



THE UNIVERSITY  
of EDINBURGH

# Assumptions & Diagnostics

## More random effects

Data Analysis for Psychology in R 3

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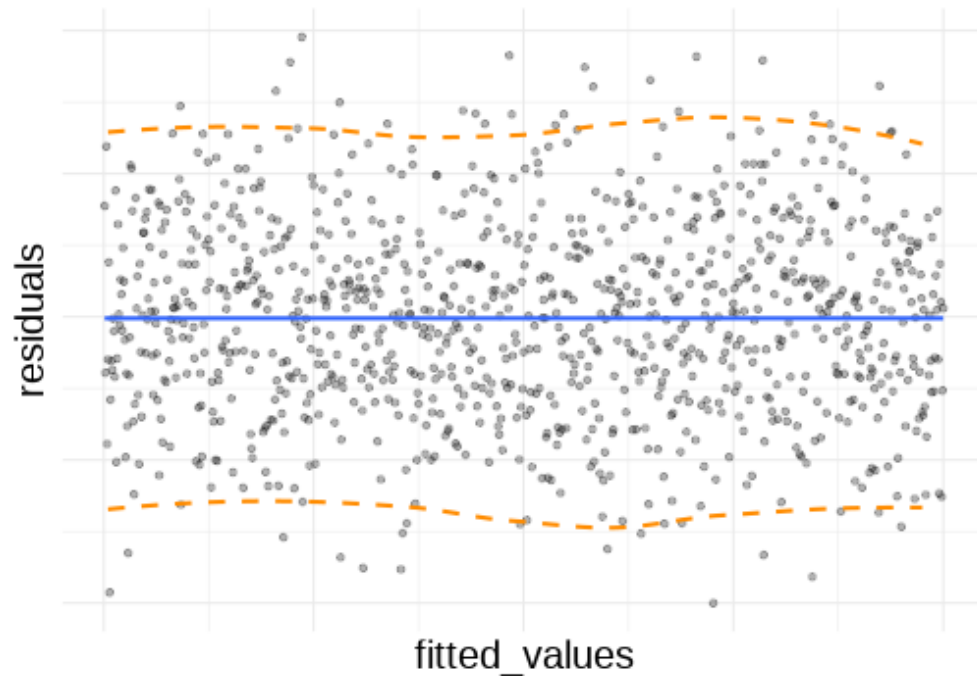
AY 2021-2022



# Assumptions in LM

The general idea

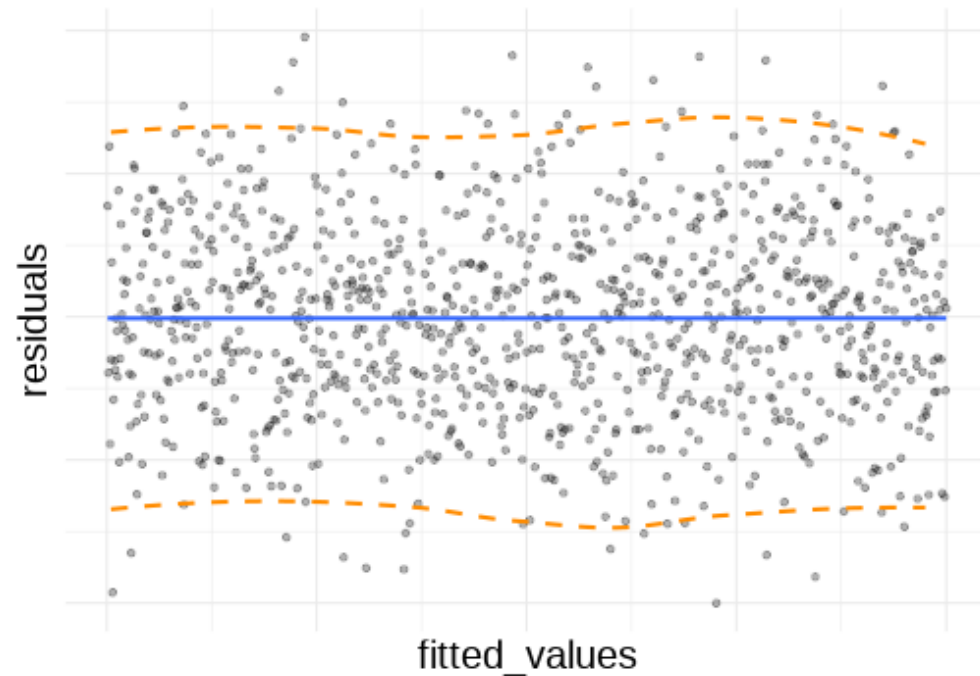
- $\varepsilon_i \sim N(0, \sigma^2)$  iid
- "zero mean and constant variance"



# Assumptions in LM

## The general idea

- $\varepsilon_i \sim N(0, \sigma^2)$  iid
- "zero mean and constant variance"



## Recipe book

- Linearity
- Independence
- Normality
- Equal Variances

# What's different in MLM?

- Not much is different!

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- General idea is unchanged: error is random

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- Not much is different!
- General idea is unchanged: error is random
- We now have residuals at multiple levels!

# Random effects as level 2 residuals



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for observation  $j$  in group  $i$

Level 1:

$$y_{ij} = \beta_{0i} \cdot 1 + \beta_{1i} \cdot x_{ij} + \varepsilon_{ij}$$

Level 2:

$$\beta_{0i} = \gamma_{00} + \zeta_{0i}$$

$$\beta_{1i} = \gamma_{10} + \zeta_{1i}$$

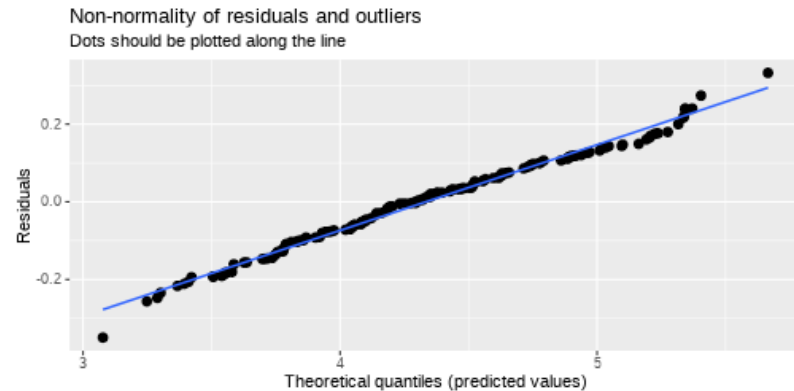
$\varepsilon$ ,  $\zeta_0$ , and  $\zeta_1$  are all assumed to be normally distributed with mean 0.

