

WEEK 2 Path Mediation

Data Analysis for Psychology in R 3

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Learning Objectives

- 1. Understand the purpose of mediation models and the conceptual challenges
- 2. Be able to describe direct, indirect and total effects in a mediation model.
- 3. Estimate and interpret a mediation model using lavaan

Part 1: Introduction to mediation

Part 2: Direct, indirect and total effects

Part 3: Estimating mediation in lavaan

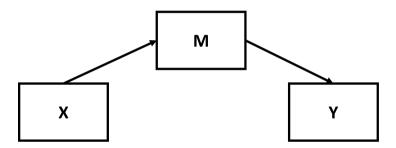
Part 4: Reporting

Mediation

- Is when a predictor X, has an effect on an outcome Y, via a mediating variable M
- The mediator transmits the effect of X to Y
- Examples of mediation hypotheses:
 - Conscientiousness (X) affects health (Y) via health behaviours (M)
 - Conduct problems (X) increase the risk of depression (Y) via peer problems (M)
 - Attitudes to smoking (X) predict intentions to smoke (M) which in turn predicts smoking behaviour (Y)
 - An intervention (X) to reduce youth crime (Y) works by increasing youth self-contol (M)

Visualising a mediation model

• In a SEM diagram we can represent mediation as:



Mediation...not to be confused with moderation

- Mediation is commonly confused with moderation
- Moderation is when a moderator z modifies the effect of X on Y
 - o e.g., the effect of X on Y is stronger at higher levels of Z
 - Also known as an interaction between X and Z
- Examples of moderation could be:
 - An intervention (X) works better to reduce bullying (Y) at older ages (Z) of school pupil
 - The relation between stress (X) and depression (Y) is lower for those scoring higher on spirituality (Z)

End of Part 1

Part 1: Introduction to mediation

Part 2: Direct, indirect and total effects

Part 3: Estimating mediation in lavaan

Part 4: Reporting

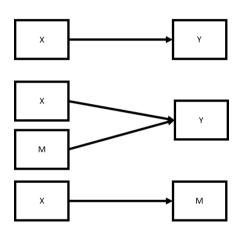
Direct and indirect effects in mediation

- We seldom hypothesise that a mediator completely explains the relation between X and Y
- More commonly, we expect both indirect effects and direct effects of X on Y
 - The indirect effects of X on Y are those transmitted via the mediator
 - The direct effect of X on Y is the remaining effect of X on Y

Visualing direct and indirect effects in mediation

Testing mediation

- Traditionally, mediation was tested using a series of separate linear models:
 - 1. Y~X
 - 2. Y~X+M
 - 3. M~X
- May see this referred to as th Baron and Kenny approach.



Traditional methods for mediation

- The three regression models:
 - 1. Y~X
 - 2. Y~X+M
 - 3. M~X

- Model 1 estimates the overall effect of X on Y
- Model 2 estimates the partial effects of X and M on Y
- Model 3 estimates the effect of X on M.
- If the following conditions were met, mediation was assumed to hold:
 - The effect of X on Y (eq.1) is significant
 - The effect of X on M (eq.3) is significant
 - The effect of X on Y becomes reduced when M is added into the model (eq.2)

Limitations of traditional methods for mediation

- Low power
- Very cumbersome for multiple mediators, predictors, or outcomes
- You don't get an estimate of the magnitude of the indirect effect
- Much better way: path mediation model

BREAK QUIZ

- Quiz question:
 - Which of these hypotheses is a mediation hypothesis?
 - 1) Vocabulary development in childhood follows a non-linear trajecrtory
 - 2) The effects of conscientiousness on academic achievement are stronger at low levels of cognitive ability
 - 3) Poverty affects child behaviour problems through increasing parental stress
 - 4) Earlier pubertal onset increases the risk of antisocial behaviour only in girls and not boys

