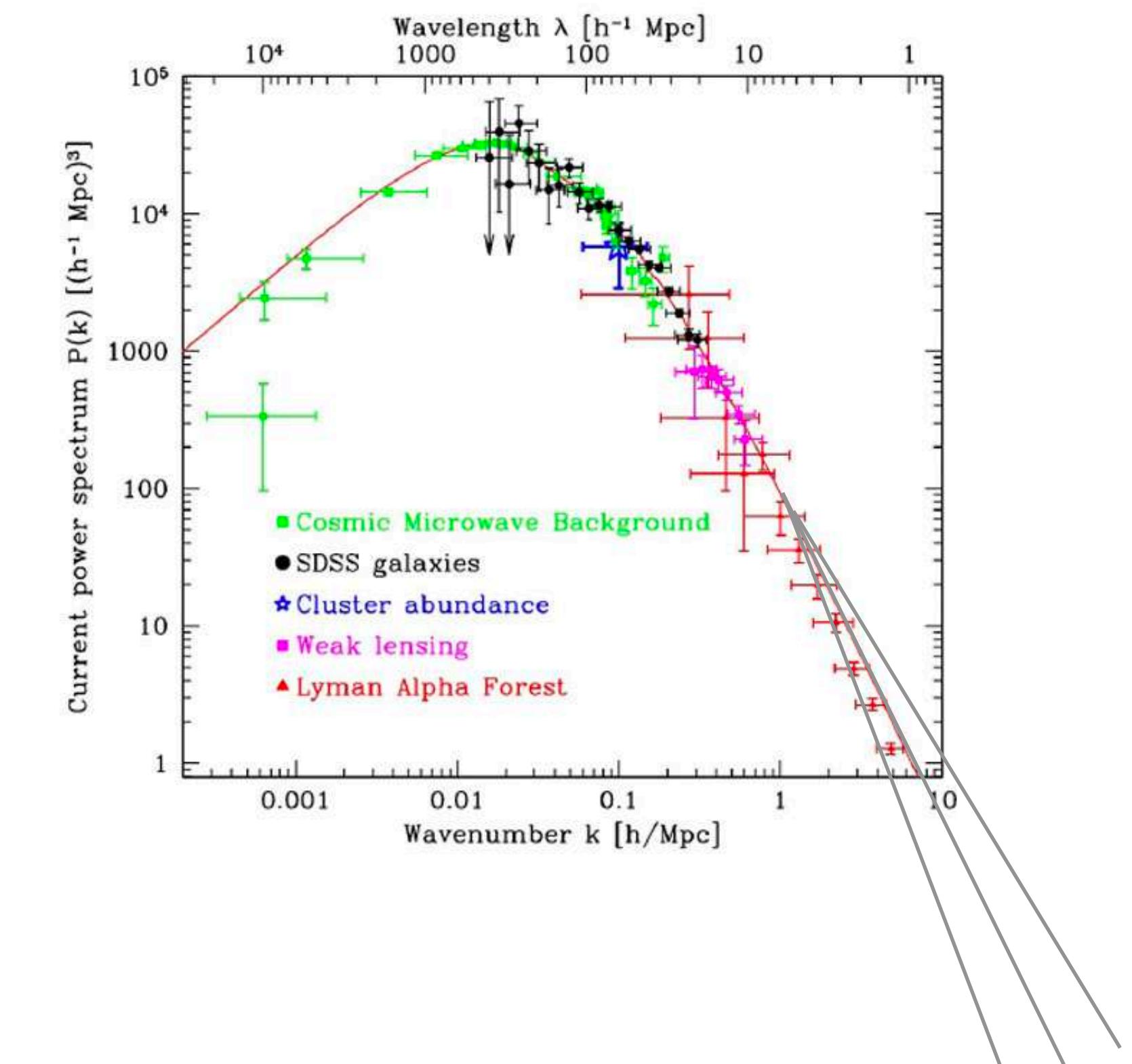
Non-gravitational
interaction?

How small self-interaction?

WDM
 $m \sim \text{keV}$

Milicharged
DM

SIDM

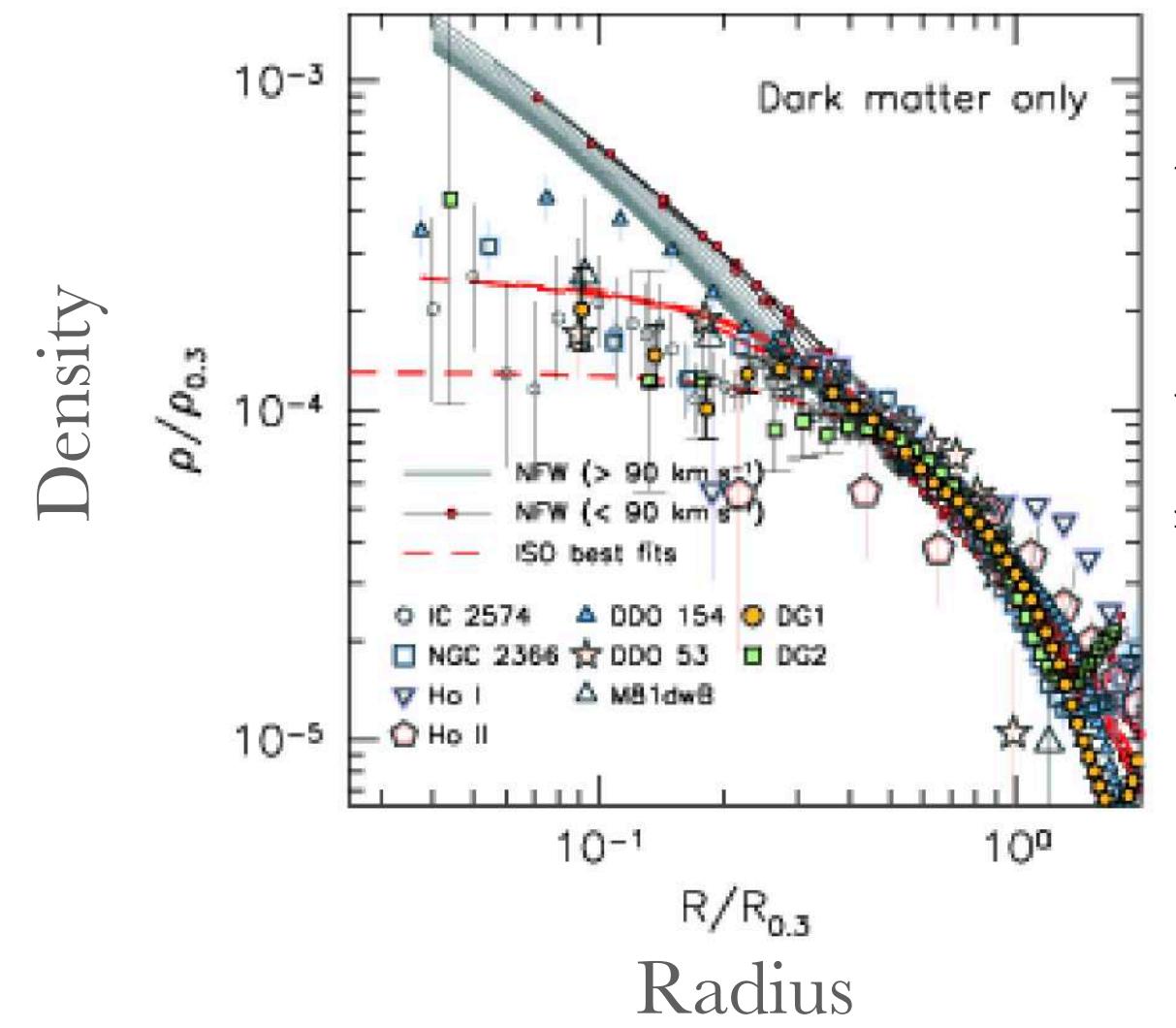


Small scale behavior: still weakly
constrained and small scale challenges

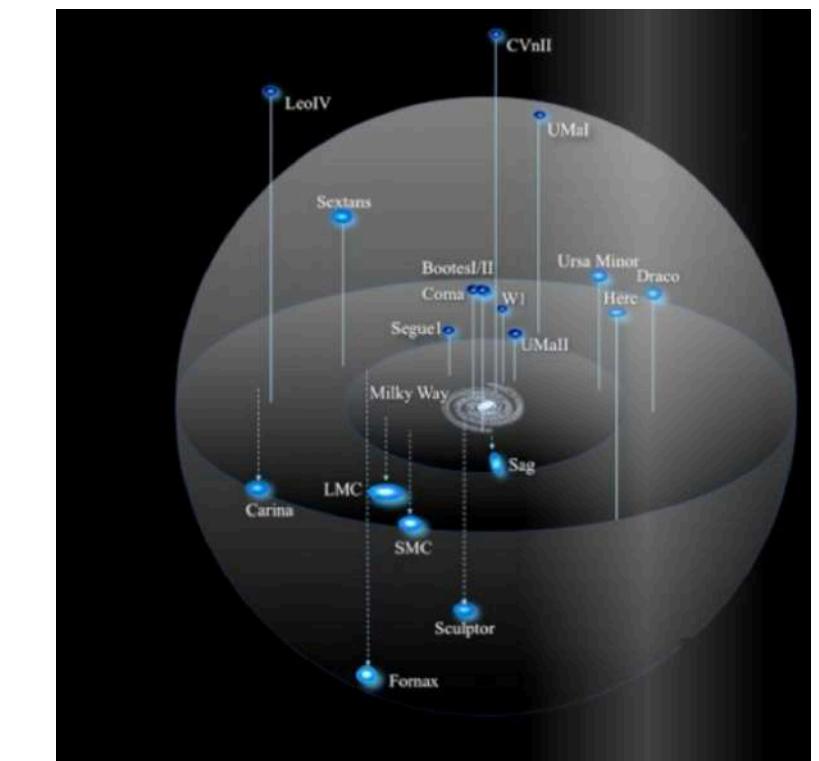
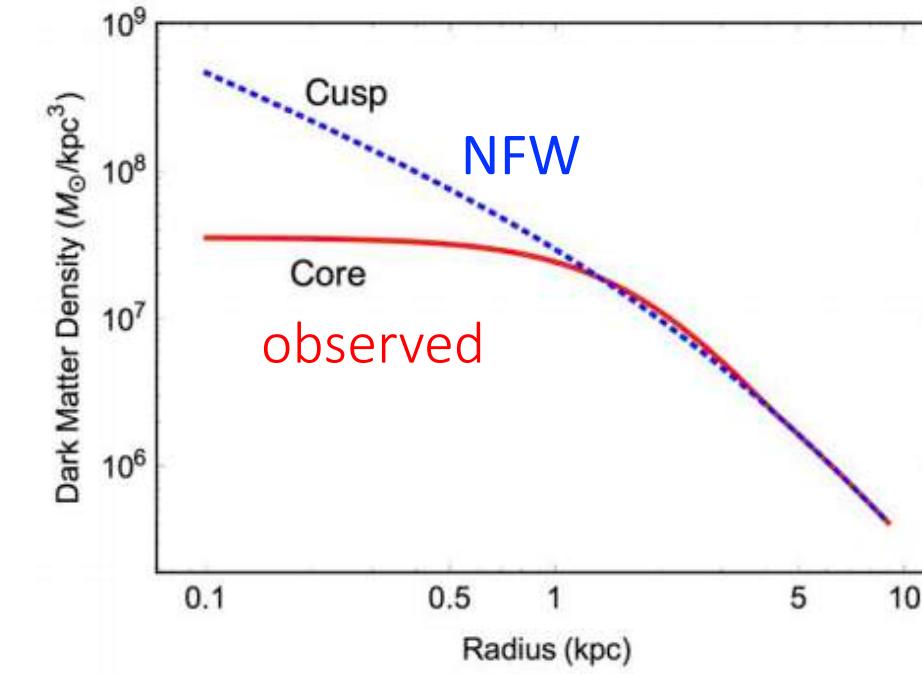
Small scale curiosities: **cusp-core**, missing satellites, BTFR, ...

Small scale challenges

Cusp-core



CDM - NFW profile



Missing satellites

Incompatibility between the # of satellites predicted by simulations using **LCDM** and the # of **observed** satellites

Regularity/diversity of rotation curves

Regularity and diversity of rotation curves

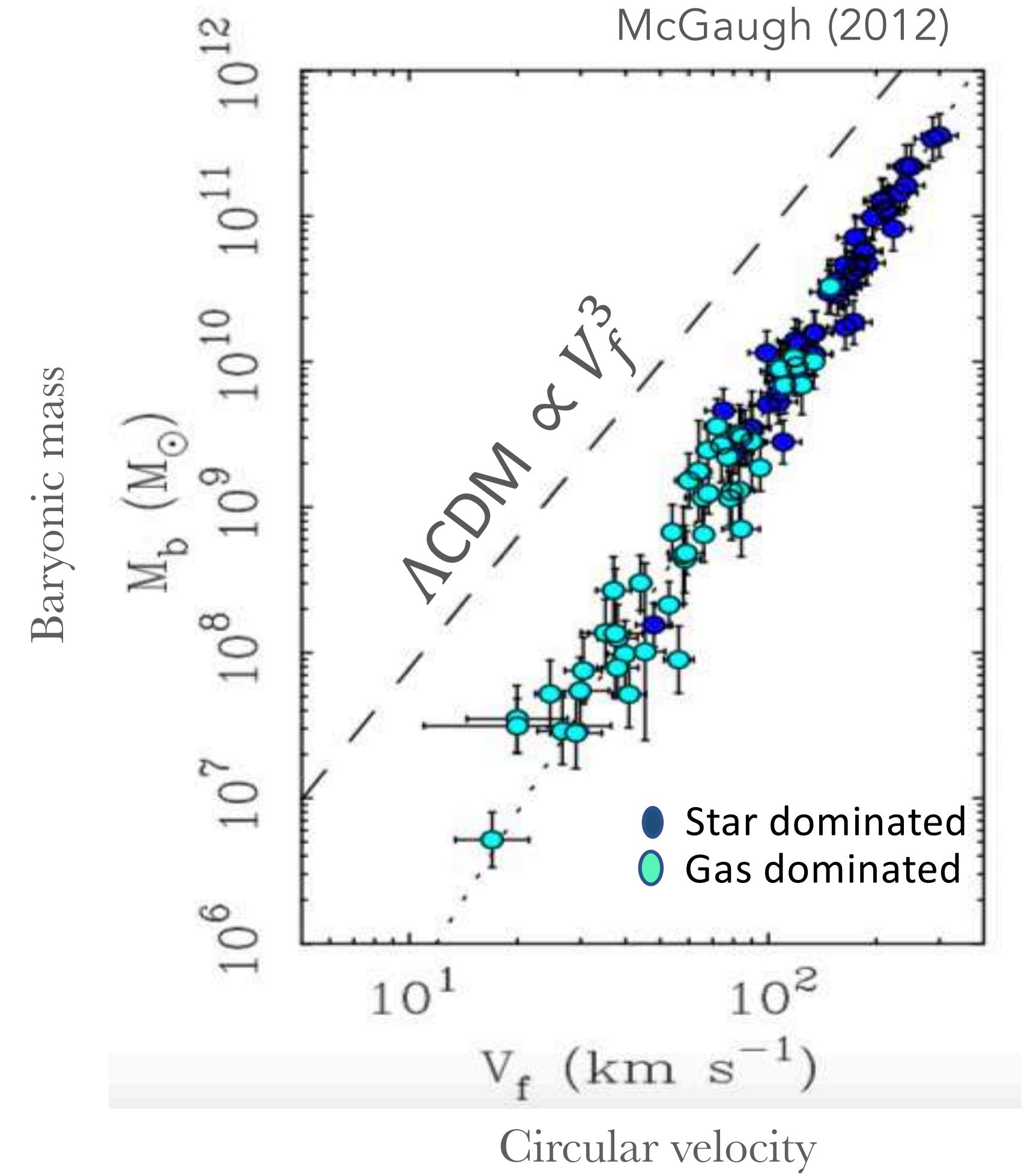
- Baryonic Tully-Fisher relation (BTFR)

Remarkably **tight** scaling relations between dynamical and baryonic properties.

Other scaling relations:

- ✓ TRF
- ✓ RAR - Radial acceleration relation
- ✓ ...

$$a_0 \simeq \frac{1}{6} H_0 \simeq 1.2 \times 10^{-8} \text{ cm/s}^2 = 2.7 \times 10^{-34} \text{ eV}.$$



Dark matter-

Large scales: CDM

Small scales:

Both?

- Feedback: Within Λ CDM

- Star formation
- Stellar evolution
- Sn rates
- BH and AGN feedback
- Stellar feedback
- ...

Questions:

- Can it solve all these?
- \neq simulations, \neq parametrizations
- Enough feedback?
- Explains tight scaling relation?

- MOND:

Modified Newtonian Dynamics

Empirical relation

$$a = \begin{cases} a_N^b, & a_N^b \gg a_0. \\ \sqrt{a_N^b a_0}, & a_N^b \ll a_0. \end{cases}$$

Curiosity: Baryons drive the dynamics!

Works extremely well for: (1) rotation curves; (2) scaling relations

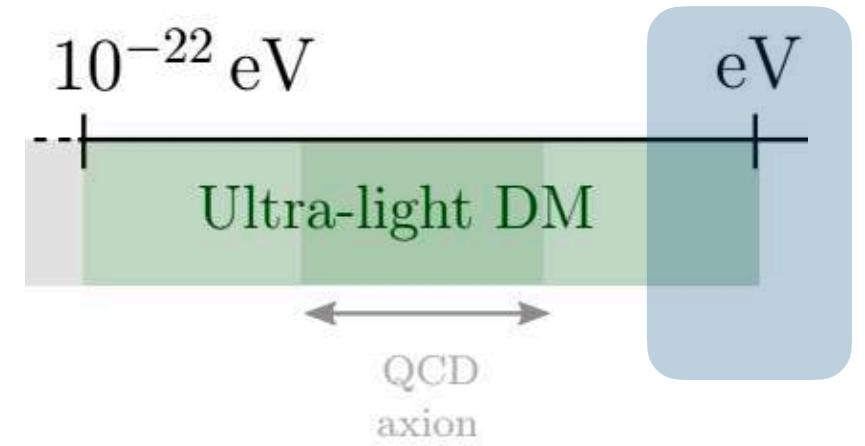
BUT:

~~MOND without DM~~

Problems explaining large scales

- Modify dark matter:

DM with different properties on small scales



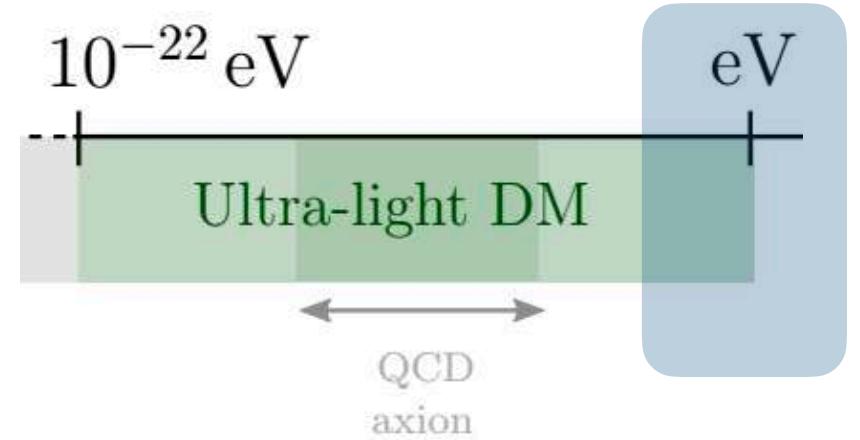
Superfluid Dark Matter



MakeAGIF.com

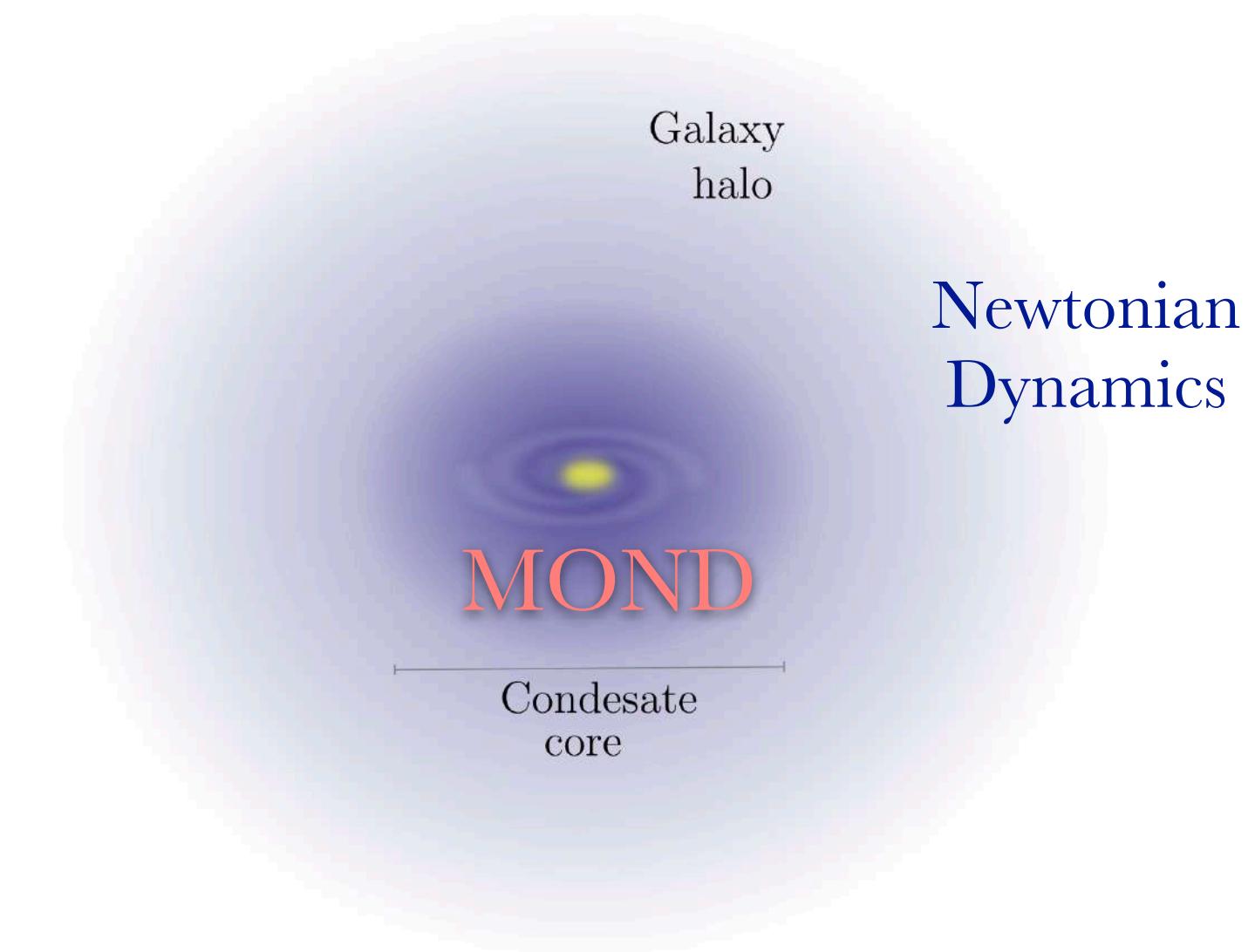


Superfluid Dark Matter



Lasha Berezhiani and Justin Khoury (2016)

Large scales:
DM behaves like standard
particle DM (**CDM**).



