

# hw2\_part1

October 16, 2023

```
[ ]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import sympy as sy

import seaborn as sns
from sklearn.metrics import confusion_matrix

from IPython.display import display, Math, Latex

import nn
```

## 1 Part 1: One Layer NN with One Output

### 1.1 Problem 2

#### 1.1.1 Create Dataset

The data is meant to be a clustering problem in 3 dimensions. Anything close to the origin has a value of 0 and anything further has a value of 1.

```
[ ]: data = pd.read_csv("A2_Data_EliWeissler.csv")
data
```

```
[ ]:      X    Y    Z  LABEL
0 -0.5  0.0 -0.5      0
1  0.5 -0.5  0.0      0
2  0.0  0.0  1.0      0
3  0.5  0.5  0.5      0
4  2.0  1.0  2.0      1
5  3.0  1.0  1.0      1
6  2.0  3.0  1.0      1
```

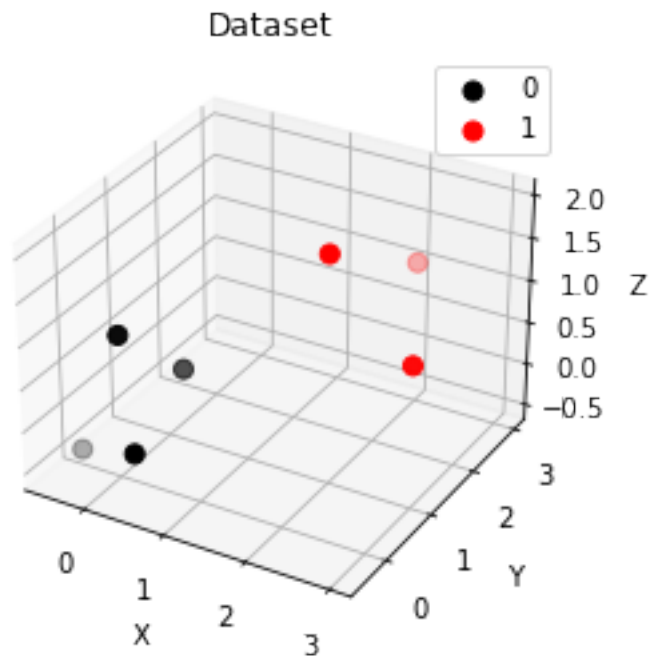
```
[ ]: fig = plt.figure()
ax = plt.axes(projection='3d')

# plotting
```

```

colors = ["k", "r"]
for i in [0, 1]:
    data_subset = data[data["LABEL"] == i]
    ax.scatter(data_subset["X"], data_subset["Y"], data_subset["Z"],
               s=50, c=colors[i], label=data_subset["LABEL"].iloc[0])
ax.set_title('Dataset')
ax.set_xlabel("X")
ax.set_ylabel("Y")
ax.set_zlabel("Z")
ax.legend()
plt.show()

```



### 1.1.2 Create X and Y

```

[ ]: X, Y = nn.normalize_data(data)
Math("X = " + sy.latex(sy.Matrix(np.round(X, 2))) + \
     "\quad Y = " + sy.latex(sy.Matrix(Y)))

```

```

[ ]:

```

$$X = \begin{bmatrix} 0 & 0.14 & 0 \\ 0.29 & 0 & 0.2 \\ 0.14 & 0.14 & 0.6 \\ 0.29 & 0.29 & 0.4 \\ 0.71 & 0.43 & 1.0 \\ 1.0 & 0.43 & 0.6 \\ 0.71 & 1.0 & 0.6 \end{bmatrix} \quad Y = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$

### 1.1.3 Do Feed Forward to H1

```
[ ]: # Define weights and biases
W1 = np.ones((3, 4))
W2 = 2*np.ones((4, 1))
B = np.zeros((1, 4))
C = 0

# First hidden layer
Z1 = X@W1 + B
H1 = nn.sigmoid(Z1)

# Show H1
np.round(H1, 2)
```

```
[ ]: array([[0.54, 0.54, 0.54, 0.54],
          [0.62, 0.62, 0.62, 0.62],
          [0.71, 0.71, 0.71, 0.71],
          [0.73, 0.73, 0.73, 0.73],
          [0.89, 0.89, 0.89, 0.89],
          [0.88, 0.88, 0.88, 0.88],
          [0.91, 0.91, 0.91, 0.91]])
```

### 1.1.4 Calculate a Loss Function

```
[ ]: # Output layer
Z2 = H1@W2 + C
yhat = nn.sigmoid(Z2)
loss = nn.loss_MSE(Y, yhat)
loss
```

```
[ ]: array([[4.86508842e-01],
          [4.93010336e-01],
          [4.96549485e-01],
          [4.96995824e-01],
          [3.01441059e-07],
          [3.60751217e-07],
          [2.36959392e-07]])
```