End of Part 2

Part 1: Introduction to mediation

Part 2: Direct, indirect and total effects

Part 3: Estimating mediation in lavaan

Part 4: Reporting

WELCOME BACK

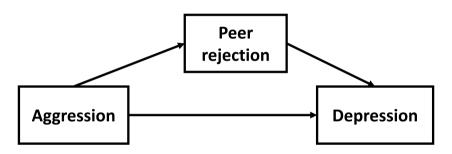
- Welcome back!
- The answer to the guiz guestion is...
 - Which of these hypotheses is a mediation hypothesis?
 - 1) Vocabulary development in childhood follows a non-linear trajecrtory
 - 2) The effects of conscientiousness on academic achievement are stronger at low levels of cognitive ability
 - 3) Poverty affects child behaviour problems through increasing parental stress
 - 4) Earlier pubertal onset increases the risk of antisocial behaviour only in girls and not boys

Testing a path mediation model in lavaan

- Specification
 - Create a lavaan syntax object
- Estimation
 - Estimate the model using e.g., maximum likelihood estimation
- Evaluation/interpretation
 - Inspect the model to judge how good it is
 - Interpret the parameter estimates

Example

• Does peer rejection mediate the association between aggression and depression?



The data

slice(agg.data2, 1:10)

```
## Dep PR Agg
## 1 -2.17142 -0.478205 -0.3425
## 2 -0.43763 -0.742841 -0.6704
## 3 -0.21199 -1.997370 -1.3641
## 4 -0.85132 -1.584195 -0.7931
## 5 -0.36378 -0.202357 1.7604
## 6 -0.18635 -0.529160 -0.5259
```

9 -0.11124 -1.139879 0.1420 ## 10 2.31793 0.928142 1.2780

0.19925 0.043562 -2.0169 -0.09919 0.004379 0.1069

Mediation Example

• Does peer rejection mediate the association between aggression and depression?

```
model1<-'Dep ~ PR  # Depression predicted by peer rejection

Dep ~ Agg  # Depression predicted by aggression (the direct effect)

PR ~ Agg  # Peer rejection predicted by aggression

'
```

Estimate the model

```
model1.est<-sem(model1, data=agg.data2)
```

The model output

```
summary(model1.est, fit.measures=T)
## lavaan 0.6-9 ended normally after 12 iterations
     Estimator
                                                        ML
     Optimization method
                                                    NLMINB
     Number of model parameters
##
##
     Number of observations
                                                       500
  Model Test User Model:
     Test statistic
                                                     0.000
     Degrees of freedom
  Model Test Baseline Model:
     Test statistic
                                                   256.476
     Degrees of freedom
##
     P-value
                                                     0.000
   User Model versus Baseline Model:
##
##
     Comparative Fit Index (CFI)
                                                     1.000
     Tucker-Lewis Index (TLI)
                                                     1.000
   Loglikelihood and Information Criteria:
##
     Loglikelihood user model (H0)
                                                 -1336.131
     Loglikelihood unrestricted model (H1)
                                                 -1336.131
```

Things to note from the model output

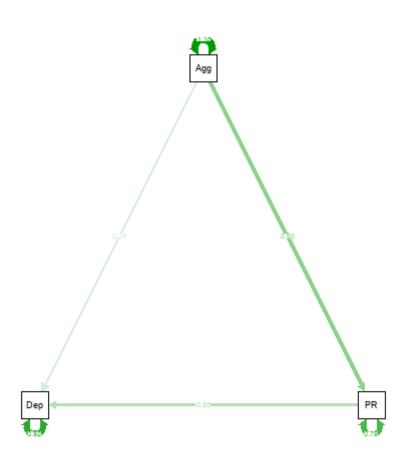
- All three regressions paths are statistically significant
- The model is just-identified
 - The degrees of freedom are equal to 0
 - The model fit cannot be tested
 - The model fit statistics (TLI, CFI, RMSEA, SRMR) all suggest perfect fit but this is meaningless