# Random effects as level 2 residuals

$\varepsilon$

`resid(model)`

mean zero, constant variance

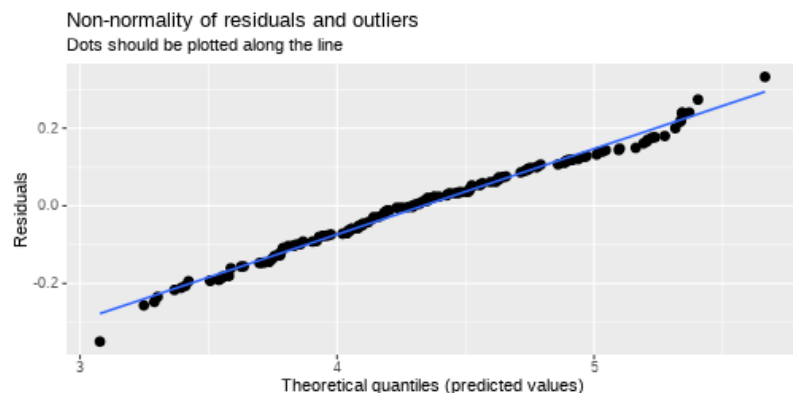


# Random effects as level 2 residuals

$\varepsilon$

`resid(model)`

mean zero, constant variance

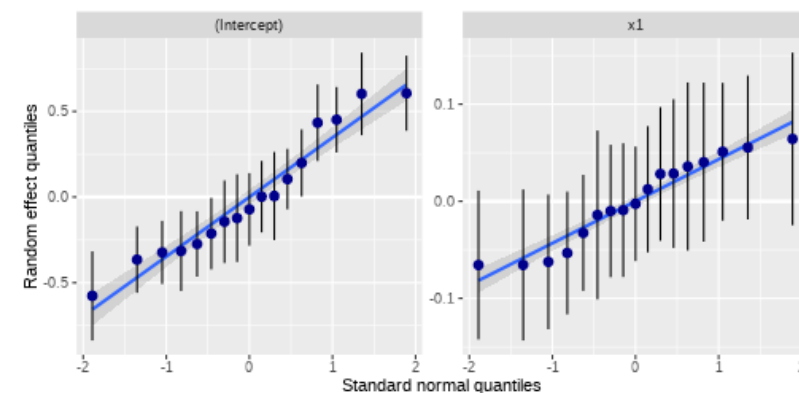


$\zeta$

`ranef(model)`

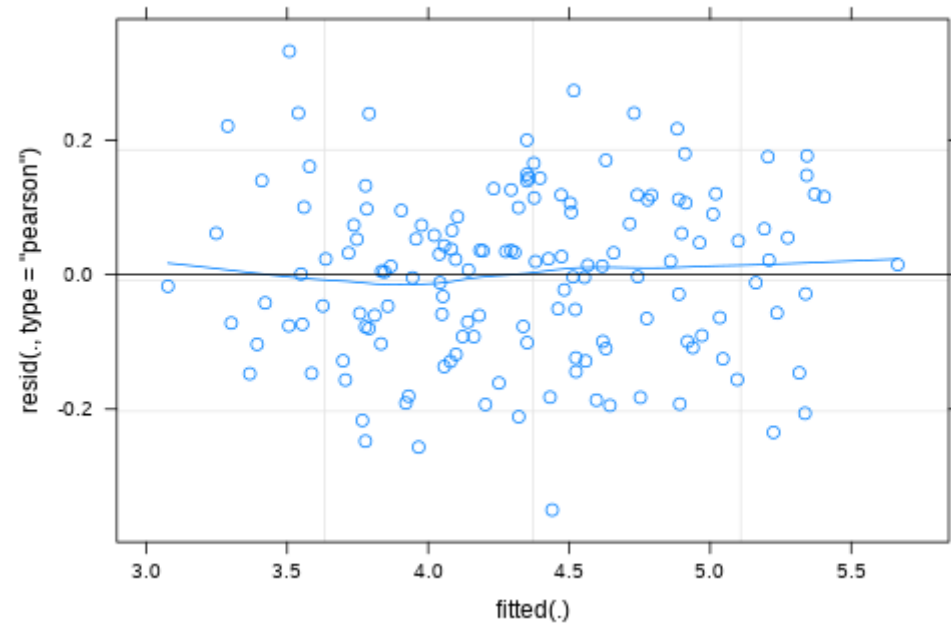
mean zero, constant variance

## \$cluster



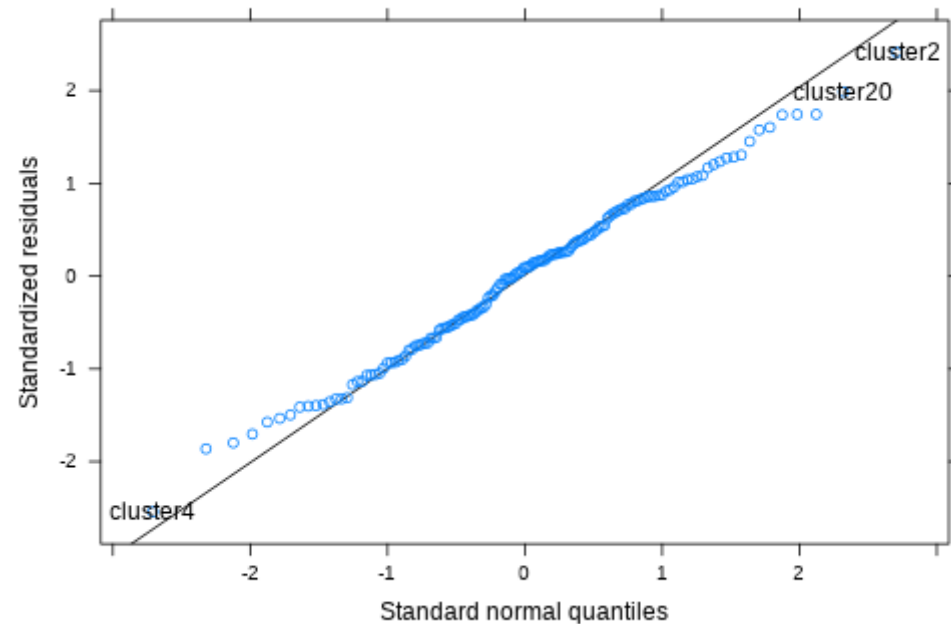
# Assumption Plots: Residuals vs Fitted

```
plot(model, type=c("p", "smooth"))
```



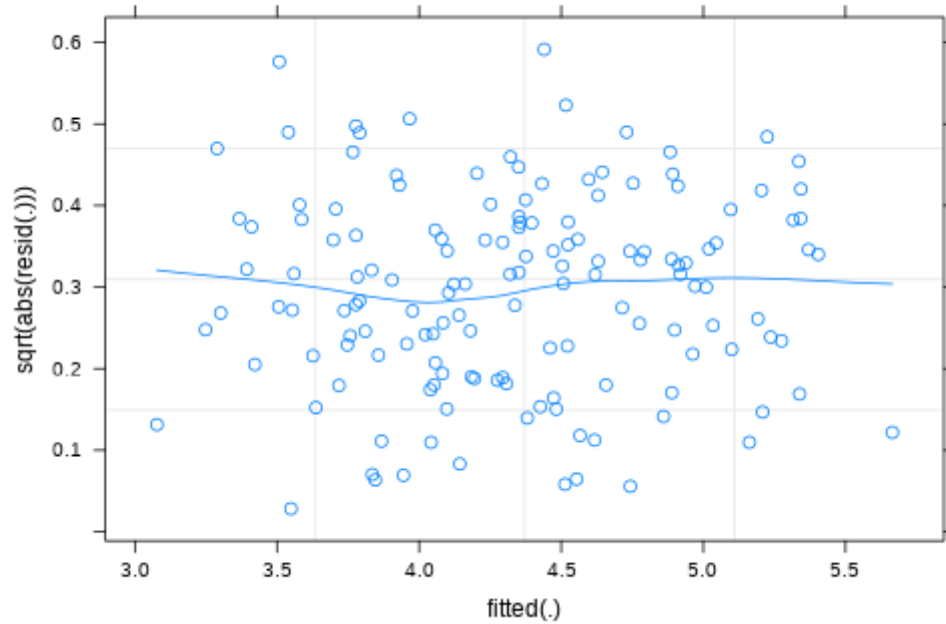
# Assumption Plots: qqplots

```
library(lattice)  
qqmath(model, id=.05)
```