## 1.2 Problem 3

### 1.2.1 Print out all the Matrices for Checking:

```
[ ]: display(Math("X = " + sy.latex(sy.Matrix(np.round(X, 2)))))
display(Math("Y = " + sy.latex(sy.Matrix(Y))))
display(Math("W^{(1)} = " + sy.latex(sy.Matrix(W1))))
display(Math("B = " + sy.latex(sy.Matrix(B))))
display(Math("Z^{(1)} = " + sy.latex(sy.Matrix(np.round(Z1, 2)))))
```

```

display(Math("H = " + sy.latex(sy.Matrix(np.round(H1,2)))))
display(Math("W^{(2)} = " + sy.latex(sy.Matrix(W2))))
display(Math("Z^{(2)} = " + sy.latex(sy.Matrix(np.round(Z2,2)))))
display(Math("C = " + str(np.round(C, 2))))
display(Math("\hat{y} = " + sy.latex(sy.Matrix(np.round(yhat,3)))))
display(Math("\hat{y}-Y = " + sy.latex(sy.Matrix(np.round(yhat-Y,5)))))
display(Math("L_{contributions} = " + sy.latex(sy.Matrix(loss))))
display(Math("L_{MSE} = " + str(np.round(np.mean(loss), 4))))

```

$$X = \begin{bmatrix} 0 & 0.14 & 0 \\ 0.29 & 0 & 0.2 \\ 0.14 & 0.14 & 0.6 \\ 0.29 & 0.29 & 0.4 \\ 0.71 & 0.43 & 1.0 \\ 1.0 & 0.43 & 0.6 \\ 0.71 & 1.0 & 0.6 \end{bmatrix}$$

$$Y = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 1 \\ 1 \end{bmatrix}$$

$$W^{(1)} = \begin{bmatrix} 1.0 & 1.0 & 1.0 & 1.0 \\ 1.0 & 1.0 & 1.0 & 1.0 \\ 1.0 & 1.0 & 1.0 & 1.0 \end{bmatrix}$$

$$B = \begin{bmatrix} 0 & 0 & 0 & 0 \end{bmatrix}$$

$$Z^{(1)} = \begin{bmatrix} 0.14 & 0.14 & 0.14 & 0.14 \\ 0.49 & 0.49 & 0.49 & 0.49 \\ 0.89 & 0.89 & 0.89 & 0.89 \\ 0.97 & 0.97 & 0.97 & 0.97 \\ 2.14 & 2.14 & 2.14 & 2.14 \\ 2.03 & 2.03 & 2.03 & 2.03 \\ 2.31 & 2.31 & 2.31 & 2.31 \end{bmatrix}$$

$$H = \begin{bmatrix} 0.54 & 0.54 & 0.54 & 0.54 \\ 0.62 & 0.62 & 0.62 & 0.62 \\ 0.71 & 0.71 & 0.71 & 0.71 \\ 0.73 & 0.73 & 0.73 & 0.73 \\ 0.89 & 0.89 & 0.89 & 0.89 \\ 0.88 & 0.88 & 0.88 & 0.88 \\ 0.91 & 0.91 & 0.91 & 0.91 \end{bmatrix}$$

$$W^{(2)} = \begin{bmatrix} 2.0 \\ 2.0 \\ 2.0 \\ 2.0 \end{bmatrix}$$

$$Z^{(2)} = \begin{bmatrix} 4.29 \\ 4.95 \\ 5.66 \\ 5.8 \\ 7.16 \\ 7.07 \\ 7.28 \end{bmatrix}$$

$$C = 0$$

$$\hat{y} = \begin{bmatrix} 0.986 \\ 0.993 \\ 0.997 \\ 0.997 \\ 0.999 \\ 0.999 \\ 0.999 \end{bmatrix}$$

$$\hat{y} - Y = \begin{bmatrix} 0.98642 \\ 0.99299 \\ 0.99654 \\ 0.99699 \\ -0.00078 \\ -0.00085 \\ -0.00069 \end{bmatrix}$$

$$L_{contributions} = \begin{bmatrix} 0.486508841756607 \\ 0.493010335700804 \\ 0.496549485396578 \\ 0.496995823907791 \\ 3.01441058794641 \cdot 10^{-7} \\ 3.607512172511 \cdot 10^{-7} \\ 2.36959392258034 \cdot 10^{-7} \end{bmatrix}$$

$$L_{MSE} = 0.2819$$

## 1.3 Problem 5/6

### 1.3.1 Try training the network

```
[ ]: # Initialize network and load data
data = pd.read_csv("A2_Data_EliWeissler.csv")
X, Y = nn.normalize_data(data)

input_size = 3
hidden_layers = [4]
```

```

output_size = 1
activation_fns = [nn.sigmoid, nn.sigmoid]
loss_fn = nn.loss_MSE
random_initialize = True
network = nn.NeuralNetwork(input_size, output_size, hidden_layers,
                           activation_fns, loss_fn,
                           random_initialize=random_initialize)

```

```

[ ]: # Train network
epochs = 5000
lr = 1
batch_size = 3
loss = network.train(X, Y, X, Y, epochs=epochs, lr=lr, batch_size=batch_size)

```

Epoch 0 (out of 5000) -- Loss: 0.2271  
Epoch 1000 (out of 5000) -- Loss: 0.0974  
Epoch 2000 (out of 5000) -- Loss: 0.0303  
Epoch 3000 (out of 5000) -- Loss: 0.0101  
Epoch 4000 (out of 5000) -- Loss: 0.0054

```

[ ]: # Predict and plot
pred = network.feed_forward(X)

nn.plot_confusion_matrix(Y, pred)
nn.plot_loss(loss, lr)

```