Galactic scales:
DM forms a **superfluid**
→ emergent **MOND** dynamics
in galaxies



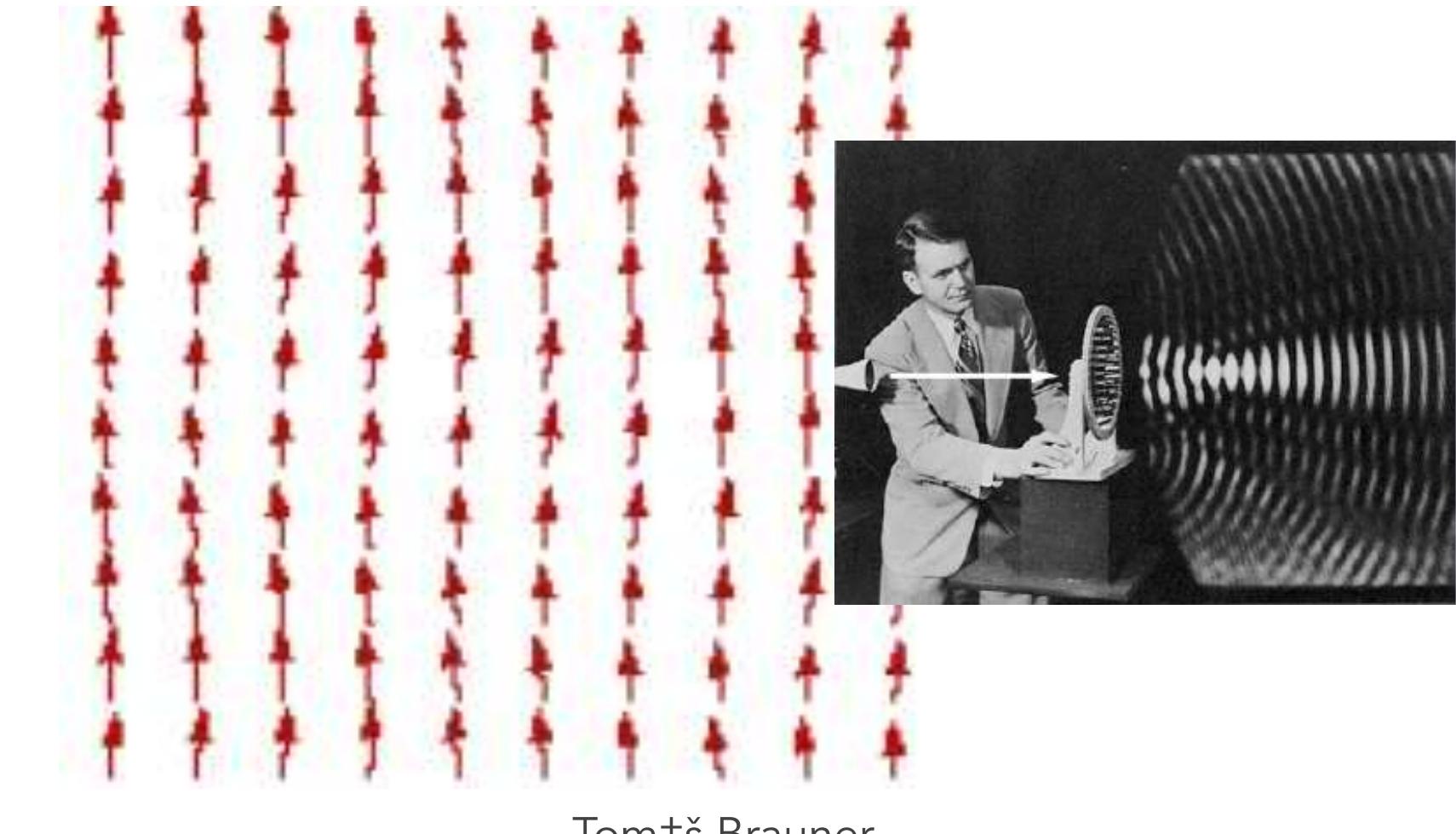
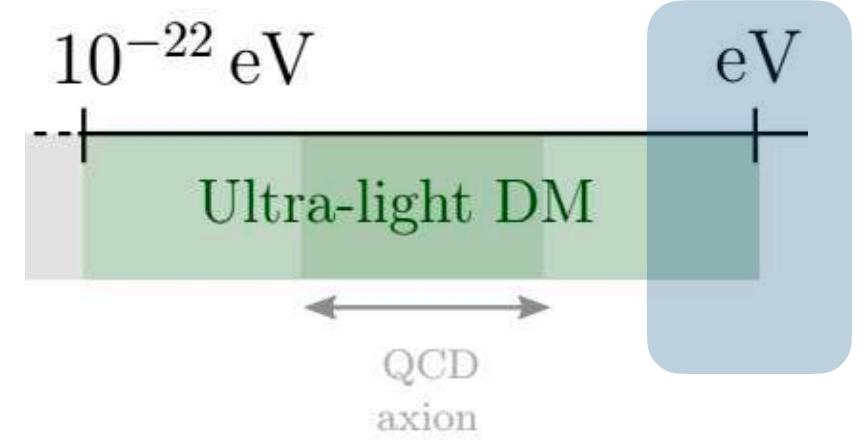
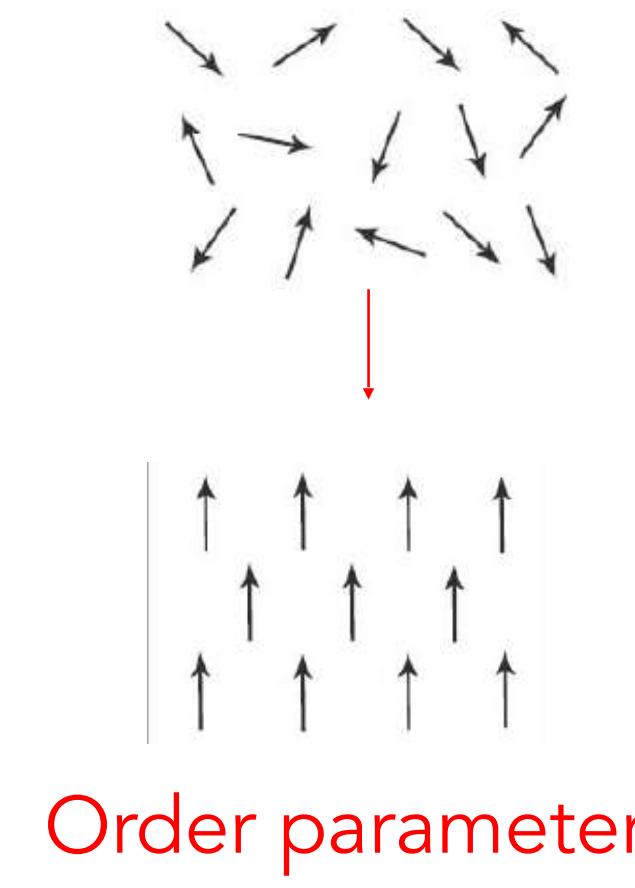
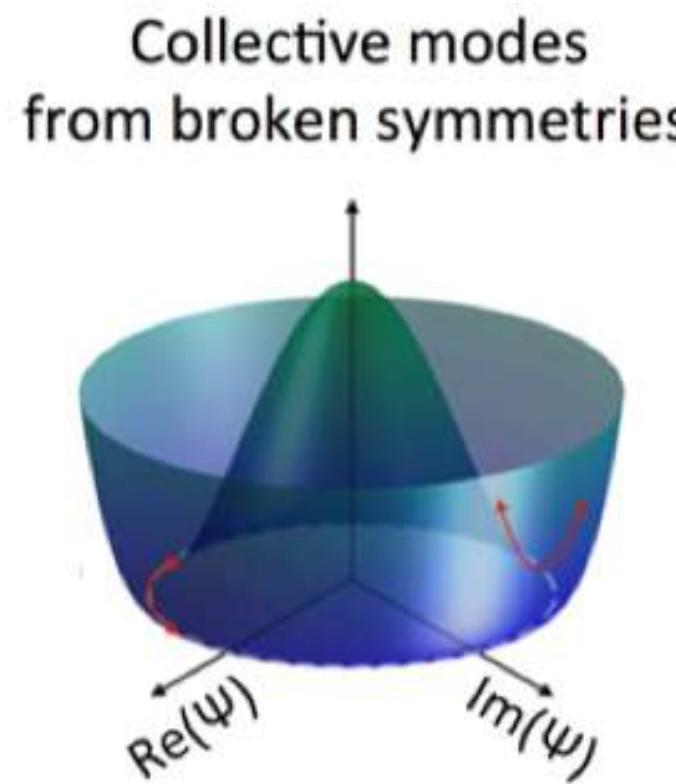
$$a = \begin{cases} a_N^b, & a_N^b \gg a_0, \\ \sqrt{a_N^b a_0}, & a_N^b \ll a_0. \end{cases}$$

Similar phenomenology than the FDM & SIFDM + explains the **rotations curves and scaling relations**

Suppresses small structures, dyn. effects, formation of cores

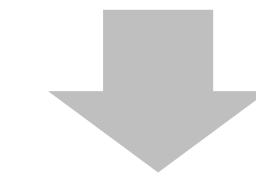
Collective modes

- Described by the **collective** behavior of the particles.
- No need for **microphysics**: symmetry alone describes the system.
- Collective modes related to symmetry = Nambu–Goldstone bosons



Tomáš Brauner

Effective degree of freedom

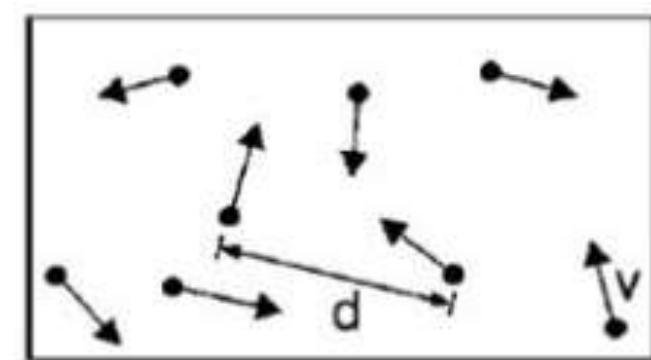


Effective dynamics

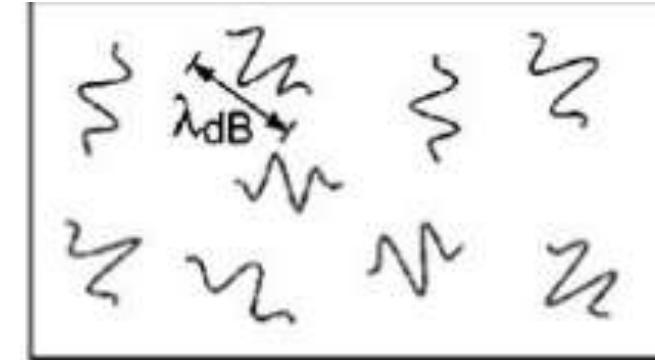
Superfluid



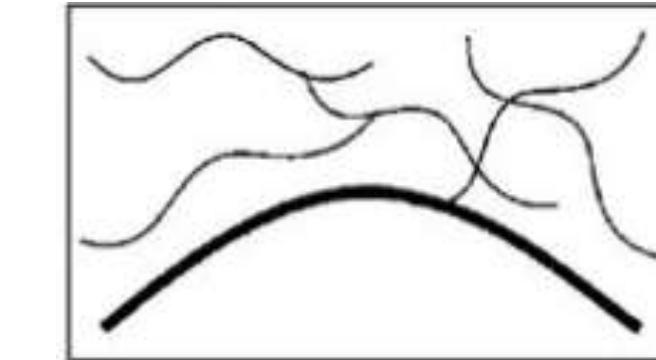
- At low temperatures, a superfluid condenses into a Bose-Einstein condensate (BEC).
- De Broglie wavelength (λ_B) of each particle is large enough that their quantum wave function overlap, and a single wave function describes the entire liquid.
- Quantum phenomenon that appears at low temperatures and macroscopic scales.
- **Effective dynamics:** fluid that can flow without friction.



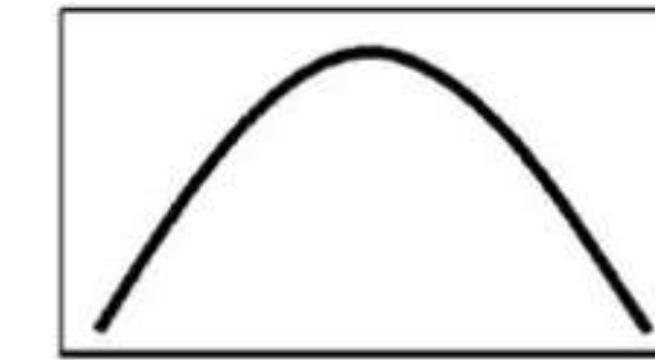
High temperature
Thermal velocities



Low temperature
 $\lambda_B \sim T^{-1/2}$
"wave packets"



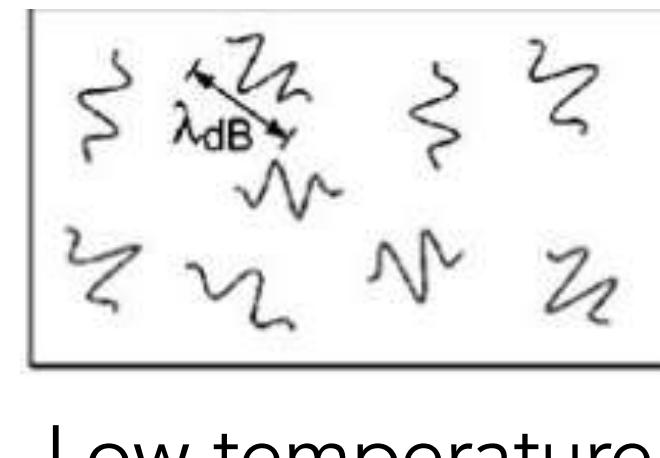
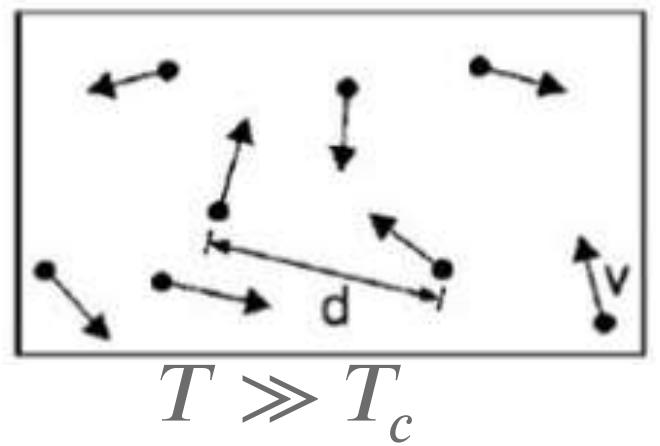
$T = T_c$
BEC
"matter wave overlap"



$T = 0$
Pure BEC
"giant matter wave"

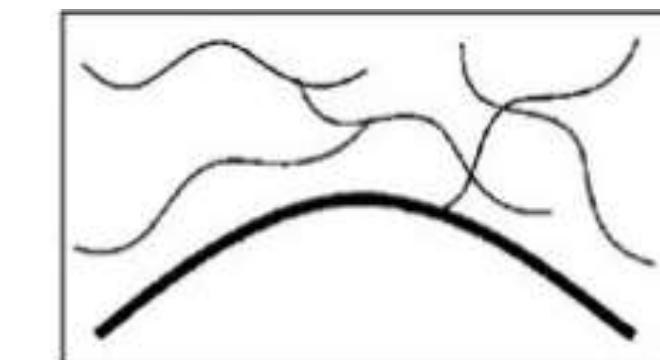
Goal:

Use this property of the **collective** behaviour to explain the **modified dynamics** at certain **scales/times** in the evolution of the universe.

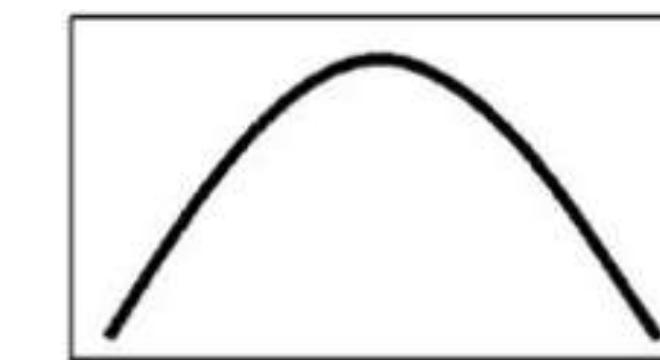


Low temperature

$$\lambda_B \sim T^{-1/2}$$

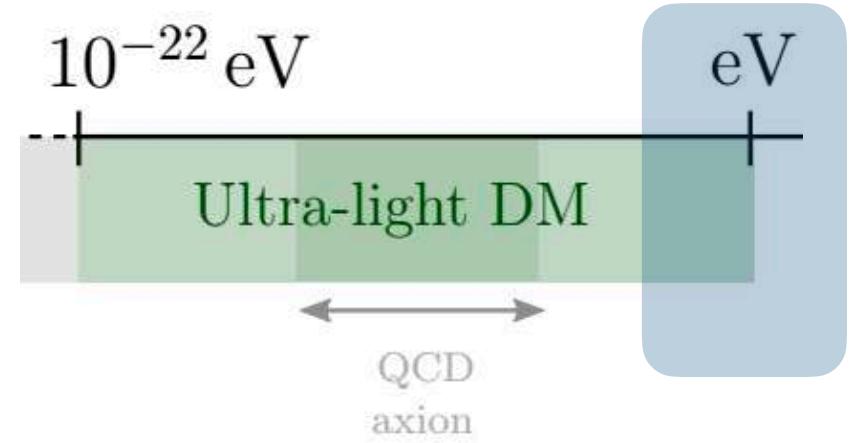


$T = T_c$
BEC



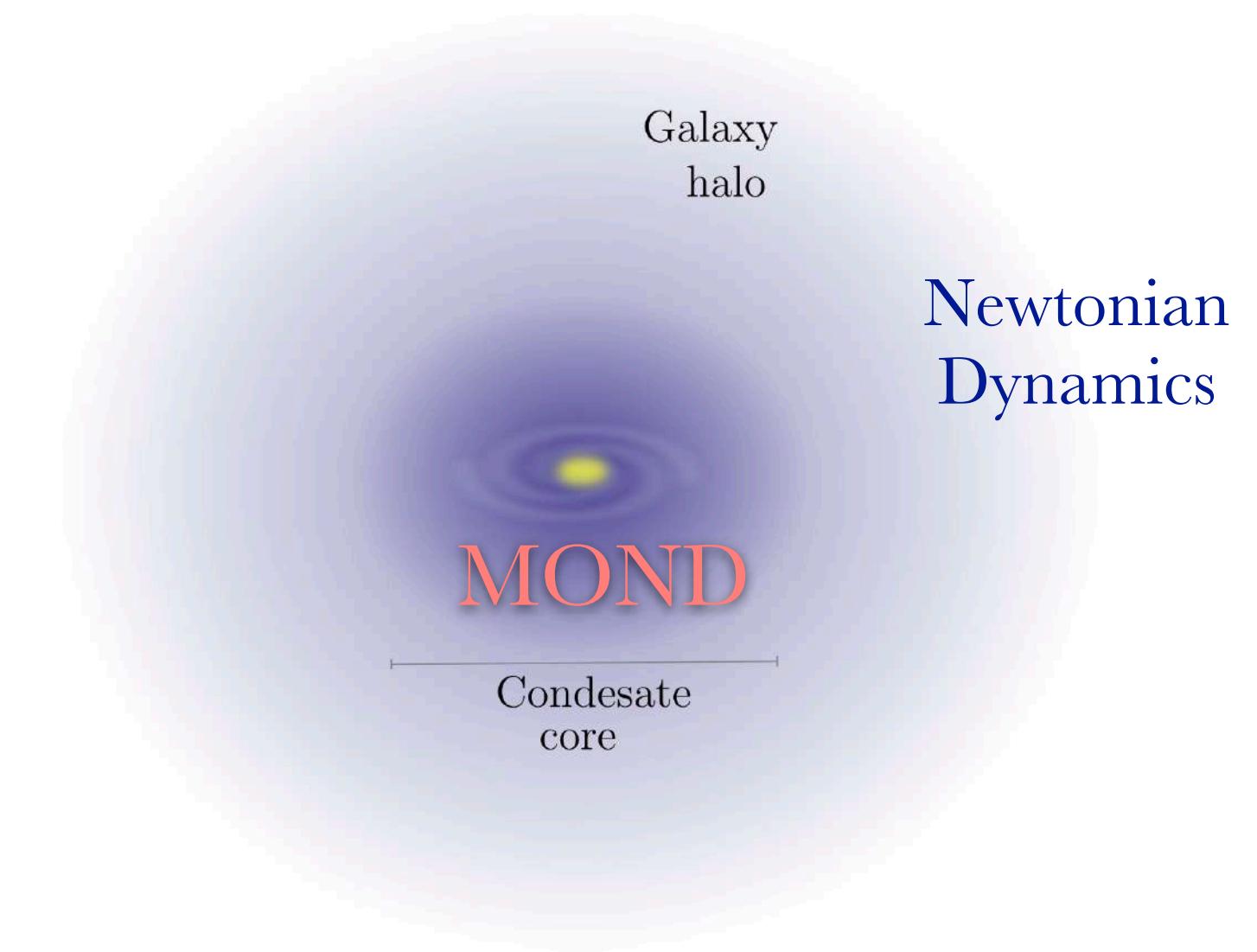
$T = 0$
Pure BEC

Superfluid Dark Matter

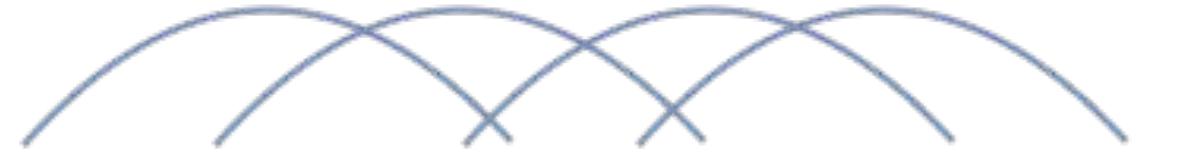


Lasha Berezhiani and Justin Khoury (2016)

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DM forms a **superfluid**
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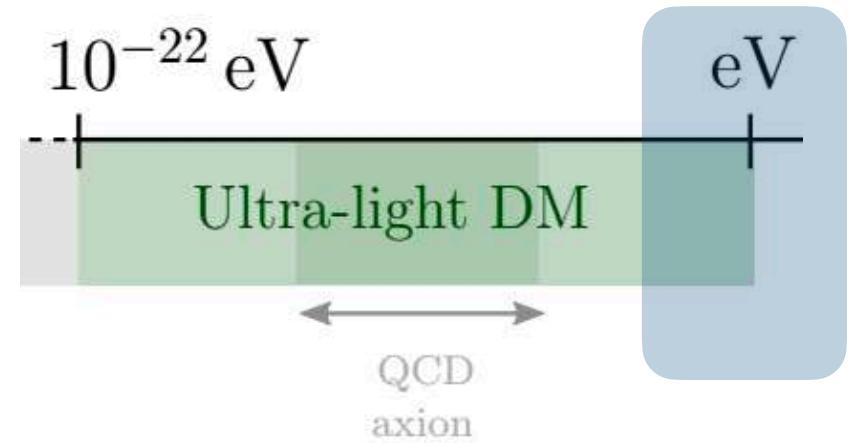


$$a = \begin{cases} a_N^b, & a_N^b \gg a_0, \\ \sqrt{a_N^b a_0}, & a_N^b \ll a_0. \end{cases}$$

Similar phenomenology than the FDM & SIFDM + explains the **rotations curves and scaling relations**

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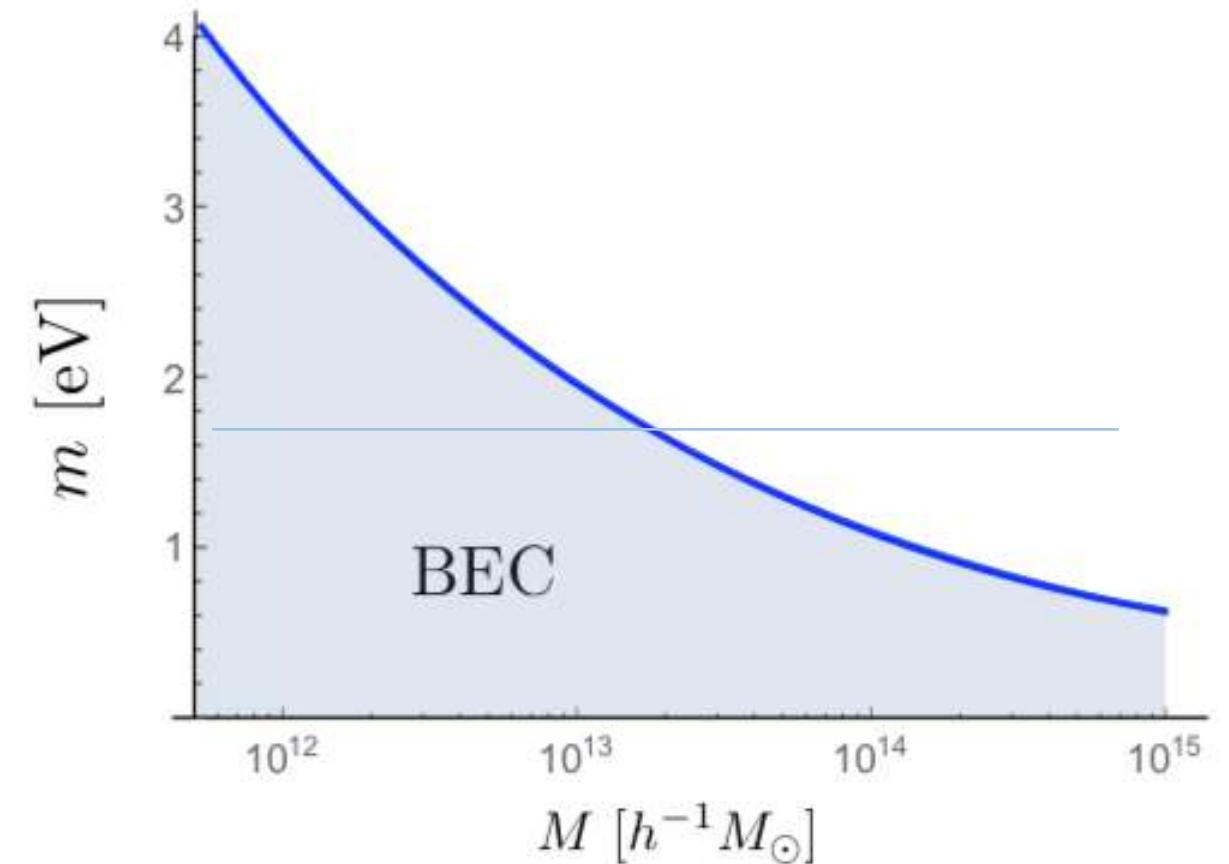
Condition for Superfluidity



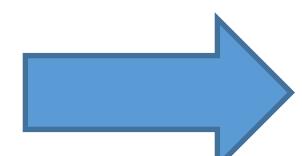
DM has to condensate in galaxies:

- de Broglie wavelength of the particles must overlap ($N_0/N = 1 - (T/T_c)^{3/2}$)

$$\lambda_b \sim \frac{1}{mv} \geq d \sim \left(\frac{m}{\rho_{vir}} \right)^{\frac{1}{3}} \implies m \leq 2\text{eV}$$

