

# Protune Negotiation Model

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This document aims at formalizing the negotiation between two entities, namely  $E_1$  and  $E_2$ . For the rest of the paper we assume that  $E_1$  is the initial requester while  $E_2$  is the provider, i.e.  $E_1$  is assumed to send a request to  $E_2$  thus starting a negotiation. Notice that during a negotiation both entities  $E_1$  and  $E_2$  may both request or provide information to each other.

Let our Policy language be a rule-based language. Such a rule language is based on normal logic program rules  $A \leftarrow L_1, \dots, L_n$  where  $A$  is a standard logical atom (called the *head* of the rule) and  $L_1, \dots, L_n$  (the *body* of the rule) are literals, i.e.  $L_i$  equals either  $B_i$  or  $\neg B_i$ , for some logical atom  $B_i$ .

**Definition 1 (Policy)** *A Policy is a set of rules, such that negation is not applied to any predicate occurring in a rule head.*

This restriction ensures that policies are *monotonic* in the sense of [?], i.e. as more credentials are released and more actions executed, the set of permissions does not decrease. Moreover, the restriction on negation makes policies *stratified programs*; therefore negation as failure has a clear, PTIME computable semantics that can be equivalently formulated as the perfect model semantics, the well-founded semantics or the stable model semantics [?].

**Definition 2 (Negotiation Message)** *A Negotiation Message is an ordered pair*

$$(p, C)$$

where

- $p \equiv$  a Policy
- $C \equiv$  a set of credentials

We will denote with  $M$  the set of all possible Negotiation Messages.

**Definition 3 (Message Sequence)** *A Message Sequence  $\sigma$  is a list of Negotiation Messages*

$$\sigma_1, \dots, \sigma_n \mid \sigma_i \in M$$

We will denote with  $|\sigma|$  the length of  $\sigma$  and with  $\sigma_i$  the  $i$ -th element of the Message Sequence  $\sigma$ .

**Definition 4 (Negotiation History)** Let  $E_1$  and  $E_2$  be the two entities involved in the negotiation. Let  $E_1$  be the initiator of such a negotiation, i.e. the sender of the first message in the negotiation. A Negotiation History  $\sigma$  for the entity  $E_j$  ( $j = 1, 2$ ) is a Message Sequence

$$\sigma_1, \dots, \sigma_n \mid \sigma_i \in M$$

Moreover let

- $M_{snt}(\sigma) = \{\sigma_i \mid i = 2k - (j \bmod 2), 1 \leq k \leq \lfloor n/2 \rfloor\}$
- $M_{rvd}(\sigma) = \{\sigma_i \mid i = 2k - 1 + (j \bmod 2), 1 \leq k \leq \lfloor n/2 \rfloor\}$

We will refer to a Negotiation History also as a *Negotiation State*.

Intuitively, messages among parties are sent alternatively, i.e. a message sent by  $E_j$  is followed by the reception of a message, which is in turn followed by the sending of a new message and so on. Therefore,  $M_{snt}(\sigma)$  (resp.  $M_{rvd}(\sigma)$ ) represents the set of messages sent (resp. received) by  $E_j$ .

Notice that according to this definition, the Negotiation History  $\sigma$  is shared by the two entities  $E_1$  and  $E_2$ , but the sets  $M_{snt}(\sigma)$  and  $M_{rvd}(\sigma)$  are swapped among them. Therefore it holds that

$$M_{snt}(E_1, \sigma) = M_{rvd}(E_2, \sigma)$$

and

$$M_{rvd}(E_1, \sigma) = M_{snt}(E_2, \sigma)$$

In order to ease the notation in the rest of the paper, given a Negotiation History  $\sigma$ , we define the following entities

- $C_{snt}(\sigma) = \bigcup \{C_i \mid \exists p_i (p_i, C_i) \in M_{snt}(\sigma)\}$
- $C_{rvd}(\sigma) = \bigcup \{C_i \mid \exists p_i (p_i, C_i) \in M_{rvd}(\sigma)\}$
- $lp_{snt}(\sigma) = p_{i_{max}} \mid i_{max} = \max\{i \mid (p_i, c_i) \in M_{snt}(\sigma)\}$
- $lp_{rcv}(\sigma) = p_{i_{max}} \mid i_{max} = \max\{i \mid (p_i, c_i) \in M_{rcv}(\sigma)\}$

Intuitively,  $C_{snt}$  (resp.  $C_{rvd}$ ) represents the set of all credentials sent (resp. received) and  $lp_{snt}$  (resp.  $lp_{rvd}$ ) represents the last policy sent (resp. received).

**Definition 5 (Negotiation State Machine)** A *Negotiation State Machine* is a tuple

$$(\Sigma, S, s_0, t)$$

such that

- $S \equiv$  a set of Negotiation States
- $s_0 \equiv$  the empty list (initial state)

- $\Sigma \equiv$  a set of Negotiation Messages.
- $t \equiv$  a function  $S \times \Sigma \rightarrow S$  such that if  $S = (\sigma_1, \dots, \sigma_n)$  then  $t(S, \sigma) = (\sigma_1, \dots, \sigma_n, \sigma_{n+1})$  (transition function)

Intuitively a Negotiation State Machine models how an entity evolves during the negotiation by the exchange of messages.  $\Sigma$  contains both sent and received Negotiation Messages and can therefore be partitioned into two subsets  $\Sigma_{snd}$  and  $\Sigma_{rcv}$ .

**Definition 6 (Negotiation Model)** A Negotiation Model is a tuple

$$(C, P, p_0, NSM, ff, ns)$$

where

- $C \equiv$  a set of credentials
  - $P \equiv$  a set of Policies
  - $p_0 \equiv$  a Policy (local Policy)
  - $NSM \equiv$  a Negotiation State Machine  $(\Sigma, S, s_0, t)$
  - $ff \equiv$  a function  $S \rightarrow P$  (Filtering Function)
  - $ns \equiv$  an ordered pair  $(csf, ta)$  where
    - $csf \equiv$  a function  $S \rightarrow C$  (Credential Selection Function)
    - $ta \equiv$  a function  $S \rightarrow \{true, false\}$  (Termination Algorithm)
- (Negotiation Strategy)

Each occurrence of  $S$  is supposed to refer to the same set of Negotiation States.

The intended meaning is as follows

- $C$  represents the set of the credentials local to the Peer
- $p_0$  represents the Peer's policy protecting the local credentials and allowing access to the local resources
- $S$  represents the set of states in which the Peer can be
- $s_0$  represents the initial state, i.e. the state in which the Peer is at the beginning of the negotiation
- $f$  represents the process of filtering the Peer's Policy according to the current state
- $csf$  represents the process of selecting the Peer's credentials to send to the other Peer
- $ta$  represent the Peer's decision about whether going on or terminating the current negotiation