

**MA 2073. HOMEWORK 7**  
**DO NOT HAND IN**

Problems from text:

*Section 6.7:* 1, 3, 4, 11, 15

*Section 7.1:* 3, 6, 7, 8, 10, 14, 17, 18

*Section 7.2:* 1, 2, 5, 6, 7, 10, 11, 21, 26, 27, 32

Additional problems:

1. Suppose  $A$  is square and invertible, with the singular value decomposition  $A = U\Sigma V^T$ . Find a singular value decomposition of  $A^{-1}$ .
2. Show that the columns of  $V$  are eigenvectors of  $A^T A$  and the columns of  $U$  are eigenvectors of  $AA^T$ . (*Hint:* use the SVD to compute  $A^T A$  and  $AA^T$ ).
3. Show that the map  $T : M_{n \times n} \rightarrow \mathbb{R}$  defined by  $T(A) = \text{trace}(A)$  is a linear transformation.
4. Show that the map  $D : M_{n \times n} \rightarrow \mathbb{R}$  defined by  $D(A) = \det(A)$  is *not* a linear transformation.