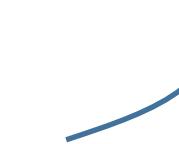


- Thermalization



Strongly interacting axion-like particle.
DM is cold: $T_c \sim \text{mK}$

Cold atoms in the lab

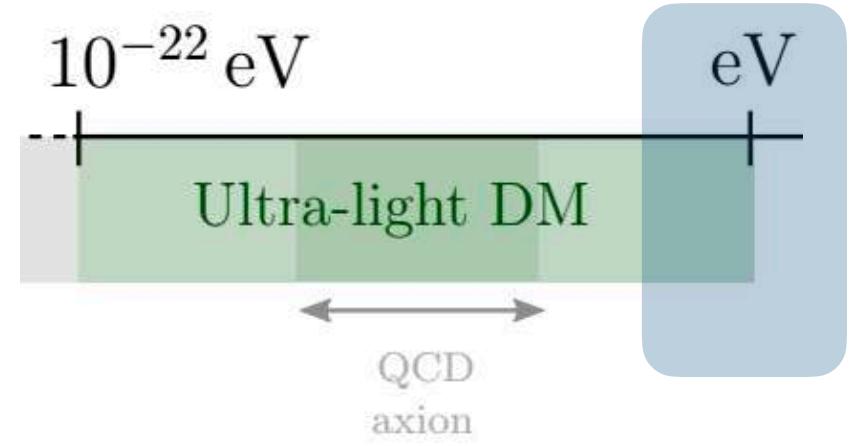


$$\frac{\sigma}{m} \gtrsim 0.1 \frac{\text{cm}^2}{\text{g}}$$

Condition for superfluidity
(Landau criteria):

$$v_s < v_c (\neq 0)$$

Description of the Superfluid



Effective field theory that describes a superfluid is represented by a:

- System with a **U(1) global symmetry** that is spontaneously broken.

$$\mathcal{L} = -|\partial\Psi|^2 - m_\Psi^2 |\Psi|^2 - \frac{\lambda}{2} |\Psi|^4 + (\dots) \quad \Psi = \Psi_0 + \delta\Psi$$

- Condensate:

$$\Psi_0 = v e^{\pi(x, t)}$$

$$\mathcal{L}_0 = (\partial_\mu v)^2 + v^2 [(\partial_\mu \pi)^2 - m^2] - \frac{\lambda}{2} v^4$$

Current: $\dot{j}_0 = v^2 \dot{\pi} = \text{const.} \Rightarrow \dot{\pi} = \mu$

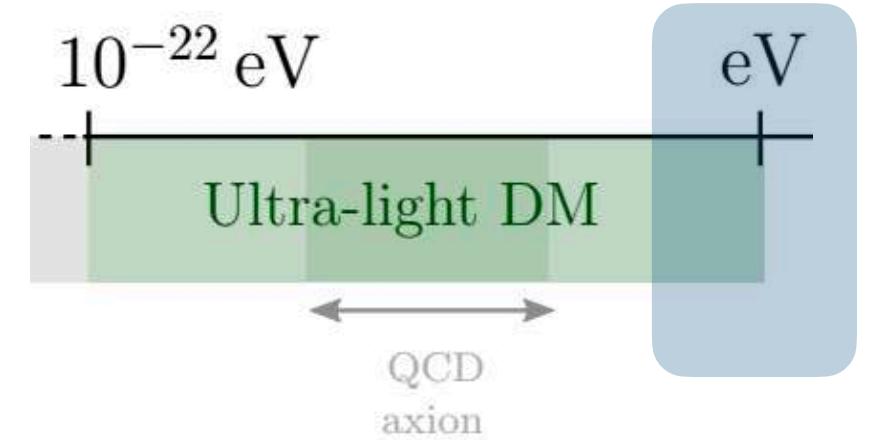
The stationary solution determines the ground state of the system



$$\Psi_0 = v e^{i\mu t}$$

$$\begin{cases} \mu^2 < m^2 & \text{Symmetry restoring phase} \\ \mu^2 > m^2 & \text{Bose Einstein condensation} \end{cases}$$

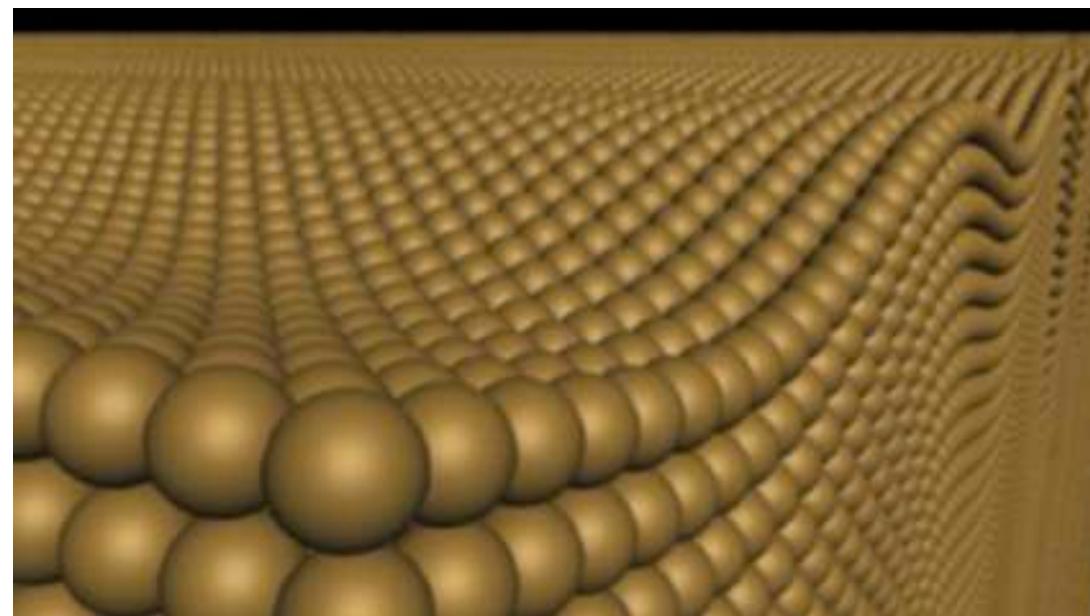
Description of the Superfluid



- System with a **U(1) global symmetry** that is spontaneously broken.

$$\mathcal{L} = -|\partial\Psi|^2 - m_\Psi^2 |\Psi|^2 - \frac{\lambda}{2} |\Psi|^4 + (\dots)$$

$$\Psi = \Psi_0 + \delta\Psi \quad \left\{ \begin{array}{l} \text{Condensate: } \Psi_0 = v e^{i\mu t} \\ \text{Excitations: } \Psi = (v + \rho) e^{i(\mu t + \theta)} \end{array} \right.$$



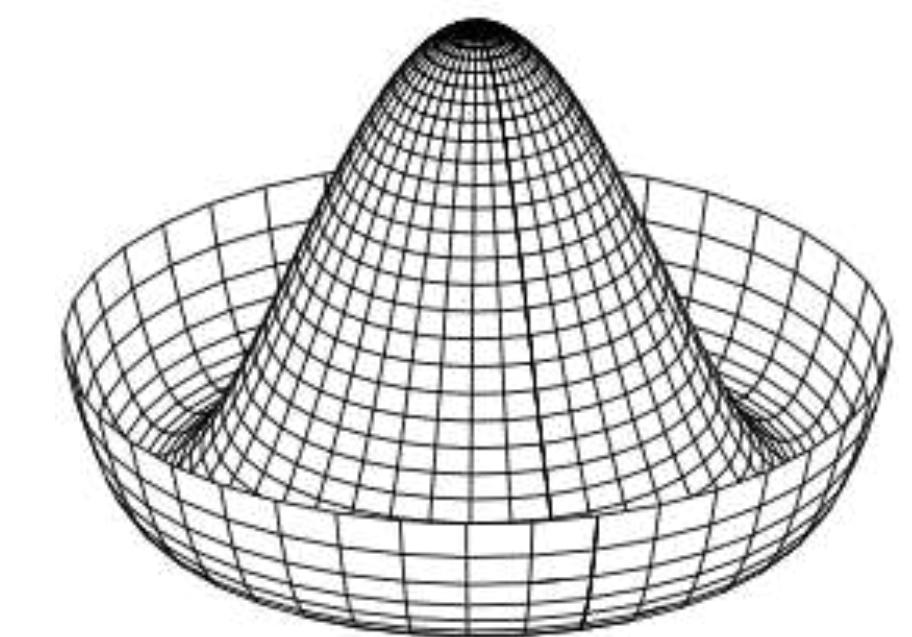
Crystal Lens

Collective excitations: massless Goldstone and massive quasi-particles.

$$\omega_k^2 = c_s^2 k^2 + \frac{1}{(2\mu)^2} k^4$$

Low energy: only θ excited - phonon $\omega \sim c_s k$

* Recover the previous description in the non-relativistic regime



Description of the Superfluid

Low energies ($\dot{\theta}/m \ll 1$)

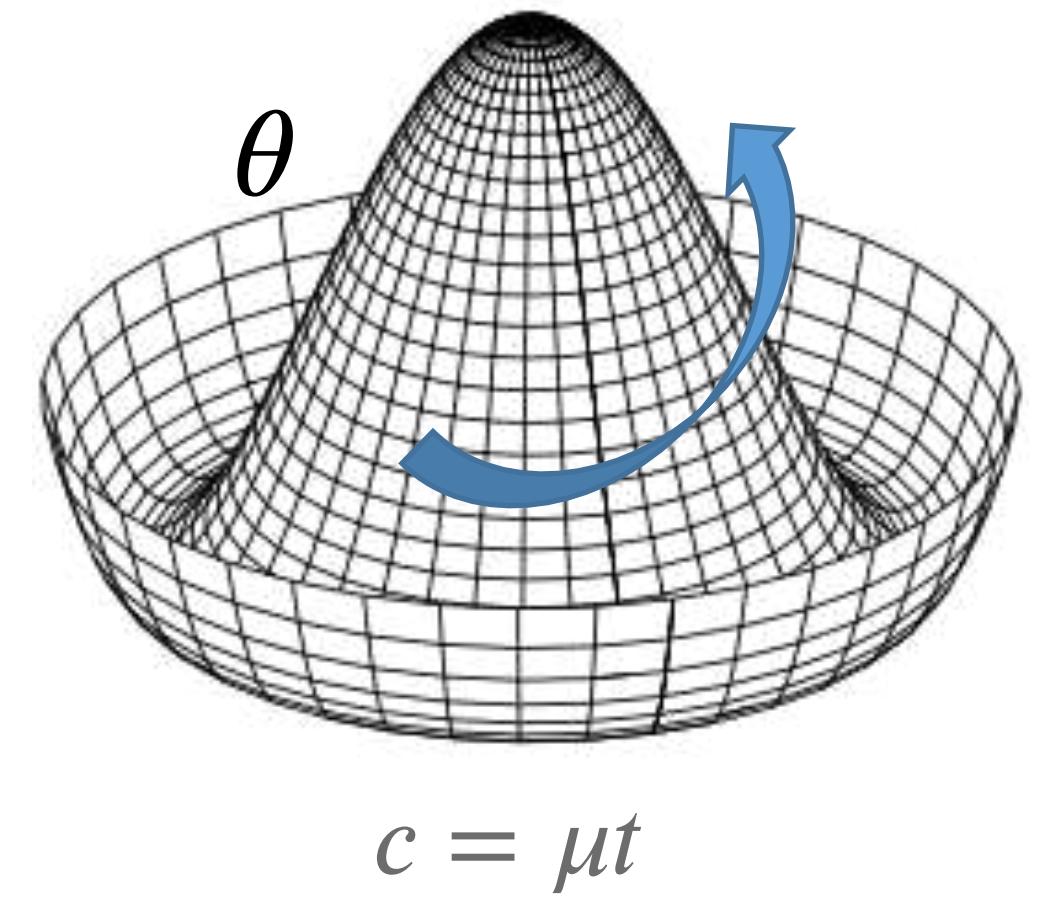
Greiter, Wilczek & Witten (1989);
Son and Wingate (2005)

- Low energy DOF: Only massless Goldstone bosons excited θ

Shift symmetry $\theta \rightarrow \theta + c$

$$\Theta = \mu t + \theta$$

Chemical potential $\xleftarrow{\quad}$ $\xrightarrow{\quad}$ Phonon excitations



In the non-relativistic regime and at lowest order in derivatives:

+ Galilean invariance

$$\mathcal{L} = P(X), \quad X = \dot{\theta} - m\Phi - \frac{(\vec{\nabla}\theta)^2}{2m} \quad \dot{\theta}/m \ll 1$$

Gravitational potential

MOND from phonons

Lasha Berezhiani and Justin Khoury (2016)

This description represents different phenomena:

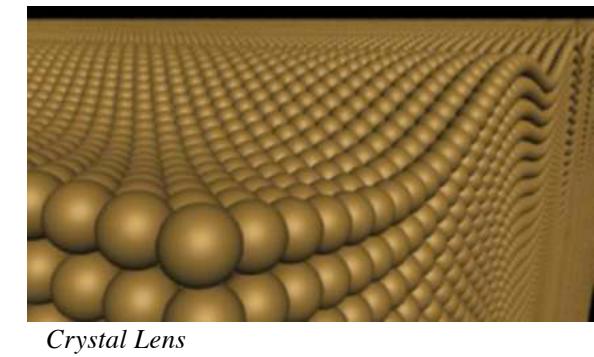
$$\mathcal{L} = P(X) = \frac{\Lambda^4}{n} \left(\frac{\dot{\theta}}{m} \right)^n$$

- $\left. \begin{array}{l} - n = 2 : \quad P \sim \rho^2 \\ - n = 3/2 : \quad P \sim \rho^3 \\ - n = 5/2 : \quad P \sim \rho^{5/3} \end{array} \right\}$
- BEC
- MOND**
- Unitary Fermi Gas

Superfluid Dark Matter

How to construct - MOND from phonons

EFT of superfluids

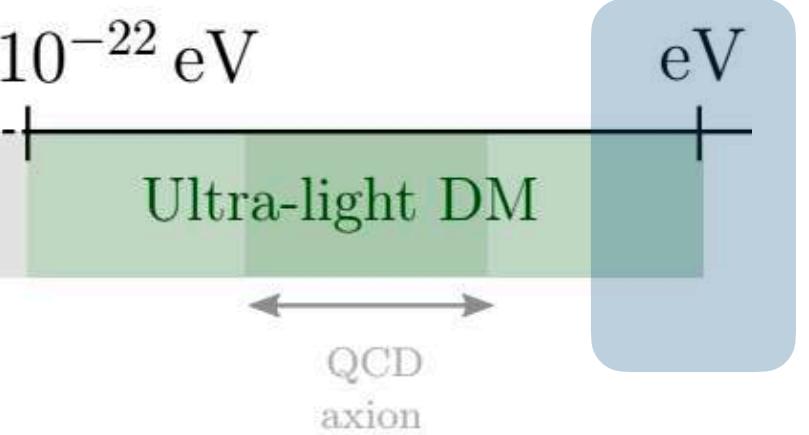


$$\mathcal{L} = P(X)$$

$$X = \dot{\theta} - m\Phi - \frac{(\vec{\nabla}\theta)^2}{2m}$$

$$\Psi = (v + \rho)e^{i(\mu t + \theta)}$$

Low energy: only θ excited - phonon
Nambu Goldstone boson



Lasha Berezhiani and Justin Khoury (2016)

Different phenomena $P(X) \propto (\dot{\theta}/m)^n$

$n = 2$: $P \sim \rho^2$ BEC

$n = 3/2$: $P \sim \rho^3$ "MOND"

$n = 5/2$: $P \sim \rho^{5/3}$ Unitary Fermi gas

To describe non-relativistic MOND, it is imposed that:

$$P(X) = \frac{2\Lambda (2m)^{3/2}}{3} X \sqrt{|X|}$$

→ Leads to an equation of state $P \sim \rho^3$
required to describe MOND

To mediate the MONDian force,
couple phonons to baryons:

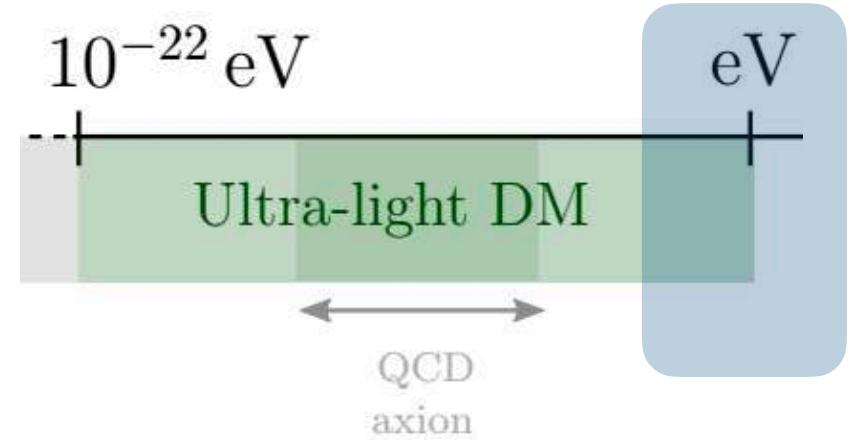
$$\mathcal{L}_{int} \sim \frac{\Lambda}{M_{pl}} \theta \rho_b$$

Softly breaks shift symmetry

$$\Lambda = \sqrt{a_0 M_{pl}} \sim 0.8 \text{ meV}$$

Description of the Superfluid

Low energies ($\dot{\theta}/m \ll 1$)



- Low energy DOF: Only massless Goldstone bosons excited θ - Shift symmetry $\theta \rightarrow \theta + c$

In the non-relativistic regime and at lowest order in derivatives:

+ Galilean invariance

$$\mathcal{L} = P(X), \quad X = \dot{\theta} - m\Phi - \frac{(\vec{\nabla}\theta)^2}{2m}$$

Different phenomena $P(X) \propto (\dot{\theta}/m)^n$

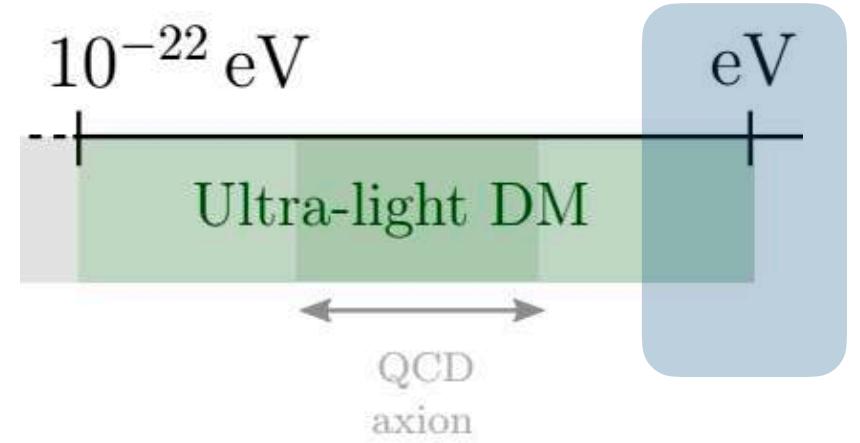
$$\begin{cases} n = 2 : & P \sim \rho^2 & \text{BEC} \\ n = 3/2 : & P \sim \rho^3 & \text{"MOND"} \\ n = 5/2 : & P \sim \rho^{5/3} & \text{Unitary Fermi gas} \end{cases}$$

Equivalence (low energies)

$$\text{2-body } \mathcal{L} = -|\partial\Psi| - m^2|\Psi|^2 - \frac{\lambda}{2}|\Psi|^4 \iff \mathcal{L} = P(X) \propto X^2 \implies p \propto \rho^2$$

$$\text{3-body } \mathcal{L} = -|\partial\Psi| - m^2|\Psi|^2 - \frac{g_3}{3}|\Psi|^6 \iff \mathcal{L} = P(X) \propto X^{3/2} \implies p \propto \rho^3$$

Superfluid Dark Matter



- Newtonian limit: $|\vec{\nabla}\Phi| > 3a_0$

$$\Rightarrow \vec{\nabla}^2\Phi = \frac{\rho_s + \rho_b}{2M_{pl}^2}$$

- MOND limit: $|\vec{\nabla}\Phi| < 3a_0$

$$\Rightarrow \vec{\nabla} \cdot \left(\frac{|\vec{\nabla}\Phi|}{a_0} \vec{\nabla}\Phi \right) = \frac{\rho_s + \rho_b}{2M_{pl}^2}$$



Higher order correction

- Higher order contributions to the quadratic Lagrangian for the phonon, can contain terms of the form:

$$\mathcal{L}_{\text{higher-order}} \supset \left(\Lambda m^{3/2} \mu^{3/2} \right)^{1 - \frac{n}{2}} \partial^n \phi_c^n$$

where $\partial \rightarrow \partial_t$ or $c_s \vec{\nabla}$ and the canonical variable is $\phi_c = \Lambda^{1/2} m^{3/4} \mu^{-1/4} \phi$

Strong coupling scale, the scale suppressing higher order terms:

$$\Lambda_s = \left(\Lambda m^{3/2} \mu^{3/2} \right)^{1/4} \simeq \left(\Lambda m^3 c_s^3 \right)^{1/4}$$

$$(c_s^2 = 2\mu/m \sim \dot{\theta}/m \ll 1)$$

Higher order corr.
neglected when

$$\frac{1}{\Lambda_s} \frac{\partial_r^2 \phi}{\partial \phi} \sim \frac{1}{\Lambda_s r} \ll 1$$

$$\rightarrow \Lambda_s \sim \text{meV} \left(\frac{M_{DM}}{10^{12} M_\odot} \right)^{3/10} \left(\frac{m}{\text{eV}} \right)^{6/5} \left(\frac{\Lambda}{\text{meV}} \right)^{2/5}$$

Fiducial parameters
(galaxies):