Visualising the model using semPaths()

- We can use semPaths() from the semPlot package to help us visualise the model
 - Shows the parameter estimates within an SEM diagram

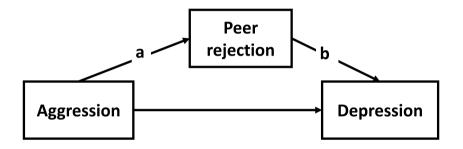
```
library(semPlot)
semPaths(model1.est, what='est')
```

Visualising the model using semPaths()



Calculating the indirect effects

- To calculate the indirect effect of X on Y in path mediation, we need to create some new parameters
- The indirect effect of X on Y via M is:
 - $\circ a * b$
 - \circ a = the regression coefficient for M~X
 - \circ b = the regression coefficient for Y~M



Calculating indirect effects in lavaan

- To calculate the indirect effect of X on Y in lavaan we:
- Use parameter labels 'a' and 'b' to label the relevant paths
 - o a is for the effect of X on M
 - o b is for the effect of M on Y
- Use the ':=' operator to create a new parameter 'ind'
 - 'ind' represents our indirect effect

```
model1<-'Dep~b*PR
Dep~Agg
PR~a*Agg
ind:=a*b
```

Indirect effects in the output

##

```
model1.est<-sem(model1, data=agg.data2)</pre>
summary(model1.est)
## lavaan 0.6-9 ended normally after 12 iterations
     Estimator
##
                                                         ML
     Optimization method
                                                     NLMINB
     Number of model parameters
##
     Number of observations
##
                                                        500
  Model Test User Model:
     Test statistic
                                                      0.000
     Degrees of freedom
##
  Parameter Estimates:
##
     Standard errors
                                                   Standard
     Information
                                                   Expected
     Information saturated (h1) model
                                                Structured
##
  Regressions:
##
                      Estimate Std.Err z-value P(>|z|)
     Dep ~
       PR
                  (b)
                          0.331
                                   0.048
                                            6.852
                                                      0.000
                          0.188
                                   0.047
                                            3.967
                                                      0.000
       Agg
     PR ~
                  (a)
                          0.496
                                   0.038
                                           13.119
                                                      0.000
       Agg
```

Statistical significance of the indirect effects

- Default method of assessing the statistical significance of indirect effects assume normal sampling distribution
- May not hold for indirect effects which are the product of regression coefficients
- Instead we can use bootstrapping
 - Allows 95% confidence intervals (CIs) to be computed
 - If 95% CI includes 0, the indirect effect is not significant at alpha=.05

Bootstapped CIs for indirect effect in lavaan

Output for bootstrapped CIs

Variances:

```
summary(model1.est, ci=T) # we add the argument ci=T to see the confidence intervals in the output
## lavaan 0.6-9 ended normally after 12 iterations
     Estimator
                                                        ML
     Optimization method
                                                    NLMINB
     Number of model parameters
##
     Number of observations
##
                                                       500
  Model Test User Model:
     Test statistic
                                                     0.000
     Degrees of freedom
  Parameter Estimates:
     Standard errors
                                                 Bootstrap
    Number of requested bootstrap draws
                                                      1000
##
     Number of successful bootstrap draws
                                                      1000
   Regressions:
                      Estimate Std.Err z-value P(>|z|) ci.lower ci.upper
##
     Dep ~
                  (b)
                                  0.052
       PR
                         0.331
                                            6.376
                                                     0.000
                                                               0.224
                                                                        0.435
                         0.188
                                  0.049
                                            3.863
                                                     0.000
                                                                        0.283
                                                              0.094
       Agg
     PR ~
##
                  (a)
                         0.496
                                  0.036
                                           13.751
                                                              0.420
                                                                        0.569
       Agg
                                                     0.000
```

Total effects in path mediation

• As well as the direct and indirect effect, it is often of interest to know the total effect of X on Y

