1. Download and Explore Movielen Latest Small

Open in Colab

```
#mengekstrak folder
import os

if·not·(os.path.exists("recsys.zip")·or·os.path.exists("recsys")):
····!wget·https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/recsys.zip····
····!unzip·recsys.zip
```

```
--2023-01-04 02:29:40--  https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/recsys.zip
Resolving github.com (github.com)... 140.82.114.4
Connecting to github.com (github.com)|140.82.114.4|:443... connected.
HTTP request sent, awaiting response... 302 Found
Location: https://raw.githubusercontent.com/nzhinusoftcm/review-on-collaborative-filtering/master/recsys.zip [following]
--2023-01-04 02:29:40--  https://raw.githubusercontent.com/nzhinusoftcm/review-on-collaborative-filtering/master/recsys.zip
Resolving raw.githubusercontent.com (raw.githubusercontent.com)... 185.199.108.133, 185.199.109.133, 185.199.110.133, ...
Connecting to raw.githubusercontent.com (raw.githubusercontent.com)|185.199.108.133|:443... connected.
HTTP request sent, awaiting response... 200 OK
Length: 15312323 (15M) [application/zip]
Saving to: ‘recsys.zip’

recsys.zip          100%[===================>]  14.60M  --.-KB/s    in 0.1s

2023-01-04 02:29:40 (115 MB/s) - ‘recsys.zip’ saved [15312323/15312323]

Archive:  recsys.zip
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  inflating: recsys/preprocessing.py
  inflating: recsys/utils.py
  inflating: recsys/requirements.txt
   creating: recsys/.vscode/
  inflating: recsys/.vscode/settings.json
   creating: recsys/__pycache__/
  inflating: recsys/__pycache__/datasets.cpython-36.pyc
  inflating: recsys/__pycache__/datasets.cpython-37.pyc
  inflating: recsys/__pycache__/utils.cpython-36.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-37.pyc
  inflating: recsys/__pycache__/datasets.cpython-38.pyc
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  inflating: recsys/__pycache__/preprocessing.cpython-38.pyc
   creating: recsys/memories/
  inflating: recsys/memories/ItemToItem.py
  inflating: recsys/memories/UserToUser.py
   creating: recsys/memories/__pycache__/
  inflating: recsys/memories/__pycache__/UserToUser.cpython-36.pyc
  inflating: recsys/memories/__pycache__/UserToUser.cpython-37.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-37.pyc
  inflating: recsys/memories/__pycache__/user2user.cpython-36.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-36.pyc
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  inflating: recsys/models/SVD.py
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  inflating: recsys/models/NonnegativeMF.py
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  inflating: recsys/models/__pycache__/SVD.cpython-36.pyc
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  inflating: recsys/models/__pycache__/ExplainableMF.cpython-37.pyc
  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-36.pyc
   creating: recsys/metrics/
  inflating: recsys/metrics/EvaluationMetrics.py
   creating: recsys/img/
  inflating: recsys/img/MF-and-NNMF.png
  inflating: recsys/img/svd.png
  inflating: recsys/img/MF.png
```

Requirements

```
matplotlib==3.2.2
numpy==1.18.1
pandas==1.0.5
python==3.6.10
scikit-learn==0.23.1
scipy==1.5.0
```

```
from recsys.datasets import mlLatestSmall

import matplotlib.pyplot as plt
import pandas as pd
import zipfile
import urllib.request
import sys
import os
```

```
#mengunduh data
ratings, movies = mlLatestSmall.load()
```

```
Download data 100.5%
Successfully downloaded ml-latest-small.zip 978202 bytes.
Unzipping the ml-latest-small.zip zip file ...
```

Data visualisation

```
ratings.head()
```

	userid	itemid	rating	timestamp
0	1	1	4.0	964982703
1	1	3	4.0	964981247
2	1	6	4.0	964982224
3	1	47	5.0	964983815

```
ratings.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 100836 entries, 0 to 100835
Data columns (total 4 columns):
 #   Column     Non-Null Count   Dtype
---  ------     --------------   -----
 0   userid     100836 non-null  int64
 1   itemid     100836 non-null  int64
 2   rating     100836 non-null  float64
 3   timestamp  100836 non-null  int64
dtypes: float64(1), int64(3)
memory usage: 3.1 MB
```

```
ratings.count()
```

```
userid       100836
itemid       100836
rating       100836
timestamp    100836
dtype: int64
```

```
movies.head()
```

	itemid	title	genres
0	1	Toy Story (1995)	Adventure|Animation|Children|Comedy|Fantasy
1	2	Jumanji (1995)	Adventure|Children|Fantasy
		Grumpier	

```
movies.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 9742 entries, 0 to 9741
Data columns (total 3 columns):
 #   Column  Non-Null Count  Dtype
---  ------  --------------  -----
 0   itemid  9742 non-null   int64
 1   title   9742 non-null   object
 2   genres  9742 non-null   object
dtypes: int64(1), object(2)
memory usage: 228.5+ KB
```

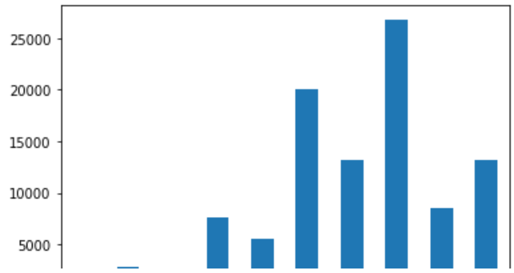
```
movies.count()
```

```
itemid    9742
title     9742
genres    9742
dtype: int64
```

Histogram of ratings

```
#visualisasi diagram batang hubungan rating dan banyak film
ratings.groupby('rating').size().plot(kind='bar')
```

```
<matplotlib.axes._subplots.AxesSubplot at 0x7fa57d8d0790>
```

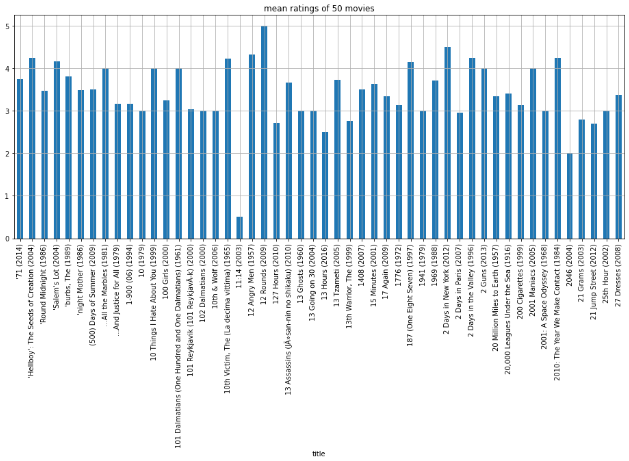


Ratings range from 0.5 to 5.0, with a step of 0.5. The above histogram presents the repartition of ratings in the dataset. the two most commun ratings are 4.0 and 3.0 and the less commun ratings are 0.5 and 1.5

Average ratings of movies

```
#menggabungkan data 'movie' dan 'ratings'
#visualisasi bar graph antara 'title' dan 'rating' pada 50 data
movie_means = ratings.join(movies['title'], on='itemid').groupby('title').rating.mean()
movie_means[:50].plot(kind='bar', grid=True, figsize=(16,6), title="mean ratings of 50 movies")
```

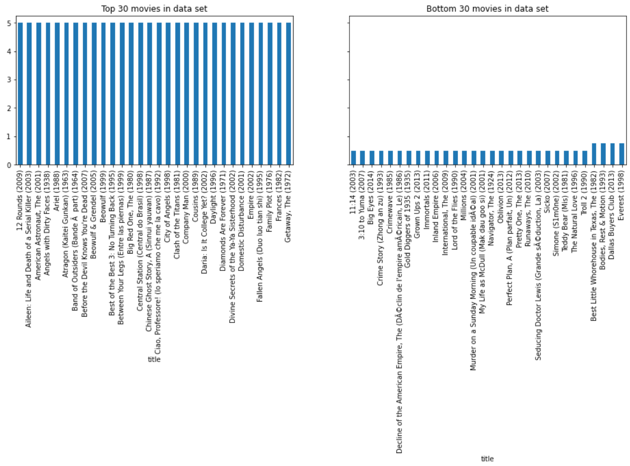
```
<matplotlib.axes._subplots.AxesSubplot at 0x7fa57d825a30>
```



30 most rated movies vs. 30 less rated movies

```
#menampilkan bar graph pada 30 'title' dengan rating tertinggi dan 30 'title' dengan rating terendah
fig, (ax1, ax2) = plt.subplots(ncols=2, figsize=(16,4), sharey=True)
movie_means.nlargest(30).plot(kind='bar', ax=ax1, title="Top 30 movies in data set")
movie_means.nsmallest(30).plot(kind='bar', ax=ax2, title="Bottom 30 movies in data set")
```

```
<matplotlib.axes._subplots.AxesSubplot at 0x7fa57d2150a0>
```



Throughout this repository, we will work with this movielen lasted small data to build collaborative filtering recommender systems.

Let's start by implementing the user-based collaborative filtering algorithm.

The idea behind the **user-based collaborative filtering** algorithm is the following :

> if two users X and Y have a similar behavior on a set of items, then X will most likely have a similar behavior > to Y on an item he did not interact with.

Click here to go to the User-based Collaborative Filtering implementation.

2. User-based Collaborative Filtering

Open in Colab

Download tools

```
#mengekstrak folder yang didalamnya terdaoat data yang akan dikerjakan
import os

if·not·(os.path.exists("recsys.zip")·or·os.path.exists("recsys")):
····!wget·https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/recsys.zip····
····!unzip·recsys.zip
```

```
--2023-01-04 02:36:35--  https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/recsys.zip
Resolving github.com (github.com)... 192.30.255.112
Connecting to github.com (github.com)|192.30.255.112|:443... connected.
HTTP request sent, awaiting response... 302 Found
Location: https://raw.githubusercontent.com/nzhinusoftcm/review-on-collaborative-filtering/master/recsys.zip [following]
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HTTP request sent, awaiting response... 200 OK
Length: 15312323 (15M) [application/zip]
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  inflating: recsys/requirements.txt
   creating: recsys/.vscode/
  inflating: recsys/.vscode/settings.json
   creating: recsys/__pycache__/
  inflating: recsys/__pycache__/datasets.cpython-36.pyc
  inflating: recsys/__pycache__/datasets.cpython-37.pyc
  inflating: recsys/__pycache__/utils.cpython-36.pyc
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  inflating: recsys/memories/__pycache__/UserToUser.cpython-36.pyc
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  inflating: recsys/memories/__pycache__/ItemToItem.cpython-36.pyc
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  inflating: recsys/models/ExplainableMF.py
  inflating: recsys/models/NonnegativeMF.py
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  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-37.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-36.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-37.pyc
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  inflating: recsys/img/MF-and-NNMF.png
  inflating: recsys/img/svd.png
  inflating: recsys/img/MF.png
```

Import requirements

```
matplotlib==3.2.2
numpy==1.19.2
pandas==1.0.5
python==3.7
scikit-learn==0.24.1
```

```
scikit-surprise==1.1.1
scipy==1.6.2
```

```
#menyiapkan library yang akan digunakan
from sklearn.neighbors import NearestNeighbors
from scipy.sparse import csr_matrix

from recsys.datasets import ml100k
from recsys.preprocessing import ids_encoder

import pandas as pd
import numpy as np
import zipfile
```

Load MovieLen ratings

```
#mengunduh data
ratings, movies = ml100k.load()
```

```
Download data 100.2%
Successfully downloaded ml-100k.zip 4924029 bytes.
Unzipping the ml-100k.zip zip file ...
```

userids and itemids encoding

```
# membuat penyandi/ pembuat kode
ratings, uencoder, iencoder = ids_encoder(ratings)
```

Transform rating dataframe to matrix

```
def ratings_matrix(ratings):
    return csr_matrix(pd.crosstab(ratings.userid, ratings.itemid, ratings.rating, aggfunc=sum).fillna(0).values)

R = ratings_matrix(ratings)
```

Memory based collaborative filtering

Memory based collaborative filtering (CF) also known as nearest neighbors based CF makes recommendation based on similar behavious of users and items. There are two types of memory based CF : **user-based** and **item-based** CF. Both of these algorithm usually proceed in three stages :

1. Similarity computation (between users or items)
2. Rating prediction (using ratings of similar users or items)
3. Top-N recommendation

1. User-based Collaborative Filtering

Idea

Let u be the user for which we plan to make recommendations.

1. Find other users whose past rating behavior is similar to that of u
2. Use their ratings on other items to predict what the current user will like

Algorithm : user-to-user collaborative filtering

The entire process of user-to-user CF algorithm is described as follow (J. Bobadilla et al. 2013): For an active user u,

1. First identify the set G_u of k most similar users. G_u is the group users similar to the active user u. The similarity between two users u and v can be measured by the cosine similarity measure as follows :

$$w_{u,v} = \frac{\vec{r}_u \cdot \vec{r}_v}{\|\vec{r}_u\|_2 * \|\vec{r}_v\|_2} = \frac{\sum_{i \in I} r_{u,i} r_{v,i}}{\sqrt{\sum_{i \in I} (r_{u,i})^2} \sqrt{\sum_{i \in I} (r_{v,i})^2}}$$

$w_{u,v}$ is the degree of similarity between users u and v. This term is computed for all $v \in U$, where U is the set of all users. There remains the question of how many neighbors to select. As experimented by (Herlocker et al. 1999), $k \in [20, 50]$ is a reasonable starting point in many domains.

2. Find the set C of candidate items, purchased by the group and not purchased by the active user u. Candidate items have to be the most frequent items purchased by the group.
3. Aggregate ratings of users in G_u to make predictions for user u on items he has not already purchased. Several aggregation approaches are often used such as **average, weighted sum, ajusted weighted sum**. By using weighted sum, the predicted rating of user u on item i denoted by $\hat{r}_{u,i}$ is computed as follow :

$$\hat{r}_{u,i} = \bar{r}_u + \frac{\sum_{v \in G_u} (r_{v,i} - \bar{r}_v) \cdot w_{u,v}}{\sum_{v \in G_u} |w_{u,v}|}.$$

Ratings of similar users are weighted by the corresponding similarity with the active user. Summation are made over all the users who have rated item i. Subtracting the user's mean rating $\bar{r}_v$ compensates for differences in users' use of the rating scale as some users will tend to give higher ratings than others (Michael D. Ekstrand, *et al.* 2011). This prediction is made for all items $i \in C$ not purchased by user u.

4. The Top-N recommendations are obtained by choosing the N items which provide most satisfaction to the user according to prediction.

Step 1. Identify G_u, the set of k users similar to an active user u

To find the k most similar users to u, we use the cosine similarity and compute $w_{u,v}$ for all $v \in U$. Fortunately, libraries such as *scikit-learn (sklearn)* are very useful for such tasks :

1. First of all, we create a nearest neighbors model with sklearn through the function `create_model()`. This function creates and fit a nearest neighbors model with user's ratings. We can choose `cosine` or `euclidian` based similarity metric. `n_neighbors=21` define the number of neighbors to return. With $k = 20$ neighbors, $|G_u| = 21$ as G_u contains 20 similar users added to the active user u. That is why `n_neighbors=21`. Each row r_u of the rating matrix R represents ratings of user u on all items of the database. Missing ratings are replaced with 0.0.

```
R[u,:] # uth row of the rating matrix R. Ratings of user u on all items in the database
```

2. Function `nearest_neighbors()` returns the knn users for each user.

```
def create_model(rating_matrix, metric):
    """
    - create the nearest neighbors model with the corresponding similarity metric
    - fit the model
    """
    model = NearestNeighbors(metric=metric, n_neighbors=21, algorithm='brute')
    model.fit(rating_matrix)
    return model


def nearest_neighbors(rating_matrix, model):
    """
    :param rating_matrix : rating matrix of shape (nb_users, nb_items)
    :param model : nearest neighbors model
    :return
        - similarities : distances of the neighbors from the referenced user
        - neighbors : neighbors of the referenced user in decreasing order of similarities
    """
    similarities, neighbors = model.kneighbors(rating_matrix)
    return similarities[:, 1:], neighbors[:, 1:]
```

Let's call functions `create_model()` and `nearest_neighbors()` to respectively create the k-NN model and compute the nearest neighbors for a given user

```
model = create_model(rating_matrix=R, metric='cosine') # we can also use the 'euclidian' distance
similarities, neighbors = nearest_neighbors(R, model)
```

Step 2. Find candidate items

The set C of candidate items are the most frequent ones purchased by users in G_u for an active user u and not purchased by u.

Function `find_candidate_items()` : find items purchased by these similar users as well as their frequency. Note that the frequency of the items in the set C can be computed by just counting the actual occurrence frequency of that items.

1. `Gu_items` : frequent items of G_u in decreasing order of frequency.
2. `active_items` : items already purchased by the active user
3. `candidates` : frequent items of G_u not purchased by the active user u

```
def find_candidate_items(userid):
    """
    Find candidate items for an active user

    :param userid : active user
    :param neighbors : users similar to the active user
    :return candidates : top 30 of candidate items
    """
    user_neighbors = neighbors[userid]
    activities = ratings.loc[ratings.userid.isin(user_neighbors)]

    # mengurutkan item dalam urutan frekuensi tertinggi ke terendah
    frequency = activities.groupby('itemid')['rating'].count().reset_index(name='count').sort_values(['count'],ascending=False)
    Gu_items = frequency.itemid
    active_items = ratings.loc[ratings.userid == userid].itemid.to_list()
    candidates = np.setdiff1d(Gu_items, active_items, assume_unique=True)[:30]

    return candidates
```

Step 3. Rating prediction

Now it's time to predict what score the active user u would have given to each of the top-30 candidate items.

To predict the score of u on a candidate item i ,we need :

1. Similarities between u and all his neighbors $v \in G_u$ who rated item i : function `nearest_neighbors()` returns similar users of a user as well as their corresponding similarities.
2. Normalized ratings of all $v \in G_u$ on item i. The normalized rating of user v on item i is defined by $r_{v,i} - \bar{r}_v$.