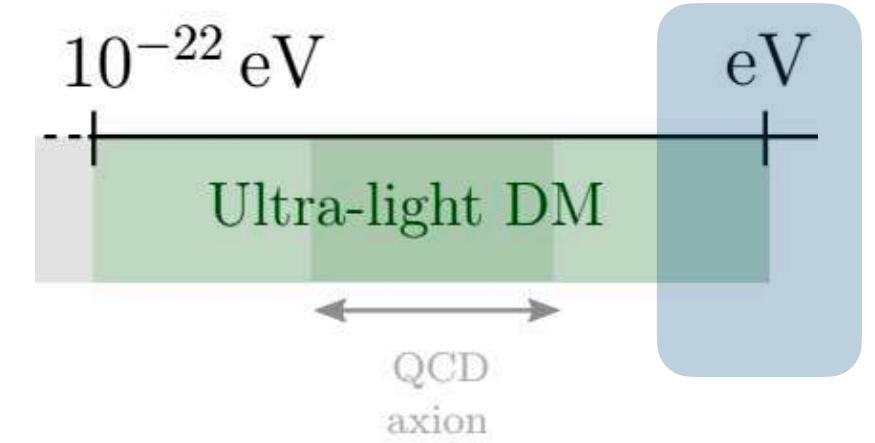
$$\Lambda_s \sim \text{meV}$$

HO corr.
neglected

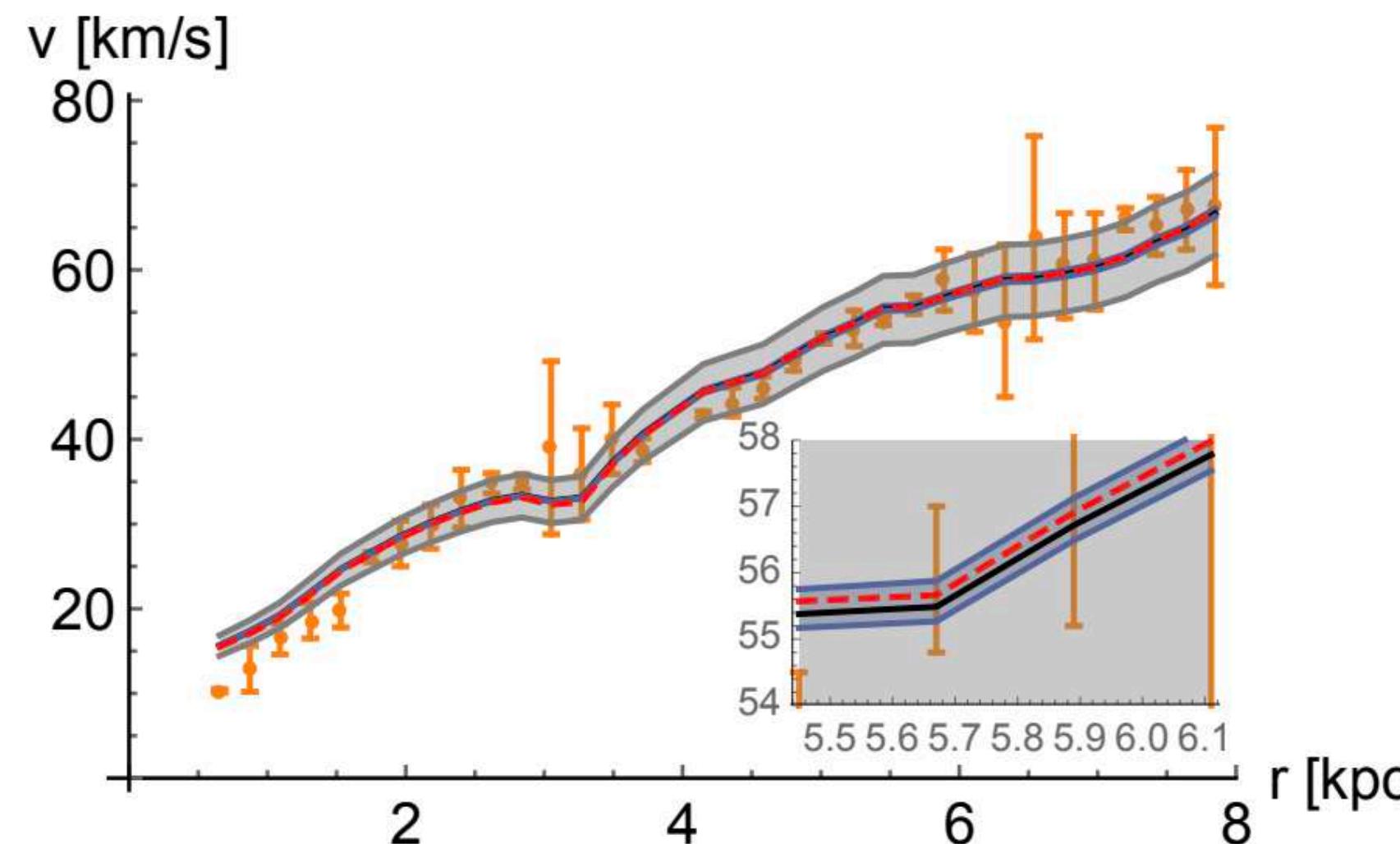
$$r \gg 0.2 \text{mm}$$

Superfluid Dark Matter

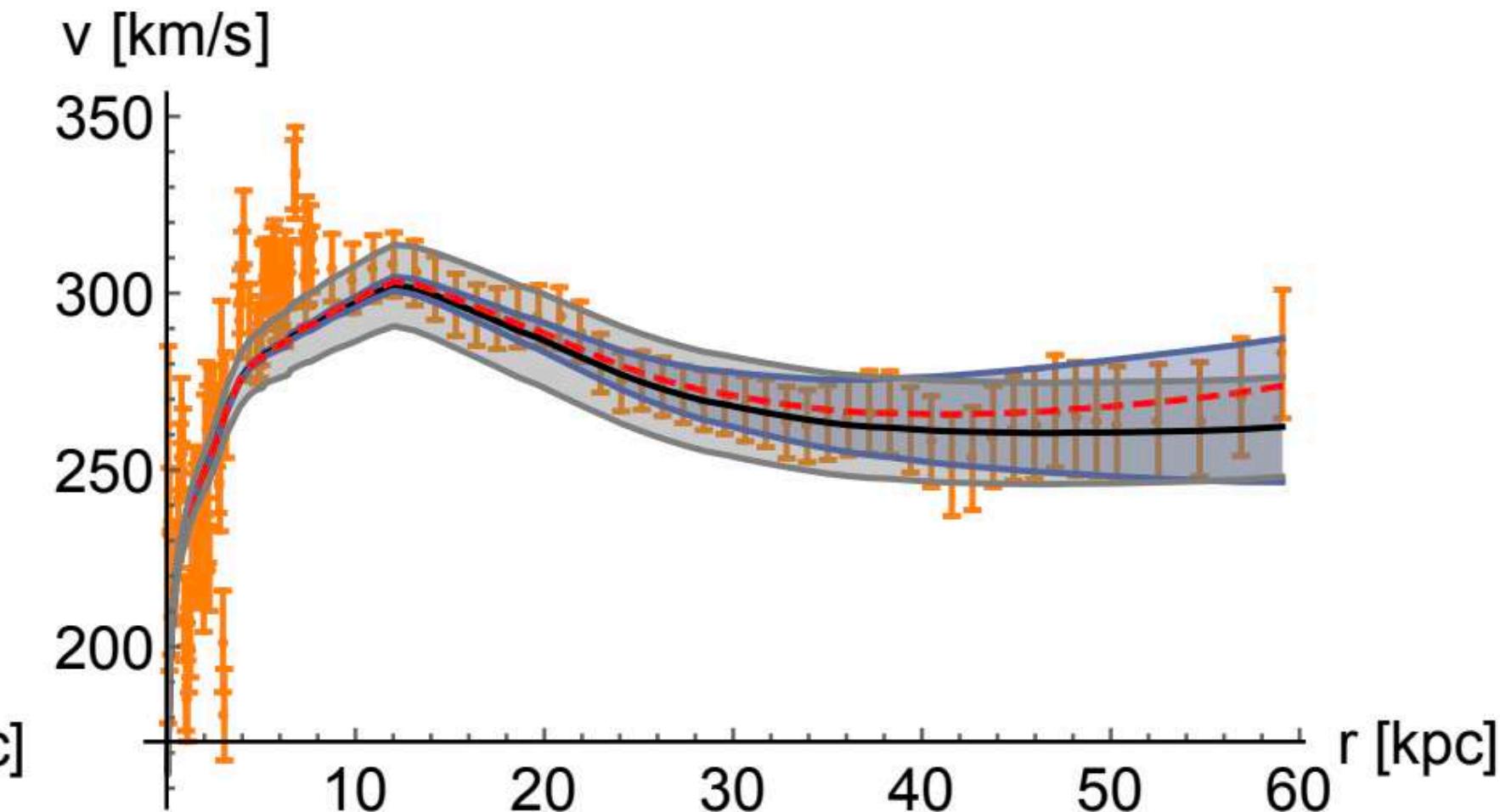
Rotation curves



Low surface brightness



High surface brightness



Superfluid core:

$$R_{halo} = 57 \text{ kpc}$$

$$R_{Sf} = 40 \text{ kpc}$$

58% of the total mass of the halo

$$R_{halo} = 445 \text{ kpc}$$

$$R_{Sf} = 79 \text{ kpc}$$

25% of the total mass of the halo

Superfluid Dark Matter

Observational consequences

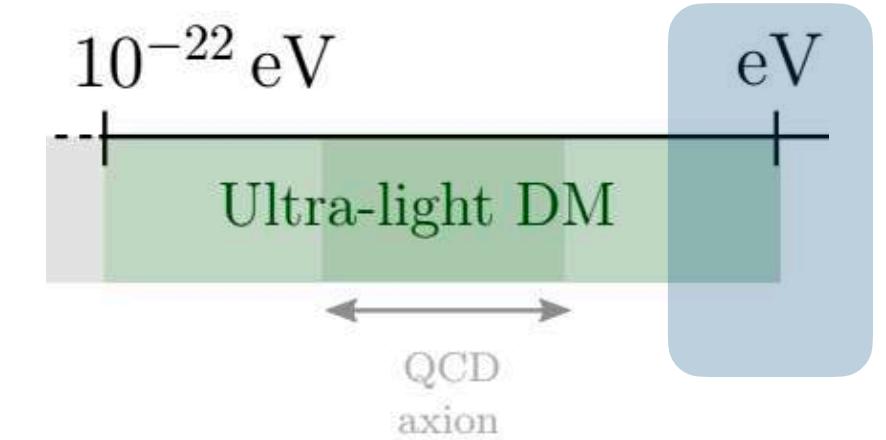
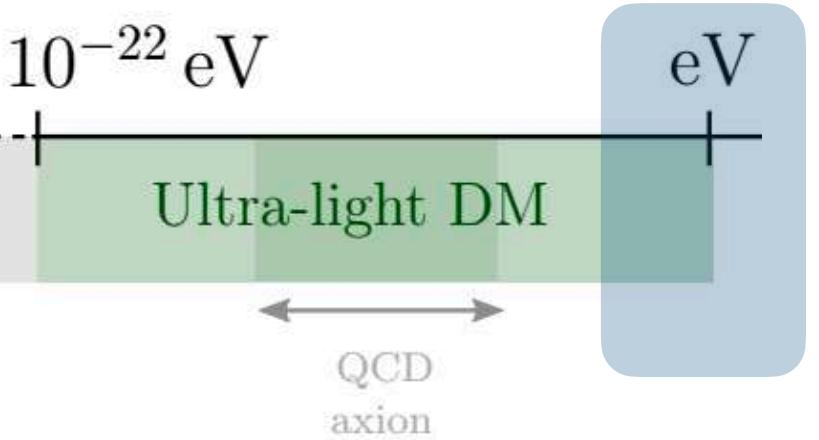


Table 2: Summary of observational consequences of superfluid DM from [124].

| System | Behavior |
|--|---|
| Rotating Systems | |
| Solar system | Newtonian |
| Galaxy rotation curve shapes | MOND (+ small DM component making HSB curves rise) |
| Baryonic Tully–Fisher Relation | MOND for rotation curves (but particle DM for lensing) |
| Bars and spiral structure in galaxies | MOND |
| Interacting Galaxies | |
| Dynamical friction | Absent in superfluid core |
| Tidal dwarf galaxies | Newtonian when outside of superfluid core |
| Spheroidal Systems | |
| Star clusters | MOND with EFE inside galaxy host core — Newton outside of core |
| Dwarf Spheroidals | MOND with EFE inside galaxy host core — MOND+DM outside of core |
| Clusters of Galaxies | Mostly particle DM (for both dynamics and lensing) |
| Ultra-diffuse galaxies | MOND without EFE outside of cluster core |
| Galaxy-galaxy lensing | |
| Driven by DM enveloppe \implies not MOND | |
| Gravitational wave observations | |
| | As in General Relativity |

Superfluid Dark Matter

Dynamical Friction

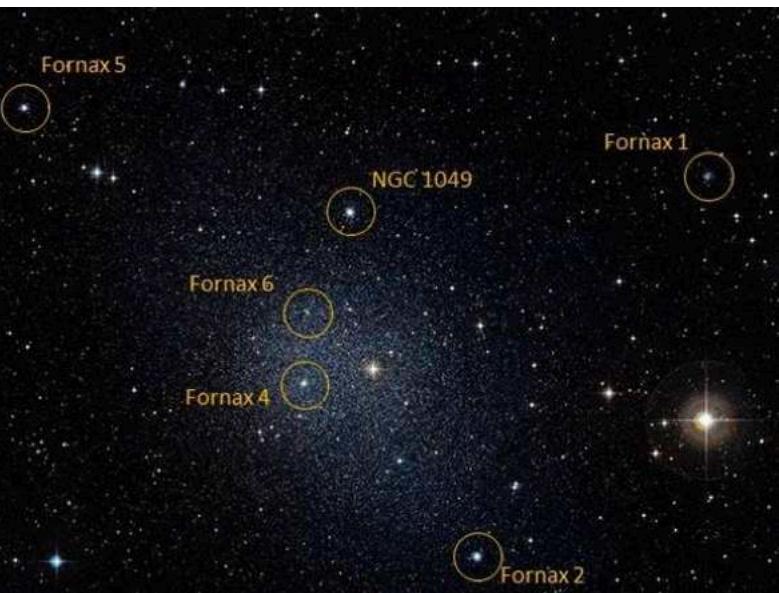


Inner region of galaxy:
Superfluid core

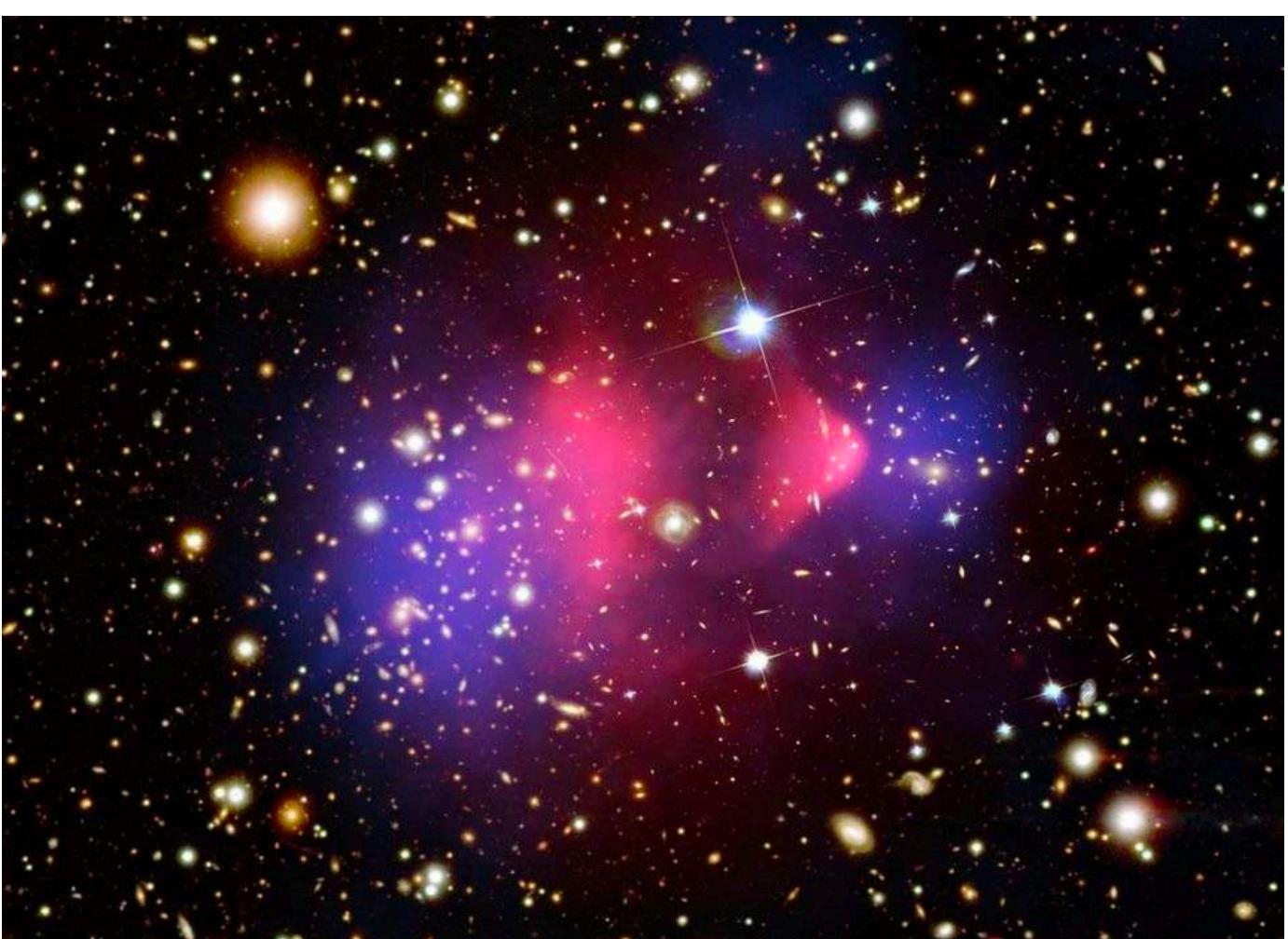


Superfluid flows **without friction**

- **Fornax:** globular cluster should have merged with Fornax due to dynamical friction.
Superfluid \rightarrow no friction
Can explain these glob. Clusters



Complete analysis in: B. Elder et al., JCAP 1910 (2019) no.10, 074

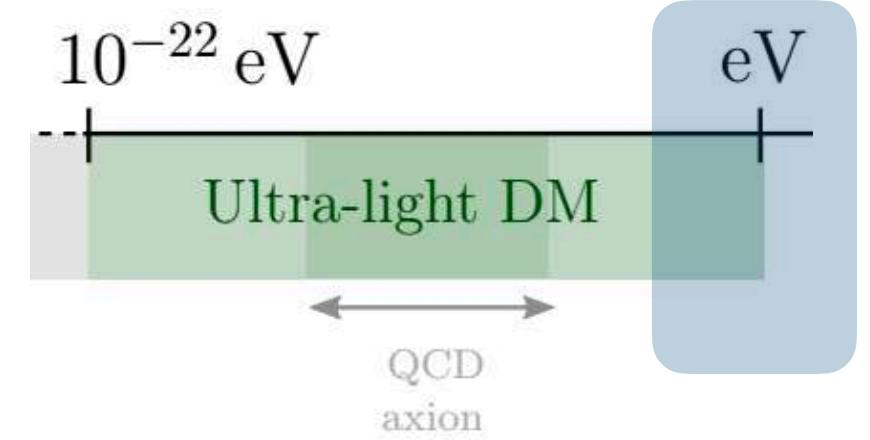


Composite Credit: X-ray: NASA/CXC/M.M. Markevitch et al.;
Lensing Map: NASA/STScI; ESO/WFI; Magellan/U.Arizona/D.Clowe et al.;
Optical: NASA/STScI; Magellan/U.Arizona/D.Clowe et al.

Large cluster **subsonic** and small
cluster **supersonic** (Sf core)
Bullet cluster as expected!

Landa criteria for
superfluid
 $v < v_c$

Superfluid Dark Matter



Superfluid DM model presents a very interesting behaviour in galaxies, being able to reproduce MOND from DM , BUT...

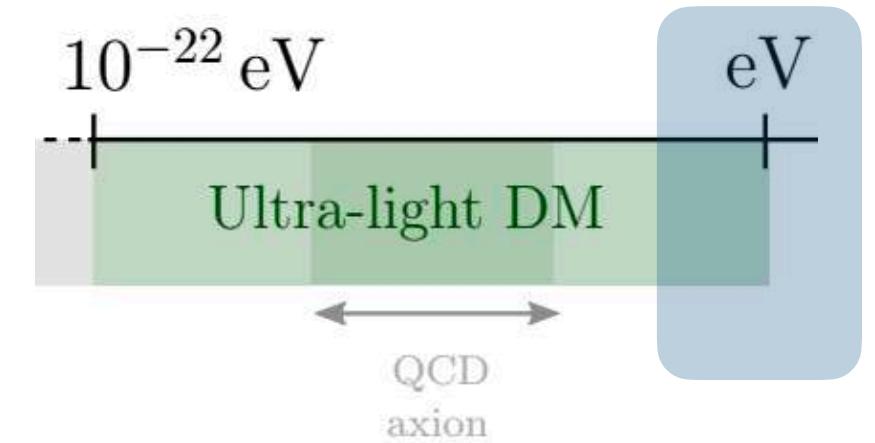
- Presents only a phenomenological non-relativistic description
- Need to develop cosmology
 \implies need a microscopic description
- Does not present many constraints yet.

(SAME AS IN FDM) Does condensation really takes place?

Presents opportunities of theoretical and observational advances!

Superfluid Dark Matter

Vertical dynamics



High Energy Physics – Phenomenology

The Inconsistency of Superfluid Dark Matter with Milky Way Dynamics

Mariangela Lisanti, Matthew Moschella, Nadav Joseph Outmezguine, Oren Sloane

(Submitted on 27 Nov 2019)

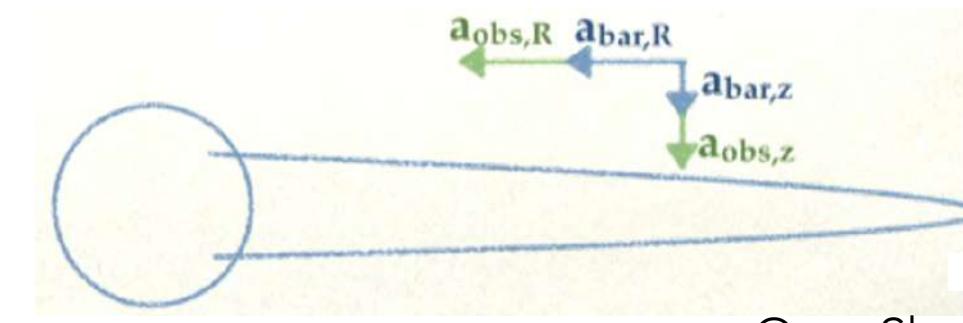
There are many well-known correlations between dark matter and baryons that exist on galactic scales. These correlations can essentially be encompassed by a simple scaling relation between observed and baryonic accelerations, historically known as the Mass Discrepancy Acceleration Relation (MDAR). The existence of such a relation has prompted many theories that attempt to explain the correlations by invoking additional fundamental forces on baryons. The standard lore has been that a theory that reduces to the MDAR on galaxy scales but behaves like cold dark matter (CDM) on larger scales provides an excellent fit to data, since CDM is desirable on scales of clusters and above. However, this statement should be revised in light of recent results showing that a fundamental force that reproduces the MDAR is challenged by Milky Way dynamics. In this study, we test this claim on the example of Superfluid Dark Matter. We find that a standard CDM model is strongly preferred over a static superfluid profile. This is due to the fact that the superfluid model over-predicts vertical accelerations, even while reproducing galactic rotation curves. Our results establish an important criterion that any dark matter model must satisfy within the Milky Way.

Comments: 6+5 pages, 2+4 figures

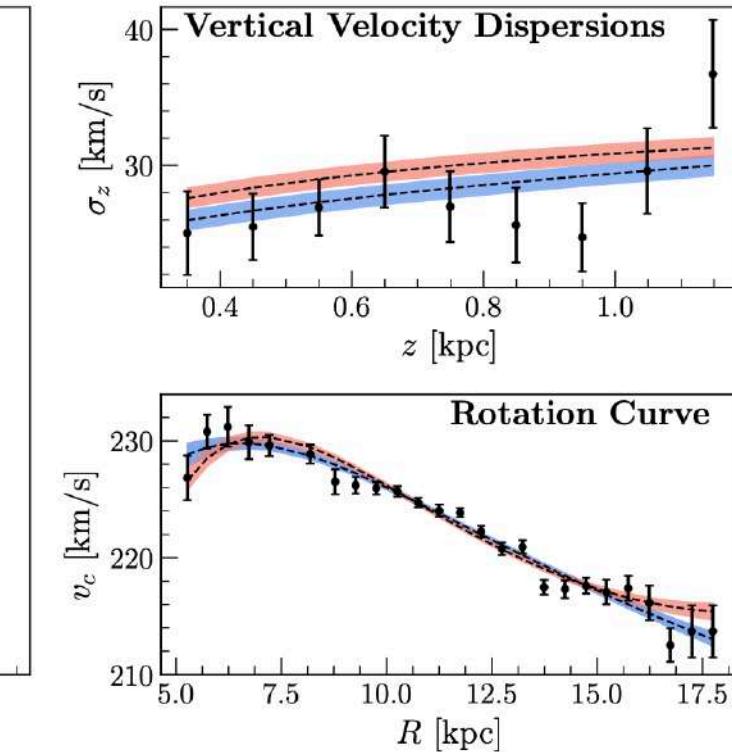
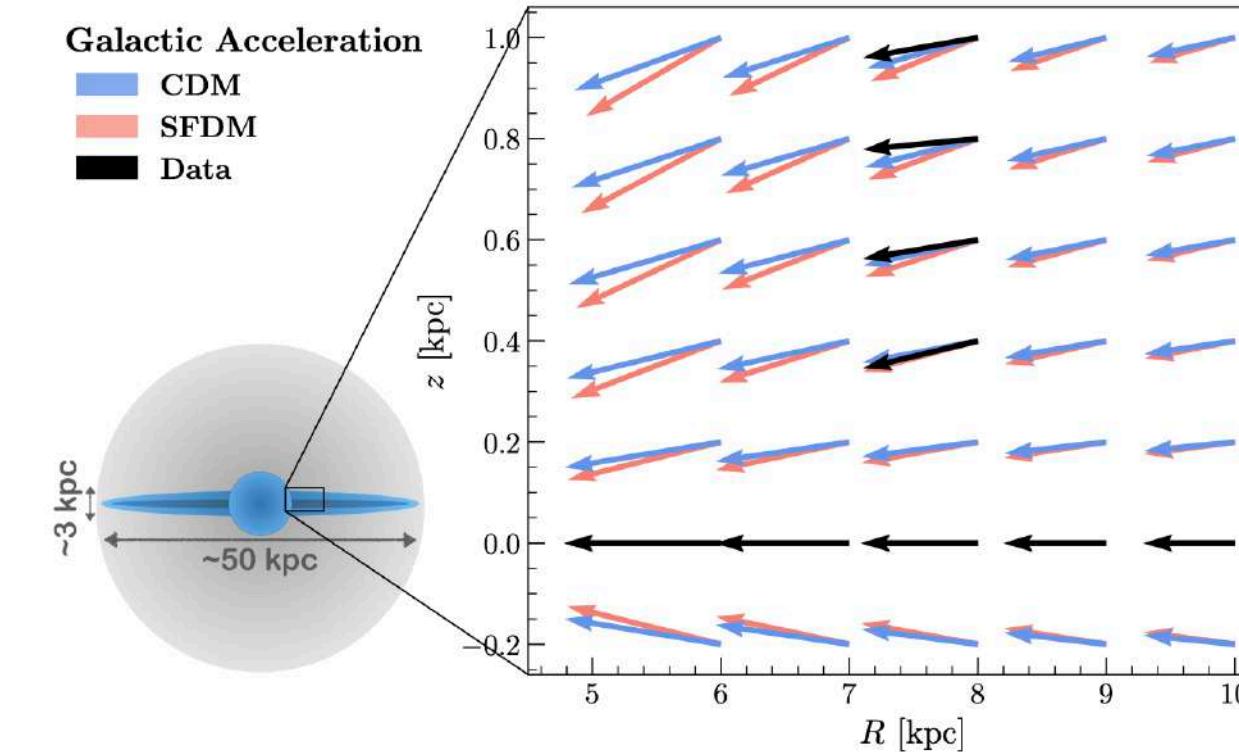
Subjects: High Energy Physics – Phenomenology (hep-ph); Cosmology and Nongalactic Astrophysics (astro-ph.CO); Astrophysics of Galaxies (astro-ph.GA)

Cite as: arXiv:1911.12365 [hep-ph]

(or arXiv:1911.12365v1 [hep-ph] for this version)



MOND-like force amplifies:
 a_R not enough
 a_z too much



Ultra-light fields as Dark Energy

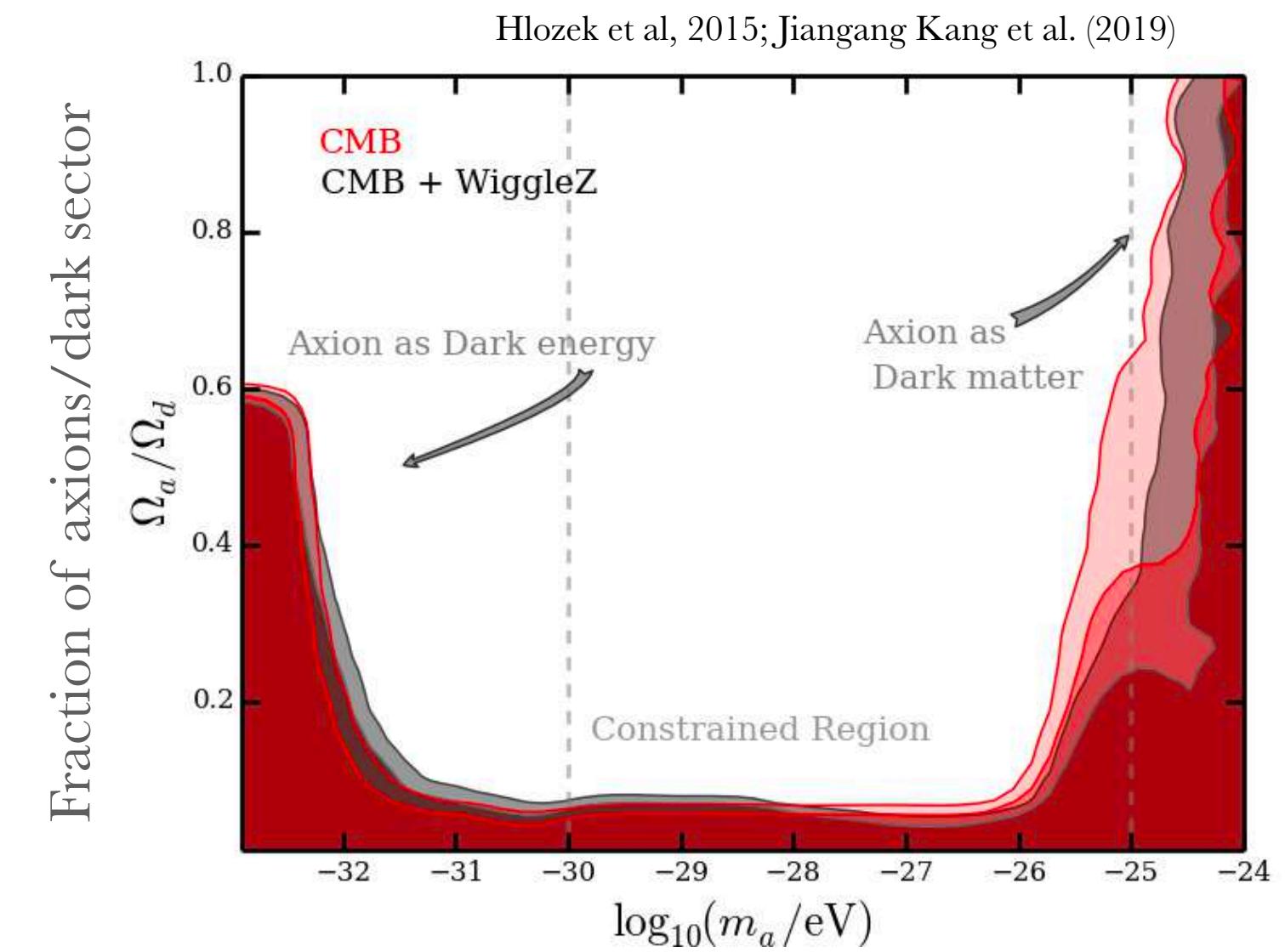


Ultra-light fields as Dark Energy

Fuzzy Dark Matter

Behave as **dark energy** with $w \sim -1$ for

$$m_{\text{fdm}} < 10^{-32} \text{ eV}$$



Ultra-light fields as Dark Energy



Unified superfluid dark sector

- DM superfluid with **two interacting distinguishable states**.
- Phonons: propagate with **different phases** for each species
→ Potential for the $(\theta_1 - \theta_2)$
- **Prediction** for clustering

Unified framework
w/ DM alone!