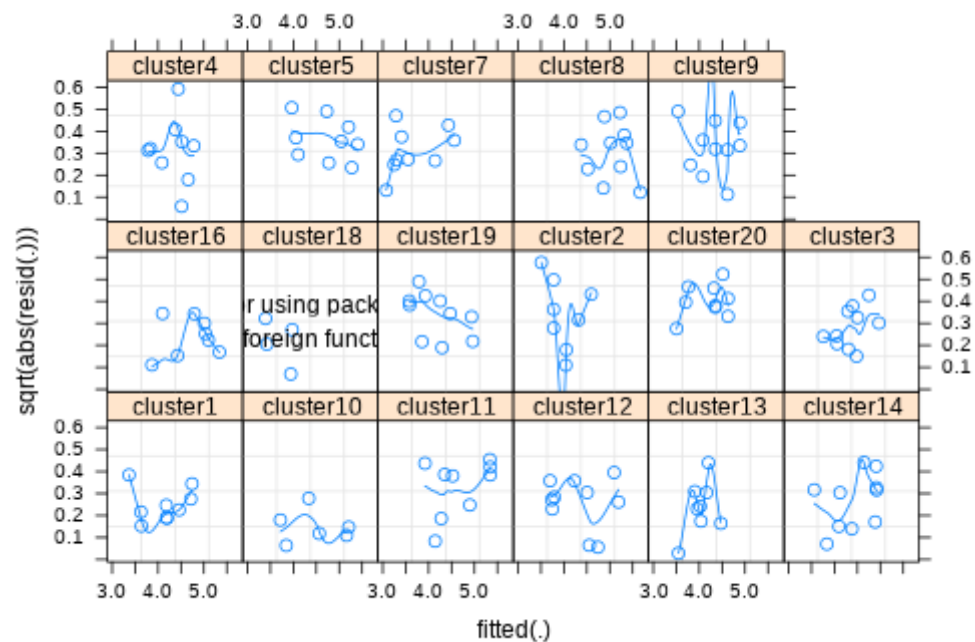
# Assumption Plots: Scale-Location

```
plot(model,  
      form = sqrt(abs(resid(.))) ~ fitted(.),  
      type = c("p", "smooth"))
```



# Assumption Plots: Scale-Location

```
plot(model,  
  form = sqrt(abs(resid(.))) ~ fitted(.) | cluster,  
  type = c("p", "smooth"))
```

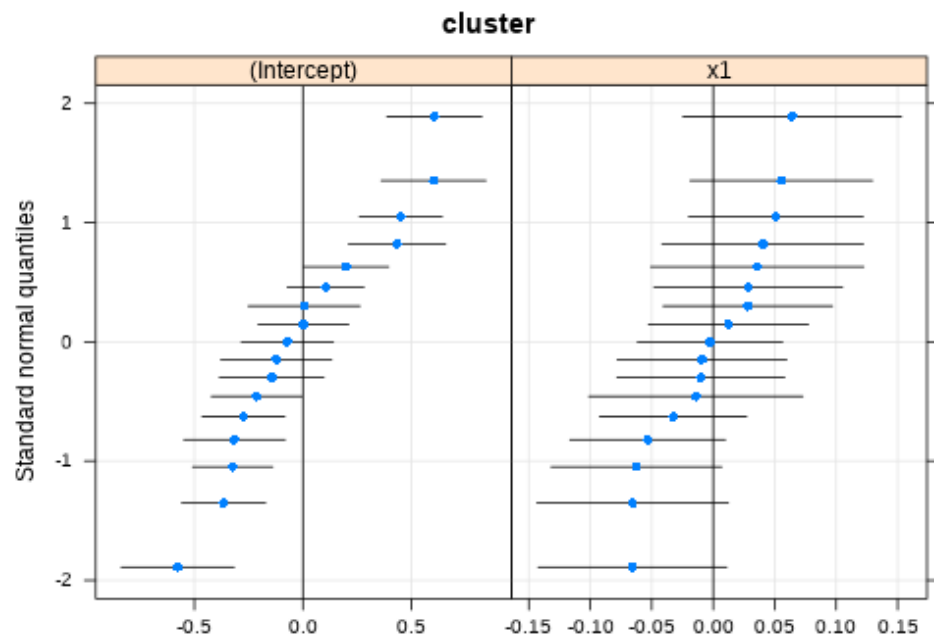




# Assumption Plots: Ranefs

```
qqmath(ranef(model))
```

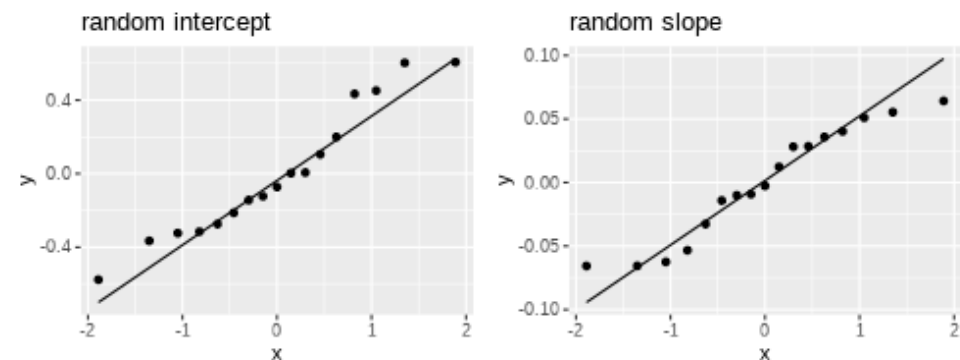
```
## $cluster
```



```
rans <- as.data.frame(ranef(model)$cluster)
```

```
ggplot(rans, aes(sample = `(Intercept)`)) +  
  stat_qq() + stat_qq_line() +  
  labs(title="random intercept")
```

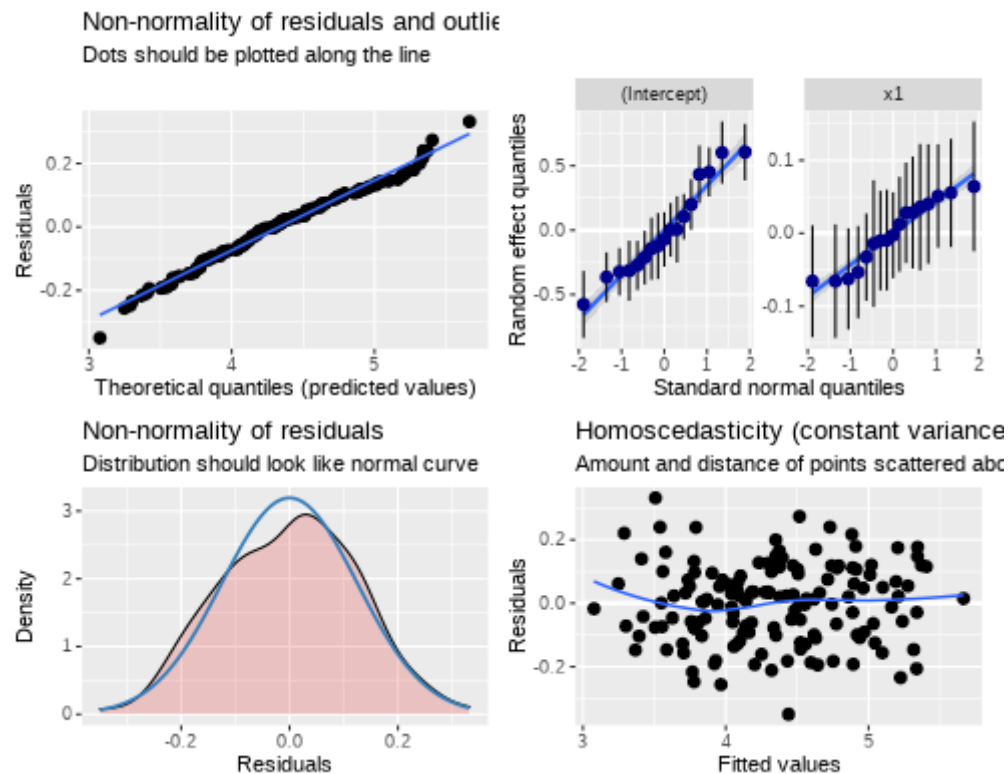
```
ggplot(rans, aes(sample = x1)) +  
  stat_qq() + stat_qq_line() +  
  labs(title="random slope")
```