Next, let's compute the mean rating of each user and the normalized ratings for each item. The DataFrame `mean` contains mean rating for each user. With the mean rating of each user, we can add an extra column `norm_rating` to the `ratings`'s DataFrame which can be accessed to make predictions.

```
# rata-rata peringkat pada masing-masing pengguna
mean = ratings.groupby(by='userid', as_index=False)['rating'].mean()
mean_ratings = pd.merge(ratings, mean, suffixes=('','_mean'), on='userid')

# normalisasi peringkat pada masing-masing item
mean_ratings['norm_rating'] = mean_ratings['rating'] - mean_ratings['rating_mean']

mean = mean.to_numpy()[:, 1]


np_ratings = mean_ratings.to_numpy()
```

Let us define function `predict` that predict rating between user u and item i. Recall that the prediction formula is defined as follow :

$$\hat{r}_{u,i} = \bar{r}_u + \frac{\sum_{v \in G_u} (r_{v,i} - \bar{r}_v) \cdot w_{u,v}}{\sum_{v \in G_u} |w_{u,v}|}.$$

```
def predict(userid, itemid):
    """
    predict what score userid would have given to itemid.

    :param
        - userid : user id for which we want to make prediction
        - itemid : item id on which we want to make prediction

    :return
        - r_hat : predicted rating of user userid on item itemid
    """
    user_similarities = similarities[userid]
    user_neighbors = neighbors[userid]
    # memperoleh rata-rata rating berdasarkan pengguna 'userid'
    user_mean = mean[userid]

    # menemukan pengguna yang memberikan rating pada item 'itemid'
    iratings = np_ratings[np_ratings[:, 1].astype('int') == itemid]

    # menemukan pengguna 'userid' yang mirip yang memberikan rating item 'itemid'
    suri = iratings[np.isin(iratings[:, 0], user_neighbors)]

    # pengguna yang mirip yang memberikan rating item saat ini (surci)
    normalized_ratings = suri[:,4]
    indexes = [np.where(user_neighbors == uid)[0][0] for uid in suri[:, 0].astype('int')]
    sims = user_similarities[indexes]

    num = np.dot(normalized_ratings, sims)
    den = np.sum(np.abs(sims))

    if num == 0 or den == 0:
        return user_mean

    r_hat = user_mean + np.dot(normalized_ratings, sims) / np.sum(np.abs(sims))

    return r_hat
```

Now, we can make rating prediction for a given user on each item in his set of candidate items.

```
def user2userPredictions(userid, pred_path):
    """
    Make rating prediction for the active user on each candidate item and save in file prediction.csv

    :param
        - userid : id of the active user
        - pred_path : where to save predictions
    """
    # menemukan kandidat item untuk pengguna yang aktif
    candidates = find_candidate_items(userid)

    # mengulang item kandidat untuk membuat prediksi
    for itemid in candidates:

        # prediksi untuk userid dan itemid
        r_hat = predict(userid, itemid)

        # menyimpan prediksi
        with open(pred_path, 'a+') as file:
            line = '{},{},{}\n'.format(userid, itemid, r_hat)
            file.write(line)
```

```
import sys

def user2userCF():
    """
    Make predictions for each user in the database.
    """
    # memperoleh daftar pengguna dalam database
    users = ratings.userid.unique()

    def _progress(count):
        sys.stdout.write('\rRating predictions. Progress status : %.1f%%' % (float(count/len(users))*100.0))
        sys.stdout.flush()

    saved_predictions = 'predictions.csv'
    if os.path.exists(saved_predictions):
        os.remove(saved_predictions)

    for count, userid in enumerate(users):
        # membuat prediksi rating untuk pengguna saat ini
        user2userPredictions(userid, saved_predictions)
        _progress(count)
```

```
user2userCF()
```

```
 Rating predictions. Progress status : 99.9%
```

Step 4. Top-N recommendation

Function `user2userRecommendation()` reads predictions for a given user and return the list of items in decreasing order of predicted rating.

```
def user2userRecommendation(userid):
    """
    """
    # menyandikan userid
    uid = uencoder.transform([userid])[0]
    saved_predictions = 'predictions.csv'

    predictions = pd.read_csv(saved_predictions, sep=',', names=['userid', 'itemid', 'predicted_rating'])
    predictions = predictions[predictions.userid==uid]
    List = predictions.sort_values(by=['predicted_rating'], ascending=False)

    List.userid = uencoder.inverse_transform(List.userid.tolist())
    List.itemid = iencoder.inverse_transform(List.itemid.tolist())

    List = pd.merge(List, movies, on='itemid', how='inner')

    return List
```

```
user2userRecommendation(212)
```

	userid	itemid	predicted_rating	title
0	212	483	4.871495	Casablanca (1942)
1	212	357	4.764547	One Flew Over the Cuckoo's Nest (1975)
2	212	50	4.660002	Star Wars (1977)
3	212	98	4.613636	Silence of the Lambs, The (1991)
4	212	64	4.550733	Shawshank Redemption, The (1994)
5	212	194	4.522336	Sting, The (1973)
6	212	174	4.521300	Raiders of the Lost Ark (1981)
7	212	134	4.414819	Citizen Kane (1941)
8	212	187	4.344531	Godfather: Part II, The (1974)
9	212	196	4.303696	Dead Poets Society (1989)
10	212	523	4.281802	Cool Hand Luke (1967)
11	212	216	4.278246	When Harry Met Sally... (1989)
12	212	100	4.260087	Fargo (1996)
13	212	168	4.206139	Monty Python and the Holy Grail (1974)
14	212	435	4.122984	Butch Cassidy and the Sundance Kid (1969)
15	212	135	4.115228	2001: A Space Odyssey (1968)
16	212	83	4.106995	Much Ado About Nothing (1993)

Let us make top n recommendation for a given user.

Evaluation with Mean Absolute Error (MAE)

```
from recsys.preprocessing import train_test_split, get_examples
```

```
# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings, labels_column='rating')

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

def evaluate(x_test, y_test):
    print('Evaluate the model on {} test data ...'.format(x_test.shape[0]))
    preds = list(predict(u,i) for (u,i) in x_test)
    mae = np.sum(np.absolute(y_test - np.array(preds))) / x_test.shape[0]
    print('\nMAE :', mae)
    return mae


evaluate(x_test, y_test)
```

```
     Evaluate the model on 10000 test data ...

     MAE : 0.7505910931068639
     0.7505910931068639
```

Summary

We have summarised all the steps of building the user-based collaborative filtering into a python class for further user. Click UserToUser.py for more details on the **UserToUser** class definition.

UserToUser : Evaluation on the ML-100k dataset

```
from recsys.memories.UserToUser import UserToUser

# load ml100k ratings
ratings, movies = ml100k.load()

# prepare data
ratings, uencoder, iencoder = ids_encoder(ratings)

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings, labels_column='rating')

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)


# create the user-based CF
usertouser = UserToUser(ratings, movies, metric='cosine')
```

```
     Normalize users ratings ...
     Initialize the similarity model ...
     Compute nearest neighbors ...
     User to user recommendation model created with success ...
```

```
# evaluate the user-based CF on the ml100k test data
usertouser.evaluate(x_test, y_test)
```

```
     Evaluate the model on 10000 test data ...

     MAE : 0.7505910931068639
     0.7505910931068639
```

Evaluation on the ML-1M dataset (this may take some time)

```
from recsys.datasets import ml1m
from recsys.preprocessing import ids_encoder, get_examples, train_test_split
from recsys.memories.UserToUser import UserToUser

# memuat data ml1m ratings
ratings, movies = ml1m.load()

# prepare data
ratings, uencoder, iencoder = ids_encoder(ratings)

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings, labels_column='rating')

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

# create the user-based CF
usertouser = UserToUser(ratings, movies, k=20, metric='cosine')
```

```
# evaluate the user-based CF on the ml1m test data
print("==========================")
usertouser.evaluate(x_test, y_test)
```

```
Download data 100.1%
Successfully downloaded ml-1m.zip 5917549 bytes.
Unzipping the ml-1m.zip zip file ...
Normalize users ratings ...
Initialize the similarity model ...
Compute nearest neighbors ...
User to user recommendation model created with success ...
==========================
Evaluate the model on 100021 test data ...

MAE : 0.732267005840993
0.732267005840993
```

Limitations of user-based CF

1. **Sparsity** : In general, users interact with less than 20% of items. This leads the rating matrix to be highly sparse. For example, the movielen-100k contains 100k ratings from 943 users on 1682 items. The pourcentage of sparsity in this case is around 94%. A recommender system based on nearest neighbor algorithms may be unable to make any item recommendations for a particular user. As a result the accuracy of recommendations may be poor (Sarwar *et al.* 2001).
2. **Stability of user's ratings** : As a user rates and re-rates items, their rating vector will change along with their similarity to other users. A user's neighborhood is determined not only by their ratings but also by the ratings of other users, so their neighborhood can change as a result of new ratings supplied by any user in the system (Michael D. Ekstrand, *et al.* 2011).
3. **Scalability** : Due to the non-stability of users ratings, finding similar users in advance is complicated. For this reason, most user-based CF systems find neighborhoods each time predictions or recommendations are needed. However, these are huge computations that grows with both the number of users and the number of items. With millions of users and items, a typical web-based recommender system running existing algorithms will suffer serious scalability concerns (Sarwar *et al.* 2001), (Michael D. Ekstrand, *et al.* 2011).

Item-based CF

With Item-based CF, it's possible to compute similarities in advance and use them for online recommendations. This allows the Item-based to be more scalable than the User-based algorithm.

Click here to go to the Item-based Implementation.

References

1. Herlocker et al. (1999) An Algorithmic Framework for Performing Collaborative Filtering
2. Sarwar et al. (2001) Item-based collaborative filtering recommendation algorithms
3. Michael D. Ekstrand, et al. (2011). Collaborative Filtering Recommender Systems
4. J. Bobadilla et al. (2013) Recommender systems survey

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● ×

3. Item-based Collaborative Filtering

Open in Colab

Item-to-Item Collaborative Filtering

Idea

Let u be the active user and i the referenced item

1. If u liked items similar to i, he will probably like item i.
2. If he hated or disliked items similar to i, he will also hate item i.

The idea is therefore to look at how an active user u rated items similar to i to know how he would have rated item i

Advantages over user-based CF

1. **Stability** : Items ratings are more stable than users ratings. New ratings on items are unlikely to significantly change the similarity between two items, particularly when the items have many ratings (Michael D. Ekstrand, *et al.* 2011).
2. **Scalability** : with stable item's ratings, it is reasonable to pre-compute similarities between items in an item-item similarity matrix (similarity between items can be computed offline). This will reduce the scalability concern of the algorithm. (Sarwar *et al.* 2001), (Michael D. Ekstrand, *et al.* 2011).

Algorithm : item-to-item collaborative filtering

The algorithm that defines item-based CF is described as follow (B. Sarwar et al. 2001)(George Karypis 2001) :

1. First identify the k most similar items for each item in the catalogue and record the corresponding similarities. To compute similarity between two items we can user the *Adjusted Cosine Similarity* that has proven to be more efficient than the basic *Cosine similarity measure* used for user-based collaborative as described in (B. Sarwar et al. 2001). The Adjusted Cosine distance between two items i and j is computed as follow

$$w_{i,j} = \frac{\sum_{u\in U}(r_{u,i}-\bar{r}_u)(r_{u,j}-\bar{r}_u)}{\sqrt{\sum_{u\in U}(r_{u,i}-\bar{r}_u)^2}\sqrt{\sum_{u\in U}(r_{u,j}-\bar{r}_u)^2}}$$

$w_{i,j}$ is the degree of similarity between items i and j. This term is computed for all users $u \in U$, where U is the set of users that rated both items i and j. Let's denote by $S^{(i)}$ the set of the k most similar items to item i.

2. To produce top-N recommendations for a given user u that has already purchased a set $I_u$ of items, do the following :
    - Find the set $C$ of candidate items by taking the union of all $S^{(i)}, \forall i\in I_u$ and removing each of the items in the set $I_u$.

$$C = \bigcup_{i\in I_u}\{S^{(i)}\} \setminus I_u$$

    - $\forall c\in C$, compute similarity between c and the set $I_u$ as follows:

$$w_{c,I_u} = \sum_{i\in I_u} w_{c,i}, \forall c \in C$$

    - Sort items in $C$ in decreasing order of w_{c,I_u}, $\forall c \in C$, and return the first N items as the Top-N recommendation list.

Before returning the first N items as top-N recommendation list, we can make predictions about what user u would have given to each items in the top-N recommendation list, rearrange the list in descending order of predicted ratings and return the rearranged list as the final recommendation list. Rating prediction for item-based CF is given by the following formular (B. Sarwar et al. 2001):

$$\hat{r}_{u,i} = \frac{\sum_{i\in S^{(i)}} r_{u,j}\cdot w_{i,j}}{\sum_{j\in S^{(i)}} |w_{i,j}|}$$

Import useful requirements

```
#mengekstrak folder yang didalamnya terdapat data yang akan diolah
import os
```

```
if not (os.path.exists("recsys.zip") or os.path.exists("recsys")):
    !wget https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/recsys.zip
    !unzip recsys.zip
```

```
Connecting to raw.githubusercontent.com (raw.githubusercontent.com)|185.199.108.133|:443... connected.
HTTP request sent, awaiting response... 200 OK
Length: 15312323 (15M) [application/zip]
Saving to: ‘recsys.zip’

recsys.zip          100%[===================>]  14.60M  --.-KB/s    in 0.1s

2023-01-04 11:21:03 (119 MB/s) - ‘recsys.zip’ saved [15312323/15312323]

Archive:  recsys.zip
   creating: recsys/
  inflating: recsys/datasets.py
  inflating: recsys/preprocessing.py
  inflating: recsys/utils.py
  inflating: recsys/requirements.txt
   creating: recsys/.vscode/
  inflating: recsys/.vscode/settings.json
   creating: recsys/__pycache__/
  inflating: recsys/__pycache__/datasets.cpython-36.pyc
  inflating: recsys/__pycache__/datasets.cpython-37.pyc
  inflating: recsys/__pycache__/utils.cpython-36.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-37.pyc
  inflating: recsys/__pycache__/datasets.cpython-38.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-36.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-38.pyc
   creating: recsys/memories/
  inflating: recsys/memories/ItemToItem.py
  inflating: recsys/memories/UserToUser.py
   creating: recsys/memories/__pycache__/
  inflating: recsys/memories/__pycache__/UserToUser.cpython-36.pyc
  inflating: recsys/memories/__pycache__/UserToUser.cpython-37.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-37.pyc
  inflating: recsys/memories/__pycache__/user2user.cpython-36.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-36.pyc
   creating: recsys/models/
  inflating: recsys/models/SVD.py
  inflating: recsys/models/MatrixFactorization.py
  inflating: recsys/models/ExplainableMF.py
  inflating: recsys/models/NonnegativeMF.py
   creating: recsys/models/__pycache__/
  inflating: recsys/models/__pycache__/SVD.cpython-36.pyc
  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-37.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-36.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-37.pyc
  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-36.pyc
   creating: recsys/metrics/
  inflating: recsys/metrics/EvaluationMetrics.py
   creating: recsys/img/
  inflating: recsys/img/MF-and-NNMF.png
  inflating: recsys/img/svd.png
  inflating: recsys/img/MF.png
   creating: recsys/predictions/
   creating: recsys/predictions/item2item/
   creating: recsys/weights/
   creating: recsys/weights/item2item/
   creating: recsys/weights/item2item/ml1m/
  inflating: recsys/weights/item2item/ml1m/similarities.npy
  inflating: recsys/weights/item2item/ml1m/neighbors.npy
   creating: recsys/weights/item2item/ml100k/
```

Import requirements

```
matplotlib==3.2.2
numpy==1.19.2
pandas==1.0.5
python==3.7
scikit-learn==0.24.1
scikit-surprise==1.1.1
scipy==1.6.2
```

```
from sklearn.neighbors import NearestNeighbors
from scipy.sparse import csr_matrix

from recsys.datasets import ml1m, ml100k
from recsys.preprocessing import ids_encoder

import pandas as pd
import numpy as np
import os
import sys
```

Load ratings

```
ratings, movies = ml100k.load()
```

```
Download data 100.2%
Successfully downloaded ml-100k.zip 4924029 bytes.
Unzipping the ml-100k.zip zip file ...
```

userids and itemids encoding

```
# membuat penyandi
ratings, uencoder, iencoder = ids_encoder(ratings)
```

Let's implements the item-based collaborative filtering algorithm described above

Step 1. Find similarities for each of the items

To compute similarity between two items i and j, we need to :

1. find all users who rated both of them,
2. Normalize their ratings on items i and j
3. Apply the cosine metric to the normalized ratings to compute similarity between i and j

Function `normalize()` process the rating dataframe to normalize ratings of all users

```
def normalize():
    # menghitung rata-rata rating untuk setiap pengguna
    mean = ratings.groupby(by='userid', as_index=False)['rating'].mean()
    norm_ratings = pd.merge(ratings, mean, suffixes=('','_mean'), on='userid')

    # menormalisasi setiap rating dengan mengurangkan rata-rata rating dari pengguna yang sesuai
    norm_ratings['norm_rating'] = norm_ratings['rating'] - norm_ratings['rating_mean']
    return mean.to_numpy()[:, 1], norm_ratings
```

```
mean, norm_ratings = normalize()
np_ratings = norm_ratings.to_numpy()
norm_ratings.head()
```

	userid	itemid	rating	rating_mean	norm_rating
0	0	0	5	3.610294	1.389706
1	0	1	3	3.610294	-0.610294
2	0	2	4	3.610294	0.389706
3	0	3	3	3.610294	-0.610294

now that each rating has been normalized, we can represent each item by a vector of its normalized ratings

```
def item_representation(ratings):
    return csr_matrix(
        pd.crosstab(ratings.itemid, ratings.userid, ratings.norm_rating, aggfunc=sum).fillna(0).values
    )
```

```
R = item_representation(norm_ratings)
```

Let's build and fit our k-NN model using sklearn

```
def create_model(rating_matrix, k=20, metric="cosine"):
    """
    :param R : numpy array of item representations
    :param k : number of nearest neighbors to return
    :return model : our knn model
    """
    model = NearestNeighbors(metric=metric, n_neighbors=k+1, algorithm='brute')
    model.fit(rating_matrix)
    return model
```

Similarities computation

Similarities between items can be measured with the *Cosine* or *Eucliedian* distance. The ***NearestNeighbors*** class from the sklearn library simplifies the computation of neighbors. We just need to specify the metric (e.g. cosine or euclidian) that will be used to compute similarities.

The above method, `create_model`, creates the kNN model and the following `nearest_neighbors` method uses the created model to kNN items. It returns nearest neighbors as well as similarities measures for each items.