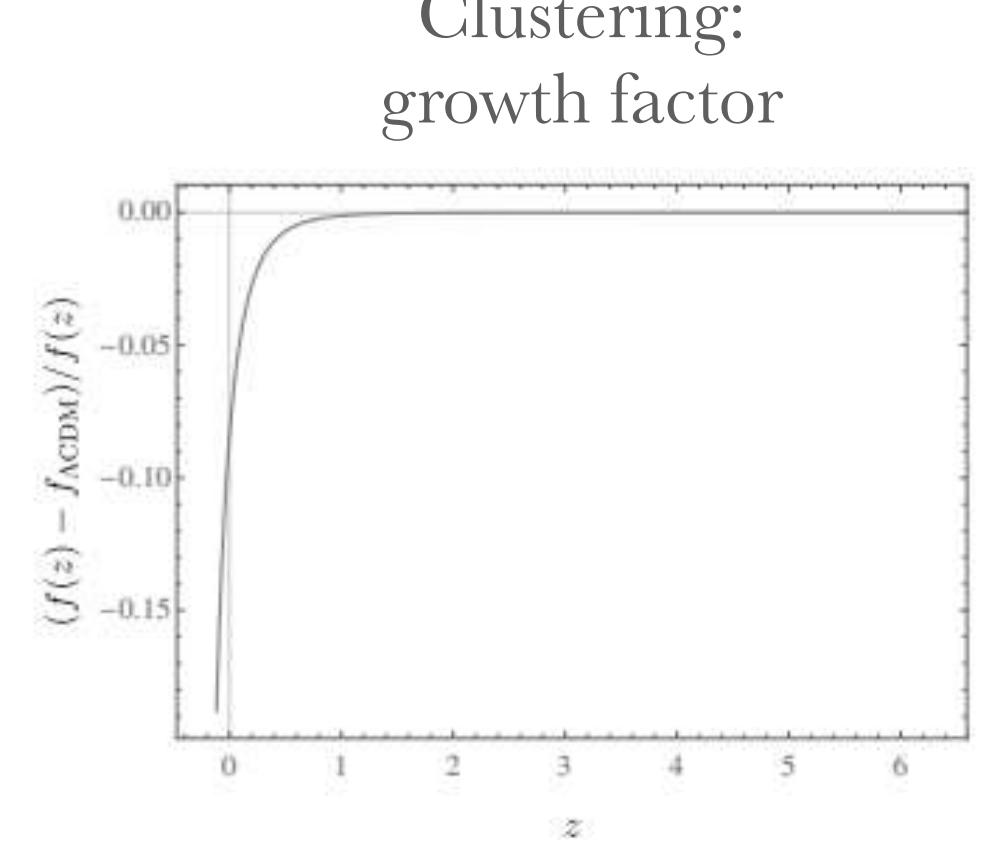
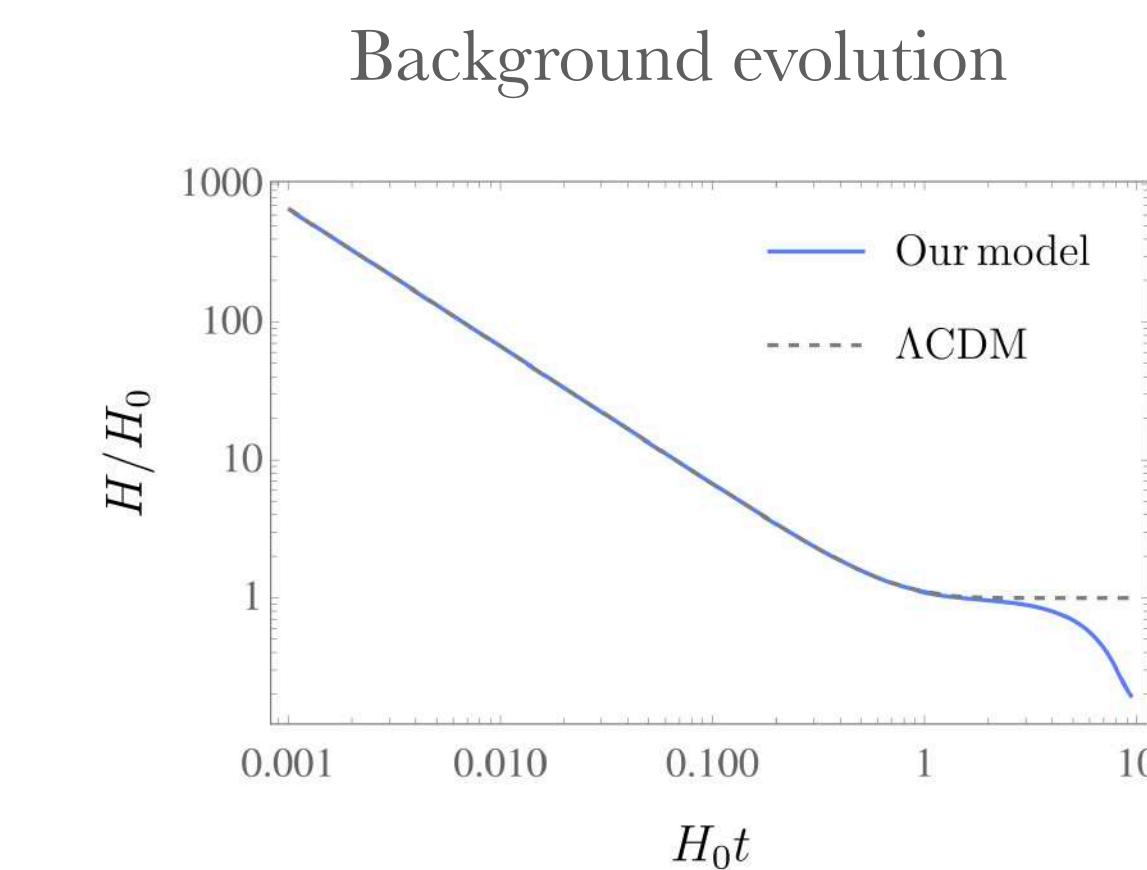
- Acceleration from **interactions** (no dark energy)
- Use condensed matter methods in cosmology – effective change of the dynamics, no change in the fundamental theory.

“*Unified superfluid dark sector*”, EF, G. Franzmann, J. Khoury, R. Brandenberger, 2018

$$\mathcal{L} = P(X_1) + P(X_2) - M^4 [1 + \cos(\theta_1 - \theta_2)/f]$$

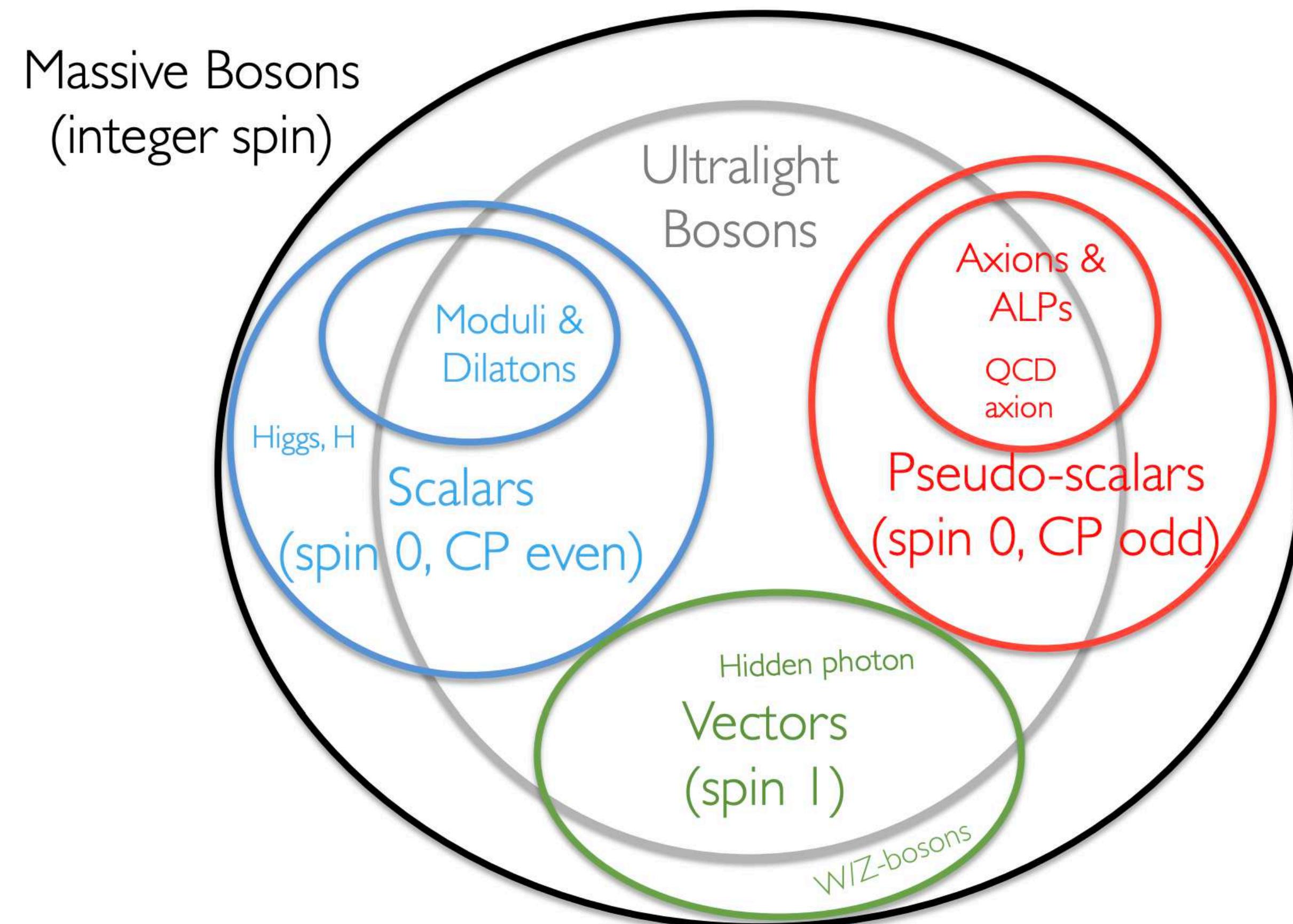
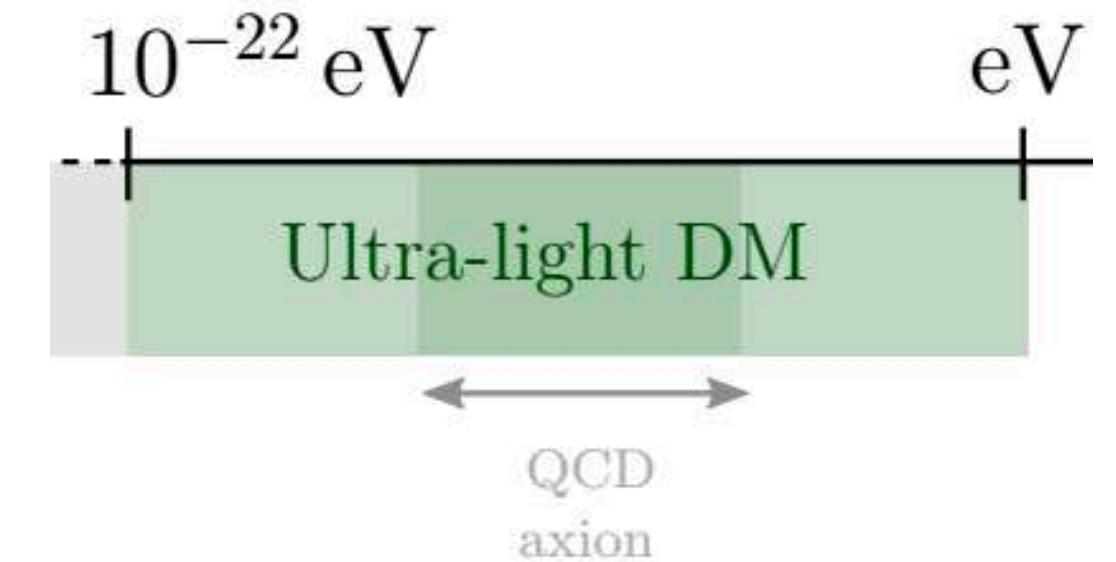
Dark matter

Potential - dark energy



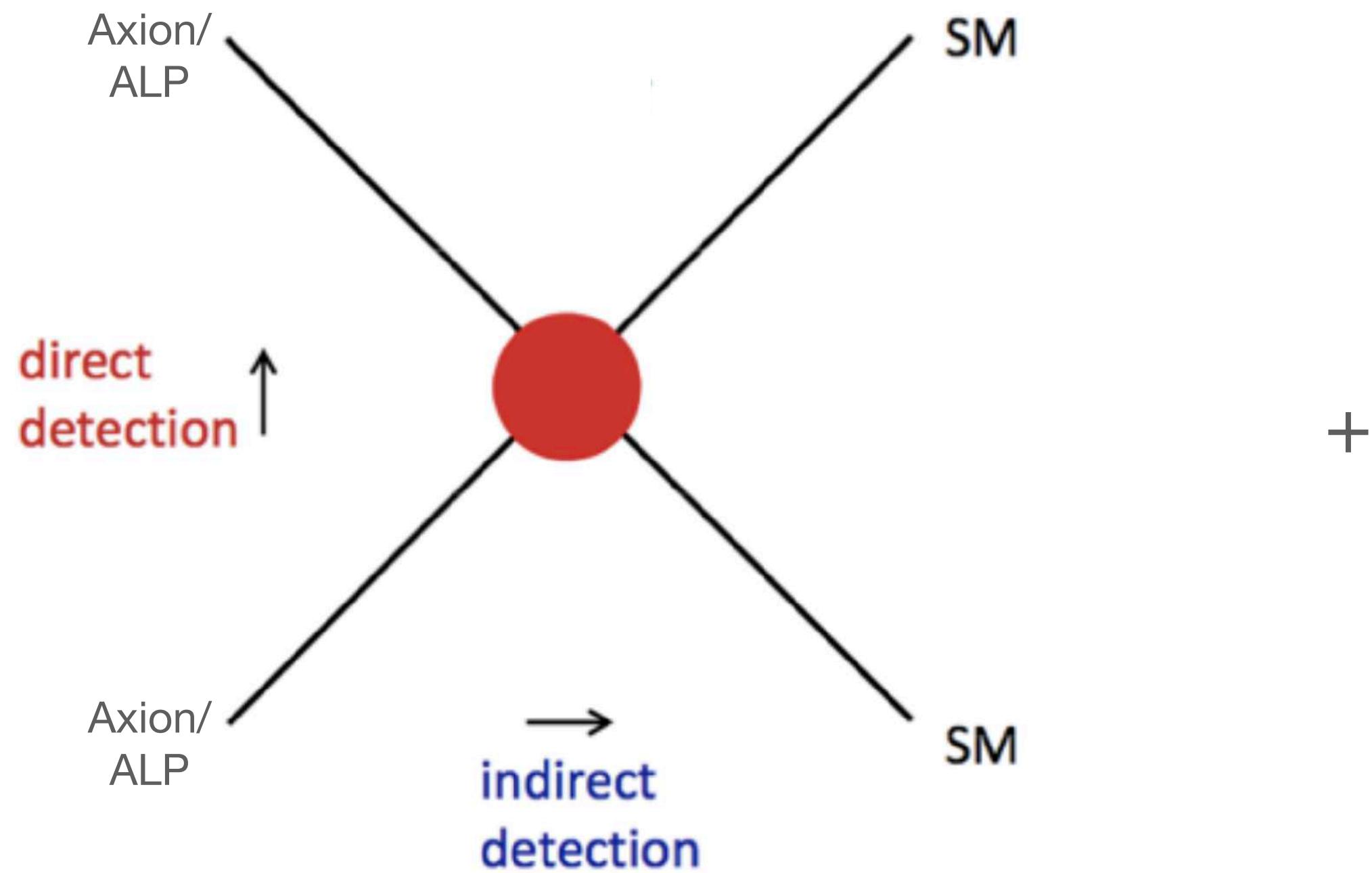
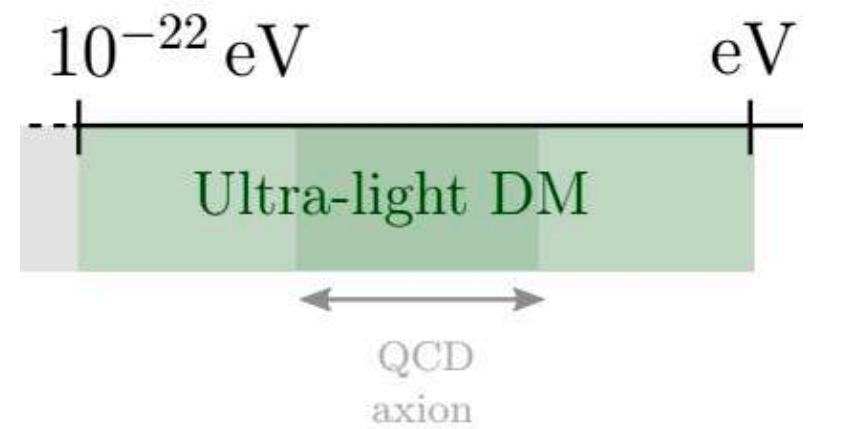
ULDM candidates

Many extensions of the Standard Model predict additional massive bosons

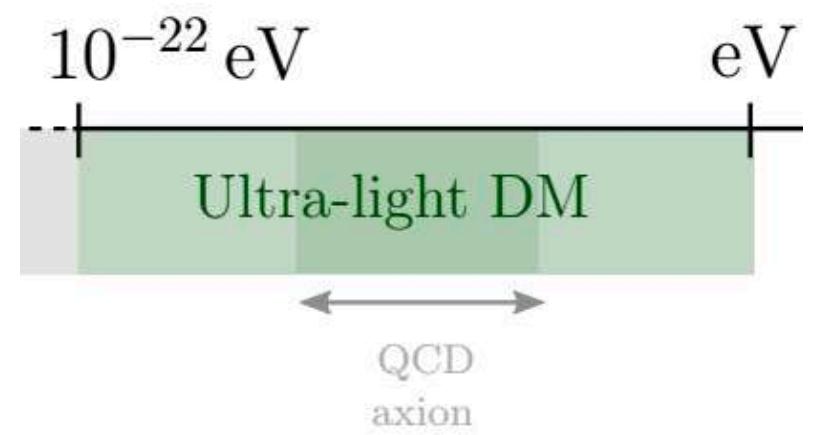


Ref.: Chadha-Day et al 2022

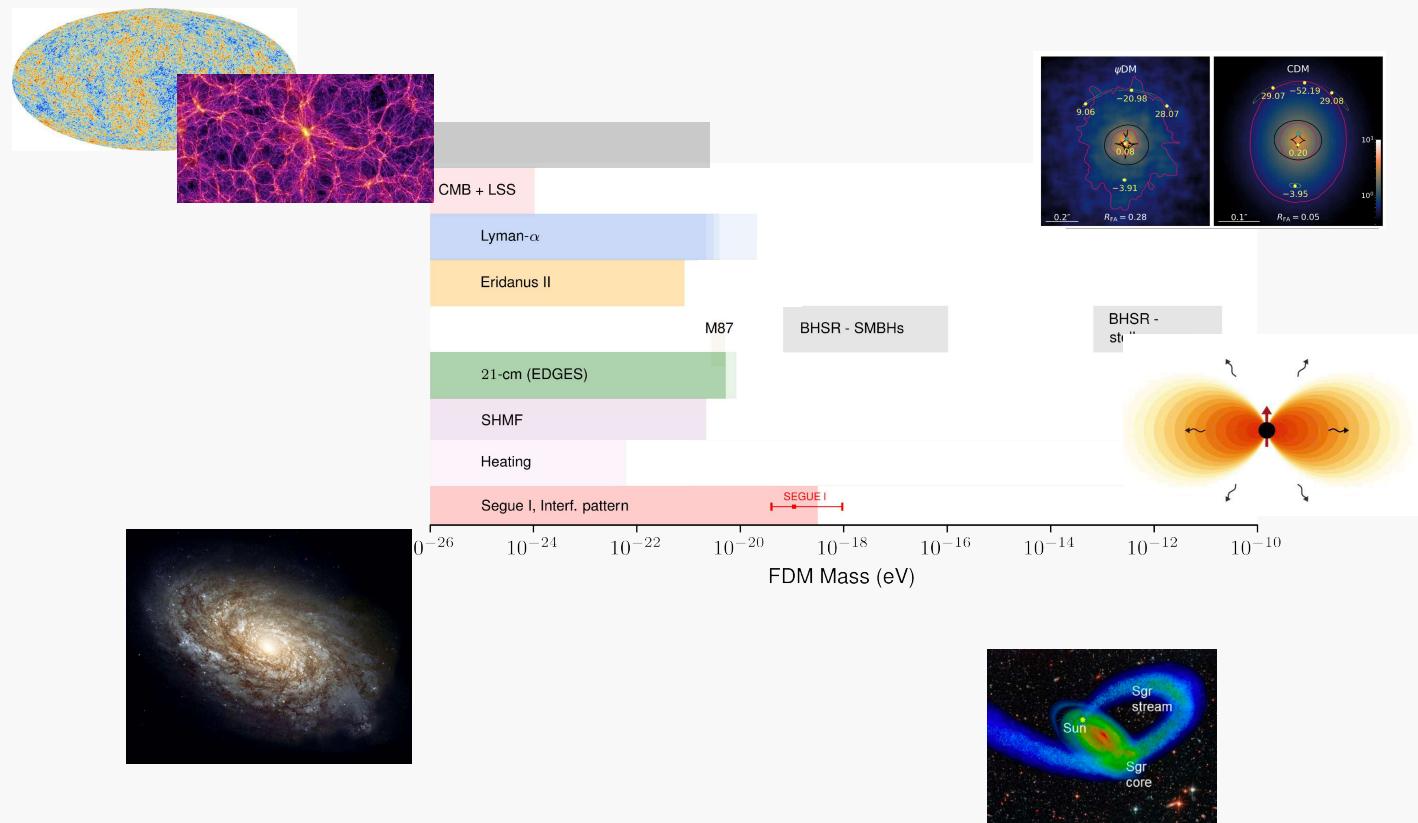
How to search for *ULDM*?