# for a quick check

if nothing else...

```
sjPlot::plot_model(model, type = "diag")
```



# Part 1: Assumptions Troubleshooting

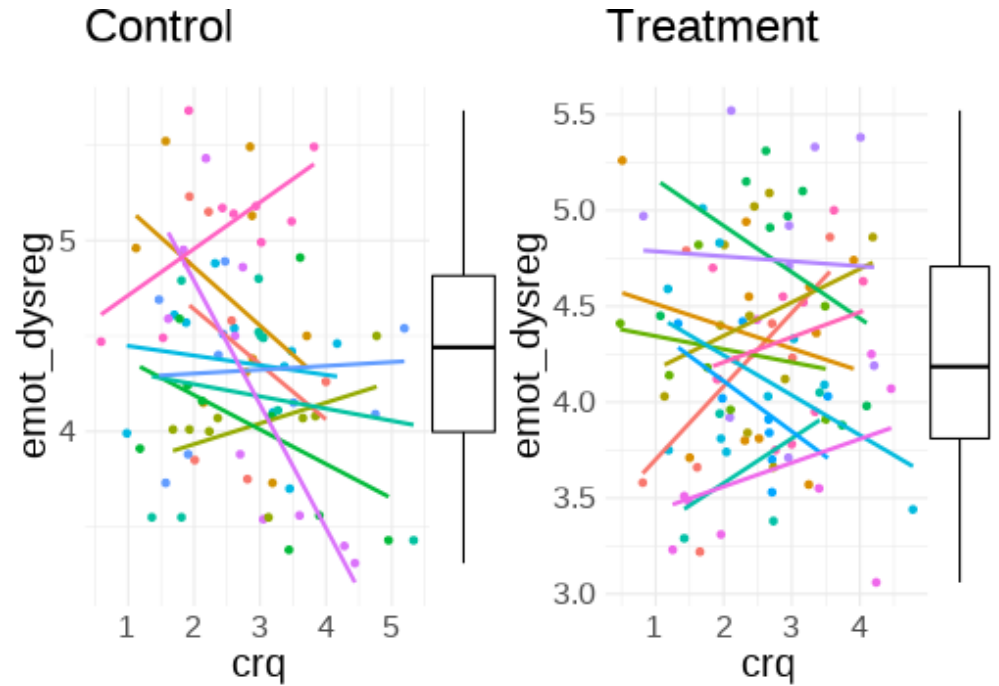
Part 2: Case Diagnostics in MLM

Part 3: Random Effect Structures

# Some Data

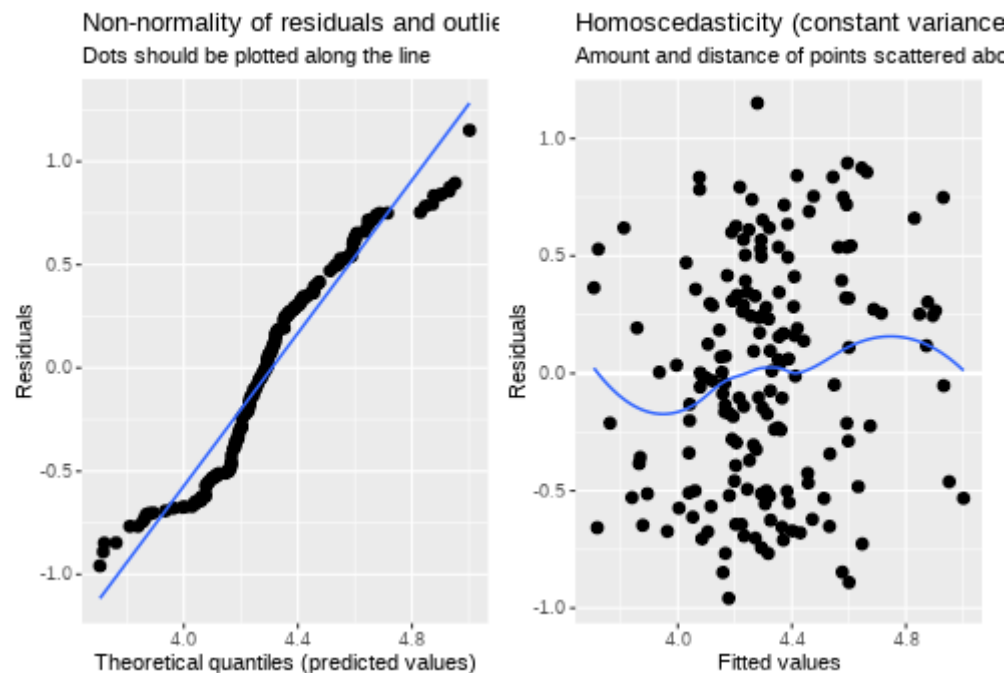
200 pupils from 20 schools completed a survey containing the Emotion Dysregulation Scale (EDS) and the Child Routines Questionnaire (CRQ). Eleven of the schools were taking part in an initiative to specifically teach emotion regulation as part of the curriculum.

Adjusting for levels of daily routines, do children from schools partaking in the intervention present with lower levels of emotional dysregulation?



# When things look wrong

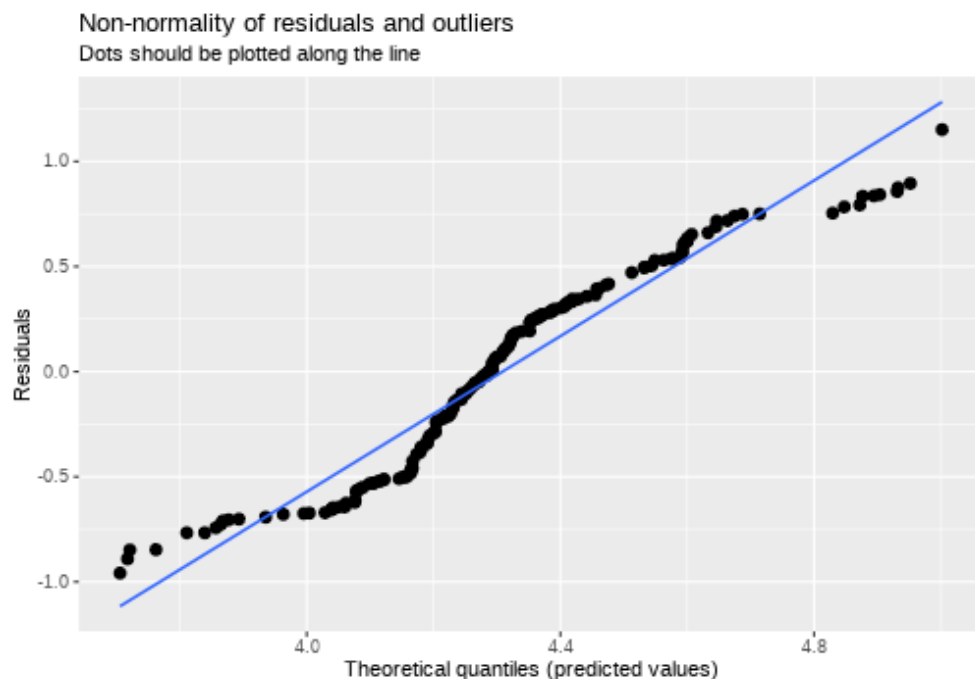
```
mymodel <- lmer(emot_dysreg ~ crq + int + (1 | schoolid), data = crq)
```