`nearest_neighbors` returns :

- `similarities` : numpy array of shape (n, k)
- `neighbors` : numpy array of shape (n, k)

where n is the total number of items and k is the number of neighbors to return, specified when creating the kNN model.

```
def nearest_neighbors(rating_matrix, model):
    """
    compute the top n similar items for each item.
    :param rating_matrix : items representations
    :param model : nearest neighbors model
    :return similarities, neighbors
    """
    similarities, neighbors = model.kneighbors(rating_matrix)
    return similarities[:,1:], neighbors[:,1:]
```

Ajusted Cosine Similarity

In the context of item-based collaborative filtering, the adjusted cosine similarity has shown to be more efficient that the cosine or the euclidian distance. Here is the formular to compute the adjusted cosine weight between two items i and j :

$$w_{i,j} = \frac{\sum_{u \in U}(r_{u,i} - \bar{r}_u)(r_{u,j} - \bar{r}_u)}{\sqrt{\sum_{u \in U}(r_{u,i} - \bar{r}_u)^2}\sqrt{\sum_{u \in U}(r_{u,j} - \bar{r}_u)^2}}.$$

This term is computed for all users $u \in U$, where U is the set of users that rated both items i and j. Since the *sklearn* library do not directly implement the adjusted cosine similarity metric, we will implement it with the method `adjusted_cosine`, with some helper function :

- `save_similarities` : since the computation of the adjusted cosine similarity is time consuming, around 5 mins for the ml100k dataset, we use this method to save the computed similarities for lated usage.
- `load_similarities` : load the saved similarities
- `cosine` : cosine distance between two vectors.

```
def save_similarities(similarities, neighbors, dataset_name):
    base_dir = 'recsys/weights/item2item'
    save_dir = os.path.join(base_dir, dataset_name)
    os.makedirs(save_dir, exist_ok=True)
    similarities_file_name = os.path.join(save_dir, 'similarities.npy')
    neighbors_file_name = os.path.join(save_dir, 'neighbors.npy')
    try:
        np.save(similarities_file_name, similarities)
        np.save(neighbors_file_name, neighbors)
    except ValueError as error:
        print(f"An error occured when saving similarities, due to : \n ValueError : {error}")


def load_similarities(dataset_name, k=20):
    base_dir = 'recsys/weights/item2item'
    save_dir = os.path.join(base_dir, dataset_name)
    similiraties_file = os.path.join(save_dir, 'similarities.npy')
    neighbors_file = os.path.join(save_dir, 'neighbors.npy')
    similarities = np.load(similiraties_file)
    neighbors = np.load(neighbors_file)
    return similarities[:,:k], neighbors[:,:k]


def cosine(x, y):
    return np.dot(x, y) / (np.linalg.norm(x) * np.linalg.norm(y))


def adjusted_cosine(np_ratings, nb_items, dataset_name):
    similarities = np.zeros(shape=(nb_items, nb_items))
    similarities.fill(-1)

    def _progress(count):
        sys.stdout.write('\rComputing similarities. Progress status : %.1f%%' % (float(count / nb_items)*100.0))
        sys.stdout.flush()

    items = sorted(ratings.itemid.unique())
    for i in items[:-1]:
        for j in items[i+1:]:
            scores = np_ratings[(np_ratings[:, 1] == i) | (np_ratings[:, 1] == j), :]
            vals, count = np.unique(scores[:,0], return_counts = True)
            scores = scores[np.isin(scores[:,0], vals[count > 1]),:]

            if scores.shape[0] > 2:
                x = scores[scores[:, 1].astype('int') == i, 4]
                y = scores[scores[:, 1].astype('int') == j, 4]
                w = cosine(x, y)

                similarities[i, j] = w
                similarities[j, i] = w
        _progress(i)
    _progress(nb_items)

    # memperoleh neighbors-neighbors dalam  dalam tingkat kemiripan yang menurun
    neighbors = np.flip(np.argsort(similarities), axis=1)

    # mengurutkan kemiripan dalam urutan menurun
    similarities = np.flip(np.sort(similarities), axis=1)

    # menyimpan kemiripann ke disk
    save_similarities(similarities, neighbors, dataset_name=dataset_name)

    return similarities, neighbors
```

now, we can call the `adjusted_cosine` function to compute and save items similarities and neighbors based on the adjusted cosine metric.

uncomment the two lines of the following cell to compute the adjusted cosine between all items. As we have already run the next cell before, we will just load the precomputed similarities for further use.

```
# nb_items = ratings.itemid.nunique()
# similarities, neighbors = adjusted_cosine(np_ratings, nb_items=nb_items, dataset_name='ml100k')
```

Among the following similarity metrics, choose the one you wish to use for the item-based collaborative filtering :

- **euclidian** or **cosine** : choose *euclidian* or *cosine* to initialise the similarity model through the sklearn library.
- **adjusted_cosine** : choose the *adjusted_cosine* metric to load similarities computed and saved through the `adjusted_cosine` function.

In this case, we will use the *adjusted_cosine* metric.

```
# metric : pilih diantara [cosine, euclidean, adjusted_cosine]

metric = 'adjusted_cosine'

if metric == 'adjusted_cosine':
    similarities, neighbors = load_similarities('ml100k')
else:
    model = create_model(R, k=21, metric=metric)
    similarities, neighbors = nearest_neighbors(R, model)


print('neighbors shape : ', neighbors.shape)
print('similarities shape : ', similarities.shape)
```

```
neighbors shape :  (1682, 20)
similarities shape :  (1682, 20)
```

`neighbors` and `similarities` are numpy array, were each entries are list of 20 neighbors with their corresponding similarities

Step 2. Top N recommendation for a given user

Top-N recommendations are made for example for a user u who has already rated a set of items I_u

2.a- Finding candidate items

To find candidate items for user u, we need to :

1. Find the set I_u of items already rated by user u,
2. Take the union of similar items as C for all items in I_u
3. exclude from the set C all items in I_u, to avoid recommend to a user items he has already purchased.

These are done in function `candidate_items()`

```
def candidate_items(userid):
    """
    :param userid : user id for which we wish to find candidate items
    :return : I_u, candidates
    """

    # 1. menemukan himpunan I_u dari produk yang sudah dirating oleh pengguna userid
    I_u = np_ratings[np_ratings[:, 0] == userid]
    I_u = I_u[:, 1].astype('int')

    # 2. mengambil gabungan produk yang mirip utnuk semua produk dala I_u ke bentuk himpunan kandidat produk
    c = set()

    for iid in I_u:
        # menambahkan neighbors produk iid dalam himpunan kadidat produk
        c.update(neighbors[iid])

    c = list(c)
    # 3. mengecualikan dari himpunan C semua produk in I_u
    candidates = np.setdiff1d(c, I_u, assume_unique=True)

    return I_u, candidates
```

```
test_user = uencoder.transform([1])[0]
i_u, u_candidates = candidate_items(test_user)
```

```
print('number of items purchased by user 1 : ', len(i_u))
print('number of candidate items for user 1 : ', len(u_candidates))
```

```
number of items purchased by user 1 :  272
number of candidate items for user 1 :  893
```

2.b- Find similarity between each candidate item and the set I_u

```
def similarity_with_Iu(c, I_u):
    """
    compute similarity between an item c and a set of items I_u. For each item i in I_u, get similarity between
    i and c, if c exists in the set of items similar to itemid.
    :param c : itemid of a candidate item
    :param I_u : set of items already purchased by a given user
    :return w : similarity between c and I_u
    """
    w = 0
    for iid in I_u :
        # get similarity between itemid and c, if c is one of the k nearest neighbors of itemid
        if c in neighbors[iid] :
            w = w + similarities[iid, neighbors[iid] == c][0]
    return w
```

2.c- Rank candidate items according to their similarities to I_u

```
def rank_candidates(candidates, I_u):
    """
    rank candidate items according to their similarities with i_u
    :param candidates : list of candidate items
    :param I_u : list of items purchased by the user
    :return ranked_candidates : dataframe of candidate items, ranked in descending order of similarities with I_u
    """

    # membuat daftar kandidat produk dipetakan ke kemiripan mereka yang sesuai dengan I_u
    sims = [similarity_with_Iu(c, I_u) for c in candidates]
    candidates = iencoder.inverse_transform(candidates)
    mapping = list(zip(candidates, sims))

    ranked_candidates = sorted(mapping, key=lambda couple:couple[1], reverse=True)
    return ranked_candidates
```

Putting all together

Now that we defined all functions necessary to build our item to item top-N recommendation, let's define function `item2item_topN()` that makes top-N recommendations for a given user

```
def topn_recommendation(userid, N=30):
    """
    Produce top-N recommendation for a given user
    :param userid : user for which we produce top-N recommendation
    :param n : length of the top-N recommendation list
    :return topn
    """
    # mencari kandidat produk
    I_u, candidates = candidate_items(userid)

    # meranking kandidat produk berdasarkan kemiripan mereka dengan I_u
    ranked_candidates = rank_candidates(candidates, I_u)

    # memperoleh bari N pertama dari raked_candidates untuk membangun daftar rekomendasi N teratas
    topn = pd.DataFrame(ranked_candidates[:N], columns=['itemid','similarity_with_Iu'])
    topn = pd.merge(topn, movies, on='itemid', how='inner')
    return topn
```

```
topn_recommendation(test_user)
```

	itemid	similarity_with_Iu	title
0	1356	52.867173	Ed's Next Move (1996)
1	1189	50.362199	Prefontaine (1997)
2	1516	31.133267	Wedding Gift, The (1994)
3	1550	31.031738	Destiny Turns on the Radio (1995)
4	1554	27.364494	Safe Passage (1994)
5	1600	27.287712	Guantanamera (1994)
6	1223	26.631850	King of the Hill (1993)
7	1388	26.624397	Gabbeh (1996)
8	766	26.590175	Man of the Year (1995)
9	691	26.461802	Dark City (1998)
10	1378	25.787842	Rhyme & Reason (1997)
11	1664	25.327445	8 Heads in a Duffel Bag (1997)
12	1261	24.785660	Run of the Country, The (1995)
13	1123	24.524028	Last Time I Saw Paris, The (1954)
14	1538	24.492453	All Over Me (1997)
15	1485	24.345312	Colonel Chabert, Le (1994)
16	1450	24.262120	Golden Earrings (1947)
17	909	23.357301	Dangerous Beauty (1998)
18	359	22.973658	Assignment, The (1997)
19	1369	22.710078	Forbidden Christ, The (Cristo proibito, Il) (1...
20	1506	22.325504	Nelly & Monsieur Arnaud (1995)
21	1537	22.061914	Cosi (1996)

This dataframe represents the top N recommendation list a user. These items are sorted in decreasing order of similarities with I_u.

Observation : The recommended items are the most similar to the set I_u of items already purchased by the user.

Top N recommendation with predictions

Before recommending the previous list to the user, we can go further and predict the ratings the user would have given to each of these items, sort them in descending order of prediction and return the reordered list as the new top N recommendation list.

Rating prediction

As stated earlier, the predicted rating $\hat{r}_{u,i}$ for a given user u on an item i is obtained by aggregating ratings given by u on items similar to i as follows:

$$\hat{r}_{u,i} = \frac{\sum_{j \in S^{(i)}} r_{u,j} \cdot w_{i,j}}{\sum_{j \in S^{(i)}} |w_{i,j}|}$$

```
def predict(userid, itemid):
    """
    Make rating prediction for user userid on item itemid
    :param userid : id of the active user
    :param itemid : id of the item for which we are making prediction
    :return r_hat : predicted rating
    """

    # Get items similar to item itemid with their corresponding similarities
    item_neighbors = neighbors[itemid]
    item_similarities = similarities[itemid]

    # get ratings of user with id userid
    uratings = np_ratings[np_ratings[:, 0].astype('int') == userid]

    # similar items rated by item the user of i
    siru = uratings[np.isin(uratings[:, 1], item_neighbors)]
    scores = siru[:, 2]
    indexes = [np.where(item_neighbors == iid)[0][0] for iid in siru[:,1].astype('int')]
    sims = item_similarities[indexes]

    dot = np.dot(scores, sims)
    som = np.sum(np.abs(sims))

    if dot == 0 or som == 0:
        return mean[userid]

    return dot / som
```

Now let's use our `predict()` function to predict what ratings the user would have given to the previous top-N list and return the reorganised list (in decreasing order of predictions) as the new top-N list

```
def topn_prediction(userid):
    """
    :param userid : id of the active user
    :return topn : initial topN recommendations returned by the function item2item_topN
    :return topn_predict : topN recommendations reordered according to rating predictions
    """
    # membuat rekomendasi N teratas untuk pengguna aktif
    topn = topn_recommendation(userid)

    # memperoleh daftar produk N teratas
    itemids = topn.itemid.to_list()

    predictions = []

    # membuat prediksi utnuk setiap produk pada daftar N teratas
    for itemid in itemids:
        r = predict(userid, itemid)

        predictions.append((itemid,r))

    predictions = pd.DataFrame(predictions, columns=['itemid','prediction'])

    # menggabungkan prediksi ke topN_list dan menyusun kembali daftar berdasarkan prediksi
    topn_predict = pd.merge(topn, predictions, on='itemid', how='inner')
    topn_predict = topn_predict.sort_values(by=['prediction'], ascending=False)

    return topn, topn_predict
```

Now, let's make recommendation for user 1 and compare the two list

```
topn, topn_predict = topn_prediction(userid=test_user)
```

```
topn_predict
```

	itemid	similarity_with_Iu	title	prediction
7	1388	26.624397	Gabbeh (1996)	4.666667
18	359	22.973658	Assignment, The (1997)	4.600000
4	1554	27.364494	Safe Passage (1994)	4.500000
14	1538	24.492453	All Over Me (1997)	4.500000
27	1448	20.846909	My Favorite Season (1993)	4.490052
29	1375	20.627152	Cement Garden, The (1993)	4.333333
26	1466	21.063269	Margaret's Museum (1995)	4.271915
2	1516	31.133267	Wedding Gift, The (1994)	4.000000
23	1467	21.861203	Saint of Fort Washington, The (1993)	4.000000
21	1537	22.061914	Cosi (1996)	4.000000
10	1378	25.787842	Rhyme & Reason (1997)	4.000000
19	1369	22.710078	Forbidden Christ, The (Cristo proibito, Il) (1...	4.000000
3	1550	31.031738	Destiny Turns on the Radio (1995)	3.777778
1	1189	50.362199	Prefontaine (1997)	3.666528
20	1506	22.325504	Nelly & Monsieur Arnaud (1995)	3.610294
15	1485	24.345312	Colonel Chabert, Le (1994)	3.610294
11	1664	25.327445	8 Heads in a Duffel Bag (1997)	3.610294
9	691	26.461802	Dark City (1998)	3.610294
6	1223	26.631850	King of the Hill (1993)	3.610294
5	1600	27.287712	Guantanamera (1994)	3.610294
17	909	23.357301	Dangerous Beauty (1998)	3.500000
12	1261	24.785660	Run of the Country, The (1995)	3.333333
24	1255	21.750924	Broken English (1996)	3.265749
13	1123	24.524028	Last Time I Saw Paris, The (1954)	3.200000
16	1450	24.262120	Golden Earrings (1947)	3.142978
22	1474	21.877034	Nina Takes a Lover (1994)	3.000000
8	766	26.590175	Man of the Year (1995)	3.000000
0	1356	52.867173	Ed's Next Move (1996)	2.280926
28	927	20.730153	Flower of My Secret, The (Flor de mi secreto, ...	1.665010
25	1499	21.529748	Grosse Fatigue (1994)	1.122032

As you will have noticed, the two lists are sorted in different ways. The second list is organized according to the predictions made for the user.

Note: When making predictions for user u on item i, user u may not have rated any of the k most similar items to i. In this case, we consider the mean rating of u as the predicted value.

Evaluation with Mean Absolute Error

```
from recsys.preprocessing import train_test_split, get_examples

# memperoleh contoh sebagai tuple userid dan itemid, dan label dari rating yang dinormalkan
raw_examples, raw_labels = get_examples(ratings, labels_column='rating')

# pemisahan data uji dan data pelatihan
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

def evaluate(x_test, y_test):
    print('Evaluate the model on {} test data ...'.format(x_test.shape[0]))
    preds = list(predict(u,i) for (u,i) in x_test)
    mae = np.sum(np.absolute(y_test - np.array(preds))) / x_test.shape[0]
    print('\nMAE :', mae)
    return mae
```

```
evaluate(x_test, y_test)
```

```
Evaluate the model on 10000 test data ...

MAE : 0.672389703640273
0.672389703640273
```

Summary

As with the User-based CF, we have also summarised the Item-based CF into the python class ItemToItem.

ItemToItem : usage

```
from recsys.memories.ItemToItem import ItemToItem
from recsys.preprocessing import ids_encoder, train_test_split, get_examples
from recsys.datasets import ml100k

# memuat data
ratings, movies = ml100k.load()

# menyiapkan data
ratings, uencoder, iencoder = ids_encoder(ratings)

# memperoleh contoh sebagai tuple userid dan itemid, dan label dari rating yang dinormalkan
raw_examples, raw_labels = get_examples(ratings, labels_column='rating')

# pemisahan data uji dan data pelatihan
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)
```

Instanciate the ItemToItem CF

Parameters :

- `k` : number of neighbors to consider for each item
- `metric` : metric to use when computing similarities : let's use **cosine**
- `dataset_name` : in this example, we use the ml100k dataset

```
# membuat CF berbasis produk
item2item = ItemToItem(ratings, movies, k=20, metric='cosine', dataset_name='ml100k')
```

```
Normalize ratings ...
Create the similarity model ...
Compute nearest neighbors ...
Item to item recommendation model created with success ...
```

```
# mengevaluasi algoritma pada dataset uji
item2item.evaluate(x_test, y_test)
```

```
Evaluate the model on 10000 test data ...

MAE : 0.507794195659005
0.507794195659005
```

Evaluate the Item-based CF on the ML-1M dataset

```
from recsys.memories.ItemToItem import ItemToItem
from recsys.preprocessing import ids_encoder, train_test_split, get_examples
from recsys.datasets import ml1m

# memuat data
ratings, movies = ml1m.load()

# menyiapkan data
ratings, uencoder, iencoder = ids_encoder(ratings)

# memperoleh contoh sebagai tuple userid dan itemid, dan label dari rating yang dinormalkan
raw_examples, raw_labels = get_examples(ratings, labels_column='rating')
```

```
# pemisahan data uji dan data pelatihan
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

# membuat CF berbasis produk
item2item = ItemToItem(ratings, movies, k=20, metric='cosine', dataset_name='ml1m')

# mengevaluasi algoritma dataset uji
print("========================")
item2item.evaluate(x_test, y_test)
     Download data 100.1%
     Successfully downloaded ml-1m.zip 5917549 bytes.
     Unzipping the ml-1m.zip zip file ...
     Normalize ratings ...
     Create the similarity model ...
     Compute nearest neighbors ...
     Item to item recommendation model created with success ...
     ========================
     Evaluate the model on 100021 test data ...

     MAE : 0.42514728655396045
     0.42514728655396045
```

Model based CF

User-based and **Item-based CF** are memory based algorithms. They directly act on the user-item interactions to compute recommendation. To the contrary, model-based algorithms are mathematical models trained on the user-item interactions and used to predict recommendation.

We will start with the SVD (Singular Value Decomposition) algorithm. Click here to go to SVD.

