

1           **OPTIMAL PREDICTION OF WALNUT HARVEST DATES**  
2                           **USING THERMAL TIME MODEL**

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4                           INTRODUCTION

5       In highly complicated systems, like the biochemical system of fruit ripening, our  
6       knowledge of the system is insufficient to develop useful mechanistic models. Instead  
7       we rely on statistical models that are informed by our understanding of the biology  
8       (Črepinšek et al., 2006). Generally speaking, there are three steps in specifying  
9       these statistical models: (1) selection of thermal time model functional form, (2)  
10      selection of cardinal temperatures for calculating thermal time, and (3) selection of  
11      thermal time accumulation length. These methods have been extensively applied  
12      to flowering and harvest prediction for a variety of fruit and nut crops over the past  
13      15 years (Mimoun and DeJong, 1998; Marra et al., 2001; DeBuse et al., 2008; Ruml  
14      et al., 2011). However, no attempts have been made to systematically optimize this  
15      process.

16      Models of thermal time accumulation can be classified by the number of param-  
17      eters they have. Models with more parameters generally more flexible, and may  
18      more closely reflect reality. However, they are computationally more intensive to  
19      fit and there is a higher risk of overfitting. Models with one or two parameters do  
20      not mimic our understanding of the biology as closely, but they are much less prone  
21      to overfitting. It is important to remember that the model with the best fit is not  
22      necessarily the model that most closely reflects reality.

23      The simplest model of thermal time accumulation includes just one parameter  
24      Yang et al. (1995).

$$GDH = T - T_b$$

where  $GDH$  is the growing degree hours accumulated,  $T$  is the current temperature and  $T_b$  is the base temperature. A slightly more complicated model includes two parameters. This allows it to flatten off as temperature increases.

$$GDH = \begin{cases} 0 & T \leq T_b \\ T - T_b & T_b \leq T \leq T_o \\ T_o & T_o \leq T \end{cases}$$

where  $T_o$  is the optimal temperature. This model still neglects the deleterious effects of very high temperatures. The simplest model that includes these effects is the three parameter triangle model from (citation?), where  $T_b$ ,  $T_o$ , and  $T_c$  are the base, optimal and critical temperatures respectively.

$$GDH = \begin{cases} 0 & T \leq T_b \\ T - T_b & T_b \leq T \leq T_o \\ \frac{(T_c - T)(T_o - T_b)}{T_c - T_o} & T_o \leq T \leq T_c \\ 0 & T_c \leq T \end{cases}$$

The most widely used model of thermal time accumulation is another three parameter model from Anderson et al. (1985).

$$GDH = \begin{cases} 0 & T \leq T_b \\ \frac{T_o - T_b}{2} \left[ 1 + \cos \left( \pi + \pi \cdot \frac{T - T_b}{T_o - T_b} \right) \right] & T_b \leq T \leq T_o \\ (T_o - T_b) \left[ 1 + \cos \left( \frac{\pi}{2} + \frac{\pi}{2} \cdot \frac{T - T_o}{T_c - T_o} \right) \right] & T_o \leq T \leq T_c \\ 0 & T_c \leq T \end{cases}$$

The most complicated model used in the literature is beta model from Marra et al. (2001).

$$GDH = T_o \cdot$$

Normally in statistical analysis

Biology tells us that trees will stop fruit development if temperatures get too low or too high. So many potential functional forms include a critical

## MATERIALS AND METHODS

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