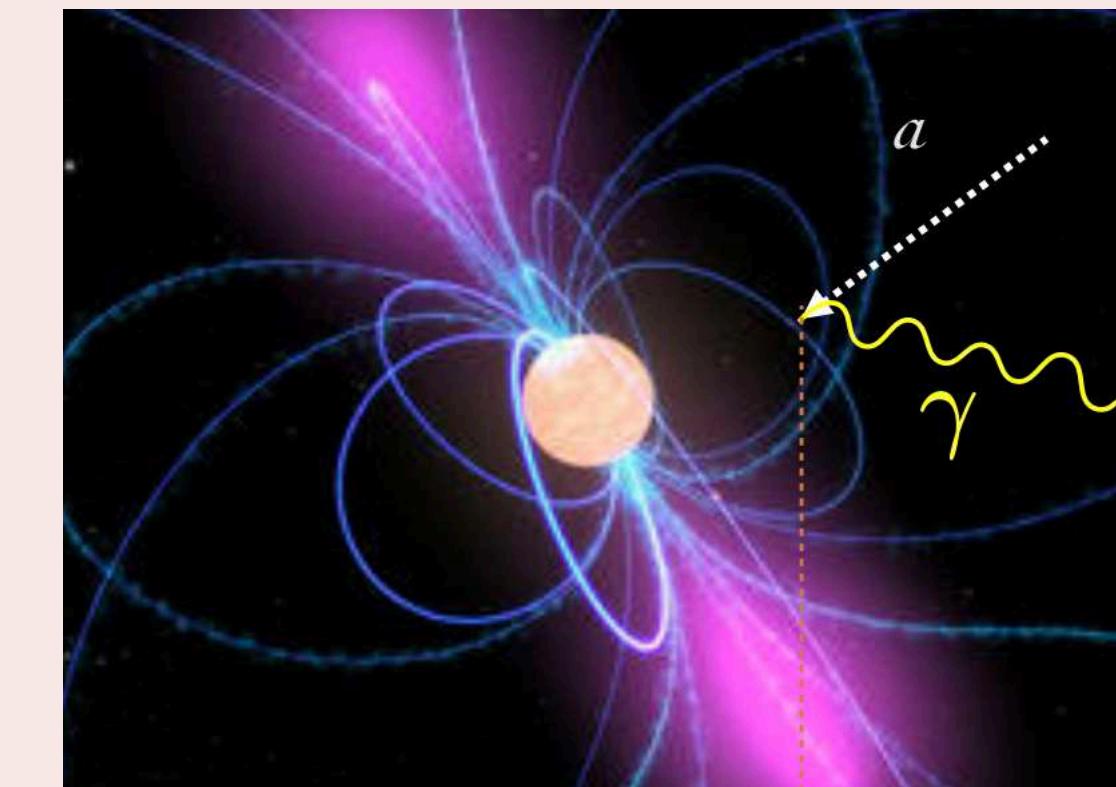
How to search for axions/ALPs?



Cosmological and astrophysical searches

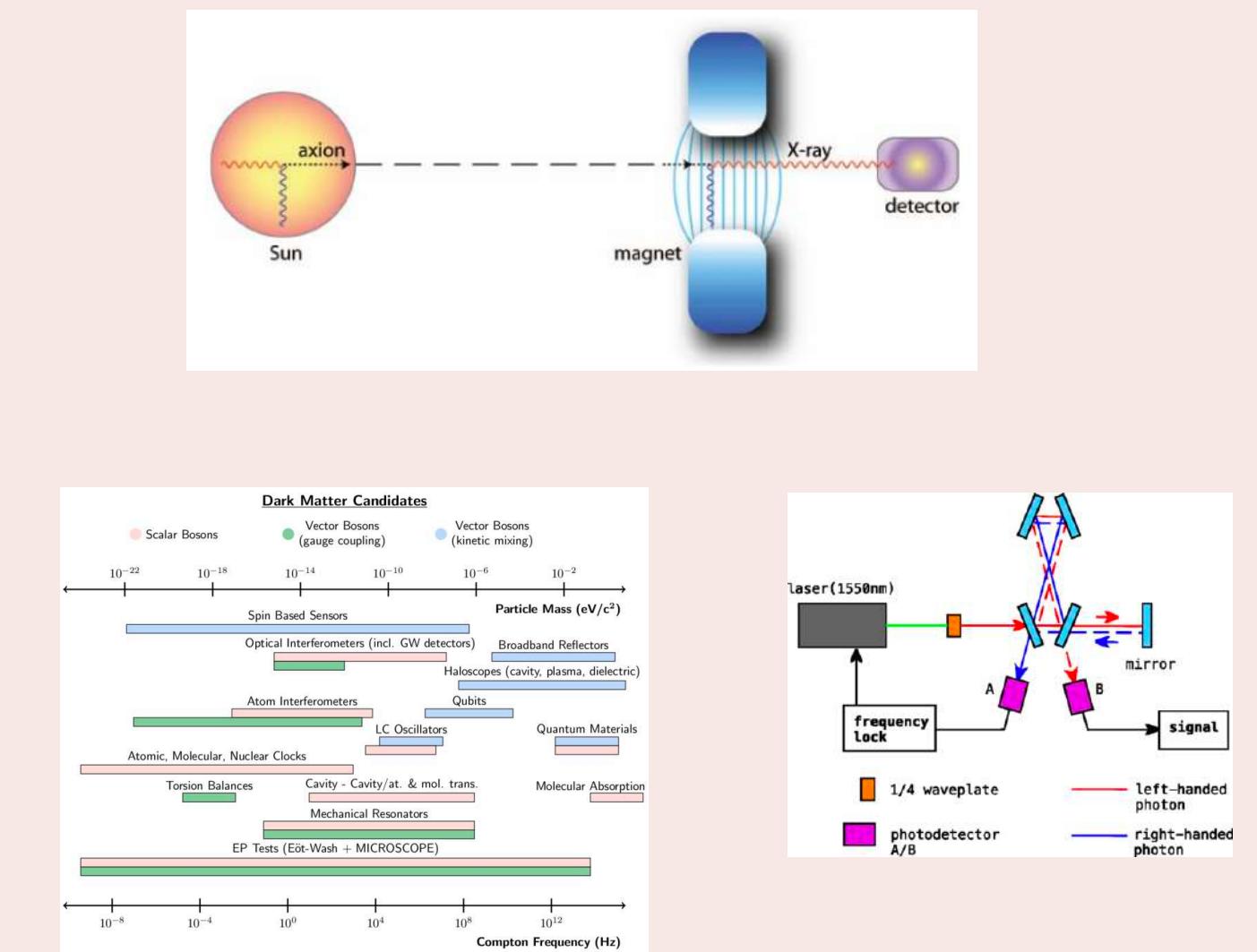


Indirect detection



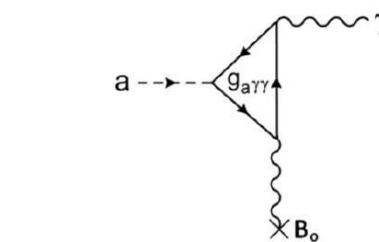
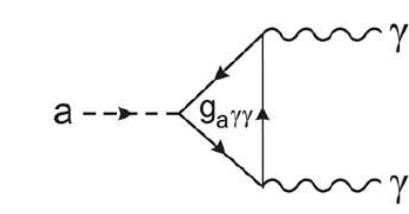
"Direct detection"

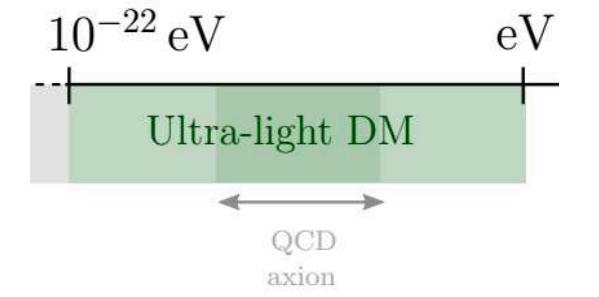
Axion/ALPs experiments



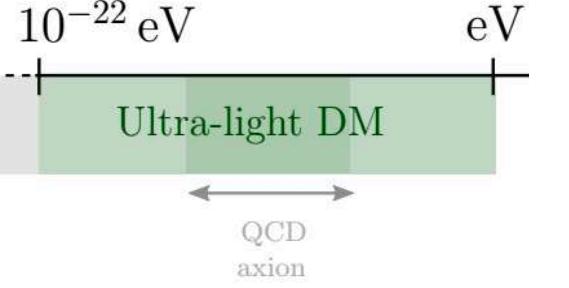
Gravitational

Interactions with the SM





Axion and ALPs interaction with the SM



Axion and ALPs interaction with the SM

Axions and ALPs interact with the standard model particles

$$\boxed{\begin{aligned} F_{\mu\nu} &= \partial_\mu A_\nu - \partial_\nu A_\mu \\ \tilde{F}^{\mu\nu} &= \frac{1}{2}\epsilon^{\mu\nu\alpha\beta}F_{\alpha\beta} \\ \mathbf{E} &= -\nabla A_0 - \dot{\mathbf{A}} \\ \mathbf{B} &= \nabla \times \mathbf{A} \end{aligned}}$$

Minimal definition: New light pseudoscalar, with coupling to photons and/or derivative couplings to fermions

$$\mathcal{L} = \frac{1}{2}(\partial_\mu a)(\partial^\mu a) - \frac{1}{2}m_a^2 a^2 - \frac{g_{a\gamma}}{4}aF_{\mu\nu}\tilde{F}^{\mu\nu} + \partial_\mu a \sum_\psi \frac{g_{a\psi}}{2m_\psi} (\bar{\psi}\gamma^\mu\gamma^5\psi)$$

Not considering here

+ a few model-dependent assumptions

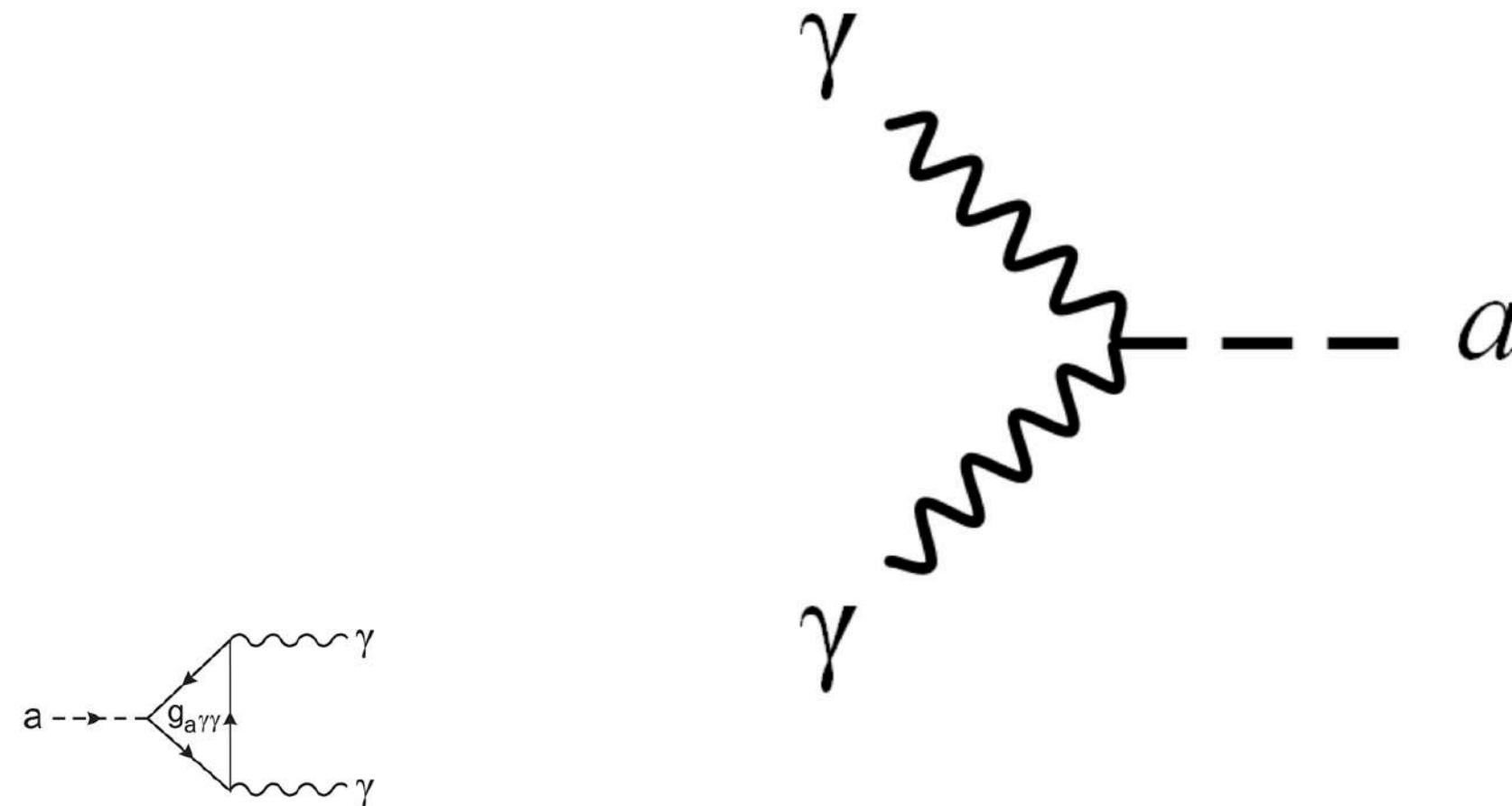
Axion and ALPs interaction with the SM

Axions and ALPs interact with the standard model particles

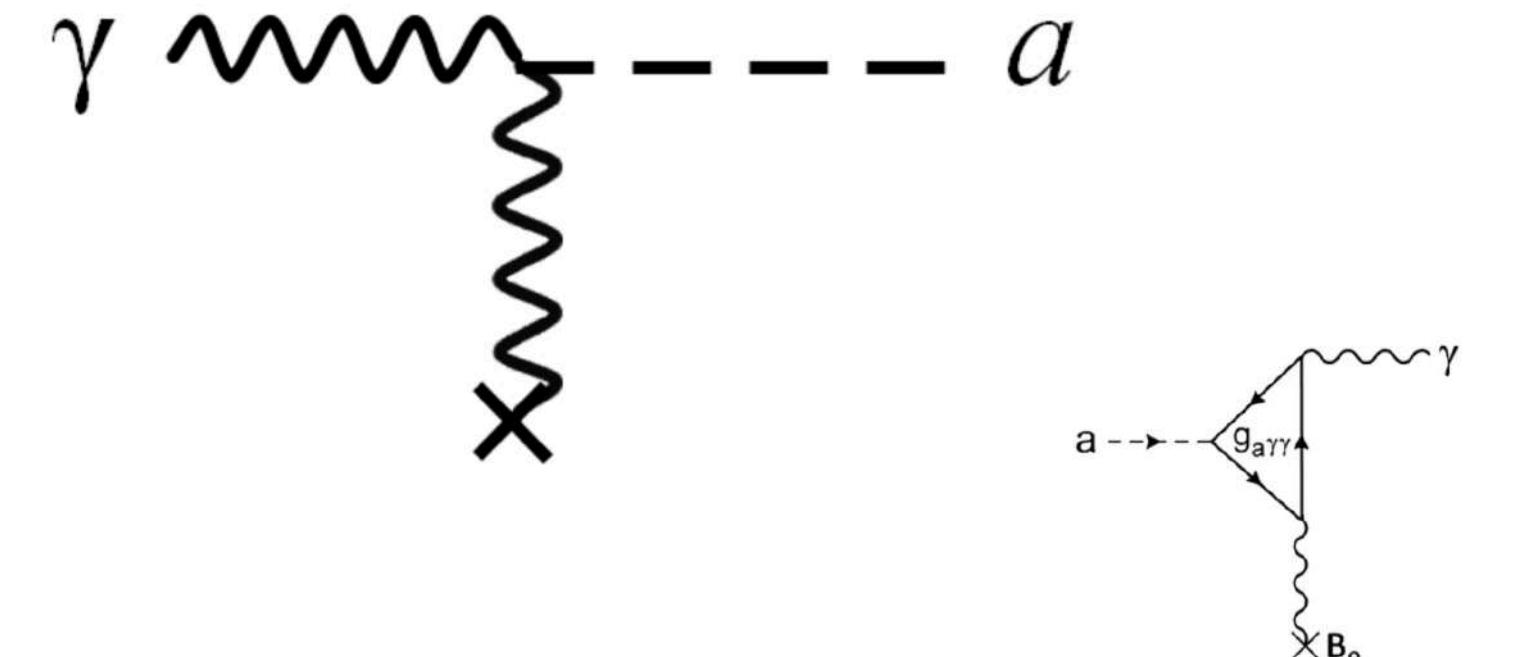
Photon - Axion electrodynamics

$$\boxed{\begin{aligned} F_{\mu\nu} &= \partial_\mu A_\nu - \partial_\nu A_\mu \\ \tilde{F}^{\mu\nu} &= \frac{1}{2}\epsilon^{\mu\nu\alpha\beta}F_{\alpha\beta} \\ \mathbf{E} &= -\nabla A_0 - \dot{\mathbf{A}} \\ \mathbf{B} &= \nabla \times \mathbf{A} \end{aligned}}$$

$$\mathcal{L}_{ALP} = \frac{1}{2}\partial^\mu a\partial_\mu a - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}g_{a\gamma\gamma}F_{\mu\nu}\tilde{F}^{\mu\nu} = \frac{1}{2}\partial^\mu a\partial_\mu a - \frac{1}{2}m_a^2 a^2 + g_{a\gamma\gamma}\mathbf{E} \cdot \mathbf{B} a$$



Photon-photon-ALP vertex with coupling constant $g_{a\gamma\gamma}$



$\gamma \rightarrow a$ conversion in the external magnetic field \mathbf{B}
(Primakoff effect)

Other diagrams...

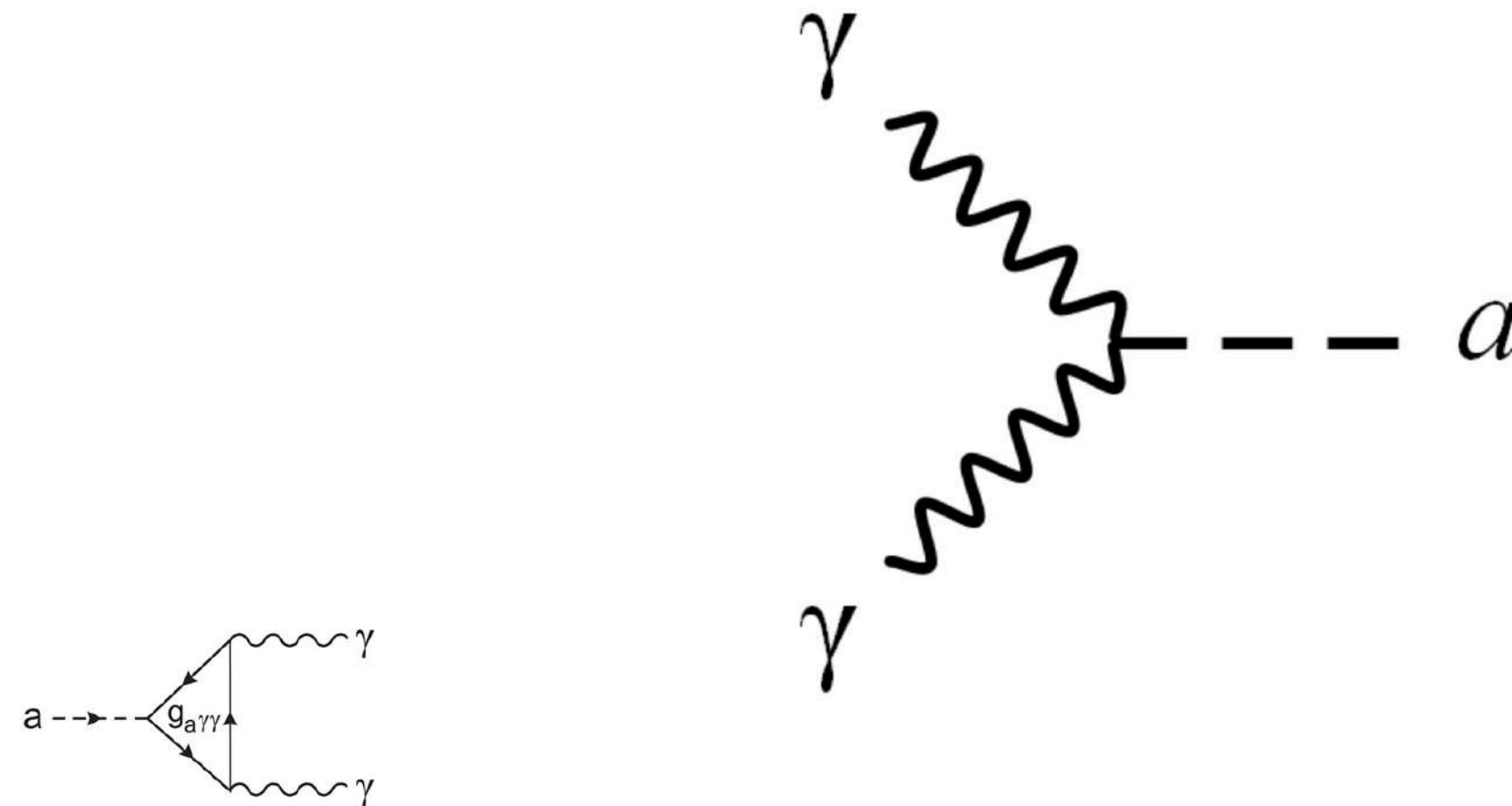
Axion and ALPs interaction with the SM

Axions and ALPs interact with the standard model particles

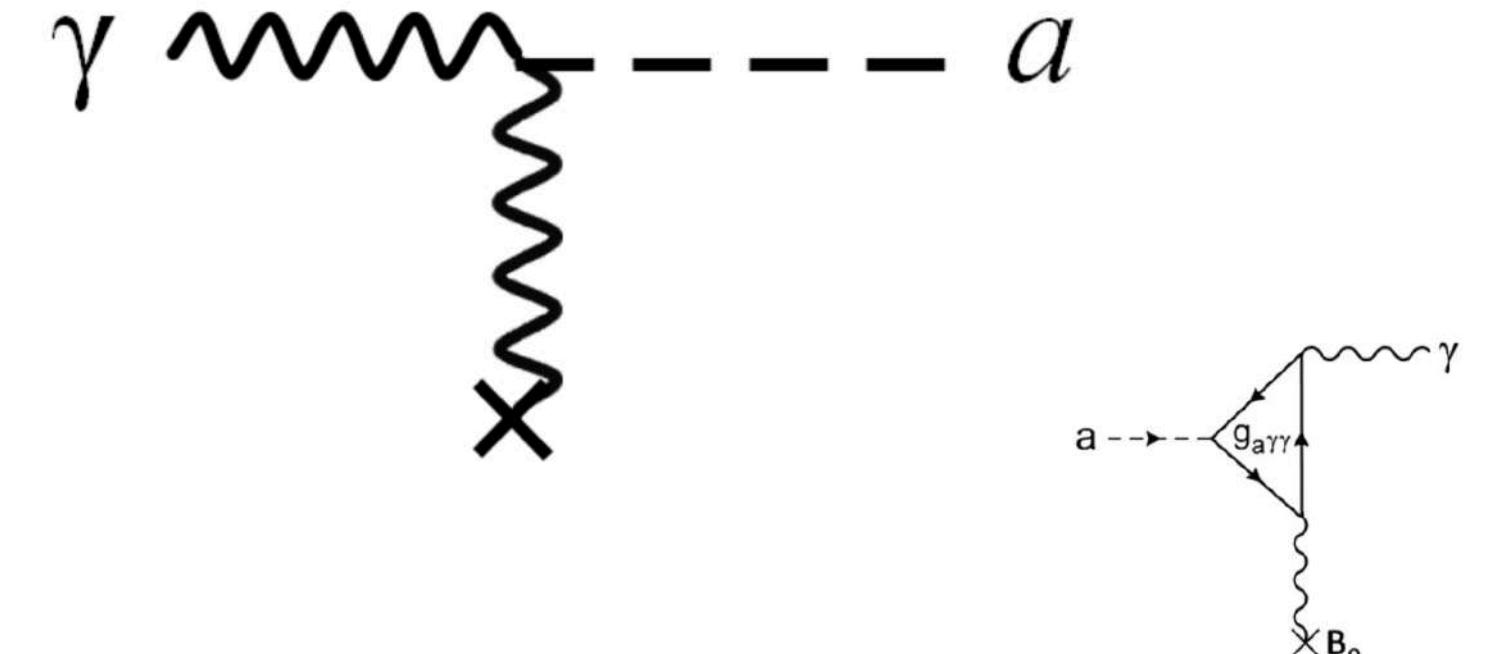
Photon - Axion electrodynamics

$$\boxed{\begin{aligned} F_{\mu\nu} &= \partial_\mu A_\nu - \partial_\nu A_\mu \\ \tilde{F}^{\mu\nu} &= \frac{1}{2}\epsilon^{\mu\nu\alpha\beta}F_{\alpha\beta} \\ \mathbf{E} &= -\nabla A_0 - \dot{\mathbf{A}} \\ \mathbf{B} &= \nabla \times \mathbf{A} \end{aligned}}$$

$$\mathcal{L}_{ALP} = \frac{1}{2}\partial^\mu a\partial_\mu a - \frac{1}{2}m_a^2 a^2 - \frac{1}{4}g_{a\gamma\gamma}F_{\mu\nu}\tilde{F}^{\mu\nu} = \frac{1}{2}\partial^\mu a\partial_\mu a - \frac{1}{2}m_a^2 a^2 + g_{a\gamma\gamma}\mathbf{E} \cdot \mathbf{B} a$$



Photon-photon-ALP vertex with coupling constant $g_{a\gamma\gamma}$



$\gamma \rightarrow a$ conversion in the external magnetic field \mathbf{B}
(Primakoff effect)

Other diagrams...