Total = Indirect + Direct

Total effects in path mediation

Total = a * b + c

Total effect in lavaan

Total effect in lavaan output

```
summary(model1.est, ci=T)
## lavaan 0.6-9 ended normally after 12 iterations
     Estimator
                                                        ML
     Optimization method
                                                    NLMINB
     Number of model parameters
##
     Number of observations
##
                                                       500
  Model Test User Model:
     Test statistic
                                                     0.000
     Degrees of freedom
  Parameter Estimates:
##
     Standard errors
                                                 Bootstrap
    Number of requested bootstrap draws
                                                      1000
##
     Number of successful bootstrap draws
                                                      1000
   Regressions:
                      Estimate Std.Err z-value P(>|z|) ci.lower ci.upper
##
     Dep ~
                  (b)
                         0.331
                                   0.049
                                                               0.237
       PR
                                            6.750
                                                     0.000
                                                                        0.431
                  (c)
                         0.188
                                  0.047
                                            3.972
                                                     0.000
                                                               0.096
                                                                        0.281
       Agg
     PR ~
##
                  (a)
                         0.496
                                   0.038
                                           13.088
                                                               0.420
                                                                        0.574
       Agg
                                                     0.000
## Variances:
```

Why code the total effect in lavaan?

- We could have just added up the coefficients for the direct and indirect effects
- By coding it in lavaan, however, we can assess the statistical significance of the total effect
- Useful because sometimes the direct and indirect effects are not individually significant but the total effect is
 - May be especially relevant in cases where there are many mediators of small effect

Interpreting the total, direct, and indirect effect coefficients

- The total effect can be interpreted as the unit increase in Y expected to occur when X increases by one unit
- The indirect effect can be interpreted as the unit increase in Y expected to occur via M when X increases by one unit
- The direct effect can be interpreted as the unit increase in Y expected to occur with a unit increase in X over and above the increase transmitted by M
- Note: 'direct' effect may not actually be direct it may be acting via other mediators not included in our model

Standardised parameters

• As with CFA models, standardised parameters can be obtained using:

```
summary(model1.est, ci=T, std=T)
```

Standardised parameters

```
## lavaan 0.6-9 ended normally after 12 iterations
##
     Estimator
                                                        ML
    Optimization method
                                                    NLMINB
     Number of model parameters
##
     Number of observations
##
                                                       500
  Model Test User Model:
##
     Test statistic
                                                     0.000
     Degrees of freedom
  Parameter Estimates:
##
     Standard errors
                                                 Bootstrap
     Number of requested bootstrap draws
                                                      1000
     Number of successful bootstrap draws
                                                      1000
   Regressions:
                      Estimate Std.Err z-value P(>|z|) ci.lower ci.upper
##
     Dep ~
                  (b)
                         0.331
                                            6.750
                                                     0.000
                                                               0.237
                                   0.049
                                                                        0.431
##
                  (c)
                         0.188
                                   0.047
                                            3.972
                                                     0.000
                                                               0.096
                                                                        0.281
       Agg
     PR ~
##
                  (a)
                         0.496
                                   0.038
                                           13.088
                                                               0.420
                                                                        0.574
       Agg
                                                     0.000
      Std.lv Std.all
##
       0.331
                0.319
                0.185
       0.188
```

BREAK QUIZ

- Time for a pause
- Quiz question
 - o If the effect of X on M is b=.30 and the effect of M on Y is b=.10, what is the indirect effect of X on Y?
 - 1) b=.40
 - **2**) b=.03
 - **3**) b=.30
 - 4) b=.10

End of Part 3

Part 1: Introduction to mediation

Part 2: Direct, indirect and total effects

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Part 4: Reporting

Welcome back

- The answer to the quiz question is...
- Quiz question
 - o If the effect of X on M is b=.30 and the effect of M on Y is b=.10, what is the indirect effect of X on Y?
 - 1) b=.40
 - 2) b=.03
 - 3) b=.30
 - 4) b=.10