References

1. George Karypis (2001)Evaluation of Item-Based Top-N Recommendation Algorithms
2. Sarwar et al. (2001) Item-based collaborative filtering recommendation algorithms
3. Michael D. Ekstrand, et al. (2011). Collaborative Filtering Recommender Systems
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5. Greg Linden, Brent Smith, and Jeremy York (2003) Amazon.com Recommendations : Item-to-Item Collaborative Filtering

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4. Singular Value Decomposition

Open in Colab

Due to the high level sparsity of the rating matrix R, **user-based** and **item-based** collaborative filtering suffer from **data sparsity** and **scalability**. These cause user and item-based collaborative filtering to be less effective and highly affect their performences.

To address the high level sparsity problem, Sarwar et al. (2000) proposed to reduce the dimensionality of the rating R using the *Singular Value Decomposition (SVD)* algorithm.

How do SVD works ?

As described is Figure 1, SVD factors the rating matrix R of size $m \times n$ into three matrices P, Σ and Q as follows :

$$R = P\Sigma Q^\top .$$

Here, P and Q are two orthogonal matrices of size $m \times \hat{k}$ and $n \times \hat{k}$ respectively and Σ is a diagonal matrix of size $\hat{k} \times \hat{k}$ (with $\hat{k}$ the rank of matrix R) having all singular values of the rating matrix R as its diagonal entries (Billsus and Pazzani, 1998, Sarwar et al. (2000)).

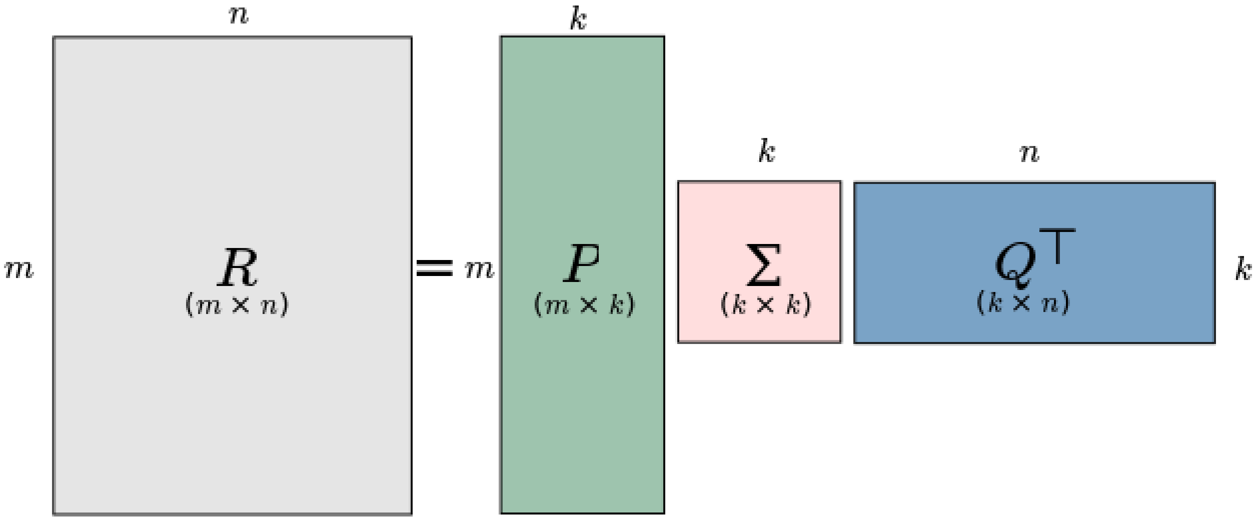

Figure 1 : Singular value decomposition of rating matrix R

After having choosen k, the dimension of factors that will represent users and items, we can truncate matrix Σ by only retaining its k largest singular values to yield Σ_k and reduce matrices P and Q accordingly to obtain P_k and Q_k. The rating matrix will then be estimated as

$$R_k = P_k \Sigma_k Q_k^\top .$$

Once these matrices are known, they can be used for rating predictions ant top-N recommendations. $P_k\Sigma_k^{\frac{1}{2}}$ represents the latent space of users and $\Sigma_k^{\frac{1}{2}}Q_k^\top$ the latent space of items. Rating prediction for user u on i is done by the following formular

$$\hat{R}_{u,i} = \left[P_k \Sigma_k^{\frac{1}{2}} \right]_u \left[\Sigma_k^{\frac{1}{2}} Q_k^\top \right]_i.$$

Before applying SVD, its important to fill in missing values of the rating matrix R. Sarwar et al. (2000) found the item's mean rating to be useful default values. The user's average rating can also be used but the former shown better performances. Adding ratings normalization by subtracting the user mean rating or other baseline predictor can improve accuracy.

SVD algorithm

> 1. Factor the normalize rating matrix R_{norm} to obtain matrices P, Σ and Q
> 2. Reduce Σ to dimension k to obtain Σ_k
> 3. Compute the square-root of Σ_k to obtain $\Sigma_k^{\frac{1}{2}}$
> 4. Compute the resultant matrices $P_k \Sigma_k^{\frac{1}{2}}$ and $\Sigma_k^{\frac{1}{2}} Q_k^\top$ that will be used to compute recommendation scores for any user and items.

Implementation details

SVD can easily be implemented using python library such as `numpy`, `scipy` or `sklearn`. As described by Andrew Ng in his Machine Learning course, it's not recommended to implement the standard SVD by ourselves. Instead, we can take advantage of matrix libraries (such as those listed before) that are optimized for matrix computations and vectorization.

Now let's implement the SVD collaborative filtering

Download useful tools

```
#mengekstrak file
import os

if not (os.path.exists("recsys.zip") or os.path.exists("recsys")):
    !wget https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/rec
    !unzip recsys.zip
```

```
--2023-01-04 03:00:53--  https://github.com/nzhinusoftcm/review-on-collaborative-f
Resolving github.com (github.com)... 140.82.113.3
Connecting to github.com (github.com)|140.82.113.3|:443... connected.
HTTP request sent, awaiting response... 302 Found
Location: https://raw.githubusercontent.com/nzhinusoftcm/review-on-collaborative-f
--2023-01-04 03:00:53--  https://raw.githubusercontent.com/nzhinusoftcm/review-on-
Resolving raw.githubusercontent.com (raw.githubusercontent.com)... 185.199.108.133
Connecting to raw.githubusercontent.com (raw.githubusercontent.com)|185.199.108.13
HTTP request sent, awaiting response... 200 OK
Length: 15312323 (15M) [application/zip]
Saving to: ‘recsys.zip’

recsys.zip          100%[===================>]  14.60M  91.3MB/s    in 0.2s
```

```
2023-01-04 03:00:54 (91.3 MB/s) - ‘recsys.zip’ saved [15312323/15312323]

Archive:  recsys.zip
   creating: recsys/
  inflating: recsys/datasets.py
  inflating: recsys/preprocessing.py
  inflating: recsys/utils.py
  inflating: recsys/requirements.txt
   creating: recsys/.vscode/
  inflating: recsys/.vscode/settings.json
   creating: recsys/__pycache__/
  inflating: recsys/__pycache__/datasets.cpython-36.pyc
  inflating: recsys/__pycache__/datasets.cpython-37.pyc
  inflating: recsys/__pycache__/utils.cpython-36.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-37.pyc
  inflating: recsys/__pycache__/datasets.cpython-38.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-36.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-38.pyc
   creating: recsys/memories/
  inflating: recsys/memories/ItemToItem.py
  inflating: recsys/memories/UserToUser.py
   creating: recsys/memories/__pycache__/
  inflating: recsys/memories/__pycache__/UserToUser.cpython-36.pyc
  inflating: recsys/memories/__pycache__/UserToUser.cpython-37.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-37.pyc
  inflating: recsys/memories/__pycache__/user2user.cpython-36.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-36.pyc
   creating: recsys/models/
  inflating: recsys/models/SVD.py
  inflating: recsys/models/MatrixFactorization.py
  inflating: recsys/models/ExplainableMF.py
  inflating: recsys/models/NonnegativeMF.py
   creating: recsys/models/__pycache__/
  inflating: recsys/models/__pycache__/SVD.cpython-36.pyc
  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-37.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-36.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-37.pyc
  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-36.pyc
   creating: recsys/metrics/
  inflating: recsys/metrics/EvaluationMetrics.py
   creating: recsys/img/
  inflating: recsys/img/MF-and-NNMF.png
```

Import requirements

```
matplotlib==3.2.2
numpy==1.19.2
pandas==1.0.5
python==3.7
scikit-learn==0.24.1
scikit-surprise==1.1.1
scipy==1.6.2
```

```
from recsys.datasets import mlLatestSmall, ml100k, ml1m
from sklearn.preprocessing import LabelEncoder
from scipy.sparse import csr_matrix

import pandas as pd
import numpy as np
import os
```

Loading movielen ratings

```
#mengunduh data yang akan diolah
ratings, movies = mlLatestSmall.load()
```

```
Download data 100.5%
Successfully downloaded ml-latest-small.zip 978202 bytes.
Unzipping the ml-latest-small.zip zip file ...
```

Let's see how our rating matrix looks like

```
pd.crosstab(ratings.userid, ratings.itemid, ratings.rating, aggfunc=sum)
```

itemid	1	2	3	4	5	6	7	8	9	10
userid										
1	4.0	NaN	4.0	NaN	NaN	4.0	NaN	NaN	NaN	NaN
2	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
3	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
4	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
5	4.0	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
...	...	...	...	...	...	...	...	...	...	...
606	2.5	NaN	NaN	NaN	NaN	NaN	2.5	NaN	NaN	NaN
607	4.0	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN

We can observe that our rating matrix has many of unobserved value. However, as we described earlier, the SVD algorithm requires that all inputs in the matrix must be defined. Let's initialize the unobserved ratings with item's average that led to better performances compared to the user's average or even a null initialization (Sarwar et al. (2000)).

We can go further and subtrat from each rating the corresponding user mean to normalize the data. This helps to improve the accuracy of the model.

```
# mendapatkan rating rata-rata pengguna
umean = ratings.groupby(by='userid')['rating'].mean()


def rating_matrix(ratings):
    """
    1. Fill NaN values with item's average ratings
    2. Normalize ratings by subtracting user's mean ratings

    :param ratings : DataFrame of ratings data
    :return
        - R : Numpy array of normalized ratings
        - df : DataFrame of normalized ratings
    """

    # mengisi nilai kosong dengan rating rata-rata produk
    df = pd.crosstab(ratings.userid, ratings.itemid, ratings.rating, aggfunc=sum)
    df = df.fillna(df.mean(axis=0))

    # megurangkan rating rat-rata pengguna untuk menormalkan data
    df = df.subtract(umean, axis=0)

    # mengubah dataframe ke dalam bentuk numpy array
    R = df.to_numpy()

    return R, df

# menghasilkan matriks rating dengan memanggil fungsi rating_matrix
R, df = rating_matrix(ratings)
```

R is our final rating matrix. This is how the final rating matrix looks like

```
df
```

itemid	1	2	3	4	5	
userid						
1	-0.366379	-0.934561	-0.366379	-2.009236	-1.294951	-0.
2	-0.027346	-0.516458	-0.688660	-1.591133	-0.876847	-0.
3	1.485033	0.995921	0.823718	-0.078755	0.635531	1.

Ids encoding

Let's encode users and items ids such that their values range from 0 to 909 (for users) and from 0 to 9723 (for items)

```
users = sorted(ratings['userid'].unique())
items = sorted(ratings['itemid'].unique())

# membuat pengkode/ penyandi id
uencoder = LabelEncoder()
iencoder = LabelEncoder()

# menyesuaikan label pengkode/ penyandi
uencoder.fit(users)
iencoder.fit(items)
```

```
    LabelEncoder()
```

SVD Algorithm

Now that our rating data has been normalize and that missing values has been filled, we can apply the SVD algorithm. Several libraries may be useful such as `numpy`, `scipy`, `sklearn`, ... Let's try it with `numpy`.

In our SVD class we provide the following function :

1. `fit()` : compute the svd of the rating matrix and save the resultant matrices P, S and Qh (Q transpose) as attributs of the SVD class.
2. `predict()` : use matrices P, S and Qh to make ratin prediction for a given u user on an item i. Computations are made over encoded values of userid and itemid. The predicted value is the dot product between u^{th} row of $P.\sqrt{S}$ and the i^{th} column of $\sqrt{S}.Qh$. **Note** that since we normalized rating before applying SVD, the predicted value will also be normalize. So, to get the final predicted rating, we have to add to the predicted value the mean rating of user u.
3. `recommend()` : use matrices P, S and Qh to make recommendations to a given user. The recommended items are those that where not rated by the user and received a high score according to the svd model.

```
class SVD:

    def __init__(self, umeam):
        """
        :param
            - umean : mean ratings of users
        """
        self.umean = umean.to_numpy()

        # init svd resultant matrices
        self.P = np.array([])
        self.S = np.array([])
        self.Qh = np.array([])

        # init users and items latent factors
        self.u_factors = np.array([])
        self.i_factors = np.array([])

    def fit(self, R):
        """
        Fit the SVD model with rating matrix R
        """
        P, s, Qh = np.linalg.svd(R, full_matrices=False)

        self.P = P
        self.S = np.diag(s)
        self.Qh = Qh

        # latent factors of users (u_factors) and items (i_factors)
        self.u_factors = np.dot(self.P, np.sqrt(self.S))
        self.i_factors = np.dot(np.sqrt(self.S), self.Qh)

    def predict(self, userid, itemid):
        """
        Make rating prediction for a given user on an item

        :param
            - userid : user's id
            - itemid : item's id

        :return
            - r_hat : predicted rating
        """
        # encode user and item ids
        u = uencoder.transform([userid])[0]
        i = iencoder.transform([itemid])[0]

        # the predicted rating is the dot product between the uth row
        # of u_factors and the ith column of i_factors
        r_hat = np.dot(self.u_factors[u,:], self.i_factors[:,i])

        # menambahkan rating rata-rata pengguna u ke nilai prediksi
        r_hat += self.umean[u]

        return r_hat
    def recommend(self, userid):
        """
        :param
            - userid : user's id
        """
        # menyandikan pengguna
        u = uencoder.transform([userid])[0]

        # dot product antara baris ke u dari u_factor dengan i_factors kembali
        # nilai prediksi untuk pengguna u pada semua produk
        predictions = np.dot(self.u_factors[u,:], self.i_factors) + self.umean[u]

        # mengurutkan id produk berdasarkan urutan prediksi menurun
        top_idx = np.flip(np.argsort(predictions))

        # decode indices to get their corresponding itemids
        top_items = iencoder.inverse_transform(top_idx)

        # urutan prediksi
        preds = predictions[top_idx]

        return top_items, preds
```

Now let's create our SVD model and provide to it user's mean rating; Fit the model with the normalized rating matrix R.

```
# membuat model svd
svd = SVD(umean)

# menyesuaikan model dengan rating yang dinormalisasikan
svd.fit(R)
```

Rating prediction

Our model has been fitted. OK ...

Let's make some predictions for users using function `predict` of our SVD class. Here are some truth ratings

```
ratings.head(10)
```

	userid	itemid	rating	timestamp
0	1	1	4.0	964982703
1	1	3	4.0	964981247
2	1	6	4.0	964982224
3	1	47	5.0	964983815
4	1	50	5.0	964982931
5	1	70	3.0	964982400

Let's apply our model to make see if our predictions make sens. We will make predictions for user 1 on the 10 items listed above.

```
# pengguna yang diprediksi
userid = 1

# daftar produk yang akan dibuat prediksi untuk pengguna 1
items = [1,3,6,47,50,70,101,110,151,157]

#prediksi
for itemid in items:
    r = svd.predict(userid=userid, itemid=itemid)
    print('prediction for userid={} and itemid={} : {}'.format(userid, itemid, r))
```

```
prediction for userid=1 and itemid=1 : 3.9999999999999996
prediction for userid=1 and itemid=3 : 4.0000000000000036
prediction for userid=1 and itemid=6 : 3.9999999999999867
prediction for userid=1 and itemid=47 : 5.0
prediction for userid=1 and itemid=50 : 4.9999999999999964
prediction for userid=1 and itemid=70 : 2.999999999999981
prediction for userid=1 and itemid=101 : 5.000000000000006
prediction for userid=1 and itemid=110 : 3.9999999999999862
prediction for userid=1 and itemid=151 : 5.0000000000000115
prediction for userid=1 and itemid=157 : 5.000000000000028
```

Our prediction error is less than 0.00001

Make recommendations

The `recommend` function makes recommendations for a given user.

```
userid = 1

# produk diurutkan berdasarkan prediksi untuk pengguna 1 (urutan menurun)
sorted_items, preds = svd.recommend(userid=userid)

##
# Mengecualikan dari daftar produk terurut yang sudah dibeli pengguna
##
```

```
    # daftar produk yang dirating pengguna
    uitems = ratings.loc[ratings.userid == userid].itemid.to_list()

    # remove from sorted_items items already in uitems and pick the top 30 ones
    # as recommendation list
    top30 = np.setdiff1d(sorted_items, uitems, assume_unique=True)[:30]

    # mendapatkan prediksi yang sesuai dari 30 produk teratas
    top30_idx = list(np.where(sorted_items == idx)[0][0] for idx in top30)
    top30_predictions = preds[top30_idx]

    # mencari judul film yang sesuai
    zipped_top30 = list(zip(top30,top30_predictions))
    top30 = pd.DataFrame(zipped_top30, columns=['itemid','predictions'])
    List = pd.merge(top30, movies, on='itemid', how='inner')

    # menunjukkan daftar
    List
```

	itemid	predictions	title	
0	148	5.0	Awfully Big Adventure, An (1995)	
1	6086	5.0	I, the Jury (1982)	Crime|D
2	136445	5.0	George Carlin: Back in Town (1996)	
3	6201	5.0	Lady Jane (1986)	Dran
4	2075	5.0	Mephisto (1981)	

The first 30 items have an equivalent rating prediction for the user 1

Voigt) (2002)

Improving memory based collaborative filtering

SVD can be applied to improve user and item-based collaborative filtering. Instead of computing similarities between user's or item's ratings, we can represent users and items by their corresponding latent factors extracted from the SVD algorithm.

8 6021 5.0 (Amerikanische Crime|Drama|My

Matrix Factorization

The **Matrix Factorization** algorithm is a variant of SVD. Also known as Regularized SVD, it uses the *Gradient Descent* optimizer to optimize the cost function while training the model.

Go to the Matrix Factorization variant of SVD.

10 136447 5.0 You Are All

Reference

1. Daniel Billsus and Michael J. Pazzani (1998). Learning Collaborative Information Filters
2. Sarwar et al. (2000). Application of Dimensionality Reduction in Recommender System – A Case Study

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● ✕

5. Matrix Factorization

Open in Colab

Matrix Factorization

User-based and **Item-based** collaborative Filtering recommender systems suffer from *data sparsity* and *scalability* for online recommendations. **Matrix Factorization** helps to address these drawbacks of memory-based collaborative filtering by reducing the dimension of the rating matrix R.