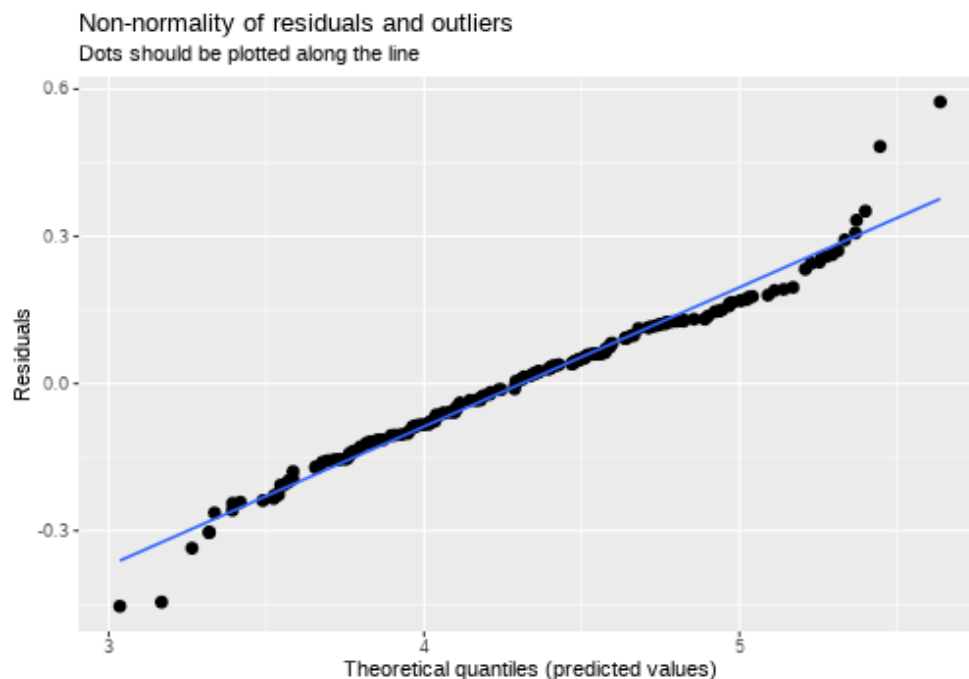
# When things look wrong

## Model mis-specification?

```
mymodel <- lmer(emot_dysreg ~ crq + int + (1 | schoolid), dat
```



```
mymodel <- lmer(emot_dysreg ~ crq + age + int + (1 | schoolid
```



# When things look wrong

## Transformations?

- Transforming your outcome variable may help to satisfy model assumptions

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- Transforming your outcome variable may help to satisfy model assumptions
- $\log(y)$
- $1/y$
- $\sqrt{y}$
- `forecast::BoxCox(y)`

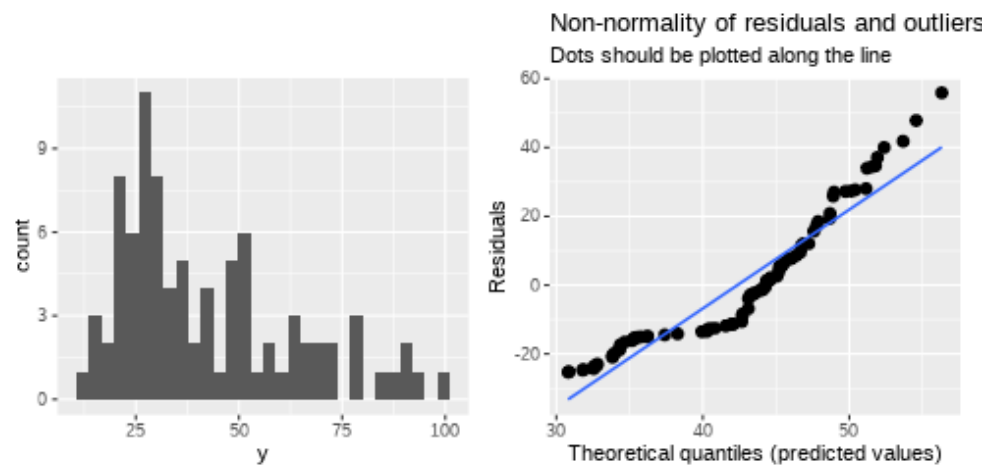


# When things look wrong

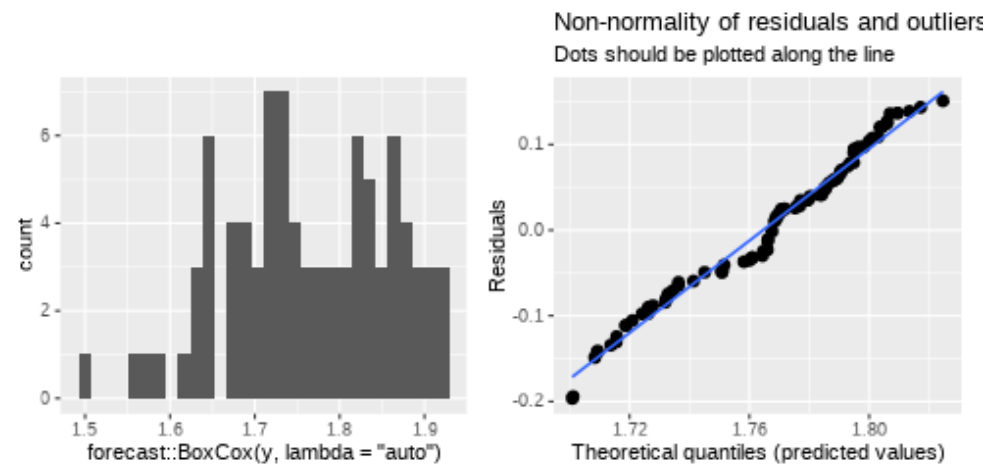
## Transformations?

- Transforming your outcome variable may help to satisfy model assumptions

```
lmer(y ~ x1 + g + (1 | cluster), df)
```



```
lmer(forecast::BoxCox(y, lambda="auto") ~ x1 + g + (1 | cluster))
```



# When things look wrong

## Transformations?

- Transforming your outcome variable may help to satisfy model assumptions **but it comes at the expense of interpretability.**

```
lmer(y ~ x1 + g + (1 | cluster), df)
```

```
## (Intercept)          x1          g  
##      36.137      1.615     10.020
```

```
lmer(forecast::BoxCox(y, lambda="auto") ~ x1 + g + (1 | cluster), df)
```

```
## (Intercept)          x1          g  
##      1.733760     0.006857     0.048426
```

# When things look wrong

## Bootstrap?

basic idea:

1. do many many times:
  - a. take a sample (e.g. sample with replacement from your data, or simulated from your model parameters)
  - b. fit the model to the sample
2. then:
  - a. based on all the models fitted in step 1, obtain a distribution of parameter estimate of interest.
  - b. based on the bootstrap distribution from 2a, compute a confidence interval for estimate.
  - c. celebrate

# Bootstrap: What do we (re)sample?

resample based on the estimated distributions of parameters?

- assumes explanatory variables are fixed, model specification and the distributions (e.g.  $\zeta \sim N(0, \sigma_\zeta)$  and  $\varepsilon \sim N(0, \sigma_\varepsilon)$ ) are correct.

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resample residuals

- $y^* = \hat{y} + \hat{\varepsilon}_{\text{sampled with replacement}}$
- assumes explanatory variables are fixed, and model specification is correct.

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resample residuals

- $y^* = \hat{y} + \hat{\varepsilon}_{\text{sampled with replacement}}$
- assumes explanatory variables are fixed, and model specification is correct.

resample cases

- **minimal** assumptions - that we have correctly specified the hierarchical structure of data
- **But** do we resample:
  - observations?
  - clusters?
  - both?

# Bootstrap: Parametric

```
reducedmodel <- lmer(emot_dysreg ~ crq + age + (1 | schoolid), data = crq)
mymodel <- lmer(emot_dysreg ~ crq + age + int + (1 | schoolid), data = crq)
```

- bootstrap LRT

```
library(pbkrtest)
PBmodcomp(mymodel, reducedmodel)
```

- bootstrap CIs

```
confint(mymodel, method="boot")
```

# Bootstrap: Parametric

```
reducedmodel <- lmer(emot_dysreg ~ crq + age + (1 | schoolid), data = crq)
mymodel <- lmer(emot_dysreg ~ crq + age + int + (1 | schoolid), data = crq)
```

- bootstrap LRT

```
library(pbkrtest)
PBmodcomp(mymodel, reducedmodel)
```

- bootstrap CIs

```
confint(mymodel, method="boot")
```

- **lmeresampler** package bootstrap() function

```
library(lmeresampler)
mymodelBS <- bootstrap(mymodel, .f = fixef, type = "parametric", B = 2000)
confint(mymodelBS, type = "norm")
```

At time of writing, there is a minor bug with the version of **lmeresampler** that you can download from CRAN, so we recommend installing directly from the package maintainer: `devtools::install_github("aloy/lmeresampler")`



# Bootstrap: Cases

```
mymodel <- lmer(emot_dysreg ~ crq + age + int + (1 | schoolid), data = crq)
```

```
# devtools::install_github("aloy/lmeresampler")
library(lmeresampler)
# resample only children, not schools
mymodelBScase <- bootstrap(mymodel, .f = fixef,
                           type = "case", B = 2000,
                           resample = c(FALSE, TRUE))
summary(mymodelBScase)
```

```
## Bootstrap type: case
```

```
##
```

```
## Number of resamples: 2000
```

```
##
```

##		term	observed	rep.mean	se	bias
## 1	(Intercept)		0.9563	0.9514	0.106136	-0.0049006
## 2	crq		-0.1004	-0.1007	0.013939	-0.0003475
## 3	age		0.2727	0.2731	0.007825	0.0004362
## 4	intTreatment		-0.1520	-0.1525	0.024481	-0.0005422

```
##
```

```
## There were 0 messages, 0 warnings, and 0 errors.
```

For a nice how-to guide on the **lmeresampler** package, see <http://aloy.github.io/lmeresampler/articles/lmeresampler-vignette.html>.