Axion and ALPs interaction with the SM

Axions and ALPs interact with the standard model particles

Axion electrodynamics

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - J^\mu A_\mu - \frac{g_{a\gamma}}{4}F_{\mu\nu}\tilde{F}^{\mu\nu}a$$

- We can interpret axion as the source of an effective current:

| |
|---|
| $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$ $\tilde{F}^{\mu\nu} = \frac{1}{2}\epsilon^{\mu\nu\alpha\beta}F_{\alpha\beta}$ $\mathbf{E} = -\nabla A_0 - \dot{\mathbf{A}}$ $\mathbf{B} = \nabla \times \mathbf{A}$ |
|---|

$$\partial_\mu F^{\mu\nu} = J^\nu - \underbrace{g_{a\gamma}\tilde{F}_{\mu\nu}\partial_\mu a}_{} \downarrow \\ J_a^\mu = g_{a\gamma}(-\mathbf{B} \cdot \nabla a, -\mathbf{E} \times \nabla a + \partial_t a \mathbf{B})$$

Maxwell's equations:

$$\nabla \cdot \mathbf{E} = \rho$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{B} = \frac{\partial \mathbf{E}}{\partial t} + \mathbf{J}$$

Extended Maxwell's equations:

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma} \mathbf{B} \cdot \nabla a$$

$$\nabla \cdot \mathbf{B} = 0$$

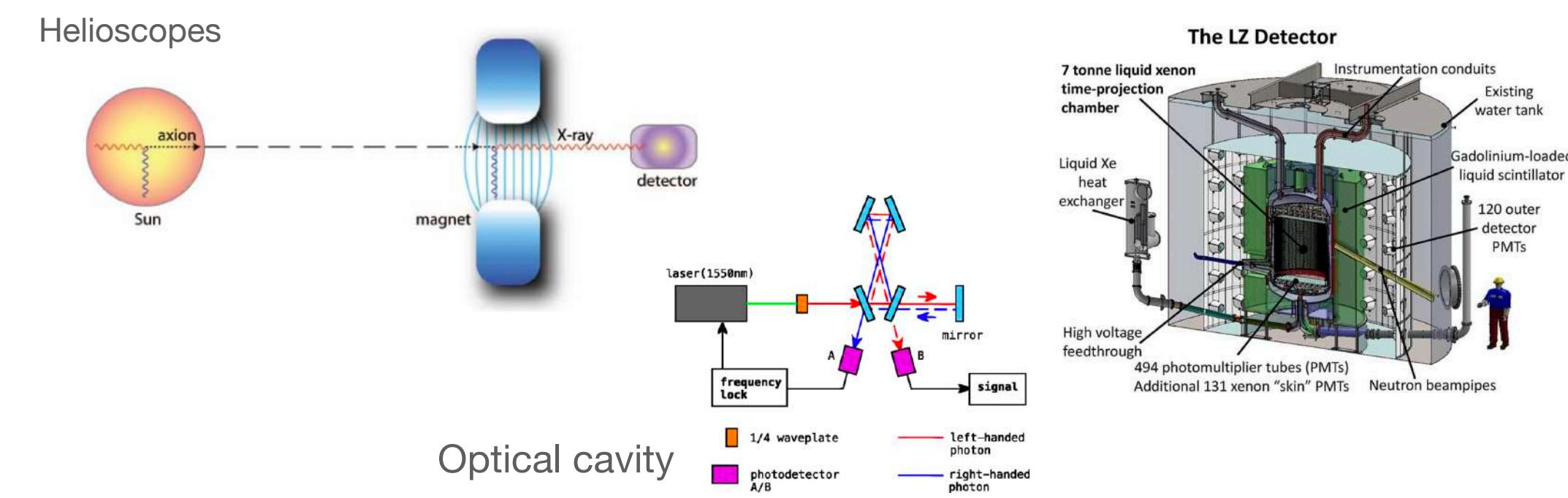
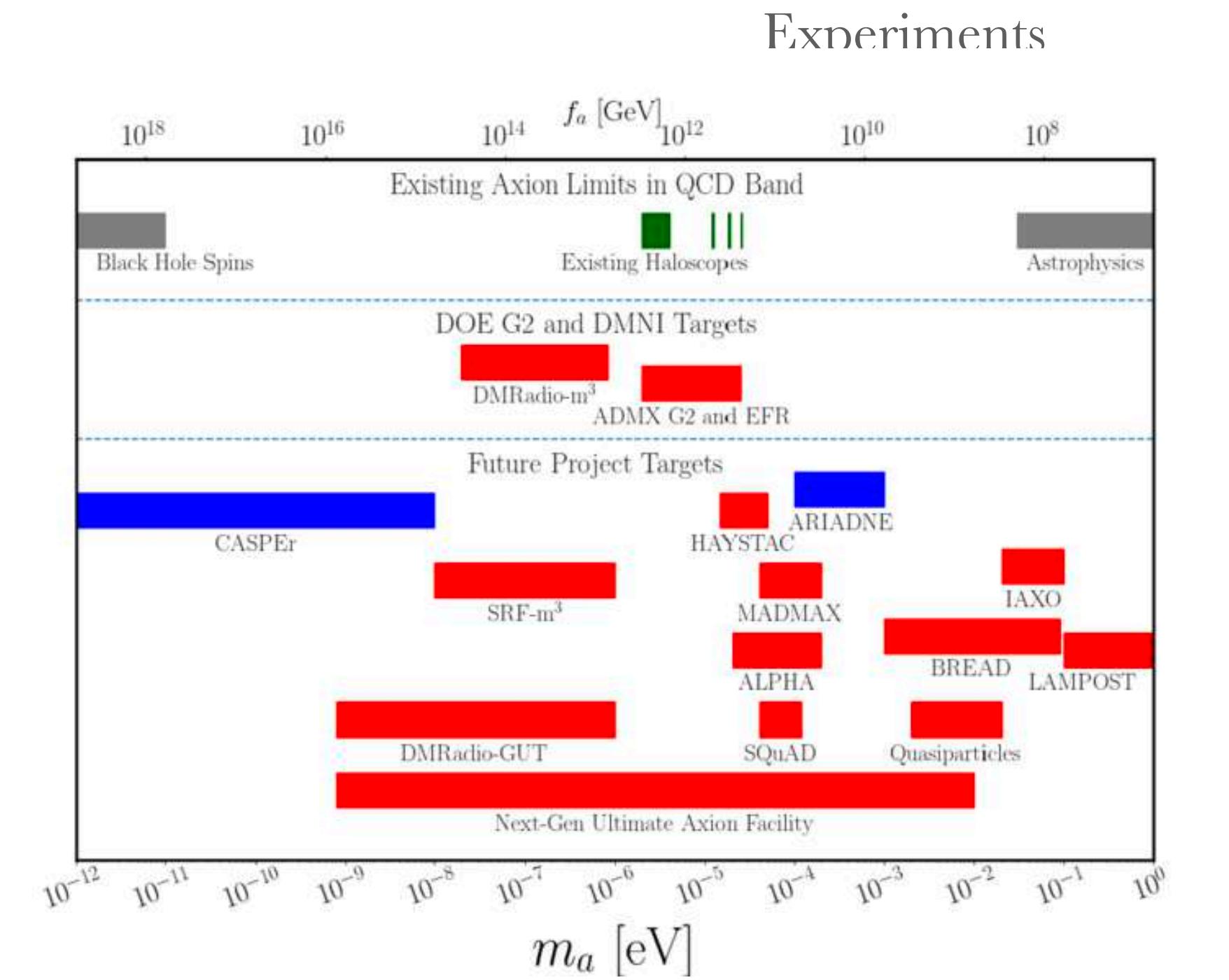
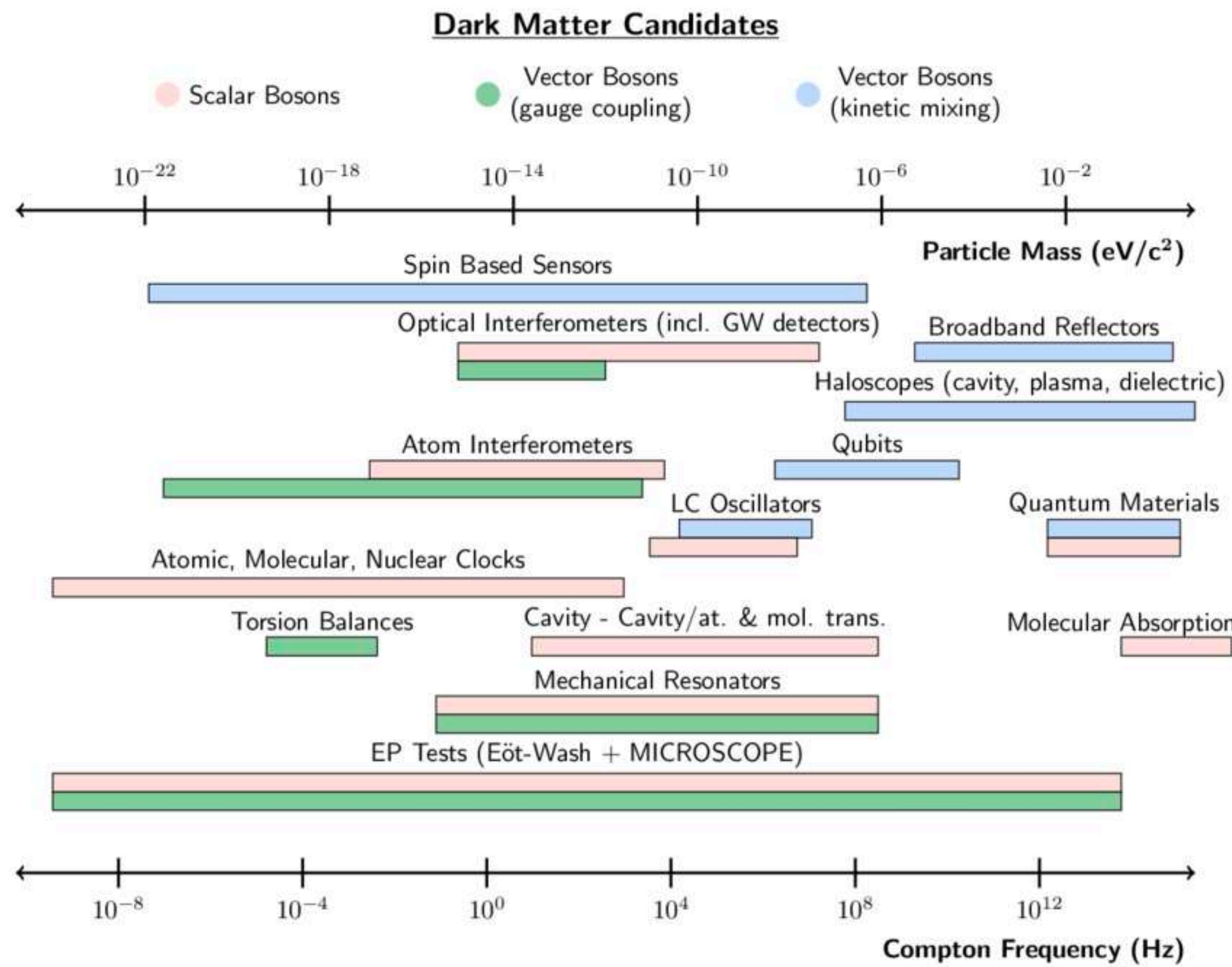
$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{B} = \frac{\partial \mathbf{E}}{\partial t} + \mathbf{J} - g_{a\gamma} \left(\mathbf{E} \times \nabla a - \frac{\partial a}{\partial t} \mathbf{B} \right)$$

Axion and ALPs interaction with the SM

"Direct Detection": axion/ALPs experiments

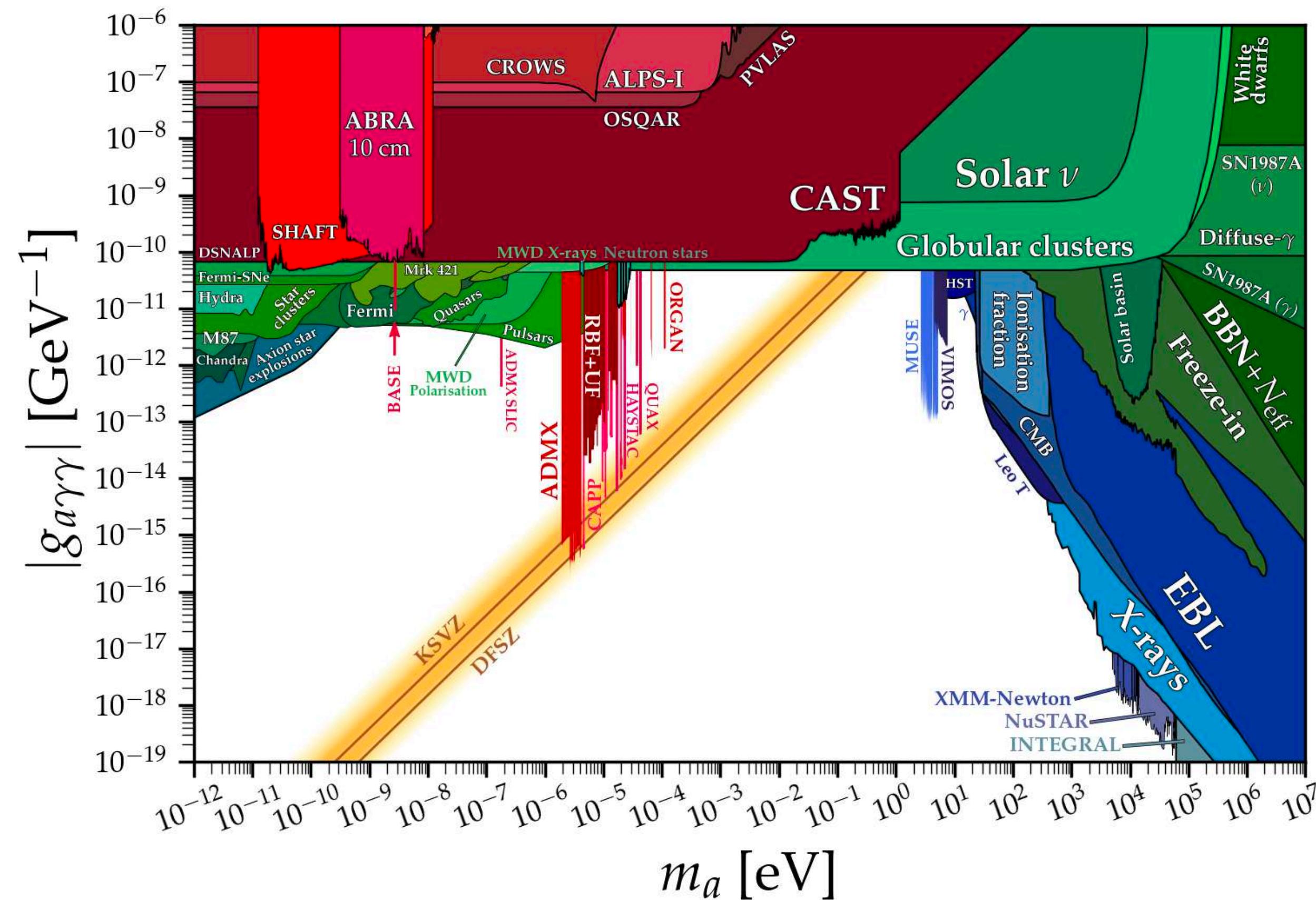
Overview of experimental techniques and the mass ranges they target



Axion and ALPs interaction with the SM

Bounds on Axion-photon coupling

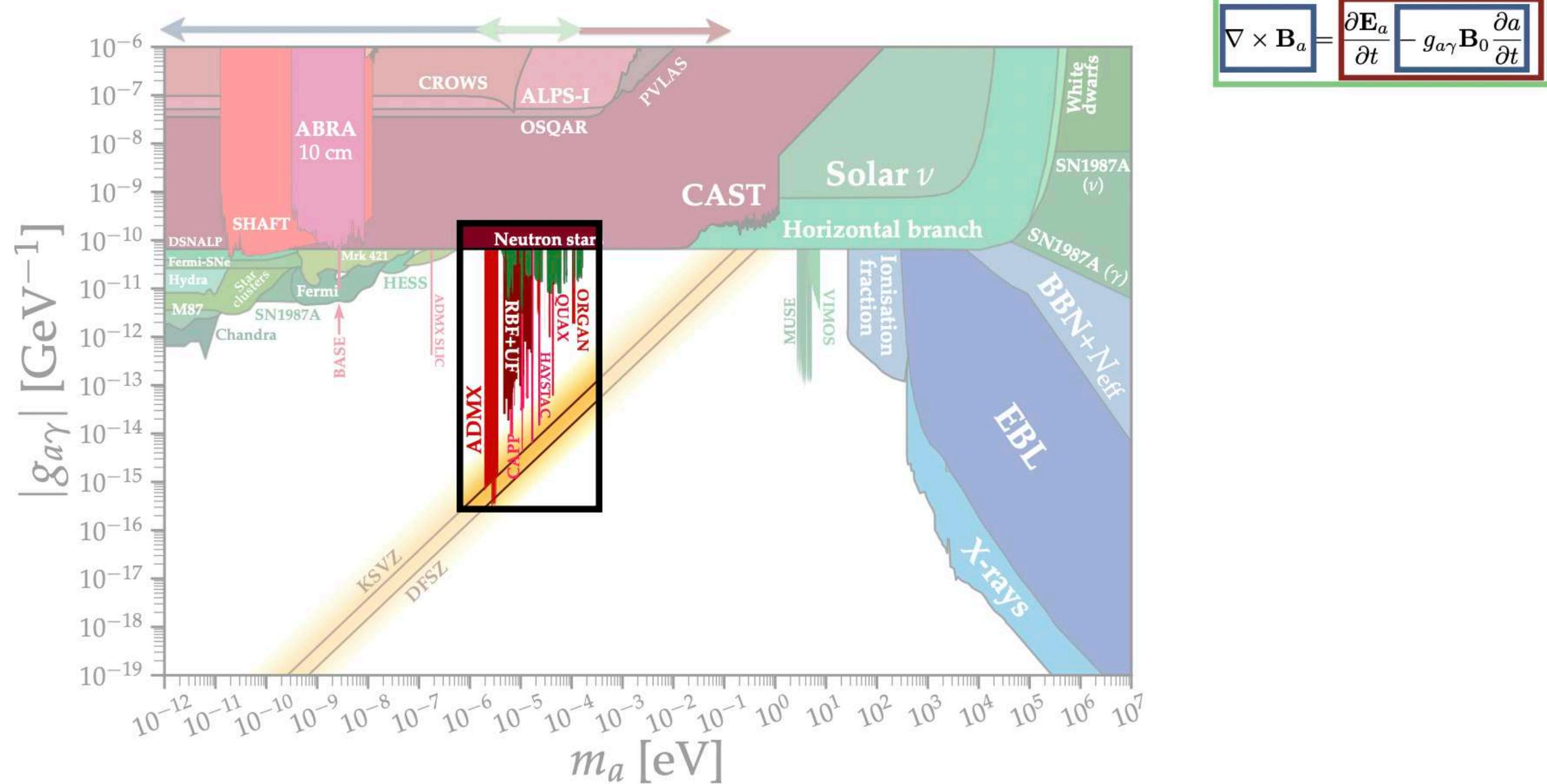
Includes direct and indirect detection



Website with up-to-date with axion/ALP bounds: <https://cajohare.github.io/AxionLimits>

Axion and ALPs interaction with the SM

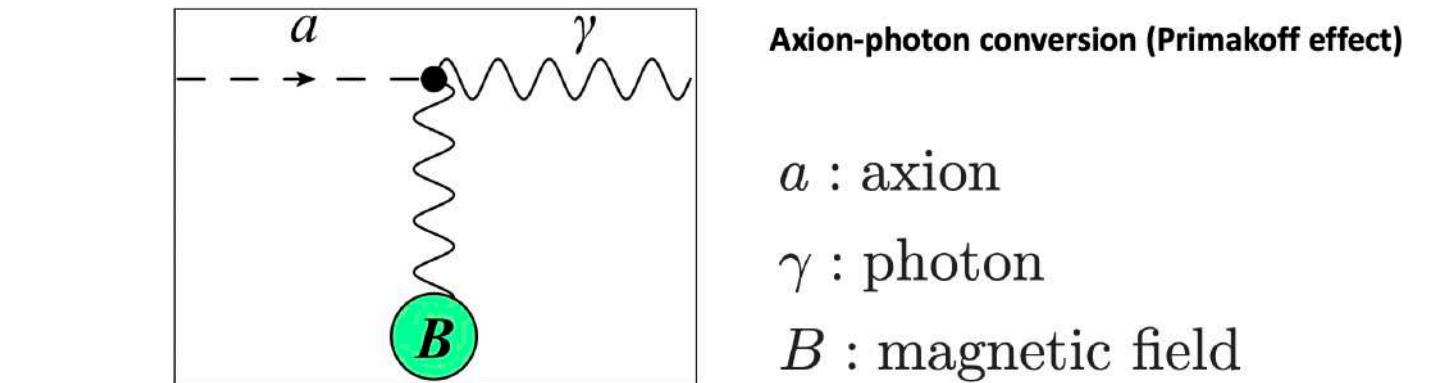
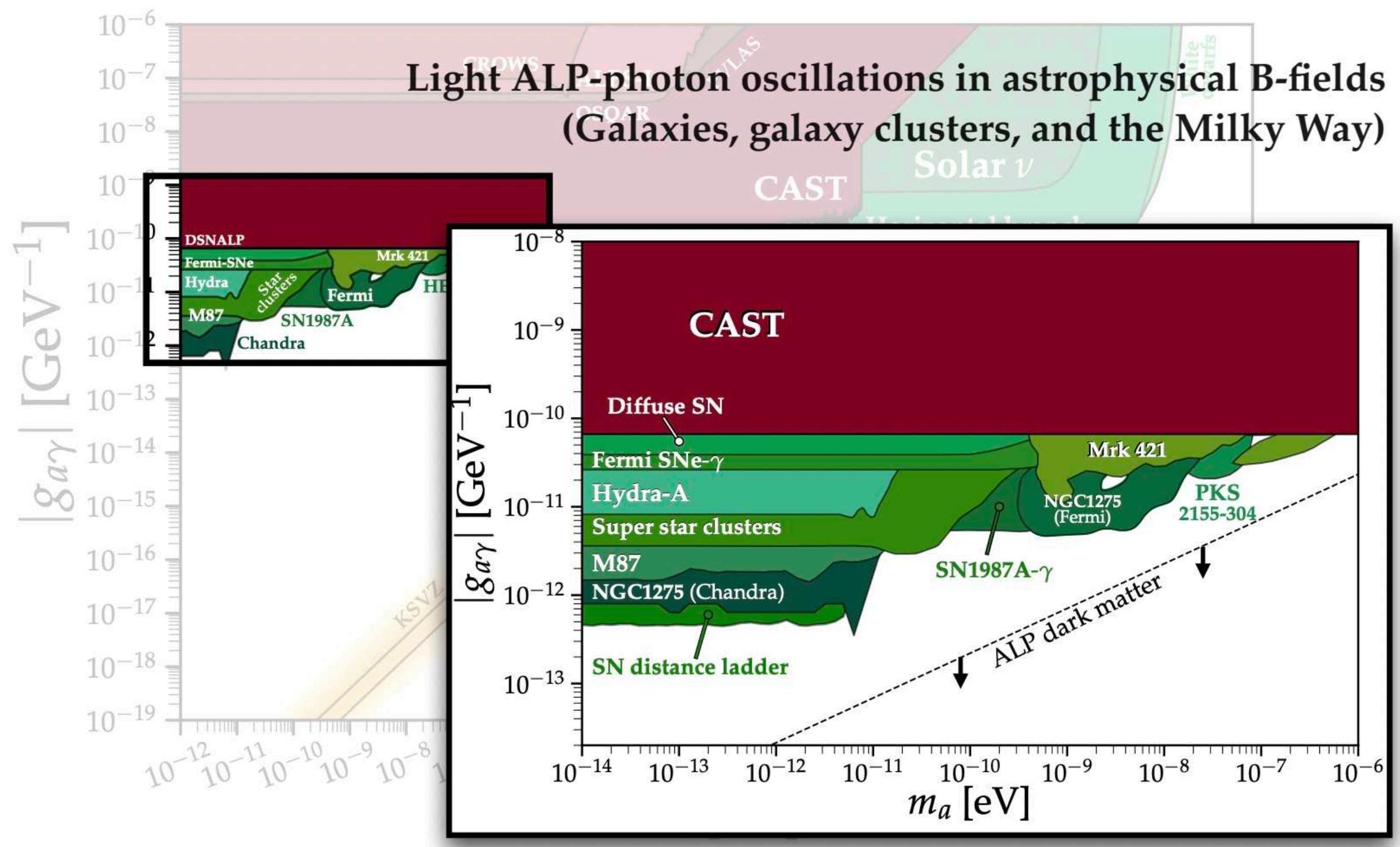
Bounds on Axion-photon coupling