The movielen lasted small dataset has 100k ratings of $m = 610$ users on $n = 9724$ items. The rating matrix in then a $m \times n$ matrix (i.e $R \in \mathbb{R}^{m \times n}$). The fact that users usually interact with less than 1% of items leads the rating matrix R to be highly sparse. For example, the degree of sparsity of the movielen lasted small dataset is

$$sparsity = 100 - \frac{\text{total \# ratings}}{m \times n} = 100 - \frac{100000}{610 \times 9724} = 98,3\%$$

This means that in this dataset, a user has interacted with less than 2% of items. To reduce the dimension of the rating matrix R, Matrix Factorization (MF) mappes both users and items to a joint latent factor space of dimensionality k such that user-item interactions are modeled as inner products in that space (Yehuda Koren et al., 2009). MF then decomposes R in two matrices as follows :

$$R = Q^\top P$$

Where $P \in \mathbb{R}^{m \times k}$ represents latent factors of users and $Q \in \mathbb{R}^{n \times k}$ is the latent factors of items. Each line of P, say $p_u \in \mathbb{R}^k$ denotes the taste of user u and each $q_i \in \mathbb{R}^k$ the features of item i. The dot product between p_u and q_i will be the rating prediction of user u on item i :

$$\hat{r}_{u,i} = q_i^\top p_u.$$

Figure 1 presents an example of decomposition of R into two matrices P and Q.

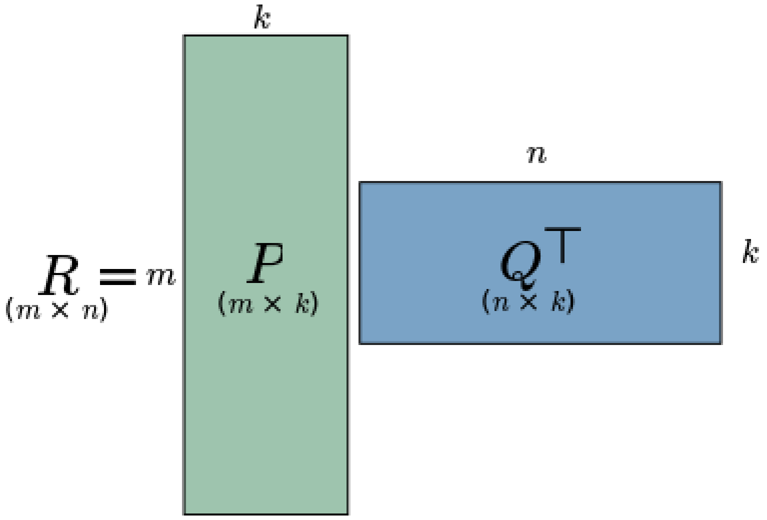
$\underset{(m \times n)}{R} = m$
k
$\underset{(m \times k)}{P}$
n
$\underset{(n \times k)}{Q^\top}$
k

Figure 1: Decomposition of R into P and Q

Learning Algorithms

As described in (Yehuda Koren et al., 2009), to minimize the cost function J, the matrix factorization algorithm predicts $\hat{r}_{u,i}$ for each given training case (existing $r_{u,i}$), and computes the associated error defined by the Mean Absolute Error (MAE) as :

$$e_{u,i} = |r_{ui} - q_i^\top p_u|.$$

Note : The overall error E is defined as :

$$E = \frac{1}{M} \sum_{(u,i)\in\kappa} e_{u,i}$$

Where M is the number of example. The update rules for parameters p_u and q_i are defined as follows :

$$q_i \leftarrow q_i - \alpha \frac{\partial}{\partial q_i} J_{u,i},$$
$$p_u \leftarrow p_u - \alpha \frac{\partial}{\partial p_u} J_{u,i}$$

where α is the learning rate and $\frac{\partial}{\partial p_u} J_{u,i}$ is the partial derivative of the cost function J according to p_u. It computes the extent to which p_u contributes to the total error.

How to compute $\frac{\partial}{\partial q_i} J_{u,i}$?

$$\begin{aligned} \frac{\partial}{\partial q_i} J_{u,i} &= \frac{1}{2} \frac{\partial}{\partial q_i} \left[(r_{ui} - q_i^\top p_u)^2 + \lambda(||p_u||^2 + ||q_i||^2) \right] \\ &= -(r_{u,i} - q_i^\top p_u) \cdot p_u + \lambda \cdot q_i \\ &= -e_{u,i} \cdot p_u + \lambda \cdot q_i \end{aligned}$$

The update rules are then given by :

$$q_i \leftarrow q_i + \alpha \cdot (e_{u,i} \cdot p_u - \lambda \cdot q_i),$$
$$p_u \leftarrow p_u + \alpha \cdot (e_{u,i} \cdot q_i - \lambda \cdot p_u)$$

Matrix Factorization : algorithm

1. Initialize P and Q with random values
2. For each training example $(u,i)\in\kappa$ with the corresponding rating $r_{u,i}$:
    - compute $\hat{r}_{u,i}$ as $\hat{r}_{u,i} = q_{i}^{\top} p_u$
    - compute the error : $e_{u,i} = |r_{ui} - \hat{r}_{u,i}|$
    - update p_u and q_i:
        - $p_u \leftarrow p_u + \alpha\cdot (e_{u,i}\cdot q_i-\lambda \cdot p_u)$
        - $q_i \leftarrow q_i + \alpha\cdot (e_{u,i}\cdot p_u-\lambda \cdot q_i)$

3. Repeat step 2 until the optimal parameters are reached.

Download useful files

```
import os
if not (os.path.exists("recsys.zip") or os.path.exists("recsys")):
    !wget https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/rec
    !unzip recsys.zip
```

```
--2023-01-04 03:05:02--  https://github.com/nzhinusoftcm/review-on-collaborative-f
Resolving github.com (github.com)... 140.82.121.4
Connecting to github.com (github.com)|140.82.121.4|:443... connected.
HTTP request sent, awaiting response... 302 Found
Location: https://raw.githubusercontent.com/nzhinusoftcm/review-on-collaborative-f
--2023-01-04 03:05:02--  https://raw.githubusercontent.com/nzhinusoftcm/review-on-
Resolving raw.githubusercontent.com (raw.githubusercontent.com)... 185.199.109.133
Connecting to raw.githubusercontent.com (raw.githubusercontent.com)|185.199.109.13
HTTP request sent, awaiting response... 200 OK
Length: 15312323 (15M) [application/zip]
Saving to: ‘recsys.zip’

recsys.zip          100%[===================>]  14.60M  --.-KB/s    in 0.06s

2023-01-04 03:05:04 (259 MB/s) - ‘recsys.zip’ saved [15312323/15312323]

Archive:  recsys.zip
   creating: recsys/
  inflating: recsys/datasets.py
  inflating: recsys/preprocessing.py
  inflating: recsys/utils.py
  inflating: recsys/requirements.txt
   creating: recsys/.vscode/
  inflating: recsys/.vscode/settings.json
   creating: recsys/__pycache__/
  inflating: recsys/__pycache__/datasets.cpython-36.pyc
  inflating: recsys/__pycache__/datasets.cpython-37.pyc
  inflating: recsys/__pycache__/utils.cpython-36.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-37.pyc
  inflating: recsys/__pycache__/datasets.cpython-38.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-36.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-38.pyc
   creating: recsys/memories/
  inflating: recsys/memories/ItemToItem.py
  inflating: recsys/memories/UserToUser.py
   creating: recsys/memories/__pycache__/
  inflating: recsys/memories/__pycache__/UserToUser.cpython-36.pyc
  inflating: recsys/memories/__pycache__/UserToUser.cpython-37.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-37.pyc
  inflating: recsys/memories/__pycache__/user2user.cpython-36.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-36.pyc
   creating: recsys/models/
  inflating: recsys/models/SVD.py
  inflating: recsys/models/MatrixFactorization.py
  inflating: recsys/models/ExplainableMF.py
  inflating: recsys/models/NonnegativeMF.py
   creating: recsys/models/__pycache__/
  inflating: recsys/models/__pycache__/SVD.cpython-36.pyc
  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-37.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-36.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-37.pyc
  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-36.pyc
   creating: recsys/metrics/
  inflating: recsys/metrics/EvaluationMetrics.py
   creating: recsys/img/
  inflating: recsys/img/MF-and-NNMF.png
```

Import requirements

```
matplotlib==3.2.2

numpy==1.19.2

pandas==1.0.5

python==3.7

scikit-learn==0.24.1

scikit-surprise==1.1.1

scipy==1.6.2
```

```python
from recsys.preprocessing import mean_ratings
from recsys.preprocessing import normalized_ratings
from recsys.preprocessing import ids_encoder
from recsys.preprocessing import train_test_split
from recsys.preprocessing import rating_matrix
from recsys.preprocessing import get_examples
from recsys.preprocessing import scale_ratings

from recsys.datasets import ml100k
from recsys.datasets import ml1m

import matplotlib.pyplot as plt
import pandas as pd
import numpy as np

import os
```

Model definition

```python
class MatrixFactorization:

    def __init__(self, m, n, k=10, alpha=0.001, lamb=0.01):
        """
        Initialization of the model
        : param
            - m : number of users
            - n : number of items
            - k : length of latent factor, both for users and items. 50 by default
            - alpha : learning rate. 0.001 by default
            - lamb : regularizer parameter. 0.02 by default
        """
        np.random.seed(32)

        # initialize the latent factor matrices P and Q (of shapes (m,k) and (n,k) respect
        self.k = k
        self.P = np.random.normal(size=(m, k))
        self.Q = np.random.normal(size=(n, k))

        # hyperparameter initialization
        self.alpha = alpha
        self.lamb = lamb

        # training history
        self.history = {
            "epochs":[],
            "loss":[],
            "val_loss":[],
            "lr":[]
        }

    def print_training_parameters(self):
        print('Training Matrix Factorization Model ...')
        print(f'k={self.k} \t alpha={self.alpha} \t lambda={self.lamb}')

    def update_rule(self, u, i, error):
        self.P[u] = self.P[u] + self.alpha * (error * self.Q[i] - self.lamb * self.P[u])
        self.Q[i] = self.Q[i] + self.alpha * (error * self.P[u] - self.lamb * self.Q[i])

    def mae(self,  x_train, y_train):
        """
        returns the Mean Absolute Error
        """
        # number of training exemples
        M = x_train.shape[0]
        error = 0
        for pair, r in zip(x_train, y_train):
            u, i = pair
            error += abs(r - np.dot(self.P[u], self.Q[i]))
        return error/M

    def print_training_progress(self, epoch, epochs, error, val_error, steps=5):
        if epoch == 1 or epoch % steps == 0 :
                print("epoch {}/{} - loss : {} - val_loss : {}".format(epoch, epochs, roun

    def learning_rate_schedule(self, epoch, target_epochs = 20):
        if (epoch >= target_epochs) and (epoch % target_epochs == 0):
                factor = epoch // target_epochs
                self.alpha = self.alpha * (1 / (factor * 20))
                print("\nLearning Rate : {}\n".format(self.alpha))

    def fit(self, x_train, y_train, validation_data, epochs=1000):
        """
        Train latent factors P and Q according to the training set
        :param
            - x_train : training pairs (u,i) for which rating r_ui is known
            - y_train : set of ratings r_ui for all training pairs (u,i)
            - validation_data : tuple (x_test, y_test)
            - epochs : number of time to loop over the entire training set.
            1000 epochs by default

        Note that u and i are encoded values of userid and itemid
        """
        self.print_training_parameters()

        # validation data
        x_test, y_test = validation_data

        # loop over the number of epochs
        for epoch in range(1, epochs+1):

            # for each pair (u,i) and the corresponding rating r
            for pair, r in zip(x_train, y_train):

                # get encoded values of userid and itemid from pair
                u,i = pair

                # compute the predicted rating r_hat
                r_hat = np.dot(self.P[u], self.Q[i])

                # compute the prediction error
                e = abs(r - r_hat)

                # update rules
                self.update_rule(u, i, e)

            # training and validation error  after this epochs
            error = self.mae(x_train, y_train)
            val_error = self.mae(x_test, y_test)

            # update history
            self.history['epochs'].append(epoch)
            self.history['loss'].append(error)
            self.history['val_loss'].append(val_error)

            # update history
            self.update_history(epoch, error, val_error)

            # print training progress after each steps epochs
            self.print_training_progress(epoch, epochs, error, val_error, steps=1)

            # leaning rate scheduler : redure the learning rate as we go deeper in the num
            # self.learning_rate_schedule(epoch)

        return self.history

    def update_history(self, epoch, error, val_error):
        self.history['epochs'].append(epoch)
        self.history['loss'].append(error)
        self.history['val_loss'].append(val_error)
        self.history['lr'].append(self.alpha)

    def evaluate(self, x_test, y_test):
        """
        compute the global error on the test set
        :param x_test : test pairs (u,i) for which rating r_ui is known
        :param y_test : set of ratings r_ui for all test pairs (u,i)
        """
        error = self.mae(x_test, y_test)
        print(f"validation error : {round(error,3)}")

        return error

    def predict(self, userid, itemid):
        """
        Make rating prediction for a user on an item
        :param userid
        :param itemid
        :return r : predicted rating
        """
        # encode user and item ids to be able to access their latent factors in
        # matrices P and Q
        u = uencoder.transform([userid])[0]
        i = iencoder.transform([itemid])[0]

        # rating prediction using encoded ids. Dot product between P_u and Q_i
        r = np.dot(self.P[u], self.Q[i])
        return r

    def recommend(self, userid, N=30):
        """
        make to N recommendations for a given user

        :return(top_items,preds) : top N items with the highest predictions
        with their corresponding predictions
        """
        # encode the userid
        u = uencoder.transform([userid])[0]

        # predictions for users userid on all product
        predictions = np.dot(self.P[u], self.Q.T)

        # get the indices of the top N predictions
        top_idx = np.flip(np.argsort(predictions))[:N]

        # decode indices to get their corresponding itemids
        top_items = iencoder.inverse_transform(top_idx)

        # take corresponding predictions for top N indices
        preds = predictions[top_idx]

        return top_items, preds
```

```
epochs = 10
```

1. MovieLens 100k

Evaluation on raw ratings

```
# memuat dataset ml100k
ratings, movies = ml100k.load()

ratings, uencoder, iencoder = ids_encoder(ratings)

m = ratings.userid.nunique()   # total number of users
n = ratings.itemid.nunique()   # total number of items

# memperoleh contoh sebagai tuple dari userid dan itemid dan label dari rating yang dinorm
raw_examples, raw_labels = get_examples(ratings)

# pemisahan antara data uji dan data latih
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_
```

```
    Download data 100.2%
    Successfully downloaded ml-100k.zip 4924029 bytes.
    Unzipping the ml-100k.zip zip file ...
```

```
# membuat model
MF = MatrixFactorization(m, n, k=10, alpha=0.01, lamb=1.5)

# menyesuaikan model pada himpunan pelatihan
history = MF.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))
```

```
    Training Matrix Factorization Model ...
    k=10     alpha=0.01      lambda=1.5
    epoch 1/10 - loss : 2.734 - val_loss : 2.779
    epoch 2/10 - loss : 1.764 - val_loss : 1.794
    epoch 3/10 - loss : 1.592 - val_loss : 1.614
    epoch 4/10 - loss : 1.538 - val_loss : 1.556
    epoch 5/10 - loss : 1.515 - val_loss : 1.531
    epoch 6/10 - loss : 1.503 - val_loss : 1.517
    epoch 7/10 - loss : 1.496 - val_loss : 1.509
    epoch 8/10 - loss : 1.491 - val_loss : 1.504
    epoch 9/10 - loss : 1.488 - val_loss : 1.5
    epoch 10/10 - loss : 1.486 - val_loss : 1.497
```

```
MF.evaluate(x_test, y_test)
```

```
    validation error : 1.497
    1.4973507972141993
```

Evaluation on normalized ratings

```
# memuat data
ratings, movies = ml100k.load()

ratings, uencoder, iencoder = ids_encoder(ratings)

m = ratings['userid'].nunique()   # total number of users
n = ratings['itemid'].nunique()   # total number of items

# normalisasi rating dengan mengurangkan rata-rata
normalized_column_name = "norm_rating"
ratings = normalized_ratings(ratings, norm_column=normalized_column_name)

# mendapatkan contoh sebagai tuple dari userid dan itemid dan label dari normalisasi ratin
raw_examples, raw_labels = get_examples(ratings, labels_column=normalized_column_name)

# pemisahan data uji dan data latih
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_


# membuat model
MF = MatrixFactorization(m, n, k=10, alpha=0.01, lamb=1.5)

# menyesuaikan model pada data latih
history = MF.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))
```

```
     Training Matrix Factorization Model ...
     k=10     alpha=0.01      lambda=1.5
     epoch 1/10 - loss : 0.851 - val_loss : 0.847
     epoch 2/10 - loss : 0.831 - val_loss : 0.831
     epoch 3/10 - loss : 0.828 - val_loss : 0.829
     epoch 4/10 - loss : 0.827 - val_loss : 0.828
     epoch 5/10 - loss : 0.827 - val_loss : 0.828
     epoch 6/10 - loss : 0.826 - val_loss : 0.828
     epoch 7/10 - loss : 0.826 - val_loss : 0.828
     epoch 8/10 - loss : 0.826 - val_loss : 0.828
     epoch 9/10 - loss : 0.826 - val_loss : 0.828
     epoch 10/10 - loss : 0.826 - val_loss : 0.828
```

```
MF.evaluate(x_test, y_test)
```

```
     validation error : 0.828
     0.8276982643684648
```

2. MovieLens 1M

Evaluation on raw data

```
# memuat dataset ml1m
ratings, movies = ml1m.load()
```

```
ratings, uencoder, iencoder = ids_encoder(ratings)

m = ratings.userid.nunique()   # jumlah pengguna
n = ratings.itemid.nunique()   # jumlah item

# mendapatkan contoh sebagai tuple dari userid dan itemid dan label dari normalisasi ratin
raw_examples, raw_labels = get_examples(ratings)

# pemisahan data uji dan data latih
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_
     Download data 100.1%
     Successfully downloaded ml-1m.zip 5917549 bytes.
     Unzipping the ml-1m.zip zip file ...
```

```
# membuat model
MF = MatrixFactorization(m, n, k=10, alpha=0.01, lamb=1.5)

# menyesuaikan model pada data latih
history = MF.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))

     Training Matrix Factorization Model ...
     k=10     alpha=0.01      lambda=1.5
     epoch 1/10 - loss : 1.713 - val_loss : 1.718
     epoch 2/10 - loss : 1.523 - val_loss : 1.526
     epoch 3/10 - loss : 1.496 - val_loss : 1.498
     epoch 4/10 - loss : 1.489 - val_loss : 1.489
     epoch 5/10 - loss : 1.485 - val_loss : 1.486
     epoch 6/10 - loss : 1.484 - val_loss : 1.484
     epoch 7/10 - loss : 1.483 - val_loss : 1.483
     epoch 8/10 - loss : 1.483 - val_loss : 1.483
     epoch 9/10 - loss : 1.482 - val_loss : 1.482
     epoch 10/10 - loss : 1.482 - val_loss : 1.482
```

```
MF.evaluate(x_test, y_test)

     validation error : 1.482
     1.4820034560467208
```