For a discussion of different bootstrap methods for multilevel models, see Leeden R., Meijer E., Busing F.M. (2008) Resampling Multilevel Models. In: Leeuw J., Meijer E. (eds) Handbook of Multilevel Analysis. Springer, New York, NY. DOI: 10.1007/978-0-387-73186-5\_11

```
confint(mymodelBScase, type = "basic")
```

```
## # A tibble: 4 × 6
```

##	term	estimate	lower	upper	type	level
##	<chr>	<dbl>	<dbl>	<dbl>	<chr>	<dbl>
## 1	(Intercept)	0.956	0.747	1.17	basic	0.95
## 2	crq	-0.100	-0.129	-0.0731	basic	0.95
## 3	age	0.273	0.257	0.288	basic	0.95
## 4	intTreatment	-0.152	-0.199	-0.104	basic	0.95

# Bootstrap: Cases

```
mymodel <- lmer(emot_dysreg ~ crq + age + int + (1 | schoolid), data = crq)
```

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summary(mymodelBScase)
```

```
## Bootstrap type: case
##
## Number of resamples: 2000
```

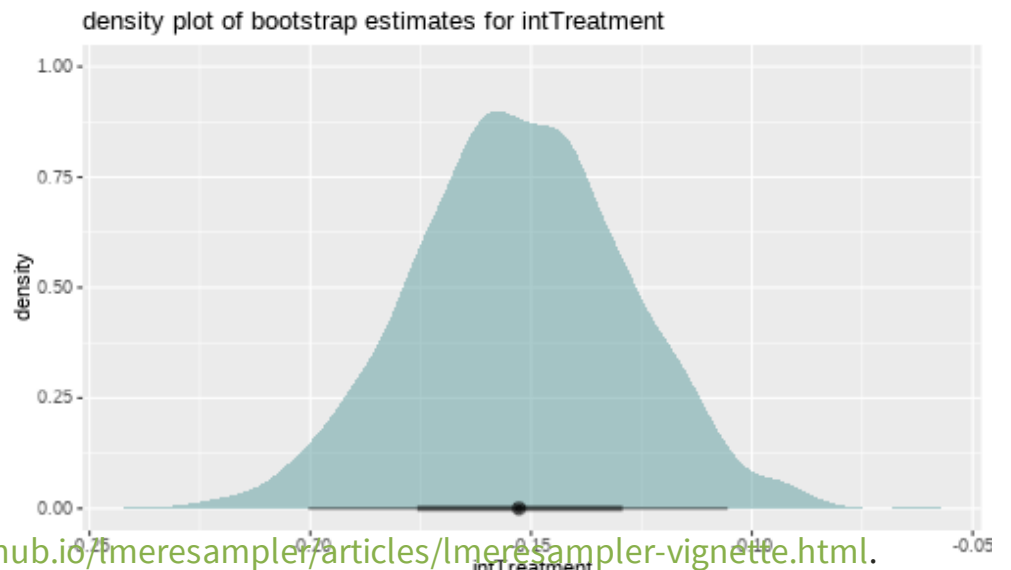
##	term	observed	rep.mean	se	bias
## 1	(Intercept)	0.9563	0.9514	0.106136	-0.0049006
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```
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```
plot(mymodelBScase, "intTreatment")
```



# Summary

- Our assumptions for multi-level models are similar to that of a standard linear model in that we are concerned with the our residuals
  - in the multi-level case, we have residuals are multiple levels.
- When assumptions appear violated, there are various courses of action to consider.
  - primarily, we should think about whether our model makes theoretical sense
- Resampling methods (e.g. Bootstrapping) can be used to obtain confidence intervals and bias-corrected estimates of model parameters.
  - There are various forms of the bootstrap, with varying assumptions.

End of Part 1

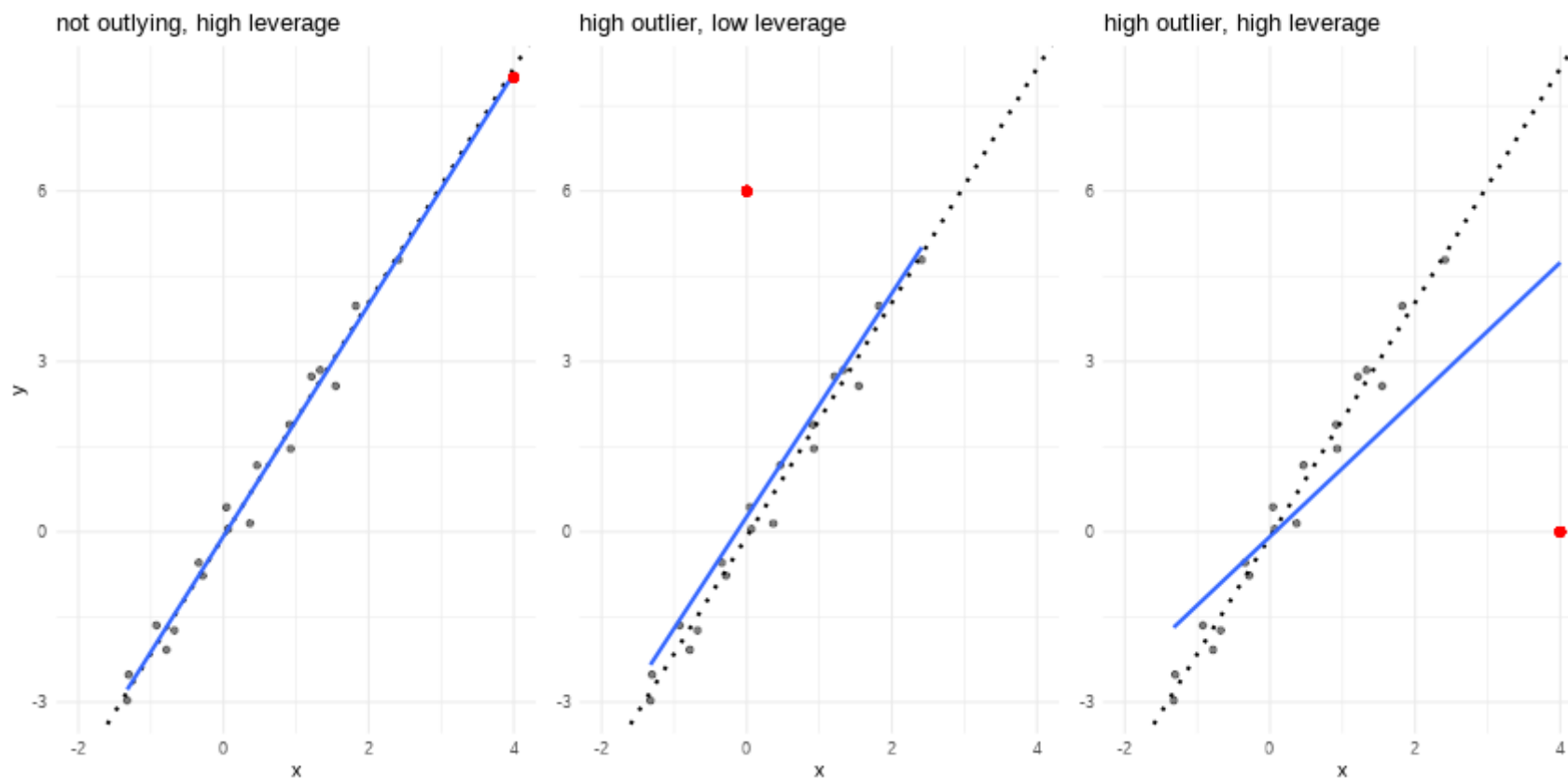
Part 1: Assumptions

Part 2: Case Diagnostics in MLM

Part 3: Random Effect Structures

# Influence

Just like standard `lm()`, observations can have unduly high influence on our model through a combination of high leverage and outlyingness.