Reporting path mediation models

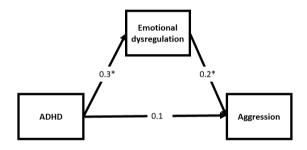
- Methods/ Analysis Strategy
 - The model being tested
 - o e.g. 'Y was regressed on both X and M and M was regressed on X'
 - The estimator used (e.g., maximum likelihood estimation)
 - The method used to test the significance of indirect effects ('bootstrapped 95% confidence intervals')

Results

- Model fit (for over-identified models)
- The parameter estimates for the path mediation and their statistical significance
- Can be useful to present these in a SEM diagram
- o The diagrams from R not considered 'publication quality' draw in powerpoint or similar

Reporting path mediation models - example of SEM diagram with results

- Include the key parameter estimates
- Indicate statistically significant paths (e.g. with an '*')
- Include a figure note that explains how statistically significant paths (and at what level) are signified



Reporting path mediation models - the indirect effects

- Results
 - The coefficient for the indirect effect and the bootstrapped 95% confidence intervals
 - Common to also report proportion mediation:

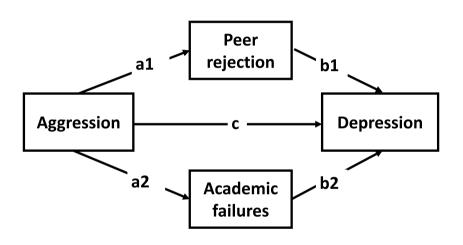
$$\frac{indirect}{total}$$

- However, important to be aware of limitations:
 - Big proportion mediation possible when total effect is small makes effect seem more impressive
 - Small proportion mediation even when total effect is big can underplay importance of effect
 - Should be interpreted in context of total effect
- Tricky interpretation if there are a mix of negative and positive effects involved

Extensions of path mediation models

- We can extend our path mediation model in various ways:
 - o Several mediators in sequence or parallel
 - Multiple outcomes
 - Multiple predictors
 - Multiple groups (e.g., comparing direct and indirect effects across males and females)
 - Add covariates to adjust for potential confounders

Example: Multiple mediation model



Other path analysis models

- Path mediation models are a common application of path models
 - But they are just one example
- Anything that can be expressed in terms of regressions between observed variables can be tested as a path model
 - Can include ordinal or binary variables
 - Can include moderation
- Other common path analysis models include:
 - Autoregressive models for longitudinal data
 - o Cross-lagged panel models for longitudinal data

Making model modifications

- You may want to make some modifications to your initially hypothesised model
 - o non-significant paths that you want to trim
 - o include some additional paths not initially included
- Remember that this now moves us into exploratory territory where:
 - Model modifications should be substantively as well as statistically justifiable
 - You must be aware of the possibility that you are capitalising on chance
 - o You should aim to replicate the modifications in independent data

Cautions regarding path analysis models

- Assumption that the paths represent causal effects is only an assumption
 - Especially if using cross-sectional data
 - Mediation models should ideally be estimated on longitudinal data.
 - o X time 1
 - o M time 2
 - o Y time 3
- The parameters are only accurate if the model is correctly specified

Cautions: Indistinguishable models

Measurement error in path analysis

- Path analysis models use observed variables
 - Assumes no measurement error in these variables
- Path coefficients likely to be attenuated due to unmodelled measurement error
- Structural equation models solve this issue
 - They are path analysis models where the paths are between latent rather than observed variables
 - ...very brief comment on this in the final week

Path analysis summary

- Path analysis can be used to fit sets of regression models
 - Common path analysis model is the path mediation model
 - o But very flexible huge range of models that can be tested
- In R, path analysis can be done using the sem() function in lavaan
- Need to be aware that we aren't testing causality but assuming it

this is optional content

End