Evaluation on normalized ratings

```
# memuat data
ratings, movies = ml1m.load()

ratings, uencoder, iencoder = ids_encoder(ratings)

m = ratings['userid'].nunique()   # total number of users
n = ratings['itemid'].nunique()   # total number of items

# normalisasi rating dengan pengurangan rata-rata
normalized_column_name = "norm_rating"
ratings = normalized_ratings(ratings, norm_column=normalized_column_name)
```

```
# mendapatkan contoh sebagai tuple dari userid dan itemid dan label dari rating yang dinor
raw_examples, raw_labels = get_examples(ratings, labels_column=normalized_column_name)

# pemisahan antara data uji dan data latih
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_

# membuat model
MF = MatrixFactorization(m, n, k=10, alpha=0.01, lamb=1.5)

# menyesuaikan model pada himpunan pelatihan
history = MF.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))
```

```
Training Matrix Factorization Model ...
k=10     alpha=0.01      lambda=1.5
epoch 1/10 - loss : 0.826 - val_loss : 0.827
epoch 2/10 - loss : 0.824 - val_loss : 0.825
epoch 3/10 - loss : 0.823 - val_loss : 0.825
epoch 4/10 - loss : 0.823 - val_loss : 0.825
epoch 5/10 - loss : 0.823 - val_loss : 0.825
epoch 6/10 - loss : 0.823 - val_loss : 0.825
epoch 7/10 - loss : 0.823 - val_loss : 0.825
epoch 8/10 - loss : 0.823 - val_loss : 0.825
epoch 9/10 - loss : 0.823 - val_loss : 0.825
epoch 10/10 - loss : 0.823 - val_loss : 0.825
```

```
MF.evaluate(x_test, y_test)
```

```
validation error : 0.825
0.8250208634455388
```

Predictions

Now that the latent factors P and Q, we can use them to make predictions and recommendations. Let's call the `predict` function of the `Matrix Factorization` class to make prediction for a given.

rating prediction for user 1 on item 1 for which the truth rating $r = 5.0$

```
ratings.userid = uencoder.inverse_transform(ratings.userid.to_list())
ratings.itemid = uencoder.inverse_transform(ratings.itemid.to_list())
ratings.head(5)
```

```
        userid  itemid  rating  rating_mean  norm_rating
```

```
4.188679 + MF.predict(userid=1, itemid=1) # menambahkan rata-rata karena harus menggunakan
```

```
4.188679163563357
```

```
     2       1     145      5     4.188679     0.811321
```

Summary

This is the link to the MatrixFactorization class : MatrixFactorization.py

Non-negative Matrix Factorization

With the Matrix Factorization model, P and Q latent factors are non interpretable since they contain arbitrary negative or positive values. This make the Matrix Factorization model to be non explainable.

The **Non-negative Matrix Factorization (NMF)** algorithm is a variant of Matrix Factorization which generate explainable latent factors for P and Q by constraining their values in the range [0,1]. This allow a probability interpretation of these latent factors, hense the explainability.

Click here to go to the NMF notebook.

6. Non Neagative Matrix Factorization

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Non-negative Matrix Factorization for Recommendations

Jusl like Matrix Factorization (MF) (Yehuda Koren et al., 2009), Non-negative Matrix Factorization (NMF in short) factors the rating matrix R in two matrices in such a way that $R = PQ^{\top}$.

One limitation of Matrix Factorization

P and Q values in MF are non interpretable since their components can take arbitrary (positive and negative) values.

Particulariy of Non-negative Matrix Factorization

NMF (Lee and Seung, 1999) allows the reconstruction of P and Q in such a way that $P, Q \geq 0$. Constraining P and Q values to be taken from $[0, 1]$ allows a probabilistic interpretation

- Latent factors represent groups of users who share the same tastes,
- The value $P_{u,l}$ represents the probability that user u belongs to the group l of users and
- The value $Q_{l,i}$ represents the probability that users in the group l likes item i.

Objective function

With the Euclidian distance, the NMF objective function is defined by

$$J = \frac{1}{2}\sum_{(u,i)\in\kappa} ||R_{u,i} - P_u Q_i^{\top}||^2 + \lambda_P||P_u||^2 + \lambda_Q||Q_i||^2$$

The goal is to minimize the cost function J by optimizing parameters P and Q, with λ_P and λ_Q the regularizer parameters.

Multiplicative update rule

According (Lee and Seung, 1999), to the multiplicative update rule for P and Q are as follows :

$$P \leftarrow P \cdot \frac{RQ}{PQ^{\top}Q}$$

$$Q \leftarrow Q \cdot \frac{R^{\top}P}{QP^{\top}P}$$

However, since R is a sparse matrix, we need to update each P_u according to existing ratings of user u. Similarily, we need to update Q_i according to existing ratings on item i. Hence :

$$P_{u,k} \leftarrow P_{u,k} \cdot \frac{\sum_{i\in I_u} Q_{i,k} \cdot r_{u,i}}{\sum_{i\in I_u} Q_{i,k} \cdot \hat{r}_{u,i} + \lambda_P|I_u|P_{u,k}}$$

$$Q_{i,k} \leftarrow Q_{i,k} \cdot \frac{\sum_{u\in U_i} P_{u,k} \cdot r_{u,i}}{\sum_{u\in U_i} P_{u,k} \cdot \hat{r}_{u,i} + \lambda_Q|U_i|Q_{i,k}}$$

Where

- $P_{u,k}$ is the k^{th} latent factor of P_u
- $Q_{i,k}$ is the k^{th} latent factor of Q_i
- I_u the of items rated by user u
- U_i the set of users who rated item i

```
import os

if not (os.path.exists("recsys.zip") or os.path.exists("recsys")):
    !wget https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/recsys.zip
    !unzip recsys.zip
```

```
--2023-01-04 03:16:21--  https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/recsys.zip
Resolving github.com (github.com)... 140.82.113.3
Connecting to github.com (github.com)|140.82.113.3|:443... connected.
HTTP request sent, awaiting response... 302 Found
Location: https://raw.githubusercontent.com/nzhinusoftcm/review-on-collaborative-filtering/master/recsys.zip [following]
--2023-01-04 03:16:21--  https://raw.githubusercontent.com/nzhinusoftcm/review-on-collaborative-filtering/master/recsys.zip
Resolving raw.githubusercontent.com (raw.githubusercontent.com)... 185.199.110.133, 185.199.109.133, 185.199.111.133, ...
Connecting to raw.githubusercontent.com (raw.githubusercontent.com)|185.199.110.133|:443... connected.
HTTP request sent, awaiting response... 200 OK
```

```
Length: 15312323 (15M) [application/zip]
Saving to: ‘recsys.zip’

recsys.zip          100%[===================>]  14.60M  --.-KB/s    in 0.1s

2023-01-04 03:16:21 (130 MB/s) - ‘recsys.zip’ saved [15312323/15312323]

Archive:  recsys.zip
   creating: recsys/
  inflating: recsys/datasets.py
  inflating: recsys/preprocessing.py
  inflating: recsys/utils.py
  inflating: recsys/requirements.txt
   creating: recsys/.vscode/
  inflating: recsys/.vscode/settings.json
   creating: recsys/__pycache__/
  inflating: recsys/__pycache__/datasets.cpython-36.pyc
  inflating: recsys/__pycache__/datasets.cpython-37.pyc
  inflating: recsys/__pycache__/utils.cpython-36.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-37.pyc
  inflating: recsys/__pycache__/datasets.cpython-38.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-36.pyc
  inflating: recsys/__pycache__/preprocessing.cpython-38.pyc
   creating: recsys/memories/
  inflating: recsys/memories/ItemToItem.py
  inflating: recsys/memories/UserToUser.py
   creating: recsys/memories/__pycache__/
  inflating: recsys/memories/__pycache__/UserToUser.cpython-36.pyc
  inflating: recsys/memories/__pycache__/UserToUser.cpython-37.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-37.pyc
  inflating: recsys/memories/__pycache__/user2user.cpython-36.pyc
  inflating: recsys/memories/__pycache__/ItemToItem.cpython-36.pyc
   creating: recsys/models/
  inflating: recsys/models/SVD.py
  inflating: recsys/models/MatrixFactorization.py
  inflating: recsys/models/ExplainableMF.py
  inflating: recsys/models/NonnegativeMF.py
   creating: recsys/models/__pycache__/
  inflating: recsys/models/__pycache__/SVD.cpython-36.pyc
  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-37.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-36.pyc
  inflating: recsys/models/__pycache__/ExplainableMF.cpython-37.pyc
  inflating: recsys/models/__pycache__/MatrixFactorization.cpython-36.pyc
   creating: recsys/metrics/
  inflating: recsys/metrics/EvaluationMetrics.py
   creating: recsys/img/
  inflating: recsys/img/MF-and-NNMF.png
  inflating: recsys/img/svd.png
  inflating: recsys/img/MF.png
```

Install and import useful packages

requirements

```
matplotlib==3.2.2
numpy==1.19.2
pandas==1.0.5
python==3.7
scikit-learn==0.24.1
scikit-surprise==1.1.1
scipy==1.6.2
```

```
from recsys.preprocessing import mean_ratings
from recsys.preprocessing import normalized_ratings
from recsys.preprocessing import ids_encoder
from recsys.preprocessing import train_test_split
from recsys.preprocessing import rating_matrix
from recsys.preprocessing import get_examples
from recsys.preprocessing import scale_ratings

from recsys.datasets import ml1m
from recsys.datasets import ml100k

import matplotlib.pyplot as plt
import pandas as pd
import numpy as np

import os
```

Load and preprocess rating

```
# memuat data
ratings, movies = ml100k.load()

# menyiapkan data
ratings, uencoder, iencoder = ids_encoder(ratings)

# mengkonversi rating dari dataframe ke bentuk numpy array
np_ratings = ratings.to_numpy()

# mendapatkan contoh sebagai tuple dari userid dan itemid dan label dari normalisasi rating
raw_examples, raw_labels = get_examples(ratings, labels_column="rating")

# pemisahan data uji dan data latih
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)
```

```
Download data 100.2%
Successfully downloaded ml-100k.zip 4924029 bytes.
Unzipping the ml-100k.zip zip file ...
```

Non-negative Matrix Factorization Model

```
class NMF:

    def __init__(self, ratings, m, n, uencoder, iencoder, K=10, lambda_P=0.01, lambda_Q=0.01):

        np.random.seed(32)

        # initialize the latent factor matrices P and Q (of shapes (m,k) and (n,k) respectively) that will be learnt
        self.ratings = ratings
        self.np_ratings = ratings.to_numpy()
        self.K = K
        self.P = np.random.rand(m, K)
        self.Q = np.random.rand(n, K)

        # hyper parameter initialization
        self.lambda_P = lambda_P
        self.lambda_Q = lambda_Q

        # menginisialisasi sandi
        self.uencoder = uencoder
        self.iencoder = iencoder

        # training history
        self.history = {
            "epochs": [],
            "loss": [],
            "val_loss": [],
        }

    def print_training_parameters(self):
        print('Training NMF ...')
        print(f'k={self.K}')

    def mae(self, x_train, y_train):
        """
        returns the Mean Absolute Error
        """
        # number of training examples
        m = x_train.shape[0]
        error = 0
        for pair, r in zip(x_train, y_train):
            u, i = pair
            error += abs(r - np.dot(self.P[u], self.Q[i]))
        return error / m

    def update_rule(self, u, i, error):
        I = self.np_ratings[self.np_ratings[:, 0] == u][:, [1, 2]]
        U = self.np_ratings[self.np_ratings[:, 1] == i][:, [0, 2]]

        num = self.P[u] * np.dot(self.Q[I[:, 0]].T, I[:, 1])
        dem = np.dot(self.Q[I[:, 0]].T, np.dot(self.P[u], self.Q[I[:, 0]].T)) + self.lambda_P * len(I) * self.P[u]
        self.P[u] = num / dem

        num = self.Q[i] * np.dot(self.P[U[:, 0]].T, U[:, 1])
        dem = np.dot(self.P[U[:, 0]].T, np.dot(self.P[U[:, 0]], self.Q[i].T)) + self.lambda_Q * len(U) * self.Q[i]
        self.Q[i] = num / dem

    @staticmethod
    def print_training_progress(epoch, epochs, error, val_error, steps=5):
        if epoch == 1 or epoch % steps == 0:
            print(f"epoch {epoch}/{epochs} - loss : {round(error, 3)} - val_loss : {round(val_error, 3)}")

    def fit(self, x_train, y_train, validation_data, epochs=10):

        self.print_training_parameters()
        x_test, y_test = validation_data
        for epoch in range(1, epochs+1):
            for pair, r in zip(x_train, y_train):
                u, i = pair
                r_hat = np.dot(self.P[u], self.Q[i])
                e = abs(r - r_hat)
                self.update_rule(u, i, e)
            # training and validation error  after this epochs
            error = self.mae(x_train, y_train)
            val_error = self.mae(x_test, y_test)
            self.update_history(epoch, error, val_error)
            self.print_training_progress(epoch, epochs, error, val_error, steps=1)

        return self.history

    def update_history(self, epoch, error, val_error):
        self.history['epochs'].append(epoch)
        self.history['loss'].append(error)
        self.history['val_loss'].append(val_error)

    def evaluate(self, x_test, y_test):
        error = self.mae(x_test, y_test)
        print(f"validation error : {round(error,3)}")
        print('MAE : ', error)
        return error

    def predict(self, userid, itemid):
        u = self.uencoder.transform([userid])[0]
        i = self.iencoder.transform([itemid])[0]
        r = np.dot(self.P[u], self.Q[i])
        return r

    def recommend(self, userid, N=30):
        # encode the userid
        u = self.uencoder.transform([userid])[0]

        # predictions for users userid on all product
        predictions = np.dot(self.P[u], self.Q.T)

        # get the indices of the top N predictions
        top_idx = np.flip(np.argsort(predictions))[:N]

        # decode indices to get their corresponding itemids
        top_items = self.iencoder.inverse_transform(top_idx)

        # take corresponding predictions for top N indices
        preds = predictions[top_idx]

        return top_items, preds
```

Train the NMF model with ML-100K dataset

model parameters :

- $k = 10$: (number of factors)
- $\lambda_P = 0.6$
- $\lambda_Q = 0.6$
- epochs = 10

Note that it may take some time to complete the training on 10 epochs (around 7 minutes).

```
m = ratings['userid'].nunique()   # total pengguna
n = ratings['itemid'].nunique()   # total item

# membuat dan melatih model
nmf = NMF(ratings, m, n, uencoder, iencoder, K=10, lambda_P=0.6, lambda_Q=0.6)
history = nmf.fit(x_train, y_train, epochs=10, validation_data=(x_test, y_test))
```

```
Training NMF ...
k=10
epoch 1/10 - loss : 0.916 - val_loss : 0.917
epoch 2/10 - loss : 0.915 - val_loss : 0.917
epoch 3/10 - loss : 0.915 - val_loss : 0.917
```

```
     epoch 4/10 - loss : 0.915 - val_loss : 0.917
     epoch 5/10 - loss : 0.915 - val_loss : 0.917
     epoch 6/10 - loss : 0.915 - val_loss : 0.917
     epoch 7/10 - loss : 0.915 - val_loss : 0.917
     epoch 8/10 - loss : 0.915 - val_loss : 0.917
     epoch 9/10 - loss : 0.915 - val_loss : 0.917
     epoch 10/10 - loss : 0.915 - val_loss : 0.917
```

```
nmf.evaluate(x_test, y_test)
```

```
     validation error : 0.917
     MAE :  0.9165041343019539
     0.9165041343019539
```

Evaluation of NMF with Scikit-suprise

We can use the scikt-suprise package to train the NMF model. It is an easy-to-use Python scikit for recommender systems.

1. Import the NMF class from the suprise scikit.
2. Load the data with the built-in function
3. Instanciate NMF with `k=10` (`n_factors`) and we use 10 epochs (`n_epochs`)
4. Evaluate the model using cross-validation with 5 folds.

```
!pip install scikit-surprise
```

```
     Looking in indexes: https://pypi.org/simple, https://us-python.pkg.dev/colab-wheels/public/simple/
     Collecting scikit-surprise
       Downloading scikit-surprise-1.1.3.tar.gz (771 kB)
          ━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━━ 772.0/772.0 KB 14.5 MB/s eta 0:00:00
       Preparing metadata (setup.py) ... done
     Requirement already satisfied: joblib>=1.0.0 in /usr/local/lib/python3.8/dist-packages (from scikit-surprise) (1.2.0)
     Requirement already satisfied: numpy>=1.17.3 in /usr/local/lib/python3.8/dist-packages (from scikit-surprise) (1.21.6)
     Requirement already satisfied: scipy>=1.3.2 in /usr/local/lib/python3.8/dist-packages (from scikit-surprise) (1.7.3)
     Building wheels for collected packages: scikit-surprise
       Building wheel for scikit-surprise (setup.py) ... done
       Created wheel for scikit-surprise: filename=scikit_surprise-1.1.3-cp38-cp38-linux_x86_64.whl size=2626439 sha256=df8a53f19d32943c
       Stored in directory: /root/.cache/pip/wheels/af/db/86/2c18183a80ba05da35bf0fb7417aac5cddbd93bcb1b92fd3ea
     Successfully built scikit-surprise
     Installing collected packages: scikit-surprise
     Successfully installed scikit-surprise-1.1.3
```

```
from surprise import NMF
from surprise import Dataset
from surprise.model_selection import cross_validate

# memuat data movielens-100k dataset
data = Dataset.load_builtin('ml-100k')

# menggunakan algoritma NMF
nmf = NMF(n_factors=10, n_epochs=10)

# menjalankan 5-fold cross-validation dan mencetak hasilnya
history = cross_validate(nmf, data, measures=['MAE'], cv=5, verbose=True)
```

```
     Dataset ml-100k could not be found. Do you want to download it? [Y/n] Y
     Trying to download dataset from https://files.grouplens.org/datasets/movielens/ml-100k.zip...
     Done! Dataset ml-100k has been saved to /root/.surprise_data/ml-100k
     Evaluating MAE of algorithm NMF on 5 split(s).

                       Fold 1  Fold 2  Fold 3  Fold 4  Fold 5  Mean    Std
     MAE (testset)     0.9626  0.9435  0.9777  0.9607  0.9510  0.9591  0.0116
     Fit time          0.80    0.75    0.85    0.58    0.60    0.72    0.11
     Test time         0.36    0.50    0.26    0.28    0.14    0.31    0.12
```

As result, the mean MAE on the test set is **mae = 0.9510** which is equivalent to the result we have obtained on *ml-100k* with our own implementation **mae = 0.9165**

ML-1M

The mean MAE on a 5-fold cross-validation is **mae = 0.9567**

This may take arount 2 minutes

```
# memuat dataset movielens-1M
data = Dataset.load_builtin('ml-1m')
```

```
# menggunakan algoritma NMF
nmf = NMF(n_factors=10, n_epochs=10)

# menjalankan 5-fold cross-validation dan mencetak hasilnya
history = cross_validate(nmf, data, measures=['MAE'], cv=5, verbose=True)
```

```
    Dataset ml-1m could not be found. Do you want to download it? [Y/n] Y
    Trying to download dataset from https://files.grouplens.org/datasets/movielens/ml-1m.zip...
    Done! Dataset ml-1m has been saved to /root/.surprise_data/ml-1m
    Evaluating MAE of algorithm NMF on 5 split(s).

                      Fold 1  Fold 2  Fold 3  Fold 4  Fold 5  Mean    Std
    MAE (testset)     0.9559  0.9580  0.9566  0.9639  0.9490  0.9567  0.0047
    Fit time          5.55    5.98    7.84    7.05    9.54    7.19    1.42
    Test time         3.62    3.35    3.32    4.06    4.72    3.81    0.52
```

Explainable Matrix Factorization

NMF introduced explainability to MF by constraining P and Q values in $[0, 1]$. It can be considered is an inner explainable model. It's possible to inject external informations into the model in order to bring explainability. This is what the **Explainable Matrix Factorization (EMF)** algorithm does. It computes explainable scores from user or item similarities taken from the user-based or item-based CF.