# multiple levels...

- Both observations (level 1 units) **and** clusters (level 2+ units) can be influential.

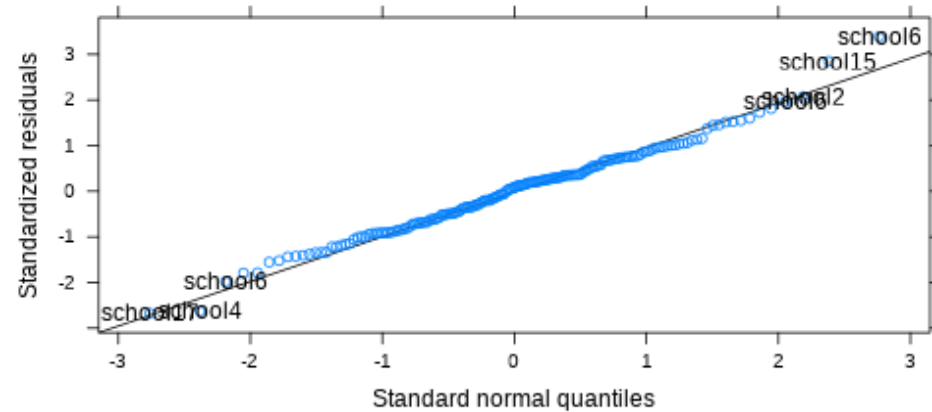
# multiple levels...

- Both observations (level 1 units) **and** clusters (level 2+ units) can be influential.
- several packages, but current recommendation is **HLMdiag**: <http://aloy.github.io/HLMdiag/index.html>



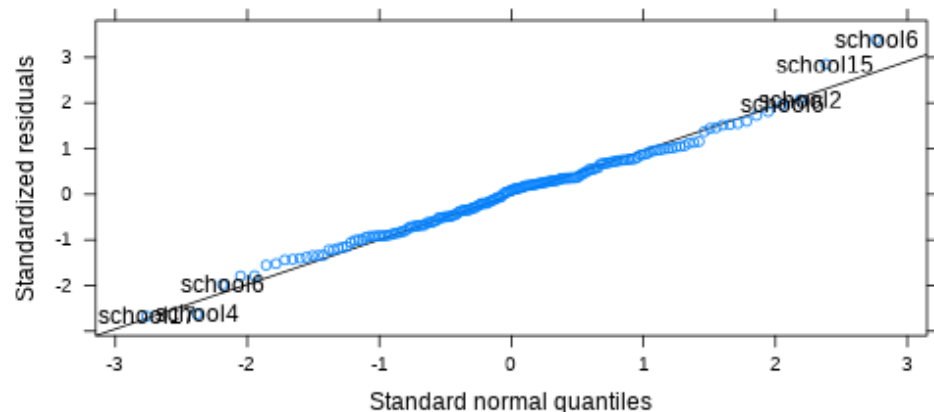
# Level 1 influential points

```
mymodel <- lmer(emot_dysreg ~ crq + age +  
               int + (1 | schoolid),  
               data = crq)  
qqmath(mymodel, id=0.05)
```



# Level 1 influential points

```
mymodel <- lmer(emot_dysreg ~ crq + age +
               int + (1 | schoolid),
               data = crq)
qqmath(mymodel, id=0.05)
```



```
library(HLMdiag)
infl1 <- hlm_influence(mymodel, level = 1)
names(infl1)
```

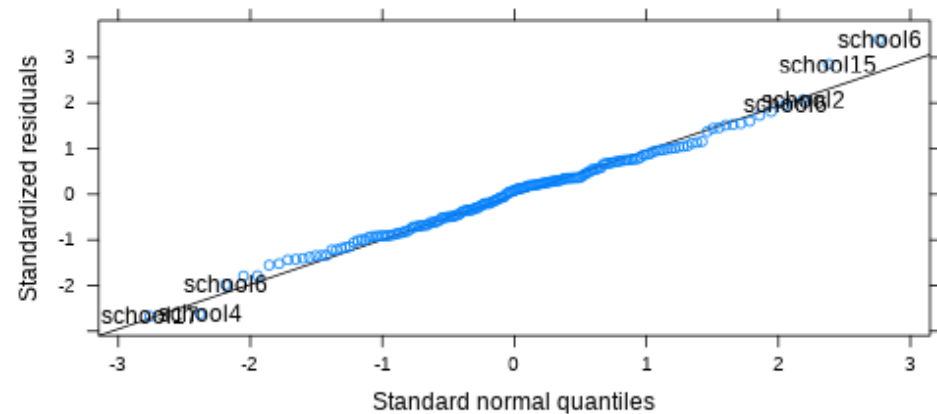
```
## [1] "id"           "emot_dysreg"  "crq"          "age"
## [5] "int"          "schoolid"     "cooks"         "mdffit"
## [9] "covtrace"     "covratio"     "leverage.overall"
```

```
infl1
```

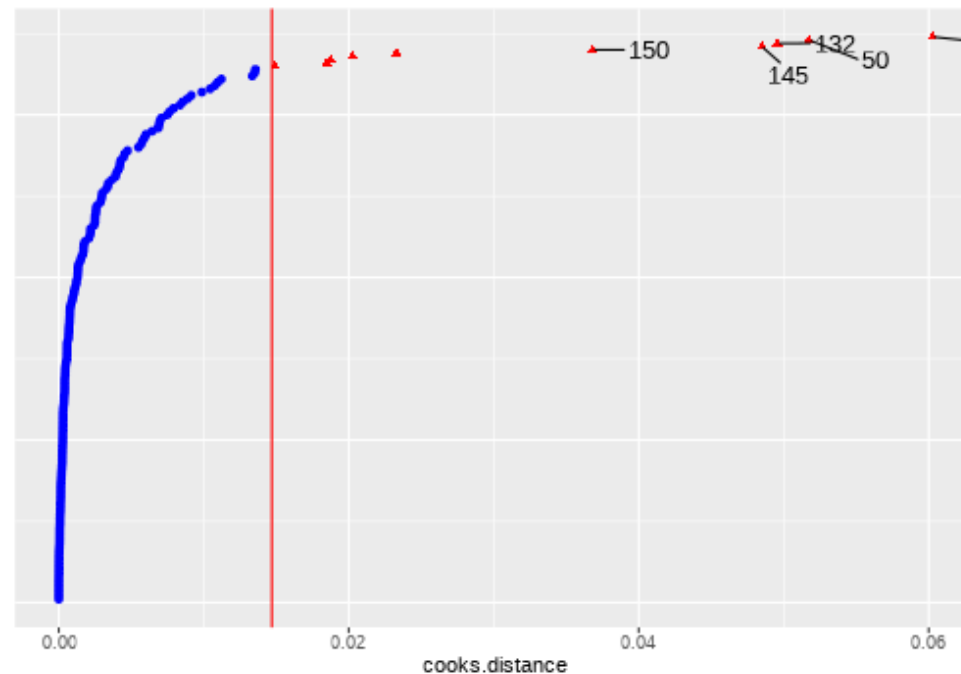
```
## # A tibble: 174 × 11
##   id emot_dysreg crq age int schoolid cooks mdffit
##   <int>      <dbl> <dbl> <dbl> <fct>   <fct>      <dbl>   <dbl>
## 1     1         4.12  1.92   14 Treatment school1  0.0000660  6.59e
## 2     2         3.22  1.65   11 Treatment school1  0.00749    7.34e
## 3     3         4.86  3.56   16 Treatment school1  0.0185    1.80e
## 4     4         4.79  1.45   16 Treatment school1  0.0000195  1.92e
## 5     5         3.58  0.81   12 Treatment school1  0.00692    6.79e
## 6     6         4.41  2.71   15 Treatment school1  0.00000410 4.07e
## 7     7         4.23  3.01   14 Treatment school1  0.00104    1.04e
## 8     8         3.66  1.61   12 Treatment school1  0.000102    1.01e
## 9     9         4.22  2.17   14 Treatment school1  0.00000750 7.50e
## 10    10         4.42  2.28   14 Treatment school2  0.000254   2.53e
## # ... with 164 more rows, and 2 more variables: covratio <dbl>,
## #   leverage.overall <dbl>
```