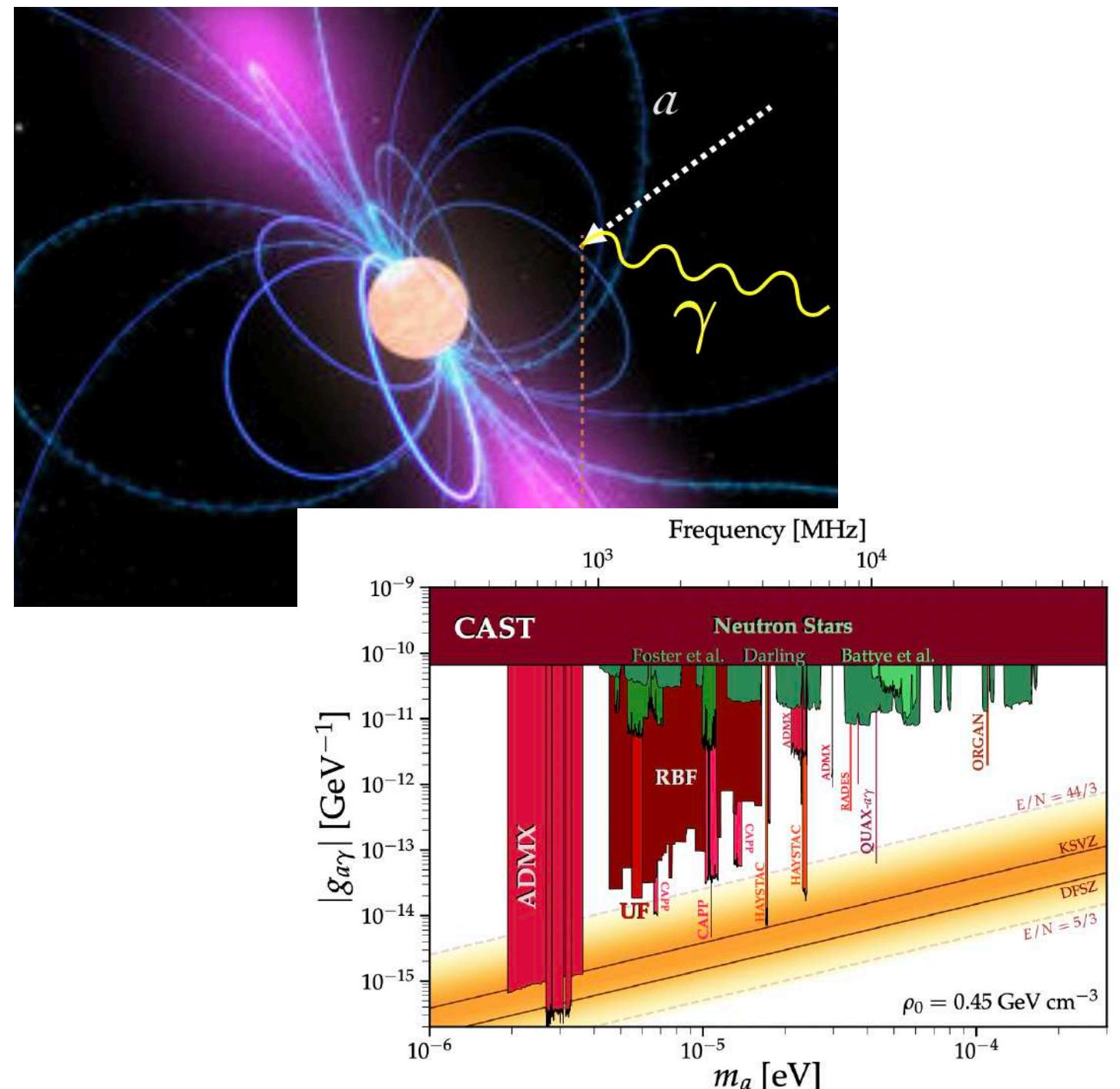
Axion and ALPs interaction with the SM

Indirect Detection

In astrophysical systems



DM axions in neutron star magnetospheres

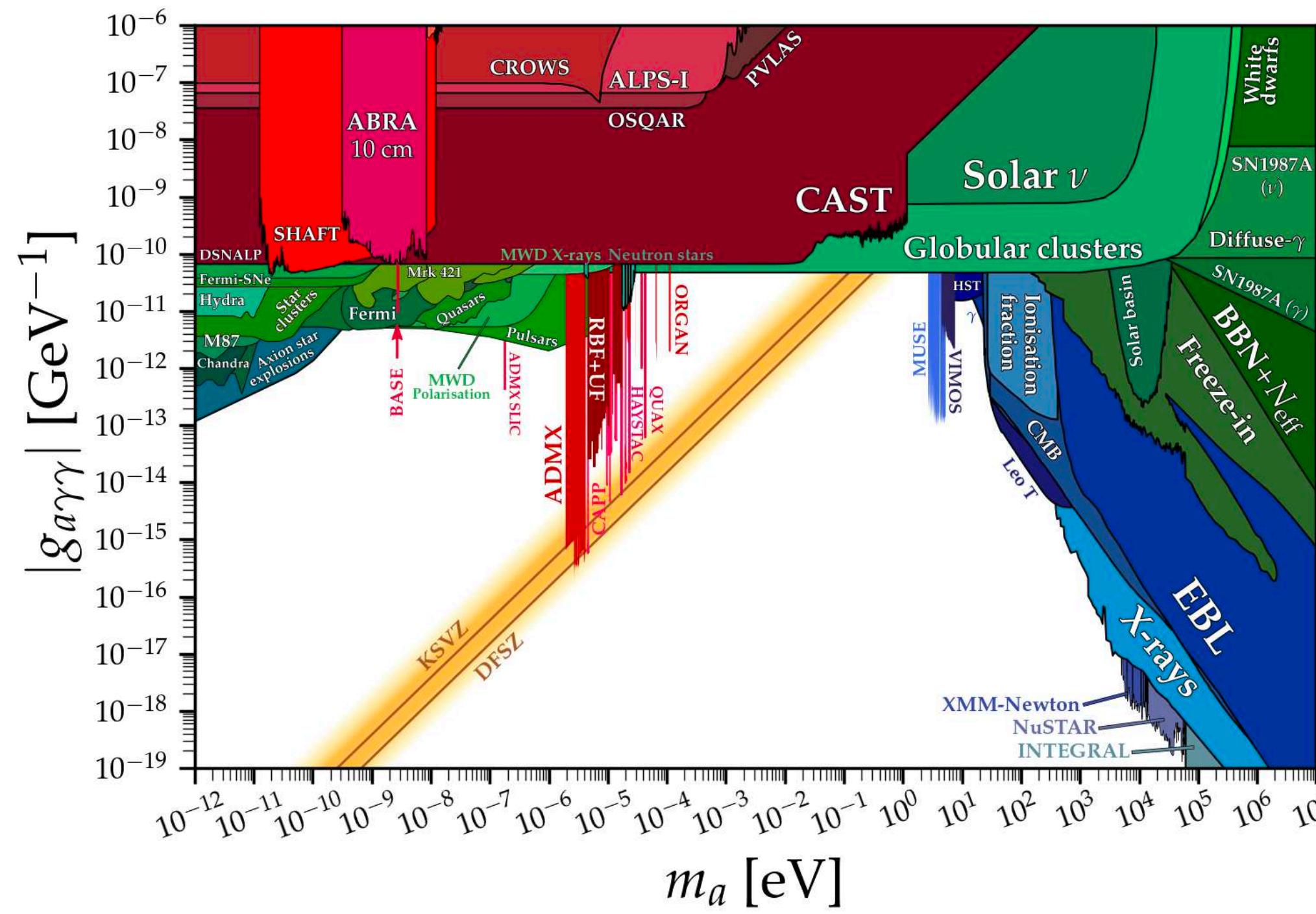


Axion and ALPs interaction with the SM

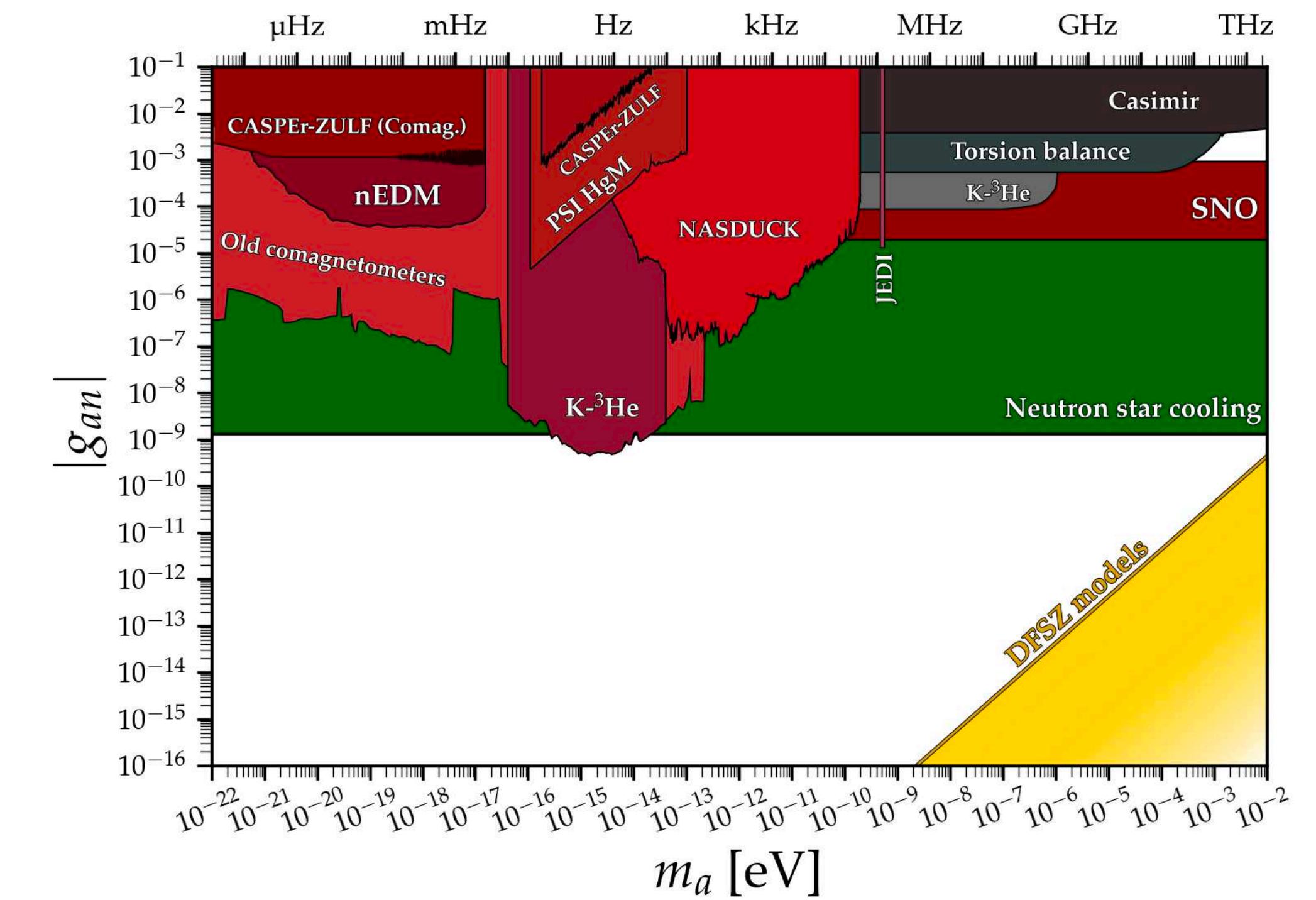
Bounds

Includes direct and indirect detection

Axion-electron coupling



Axion-neutron coupling



+ many more: axion-proton, dark photon, ...

Website with up-to-date with axion/ALP bounds: <https://cajohare.github.io/AxionLimits>
(Includes notebooks)

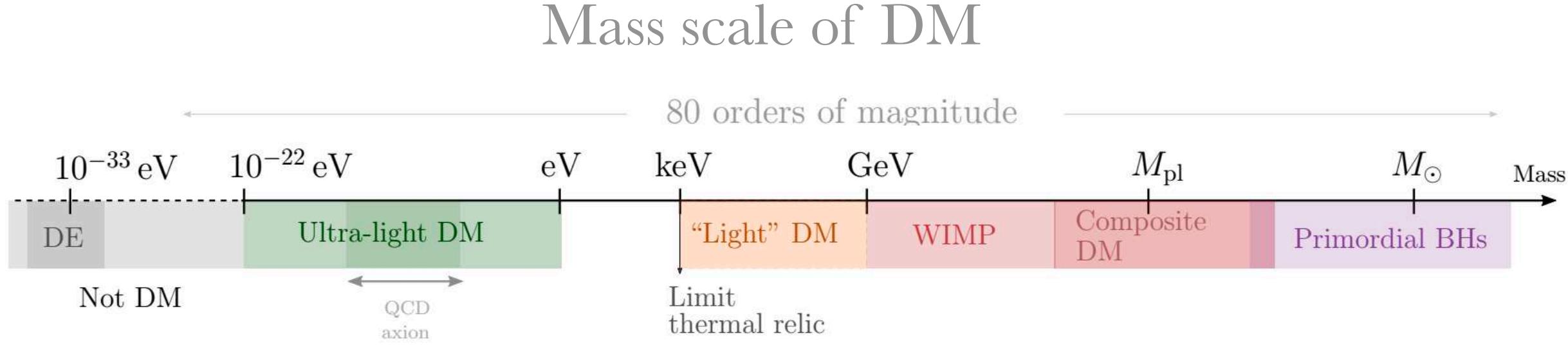
Summary

DM builder's guide

What we learned from observations

- **Cold or warm** Thermal candidate: $m_{dm} \geq \text{keV}$
Or produced cold by a non-thermal mechanism
- **Reproduce large and small scale distribution**
Clusters like CDM on large scales $k \lesssim 10 \text{ Mpc}^{-1}$
Clustering on scales smaller than $k \gtrsim 10 \text{ Mpc}^{-1}$ highly unconstrained
- **Non-interacting or weakly interacting**
Can have a small electromagnetic interaction. Bound < **milicharge**
Can have a small **self interaction**.
Can interact via the **weak force**
- **Abundance** $\Omega_m = 0.308 \pm 0.012$ (Planck 2018)
- **Stable**

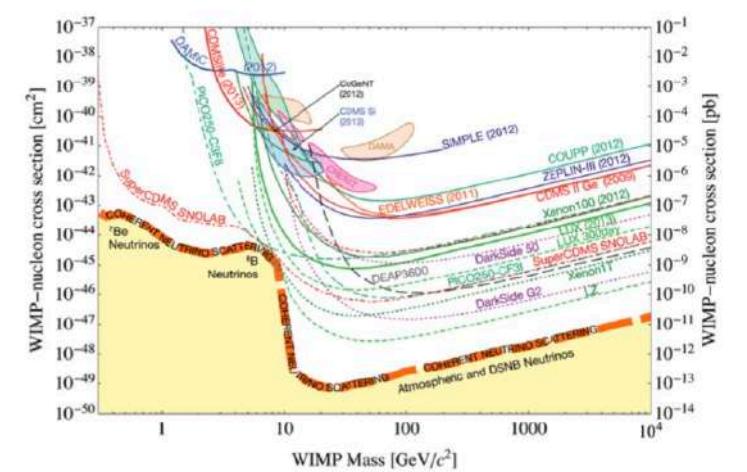
DE



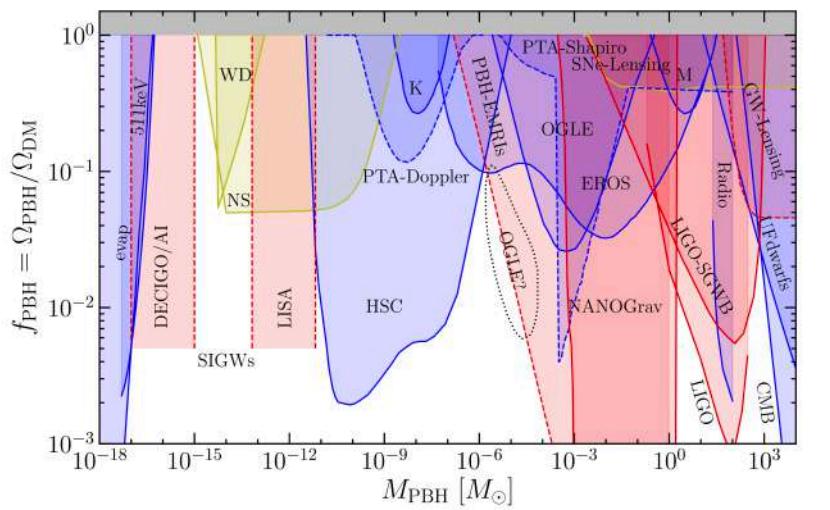
DM Landscape

Search for DM

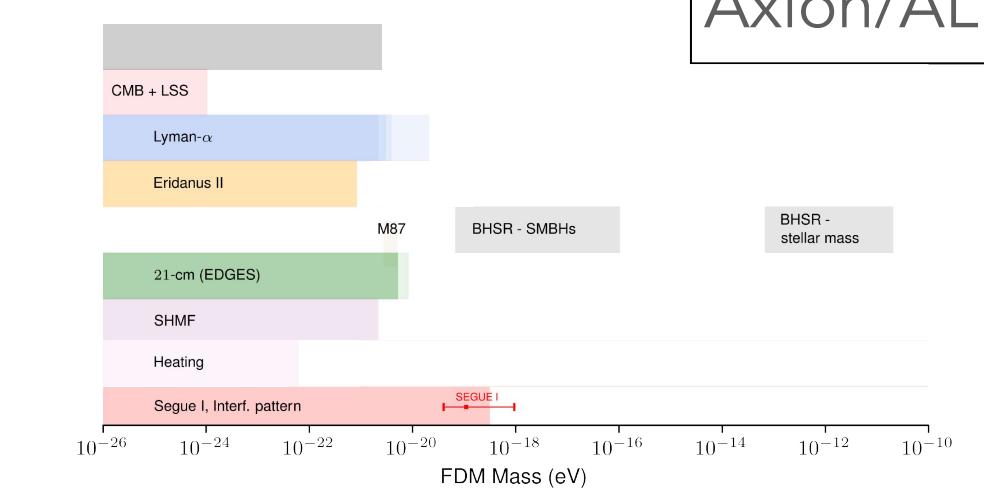
WIMPS



PBHs



Axion/ALP





Thank you very much!

EXTRA slides

EXTRA slides

FDM simulation

Spectral technique to solve the SP system

$$i\hbar\partial_t\psi_c(t, \mathbf{x}) = -\frac{\hbar^2}{2m a(t)^2} \nabla_c^2 \psi_c(t, \mathbf{x}) + \frac{m}{a(t)} \Phi_c \psi_c(t, \mathbf{x})$$

$$\nabla_c^2 \Phi_c(t, \mathbf{x}) = 4\pi G m \left(|\psi_c(t, \mathbf{x})|^2 - \langle |\psi_c|^2 \rangle(t) \right)$$

Time evolution of the wave function

$$\Psi(\mathbf{x}, t + \Delta t) = T \exp \left[-\frac{i\Delta t}{\hbar} \int dt' \left(-\frac{\hbar^2}{2m} \nabla^2 + mV(\mathbf{x}, t') \right) \right] \Psi(\mathbf{x}, t)$$

Small Δt :

$$\Psi(\mathbf{x}, t + \Delta t) = \exp \left(\frac{i\hbar\Delta t}{2m} \nabla^2 - \frac{im\Delta t}{2\hbar} V(\mathbf{x}, t + \Delta t) - \frac{im\Delta t}{2\hbar} V(\mathbf{x}, t) \right) \Psi(\mathbf{x}, t),$$

Split into 3 operations (Baker-Campbell-Haussdorff formula)

$$\Psi(\mathbf{x}, t + \Delta t) = \exp \left(-\frac{im\Delta t}{2\hbar} V(\mathbf{x}, t + \Delta t) \right) \exp \left(\frac{i\hbar\Delta t}{2m} \nabla^2 \right) \exp \left(-\frac{im\Delta t}{2\hbar} V(\mathbf{x}, t) \right) \Psi(\mathbf{x}, t)$$

Operator Splitting Spectral Method

$$\psi_c^{n+1} \approx e^{i\Phi_c \Delta t / 2} \mathcal{F}^{-1} \left[e^{ik^2 \Delta t} \mathcal{F}^{-1} \left[e^{i\Phi_c \Delta t / 2} \psi_c^n \right] \right]$$

3rd

2nd

1st

$$\Delta t \sim \Delta x^2$$

Timestep criteria

FDM simulation

Spectral technique to solve the SP system

$$i\hbar\partial_t\psi_c(t, \mathbf{x}) = -\frac{\hbar^2}{2m a(t)^2} \nabla_c^2 \psi_c(t, \mathbf{x}) + \frac{m}{a(t)} \Phi_c \psi_c(t, \mathbf{x})$$
$$\nabla_c^2 \Phi_c(t, \mathbf{x}) = 4\pi G m \left(|\psi_c(t, \mathbf{x})|^2 - \langle |\psi_c|^2 \rangle(t) \right)$$

Operator Splitting Spectral Method

$$\psi_c^{n+1} \approx e^{i\Phi_c \Delta t / 2} \mathcal{F}^{-1} \left[e^{ik^2 \Delta t} \mathcal{F}^{-1} \left[e^{i\Phi_c \Delta t / 2} \psi_c^n \right] \right]$$


$$\Delta t \sim \Delta x^2$$

Timestep criteria

FDM simulation

The fields ψ and Φ are discretised on a uniform Cartesian mesh with N^3 grid points - allow numerical computations using Fast Fourier transform. It follows the operations:

- Calculate the potential

$$\bullet \quad \psi_c \leftarrow e^{-i\frac{m}{\hbar} \frac{1}{a} \frac{\Delta t}{2} \Phi_c} \psi_c \quad (\text{kick}) \quad (20a)$$

$$\bullet \quad \psi_c \leftarrow \text{FFT}^{-1} \left(e^{-i\frac{\hbar}{m} \frac{1}{a^2} \frac{\Delta t}{2} k^2} \text{FFT}(\psi_c) \right) \quad (\text{drift}) \quad (20b)$$

$$\bullet \quad \Phi_c \leftarrow \text{FFT}^{-1} \left(-\frac{1}{k^2} \text{FFT} \left(4\pi G m \left(|\psi_c|^2 - \langle |\psi_c|^2 \rangle \right) \right) \right) \quad (\text{update potential}) \quad (20c)$$

$$\bullet \quad \psi_c \leftarrow e^{-i\frac{m}{\hbar} \frac{1}{a} \frac{\Delta t}{2} \Phi_c} \psi_c \quad (\text{kick}) \quad (20d)$$

$$\bullet \quad \text{Go to step (20a)} \quad (20e)$$

Schrödinger-Poisson system

$$i\hbar \partial_t \psi_c(t, \mathbf{x}) = -\frac{\hbar^2}{2m a(t)^2} \nabla_c^2 \psi_c(t, \mathbf{x}) + \frac{m}{a(t)} \Phi_c \psi_c(t, \mathbf{x})$$

$$\nabla_c^2 \Phi_c(t, \mathbf{x}) = 4\pi G m \left(|\psi_c(t, \mathbf{x})|^2 - \langle |\psi_c|^2 \rangle(t) \right)$$

May et al. 2020

Steps (20a) to (20e) implemented as a module in the AREPO code

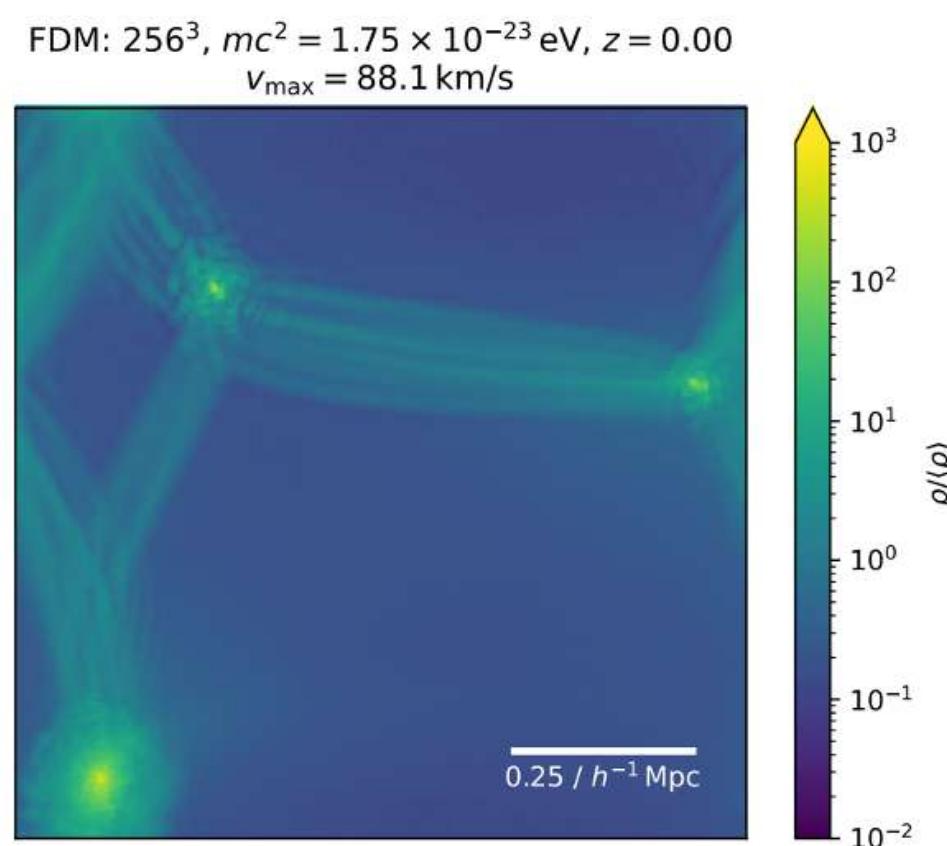
Jowett

Own implementation

FDM simulation

May et al 2020: Box size and resolution

Largest three-dimensional cosmological simulations of FDM structure formation to low redshifts



Simulations: $\{\Omega_m = 0.3, \Omega_b = 0, \Omega_\Lambda = 0.7, H_0 = 70 \text{ km s}^{-1} (h = 0.7), \sigma_8 = 0.9\}$

IC: $z = 127$

| Type | Res. el. | $L / h^{-1} \text{ Mpc}$ | mc^2 / eV | Resolution |
|------|----------|--------------------------|----------------------------|-----------------------------------|
| FDM | 8640^3 | 10 | 7×10^{-23} | $1.16 h^{-1} \text{ kpc}$ |
| FDM | 4320^3 | 10 | $(3.5, 7) \times 10^{-23}$ | $2.31 h^{-1} \text{ kpc}$ |
| FDM | 3072^3 | 10 | $(3.5, 7) \times 10^{-23}$ | $3.26 h^{-1} \text{ kpc}$ |
| FDM | 2048^3 | 10 | $(3.5, 7) \times 10^{-23}$ | $4.88 h^{-1} \text{ kpc}$ |
| FDM | 4320^3 | 5 | 7×10^{-23} | $1.16 h^{-1} \text{ kpc}$ |
| FDM | 3072^3 | 5 | $(3.5, 7) \times 10^{-23}$ | $1.63 h^{-1} \text{ kpc}$ |
| FDM | 2048^3 | 5 | $(3.5, 7) \times 10^{-23}$ | $2.44 h^{-1} \text{ kpc}$ |
| FDM | 1024^3 | 5 | $(3.5, 7) \times 10^{-23}$ | $4.88 h^{-1} \text{ kpc}$ |
| CDM | 2048^3 | 10 | — | $9.69 \times 10^3 h^{-1} M_\odot$ |
| CDM | 1024^3 | 10 | — | $7.75 \times 10^4 h^{-1} M_\odot$ |
| CDM | 512^3 | 10 | — | $6.20 \times 10^5 h^{-1} M_\odot$ |
| CDM | 1024^3 | 5 | — | $9.69 \times 10^3 h^{-1} M_\odot$ |
| CDM | 512^3 | 5 | — | $7.75 \times 10^4 h^{-1} M_\odot$ |

Table 1. List of performed simulations with important characteristics. The lengths given for the box sizes and resolutions are comoving.