Click here to open the EMF notebook.

Reference

1. Daniel D. Lee & H. Sebastian Seung (1999). Learning the parts of objects by non-negative matrix factorization
2. Deng Cai et al. (2008). Non-negative Matrix Factorization on Manifold
3. Yu-Xiong Wang and Yu-Jin Zhang (2011). Non-negative Matrix Factorization: a Comprehensive Review
4. Nicolas Gillis (2014). The Why and How of Nonnegative Matrix Factorization

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7. Explainable Matrix Factorization

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Explainable Matrix Factorization (EMF)

How to quantify explainability ?

- Use the rating distribution within the active user's neighborhood.
- If many neighbors have rated the recommended item, then this can provide a basis upon which to explain the recommendations, using neighborhood style explanation mechanisms

According to (Abdollahi and Nasraoui, 2016), an item i is consider to be explainable for user u if a considerable number of its neighbors rated item i. The explainability score E_{ui} is the percentage of user u's neighbors who have rated item i.

$$E_{ui} = \frac{|N_k^{(i)}(u)|}{|N_k(u)|},$$

where $N_k(u)$ is the set of k nearest neighbors of user u and $N_k^{(i)}(u)$ is the set of user u's neighbors who have rated item i. However, only explainable scores above an optimal threshold θ are accepted.

$$W_{ui} = \begin{cases} E_{ui} \; if \; E_{ui} > \theta \\ 0 \; otherwise \end{cases},$$

By including explainability weight in the training algorithm, the new objective function, to be minimized over the set of known ratings, has been formulated by (Abdollahi and Nasraoui, 2016) as:

$$J = \sum_{(u,i)\in\kappa} (R_{ui} - \hat{R}_{ui})^2 + \frac{\beta}{2}(||P_u||^2 + ||Q_i||^2) + \frac{\lambda}{2}(P_u - Q_i)^2 W_{ui},$$

here, $\frac{\beta}{2}(||P_u||^2 + ||Q_i||^2)$ is the L_2 regularization term weighted by the coefficient β, and λ is an explainability regularization coefficient that controls the smoothness of the new representation and tradeoff between explainability and accuracy. The idea here is that if item i is explainable for user u, then their representations in the latent space, Q_i and P_u, should be close to each other. Stochastic Gradient descent can be used to optimize the objectve function.

$$P_u \leftarrow P_u + \alpha \left(2(R_{u,i} - P_u Q_i^\top) Q_i - \beta P_u - \lambda (P_u - Q_i) W_{ui}\right)$$
$$Q_i \leftarrow Q_i + \alpha \left(2(R_{u,i} - P_u Q_i^\top) P_u - \beta Q_i + \lambda (P_u - Q_i) W_{ui}\right)$$

Explainable Matrix Factorization : Model definition

```
import os

if not (os.path.exists("recsys.zip") or os.path.exists("recsys")):
    !wget https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/recsys.zip
    !unzip recsys.zip
```

```
Connecting to raw.githubusercontent.com (raw.githubusercontent.com)|185.199.108.133|:443... connected.
HTTP request sent, awaiting response... 200 OK
Length: 15312323 (15M) [application/zip]
Saving to: ‘recsys.zip’

recsys.zip          100%[===================>]  14.60M  --.-KB/s    in 0.05s

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Archive:  recsys.zip
   creating: recsys/
  inflating: recsys/datasets.py
  inflating: recsys/preprocessing.py
  inflating: recsys/utils.py
  inflating: recsys/requirements.txt
   creating: recsys/.vscode/
  inflating: recsys/.vscode/settings.json
```

```
         creating: recsys/memories/
        inflating: recsys/memories/ItemToItem.py
        inflating: recsys/memories/UserToUser.py
         creating: recsys/memories/__pycache__/
        inflating: recsys/memories/__pycache__/UserToUser.cpython-36.pyc
        inflating: recsys/memories/__pycache__/UserToUser.cpython-37.pyc
        inflating: recsys/memories/__pycache__/ItemToItem.cpython-37.pyc
        inflating: recsys/memories/__pycache__/user2user.cpython-36.pyc
        inflating: recsys/memories/__pycache__/ItemToItem.cpython-36.pyc
         creating: recsys/models/
        inflating: recsys/models/SVD.py
        inflating: recsys/models/MatrixFactorization.py
        inflating: recsys/models/ExplainableMF.py
        inflating: recsys/models/NonnegativeMF.py
         creating: recsys/models/__pycache__/
        inflating: recsys/models/__pycache__/SVD.cpython-36.pyc
        inflating: recsys/models/__pycache__/MatrixFactorization.cpython-37.pyc
        inflating: recsys/models/__pycache__/ExplainableMF.cpython-36.pyc
        inflating: recsys/models/__pycache__/ExplainableMF.cpython-37.pyc
        inflating: recsys/models/__pycache__/MatrixFactorization.cpython-36.pyc
         creating: recsys/metrics/
        inflating: recsys/metrics/EvaluationMetrics.py
         creating: recsys/img/
        inflating: recsys/img/MF-and-NNMF.png
        inflating: recsys/img/svd.png
        inflating: recsys/img/MF.png
         creating: recsys/predictions/
         creating: recsys/predictions/item2item/
         creating: recsys/weights/
         creating: recsys/weights/item2item/
         creating: recsys/weights/item2item/ml1m/
        inflating: recsys/weights/item2item/ml1m/similarities.npy
        inflating: recsys/weights/item2item/ml1m/neighbors.npy
         creating: recsys/weights/item2item/ml100k/
```

requirements

```
matplotlib==3.2.2
numpy==1.18.1
pandas==1.0.5
python==3.6.10
scikit-learn==0.23.1
scipy==1.5.0
```

```
from recsys.memories.UserToUser import UserToUser

from recsys.preprocessing import mean_ratings
from recsys.preprocessing import normalized_ratings
from recsys.preprocessing import ids_encoder
from recsys.preprocessing import train_test_split
from recsys.preprocessing import rating_matrix
from recsys.preprocessing import get_examples

from recsys.datasets import ml100k, ml1m

import matplotlib.pyplot as plt
import pandas as pd
import numpy as np

import sys
import os
```

Compute Explainable Scores

Explainable score are computed using neighborhood based similarities. Here, we are using the user based algorithme to compute similarities

```
def explainable_score(user2user, users, items, theta=0):

    def _progress(count):
        sys.stdout.write('\rCompute Explainable score. Progress status : %.1f%%'%(float(count/len(users))*100.0))
        sys.stdout.flush()
    # initialize explainable score to zeros
    W = np.zeros((len(users), len(items)))

    for count, u in enumerate(users):
        candidate_items = user2user.find_user_candidate_items(u)
        for i in candidate_items:
            user_who_rated_i, similar_user_who_rated_i = \
                user2user.similar_users_who_rated_this_item(u, i)
            if user_who_rated_i.shape[0] == 0:
                w = 0.0
            else:
                w = similar_user_who_rated_i.shape[0] / user_who_rated_i.shape[0]
            W[u,i] =  w  if w > theta else 0.0
        _progress(count)
    return W
```

Explainable Matrix Factorization Model

```
class ExplainableMatrixFactorization:

    def __init__(self, m, n, W, alpha=0.001, beta=0.01, lamb=0.1, k=10):
        """
            - R : Rating matrix of shape (m,n)
            - W : Explainability Weights of shape (m,n)
            - k : number of latent factors
            - beta : L2 regularization parameter
            - lamb : explainability regularization coefficient
            - theta : threshold above which an item is explainable for a user
        """
        self.W = W
        self.m = m
        self.n = n

        np.random.seed(64)

        # initialize the latent factor matrices P and Q (of shapes (m,k) and (n,k) respectively) that will be learnt
        self.k = k
        self.P = np.random.normal(size=(self.m,k))
        self.Q = np.random.normal(size=(self.n,k))

        # hyperparameter initialization
        self.alpha = alpha
        self.beta = beta
        self.lamb = lamb

        # training history
        self.history = {
            "epochs":[],
            "loss":[],
            "val_loss":[],
        }

    def print_training_parameters(self):
        print('Training EMF')
        print(f'k={self.k} \t alpha={self.alpha} \t beta={self.beta} \t lambda={self.lamb}')

    def update_rule(self, u, i, error):
        self.P[u] = self.P[u] + \
            self.alpha*(2 * error*self.Q[i] - self.beta*self.P[u] - self.lamb*(self.P[u] - self.Q[i]) * self.W[u,i])

        self.Q[i] = self.Q[i] + \
            self.alpha*(2 * error*self.P[u] - self.beta*self.Q[i] + self.lamb*(self.P[u] - self.Q[i]) * self.W[u,i])

    def mae(self,  x_train, y_train):
        """
        returns the Mean Absolute Error
        """
        # number of training exemples
        M = x_train.shape[0]
        error = 0
        for pair, r in zip(x_train, y_train):
            u, i = pair
            error += np.absolute(r - np.dot(self.P[u], self.Q[i]))
        return error/M

    def print_training_progress(self, epoch, epochs, error, val_error, steps=5):
        if epoch == 1 or epoch % steps == 0 :
                print(f"epoch {epoch}/{epochs} - loss : {round(error,3)} - val_loss : {round(val_error,3)}")

    def learning_rate_schedule(self, epoch, target_epochs = 20):
        if (epoch >= target_epochs) and (epoch % target_epochs == 0):
                factor = epoch // target_epochs
                self.alpha = self.alpha * (1 / (factor * 20))
                print("\nLearning Rate : {}\n".format(self.alpha))

    def fit(self, x_train, y_train, validation_data, epochs=10):
        """
        Train latent factors P and Q according to the training set
        :param
            - x_train : training pairs (u,i) for which rating r_ui is known
            - y_train : set of ratings r_ui for all training pairs (u,i)
            - validation_data : tuple (x_test, y_test)
            - epochs : number of time to loop over the entire training set.
            10 epochs by default

        Note that u and i are encoded values of userid and itemid
        """
        self.print_training_parameters()

        # get validation data
        x_test, y_test = validation_data

        for epoch in range(1, epochs+1):
            for pair, r in zip(x_train, y_train):
                u,i = pair
                r_hat = np.dot(self.P[u], self.Q[i])
                e = r - r_hat
                self.update_rule(u, i, error=e)

            # training and validation error  after this epochs
            error = self.mae(x_train, y_train)
            val_error = self.mae(x_test, y_test)
            self.update_history(epoch, error, val_error)
            self.print_training_progress(epoch, epochs, error, val_error, steps=1)

        return self.history

    def update_history(self, epoch, error, val_error):
        self.history['epochs'].append(epoch)
        self.history['loss'].append(error)
        self.history['val_loss'].append(val_error)

    def evaluate(self, x_test, y_test):
        """
        compute the global error on the test set

        :param
            - x_test : test pairs (u,i) for which rating r_ui is known
            - y_test : set of ratings r_ui for all test pairs (u,i)
        """
        error = self.mae(x_test, y_test)
        print(f"validation error : {round(error,3)}")

    def predict(self, userid, itemid):
        """
        Make rating prediction for a user on an item

        :param
        - userid
        - itemid

        :return
        - r : predicted rating
        """
        # encode user and item ids to be able to access their latent factors in
        # matrices P and Q
        u = uencoder.transform([userid])[0]
        i = iencoder.transform([itemid])[0]

        # rating prediction using encoded ids. Dot product between P_u and Q_i
        r = np.dot(self.P[u], self.Q[i])

        return r

    def recommend(self, userid, N=30):
        """
        make to N recommendations for a given user

        :return
        - (top_items,preds) : top N items with the highest predictions
        """
        # encode the userid
        u = uencoder.transform([userid])[0]

        # predictions for this user on all product
        predictions = np.dot(self.P[u], self.Q.T)

        # get the indices of the top N predictions
        top_idx = np.flip(np.argsort(predictions))[:N]
        # decode indices to get their corresponding itemids
        top_items = iencoder.inverse_transform(top_idx)

        # take corresponding predictions for top N indices
        preds = predictions[top_idx]

        return top_items, preds
```

```
epochs = 10
```

Model Evaluation

1. MovieLens 100K

1.1. Evaluation on raw data

```
# load data
ratings, movies = ml100k.load()

# encode users and items ids
ratings, uencoder, iencoder = ids_encoder(ratings)

users = sorted(ratings.userid.unique())
items = sorted(ratings.itemid.unique())

m = len(users)
n = len(items)

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings)

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)
```

```
     Download data 100.2%
     Successfully downloaded ml-100k.zip 4924029 bytes.
     Unzipping the ml-100k.zip zip file ...
```

```
# create the user to user model for similarity measure
usertouser = UserToUser(ratings, movies)

# compute explainable score
W = explainable_score(usertouser, users, items)
```

```
     Normalize users ratings ...
     Initialize the similarity model ...
     Compute nearest neighbors ...
     User to user recommendation model created with success ...
     Compute Explainable score. Progress status : 99.9%
```

```
# initialize the model
EMF = ExplainableMatrixFactorization(m, n, W, alpha=0.01, beta=0.4, lamb=0.01, k=10)

history = EMF.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))
```

```
     Training EMF
     k=10     alpha=0.01      beta=0.4        lambda=0.01
     epoch 1/10 - loss : 0.922 - val_loss : 1.036
     epoch 2/10 - loss : 0.79 - val_loss : 0.873
     epoch 3/10 - loss : 0.766 - val_loss : 0.837
     epoch 4/10 - loss : 0.757 - val_loss : 0.822
     epoch 5/10 - loss : 0.753 - val_loss : 0.814
     epoch 6/10 - loss : 0.751 - val_loss : 0.808
     epoch 7/10 - loss : 0.749 - val_loss : 0.805
     epoch 8/10 - loss : 0.748 - val_loss : 0.802
     epoch 9/10 - loss : 0.746 - val_loss : 0.799
     epoch 10/10 - loss : 0.745 - val_loss : 0.797
```

```
EMF.evaluate(x_test, y_test)
```

```
     validation error : 0.797
```

1.2. Evaluation on normalized data

```
# memuat data
ratings, movies = ml100k.load()
```

```
# menyandikan id pengguna dan item
ratings, uencoder, iencoder = ids_encoder(ratings)

users = sorted(ratings.userid.unique())
items = sorted(ratings.itemid.unique())

m = len(users)
n = len(items)

# menormalisasi rating dengan mengurangkan rata-rata
normalized_column_name = "norm_rating"
ratings = normalized_ratings(ratings, norm_column=normalized_column_name)

# mendapatkan contoh sebagai tuple userid dan itemid dan label dari normalisasi rating
raw_examples, raw_labels = get_examples(ratings, labels_column=normalized_column_name)

# oemisahan data uji dan data latih
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)
```

```
# initialize the model
EMF = ExplainableMatrixFactorization(m, n, W, alpha=0.022, beta=0.65, lamb=0.01, k=10)

history = EMF.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))
```

```
Training EMF
k=10     alpha=0.022     beta=0.65       lambda=0.01
epoch 1/10 - loss : 0.809 - val_loss : 0.842
epoch 2/10 - loss : 0.809 - val_loss : 0.829
epoch 3/10 - loss : 0.807 - val_loss : 0.821
epoch 4/10 - loss : 0.799 - val_loss : 0.811
epoch 5/10 - loss : 0.789 - val_loss : 0.8
epoch 6/10 - loss : 0.782 - val_loss : 0.793
epoch 7/10 - loss : 0.778 - val_loss : 0.789
epoch 8/10 - loss : 0.776 - val_loss : 0.786
epoch 9/10 - loss : 0.774 - val_loss : 0.784
epoch 10/10 - loss : 0.773 - val_loss : 0.783
```

2. MovieLens 1M

2.1. Evaluation on raw data

```
# memuat data
ratings, movies = ml1m.load()

# menyandikan id pengguna dan item
ratings, uencoder, iencoder = ids_encoder(ratings)

users = sorted(ratings.userid.unique())
items = sorted(ratings.itemid.unique())

m = len(users)
n = len(items)

# mendapatkan contoh sebagai tuple userid dan itemid dan label dari normalisasi rating
raw_examples, raw_labels = get_examples(ratings)

# pemisahan data tes dan data uji
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)
```

```
Download data 100.1%
Successfully downloaded ml-1m.zip 5917549 bytes.
Unzipping the ml-1m.zip zip file ...
```

```
# membuat user pada model usel untuk perhitungan kemiripan
usertouser = UserToUser(ratings, movies)

# menghitung skor yang dapat dijelaskan
W = explainable_score(usertouser, users, items)
```

```
Normalize users ratings ...
Initialize the similarity model ...
Compute nearest neighbors ...
User to user recommendation model created with success ...
Compute Explainable score. Progress status : 100.0%
```

```
# menginisialisasi model
EMF = ExplainableMatrixFactorization(m, n, W, alpha=0.01, beta=0.4, lamb=0.01, k=10)
```

```
history = EMF.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))
```

```
     Training EMF
     k=10     alpha=0.01      beta=0.4        lambda=0.01
     epoch 1/10 - loss : 0.782 - val_loss : 0.807
     epoch 2/10 - loss : 0.762 - val_loss : 0.781
     epoch 3/10 - loss : 0.76 - val_loss : 0.775
     epoch 4/10 - loss : 0.758 - val_loss : 0.771
     epoch 5/10 - loss : 0.757 - val_loss : 0.769
     epoch 6/10 - loss : 0.756 - val_loss : 0.767
     epoch 7/10 - loss : 0.754 - val_loss : 0.764
     epoch 8/10 - loss : 0.752 - val_loss : 0.762
     epoch 9/10 - loss : 0.751 - val_loss : 0.761
     epoch 10/10 - loss : 0.75 - val_loss : 0.76
```

