

Assignment 2.

Using OpenGL library for drawing planar curves.

1. In this example, the OpenGL begin/end paradigm (GL_LINE_STRIP) was used for drawing polygonal lines corresponding to:

1. the graph of the function: $|\sin x| \cdot e^{-\sin x}, x \in [0, 8\pi]$ and
2. the graph of the Conchoid of Nicomedes:

$$x = a \pm b \cos t, y = a \tan t \pm b \sin t, t \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right).$$

2. As for assignment 1, add in the example program lines of code in order to draw the following graphs:

1. The graph of the [function](#) $f(x) = \begin{cases} 1 & , \quad x = 0 \\ \frac{d(x)}{x} & , \quad 0 < x \leq 100 \end{cases}$,

where $d(x)$ is the distance from x to the nearest integer.

2. The following curves are given by parametric equations (for each example, the values of various parameters, called a , b , etc., can be found inside the images):

1. [The trisectrix of Longchamps](#):

$$x = \frac{a}{4 \cos^2 t - 3}, \quad y = \frac{a \tan t}{4 \cos^2 t - 3}, \quad t \in \left(-\frac{\pi}{2}, \frac{\pi}{2}\right) \setminus \left\{\pm \frac{\pi}{6}\right\}.$$

Hint: First, draw the graph of the trisectrix of Longchamps (please note that the [image](#) is not the graph!). Use no scaling, use GL_POINTS

and vary the ratio of arithmetic progression. Then overlap your window on the image requested and notice some patterns, the geometric objects etc. If your image has some/many pixels in the middle it is still considered correct.

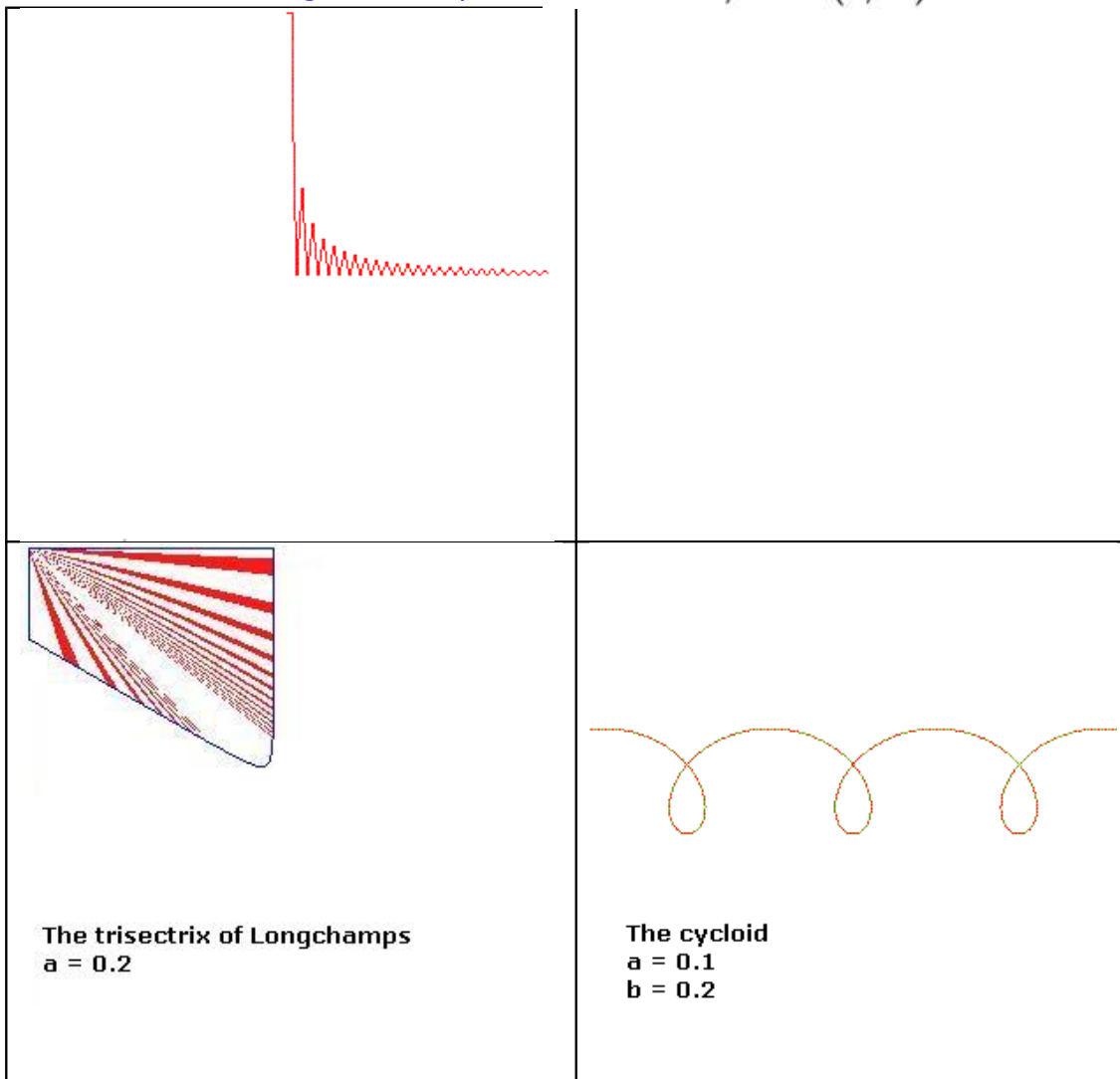
2. [The cycloid](#):

$$x = a \cdot t - b \sin t, \quad y = a - b \cos t, \quad t \in \mathbb{R}.$$

3. Some curves are specified by polar equations: the polar coordinates are (r, t) ,

where $t \in [a, b]$ and $r = f(t)$. The polar coordinates (r, t) are transformed in cartesian coordinates as following $x = r \cos t$ and $y = r \sin t$. Add in the example program lines of code in order to draw the following curves specified by polar equations:

1. [The lemniscate of Bernoulli](#): $r = \pm a \cdot \sqrt{2 \cos 2t}$, $t \in (-\frac{\pi}{4}, \frac{\pi}{4})$,
2. [The logarithmic spiral](#): $r = a \cdot e^{1+t}$, $t \in (0, \infty)$.





The lemniscate of Bernoulli
 $a = 0.4$



The logarithmic spiral
 $a = 0.02$