2.2. Evaluation on normalized data

```
# memuat data
ratings, movies = ml1m.load()

# menyandi id pengguna dan item
ratings, uencoder, iencoder = ids_encoder(ratings)

# menormalisasi rating dengan mengurangkan rata-rata
normalized_column_name = "norm_rating"
ratings = normalized_ratings(ratings, norm_column=normalized_column_name)

# mendapatkan contoh sebagai tuple userid dan itemid dan label dari normalisasi rating
raw_examples, raw_labels = get_examples(ratings, labels_column=normalized_column_name)

# pemisahan data uji dan data latih
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)


# menginisialisasi model
EMF = ExplainableMatrixFactorization(m, n, W, alpha=0.023, beta=0.59, lamb=0.01, k=10)

history = EMF.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))
```

```
     Training EMF
     k=10     alpha=0.023     beta=0.59       lambda=0.01
     epoch 1/10 - loss : 0.805 - val_loss : 0.814
     epoch 2/10 - loss : 0.764 - val_loss : 0.77
     epoch 3/10 - loss : 0.756 - val_loss : 0.762
     epoch 4/10 - loss : 0.755 - val_loss : 0.759
     epoch 5/10 - loss : 0.754 - val_loss : 0.759
     epoch 6/10 - loss : 0.754 - val_loss : 0.758
     epoch 7/10 - loss : 0.754 - val_loss : 0.758
     epoch 8/10 - loss : 0.753 - val_loss : 0.758
     epoch 9/10 - loss : 0.753 - val_loss : 0.758
     epoch 10/10 - loss : 0.753 - val_loss : 0.758
```

Ratings prediction

```
# mendapatkan daftar N item teratas dengan prediksi rating yang sesuai
userid = 42
recommended_items, predictions = EMF.recommend(userid=userid)

# mencari judul film yang bersesuaian
top_N = list(zip(recommended_items,predictions))
top_N = pd.DataFrame(top_N, columns=['itemid','predictions'])
top_N.predictions = top_N.predictions + ratings.loc[ratings.userid==userid].rating_mean.values[0]
List = pd.merge(top_N, movies, on='itemid', how='inner')

# menampilkan daftar
List
```

	itemid	predictions	title	genres
0	3460	4.364036	Hillbillys in a Haunted House (1967)	Comedy
1	701	4.324177	Daens (1992)	Drama
2	3057	4.307404	Where's Marlowe? (1999)	Comedy
3	2214	4.304979	Number Seventeen (1932)	Thriller
4	1145	4.299559	Snowriders (1996)	Documentary
5	2258	4.292125	Master Ninja I (1984)	Action
6	3353	4.281912	Closer You Get, The (2000)	Comedy|Romance
7	868	4.278937	Death in Brunswick (1991)	Comedy
8	826	4.269901	Diebinnen (1995)	Drama
9	3305	4.266769	Bluebeard (1944)	Film-Noir|Horror
10	2619	4.265997	Mascara (1999)	Drama
11	763	4.264092	Last of the High Kings, The (a.k.a. Summer Fli...	Drama
			Love Walked	

Note: The recommendation list may content items already purchased by the user. This is just an illustration of how to implement matrix factorization recommender system. You can optimize the recommended list and return the top rated items that the user has not already purchased.

Putting all together

This repository covers the following algorithms for collaborative filtering

1. User-based CF
2. Item-based CF
3. Singular Value Decomposition (SVD)
4. Matrix Factorization (MF)
5. Non-negative Matrix Factorization (NMF)
6. Explainable Matrix Factorization (EMF)

In the next notebook, we present performances comparison of all these models.

Reference

1. Yehuda Koren et al. (2009). Matrix Factorization Techniques for Recommender Systems
2. Abdollahi and Nasraoui (2016). Explainable Matrix Factorization for Collaborative Filtering
3. Abdollahi and Nasraoui (2017). Using Explainability for Constrained Matrix Factorization
4. Shuo Wang et al, (2018). Explainable Matrix Factorization with Constraints on Neighborhood in the Latent Space

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✓ 0s completed at 11:14 AM ● ×

8. Performance Measure

Open in Colab

```
import os

if not (os.path.exists("recsys.zip") or os.path.exists("recsys")):
    !wget https://github.com/nzhinusoftcm/review-on-collaborative-filtering/raw/master/recsys.zip
    !unzip recsys.zip
```

requirements

```
matplotlib==3.2.2
numpy==1.19.2
pandas==1.0.5
python==3.7
scikit-learn==0.24.1
scikit-surprise==1.1.1
scipy==1.6.2
```

```
from recsys.memories.UserToUser import UserToUser
from recsys.memories.ItemToItem import ItemToItem

from recsys.models.MatrixFactorization import MF
from recsys.models.ExplainableMF import EMF, explainable_score

from recsys.preprocessing import normalized_ratings
from recsys.preprocessing import train_test_split
from recsys.preprocessing import rating_matrix
from recsys.preprocessing import scale_ratings
from recsys.preprocessing import mean_ratings
from recsys.preprocessing import get_examples
from recsys.preprocessing import ids_encoder

from recsys.datasets import ml100k
from recsys.datasets import ml1m

from sklearn.preprocessing import LabelEncoder

import matplotlib.pyplot as plt
import pandas as pd
import numpy as np

import os
```

1. Results on MovieLens 100k

1.1. User-based CF

```
# load data
ratings, movies = ml100k.load()

# prepare data
ratings, uencoder, iencoder = ids_encoder(ratings)

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings, labels_column='rating')

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

# evaluate with Euclidean distance
usertouser = UserToUser(ratings, movies, metric='euclidean')
print("==========================")
usertouser.evaluate(x_test, y_test)
```

```
     Normalize users ratings ...
     Initialize the similarity model ...
     Compute nearest neighbors ...
     User to user recommendation model created with success ...
     ==========================
     Evaluate the model on 10000 test data ...

     MAE : 0.8125945111976461
     0.8125945111976461
```

```
# evaluate with cosine similarity
usertouser = UserToUser(ratings, movies, metric='cosine')
print("=========================")
usertouser.evaluate(x_test, y_test)
```

```
     Normalize users ratings ...
     Initialize the similarity model ...
     Compute nearest neighbors ...
     User to user recommendation model created with success ...
     =========================
     Evaluate the model on 10000 test data ...

     MAE : 0.7505910931068639
     0.7505910931068639
```

1.2. Item-based CF

```
# load data
ratings, movies = ml100k.load()

# prepare data
ratings, uencoder, iencoder = ids_encoder(ratings)

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings, labels_column='rating')

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

# evaluation with cosine similarity
itemtoitem = ItemToItem(ratings, movies, metric='cosine')
print("==================")
itemtoitem.evaluate(x_test, y_test)
```

```
     Normalize ratings ...
     Create the similarity model ...
     Compute nearest neighbors ...
     Item to item recommendation model created with success ...
     ==================
     Evaluate the model on 10000 test data ...

     MAE : 0.507794195659005
     0.507794195659005
```

Evaluation with Euclidean distance

```
# evaluation with Euclidean distance
itemtoitem = ItemToItem(ratings, movies, metric='euclidean')
print("==================")
itemtoitem.evaluate(x_test, y_test)
```

```
     Normalize ratings ...
     Create the similarity model ...
     Compute nearest neighbors ...
     Item to item recommendation model created with success ...
     ==================
     Evaluate the model on 10000 test data ...

     MAE : 0.8277111416143341
     0.8277111416143341
```

1.3. Matrix Factorization

```
epochs = 10
```

```
# load the ml100k dataset
ratings, movies = ml100k.load()

ratings, uencoder, iencoder = ids_encoder(ratings)
```

```
m = ratings.userid.nunique()   # total number of users
n = ratings.itemid.nunique()   # total number of items

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings)

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

# create and train the model
mf = MF(m, n, k=10, alpha=0.01, lamb=1.5)

# fit the model on the training set
history = mf.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))
```

```
Training Matrix Factorization Model ...
k=10     alpha=0.01      lambda=1.5
epoch 1/10 - loss : 2.734 - val_loss : 2.779
epoch 2/10 - loss : 1.764 - val_loss : 1.794
epoch 3/10 - loss : 1.592 - val_loss : 1.614
epoch 4/10 - loss : 1.538 - val_loss : 1.556
epoch 5/10 - loss : 1.515 - val_loss : 1.531
epoch 6/10 - loss : 1.503 - val_loss : 1.517
epoch 7/10 - loss : 1.496 - val_loss : 1.509
epoch 8/10 - loss : 1.491 - val_loss : 1.504
epoch 9/10 - loss : 1.488 - val_loss : 1.5
epoch 10/10 - loss : 1.486 - val_loss : 1.497
```

1.4. Non-negative Matrix Factorization

```
!pip install scikit-surprise
```

```
Looking in indexes: https://pypi.org/simple, https://us-python.pkg.dev/colab-wheels/public/simple/
Requirement already satisfied: scikit-surprise in /usr/local/lib/python3.8/dist-packages (1.1.3)
Requirement already satisfied: scipy>=1.3.2 in /usr/local/lib/python3.8/dist-packages (from scikit-surprise) (1.7.3)
Requirement already satisfied: joblib>=1.0.0 in /usr/local/lib/python3.8/dist-packages (from scikit-surprise) (1.2.0)
Requirement already satisfied: numpy>=1.17.3 in /usr/local/lib/python3.8/dist-packages (from scikit-surprise) (1.21.6)
```

```
from surprise import NMF
from surprise import Dataset
from surprise.model_selection import cross_validate

# Load the movielens-100k dataset (download it if needed).
data = Dataset.load_builtin('ml-100k')

# Use the NMF algorithm.
nmf = NMF(n_factors=10, n_epochs=10)

# Run 5-fold cross-validation and print results.
history = cross_validate(nmf, data, measures=['MAE'], cv=5, verbose=True)
```

```
Evaluating MAE of algorithm NMF on 5 split(s).

                  Fold 1  Fold 2  Fold 3  Fold 4  Fold 5  Mean    Std
MAE (testset)     0.9615  0.9501  0.9548  0.9582  0.9675  0.9584  0.0059
Fit time          0.57    0.63    0.59    0.64    0.54    0.59    0.04
Test time         0.21    0.14    0.14    0.15    0.24    0.18    0.04
```

1.5. Explainable Matrix Factorization

```
# load data
ratings, movies = ml100k.load()

# encode users and items ids
ratings, uencoder, iencoder = ids_encoder(ratings)

users = sorted(ratings.userid.unique())
items = sorted(ratings.itemid.unique())

m = len(users)
n = len(items)

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings)

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)
```

```
# create the user to user model for similarity measure
usertouser = UserToUser(ratings, movies)

# compute explainable score
W = explainable_score(usertouser, users, items)

print("===================")
# initialize the model
emf = EMF(m, n, W, alpha=0.01, beta=0.4, lamb=0.01, k=10)

history = emf.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))

print("===================")
emf.evaluate(x_test, y_test)
```

```
Normalize users ratings ...
Initialize the similarity model ...
Compute nearest neighbors ...
User to user recommendation model created with success ...
Compute explainable scores ...
===================
Training EMF
k=10     alpha=0.01      beta=0.4        lambda=0.01
epoch 1/10 - loss : 0.922 - val_loss : 1.036
epoch 2/10 - loss : 0.79 - val_loss : 0.873
epoch 3/10 - loss : 0.766 - val_loss : 0.837
epoch 4/10 - loss : 0.757 - val_loss : 0.822
epoch 5/10 - loss : 0.753 - val_loss : 0.814
epoch 6/10 - loss : 0.751 - val_loss : 0.808
epoch 7/10 - loss : 0.749 - val_loss : 0.805
epoch 8/10 - loss : 0.748 - val_loss : 0.802
epoch 9/10 - loss : 0.746 - val_loss : 0.799
epoch 10/10 - loss : 0.745 - val_loss : 0.797
===================
MAE : 0.797
0.797347824723284
```

2. Results on MovieLens 1M (ML-1M)

2.1. User-based CF

```
# load ml100k ratings
ratings, movies = ml1m.load()

# prepare data
ratings, uencoder, iencoder = ids_encoder(ratings)

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings, labels_column='rating')

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

# metric : cosine

# create the user-based CF
usertouser = UserToUser(ratings, movies, k=20, metric='cosine')

# evaluate the user-based CF on the ml1m test data
print("==========================")
usertouser.evaluate(x_test, y_test)
```

```
Normalize users ratings ...
Initialize the similarity model ...
Compute nearest neighbors ...
User to user recommendation model created with success ...
==========================
Evaluate the model on 100021 test data ...

MAE : 0.732267005840993
0.732267005840993
```

```
# metric : euclidean

# create the user-based CF
usertouser = UserToUser(ratings, movies, k=20, metric='euclidean')

# evaluate the user-based CF on the ml1m test data
```

```
print("=========================")
usertouser.evaluate(x_test, y_test)
```

```
Normalize users ratings ...
Initialize the similarity model ...
Compute nearest neighbors ...
User to user recommendation model created with success ...
=========================
Evaluate the model on 100021 test data ...

MAE : 0.8069332535426614
0.8069332535426614
```

2.2. Item-based CF

Cosine similarity

```
itemtoitem = ItemToItem(ratings, movies, metric='cosine')
print("=========================")
itemtoitem.evaluate(x_test, y_test)
```

```
Normalize ratings ...
Create the similarity model ...
Compute nearest neighbors ...
Item to item recommendation model created with success ...
=========================
Evaluate the model on 100021 test data ...

MAE : 0.42514728655396045
0.42514728655396045
```

Euclidean distance

```
itemtoitem = ItemToItem(ratings, movies, metric='euclidean')
print("=========================")
itemtoitem.evaluate(x_test, y_test)
```

```
Normalize ratings ...
Create the similarity model ...
Compute nearest neighbors ...
Item to item recommendation model created with success ...
=========================
Evaluate the model on 100021 test data ...

MAE : 0.82502173206615
0.82502173206615
```

2.3. Matrix Factorization

```
# load the ml1m dataset
ratings, movies = ml1m.load()

ratings, uencoder, iencoder = ids_encoder(ratings)

m = ratings.userid.nunique()   # total number of users
n = ratings.itemid.nunique()   # total number of items

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings)

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

# create the model
model = MF(m, n, k=10, alpha=0.01, lamb=1.5)

# fit the model on the training set
history = model.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))

print("===================")
model.evaluate(x_test, y_test)
```

```
Training Matrix Factorization Model ...
k=10     alpha=0.01      lambda=1.5
epoch 1/10 - loss : 1.713 - val_loss : 1.718
epoch 2/10 - loss : 1.523 - val_loss : 1.526
epoch 3/10 - loss : 1.496 - val_loss : 1.498
epoch 4/10 - loss : 1.489 - val_loss : 1.489
epoch 5/10 - loss : 1.485 - val_loss : 1.486
epoch 6/10 - loss : 1.484 - val_loss : 1.484
epoch 7/10 - loss : 1.483 - val_loss : 1.483
epoch 8/10 - loss : 1.483 - val_loss : 1.483
epoch 9/10 - loss : 1.482 - val_loss : 1.482
epoch 10/10 - loss : 1.482 - val_loss : 1.482
==================
validation error : 1.482
1.4820034560467208
```

2.4. Non-negative Matrix Factorization

```
from surprise import NMF
from surprise import Dataset
from surprise.model_selection import cross_validate

# Load the movielens-100k dataset (download it if needed).
data = Dataset.load_builtin('ml-1m')

# Use the NMF algorithm.
nmf = NMF(n_factors=10, n_epochs=10)

# Run 5-fold cross-validation and print results.
history = cross_validate(nmf, data, measures=['MAE'], cv=5, verbose=True)
```

```
Evaluating MAE of algorithm NMF on 5 split(s).

                  Fold 1  Fold 2  Fold 3  Fold 4  Fold 5  Mean    Std
MAE (testset)     0.9435  0.9456  0.9527  0.9546  0.9524  0.9498  0.0044
Fit time          4.60    5.04    5.11    5.17    5.90    5.16    0.42
Test time         2.28    3.10    2.40    2.93    3.01    2.74    0.34
```

2.5. Explainable Matrix Factorization

```
# load data
ratings, movies = ml1m.load()

# encode users and items ids
ratings, uencoder, iencoder = ids_encoder(ratings)

users = sorted(ratings.userid.unique())
items = sorted(ratings.itemid.unique())

m = len(users)
n = len(items)

# get examples as tuples of userids and itemids and labels from normalize ratings
raw_examples, raw_labels = get_examples(ratings)

# train test split
(x_train, x_test), (y_train, y_test) = train_test_split(examples=raw_examples, labels=raw_labels)

# create the user to user model for similarity measure
usertouser = UserToUser(ratings, movies)

# compute explainable score
W = explainable_score(usertouser, users, items)

# initialize the model
emf = EMF(m, n, W, alpha=0.01, beta=0.4, lamb=0.01, k=10)

history = emf.fit(x_train, y_train, epochs=epochs, validation_data=(x_test, y_test))
```

```
Normalize users ratings ...
Initialize the similarity model ...
Compute nearest neighbors ...
User to user recommendation model created with success ...
Compute explainable scores ...
Training EMF
k=10     alpha=0.01      beta=0.4        lambda=0.01
epoch 1/10 - loss : 0.782 - val_loss : 0.807
epoch 2/10 - loss : 0.762 - val_loss : 0.781
epoch 3/10 - loss : 0.76 - val_loss : 0.775
epoch 4/10 - loss : 0.758 - val_loss : 0.771
epoch 5/10 - loss : 0.757 - val_loss : 0.769
epoch 6/10 - loss : 0.756 - val_loss : 0.767
epoch 7/10 - loss : 0.754 - val_loss : 0.764
epoch 8/10 - loss : 0.752 - val_loss : 0.762
epoch 9/10 - loss : 0.751 - val_loss : 0.761
epoch 10/10 - loss : 0.75 - val_loss : 0.76
```

Summary

MAE comparison between User-based and Item-based CF

Metric	Dataset	User-based	Item-based
Euclidean	ML-100k	0.81	0.83
Euclidean	ML-1M	0.81	0.82
Cosine	ML-100k	0.75	0.51
Cosine	ML-1M	0.73	0.42

MAE comparison between MF, NMF and EMF

Preprocessing	Dataset	MF	NMF	EMF
Raw data	ML-100k	1.497	0.951	0.797
Raw data	ML-1M	1.482	0.9567	0.76
Normalized data	ML-100k	0.828	---	0.783
Normalized data	ML-1M	0.825	---	0.758

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