# Level 1 influential points

```
mymodel <- lmer(emot_dysreg ~ crq + age +  
  int + (1 | schoolid),  
  data = crq)  
qqmath(mymodel, id=0.05)
```

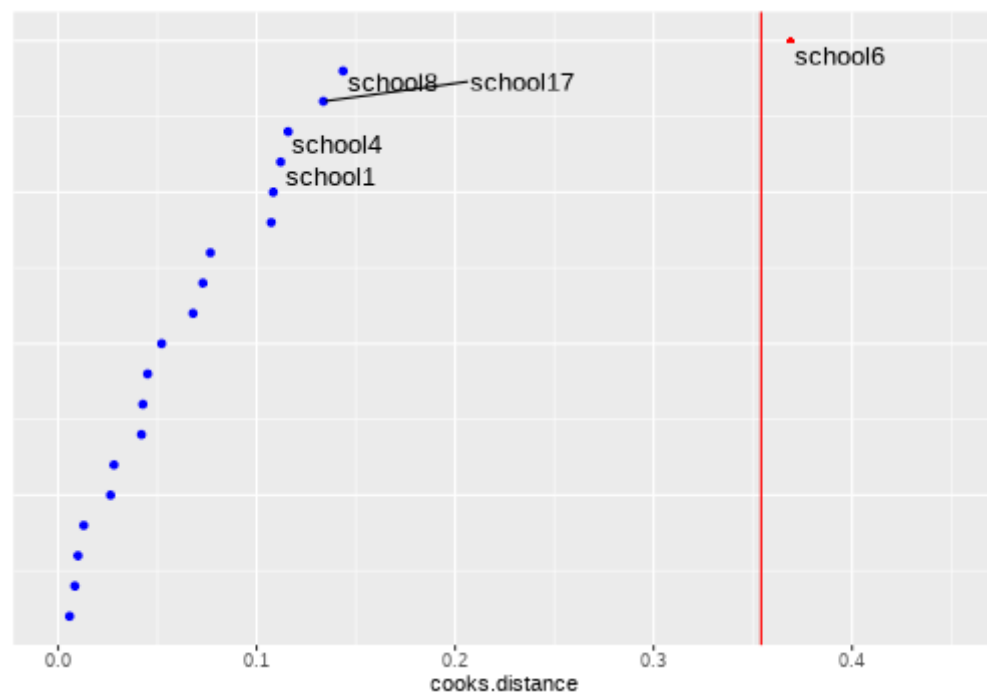


```
library(HLMdiag)  
infl1 <- hlm_influence(mymodel, level = 1)  
dotplot_diag(infl1$cooks, cutoff = "internal")
```



# Level 2 influential clusters

```
infl2 <- hlm_influence(mymodel, level = "schoolid")  
dotplot_diag(infl2$cooks, cutoff = "internal", index=infl2$schoolid)
```



# What to do?

- In this context (children from schools), I would be inclined not to worry too much about the individual children who have high values on cook's distance, **if** we plan on case-based bootstrap for our inferential tests (and plan on resampling the level 1 units - the children).

# What to do?

- In this context (children from schools), I would be inclined not to worry too much about the individual children who have high values on cook's distance, **if** we plan on case-based bootstrap for our inferential tests (and plan on resampling the level 1 units - the children).
- It's worth looking into school 6 a bit further.
- **mdffits** is a measure of multivariate "difference in fixed effects"

```
infl2 %>% arrange(desc(mdffits))
```

```
## # A tibble: 20 × 6
##   schoolid cooks mdffits covtrace covratio leverage.overall
##   <fct>      <dbl>   <dbl>   <dbl>   <dbl>         <dbl>
## 1 school6  0.369   0.330   0.253   1.27         0.107
## 2 school8  0.144   0.128   0.245   1.26         0.131
## 3 school17 0.134   0.121   0.267   1.29         0.108
## 4 school1  0.112   0.104   0.193   1.20         0.117
## 5 school4  0.116   0.103   0.267   1.29         0.111
## 6 school5  0.108   0.0992  0.239   1.26         0.129
## 7 school11 0.107   0.0990  0.229   1.24         0.110
## 8 school7  0.0767  0.0701  0.283   1.31         0.148
## 9 school18 0.0730  0.0675  0.118   1.12         0.126
## 10 school16 0.0680  0.0620  0.195   1.21         0.122
## 11 school15 0.0522  0.0503  0.185   1.19         0.122
## 12 school20 0.0451  0.0426  0.242   1.26         0.105
## 13 school2  0.0427  0.0411  0.148   1.15         0.171
## 14 school9  0.0420  0.0405  0.186   1.20         0.122
## 15 school12 0.0281  0.0259  0.256   1.28         0.126
```

# What to do?

- In this context (children from schools), I would be inclined not to worry too much about the individual children who have high values on cook's distance, **if** we plan on bootstrapping our inferential tests (and plan on resampling the level 1 units - the children).
- It's worth looking into school 6 a bit further.
- examine fixed effects upon deletion of schools 6

```
delete6 <- case_delete(mymodel, level = "schoolid", type = "fixef", delete = "school6")  
cbind(delete6$fixef.original, delete6$fixef.delete)
```

```
##           [,1]      [,2]  
## (Intercept)  0.9563  1.06034  
## crq         -0.1004 -0.08985  
## age          0.2727  0.26519  
## intTreatment -0.1520 -0.18202
```

# Sensitivity Analysis?

Would our conclusions change if we excluded these schools?

```
mymodelrm6 <- lmer(emot_dysreg ~ crq + age +  
  int + (1 | schoolid),  
  data = crq %>%  
  filter(!schoolid %in% c("school6"))  
mymodelrm6BS <- bootstrap(mymodelrm6, .f = fixef,  
  type = "case", B = 2000,  
  resample = c(FALSE, TRUE))  
confint(mymodelrm6BS, type = "basic")
```

```
## # A tibble: 4 × 6  
##   term      estimate lower  upper type level  
##   <chr>      <dbl> <dbl>  <dbl> <chr> <dbl>  
## 1 (Intercept)  1.06  0.857  1.26  basic  0.95  
## 2 crq        -0.0899 -0.117 -0.0627 basic  0.95  
## 3 age         0.265  0.251  0.280  basic  0.95  
## 4 intTreatment -0.182 -0.229 -0.136  basic  0.95
```



# Summary

- Influence can be exerted by individual observations and higher level groups of observations
  - e.g. by children and by schools, or by individual trials and by participants.
- We can get measures of influence at different levels, and consider how estimates and conclusions might change when certain observations (or groups) are excluded
- Bootstrapping is relevant as whether we are resampling at the level of an influential group/observation is going to affect the extent to which our estimates are biased by that observation/group

End of Part 3

Part 1: Assumptions

Part 2: Case Diagnostics in MLM

Part 3: Random Effect Structures

# What have we seen so far?

- children within schools
- birds within gardens
- measurements within participants
- nurses within hospitals
- and probably some others...

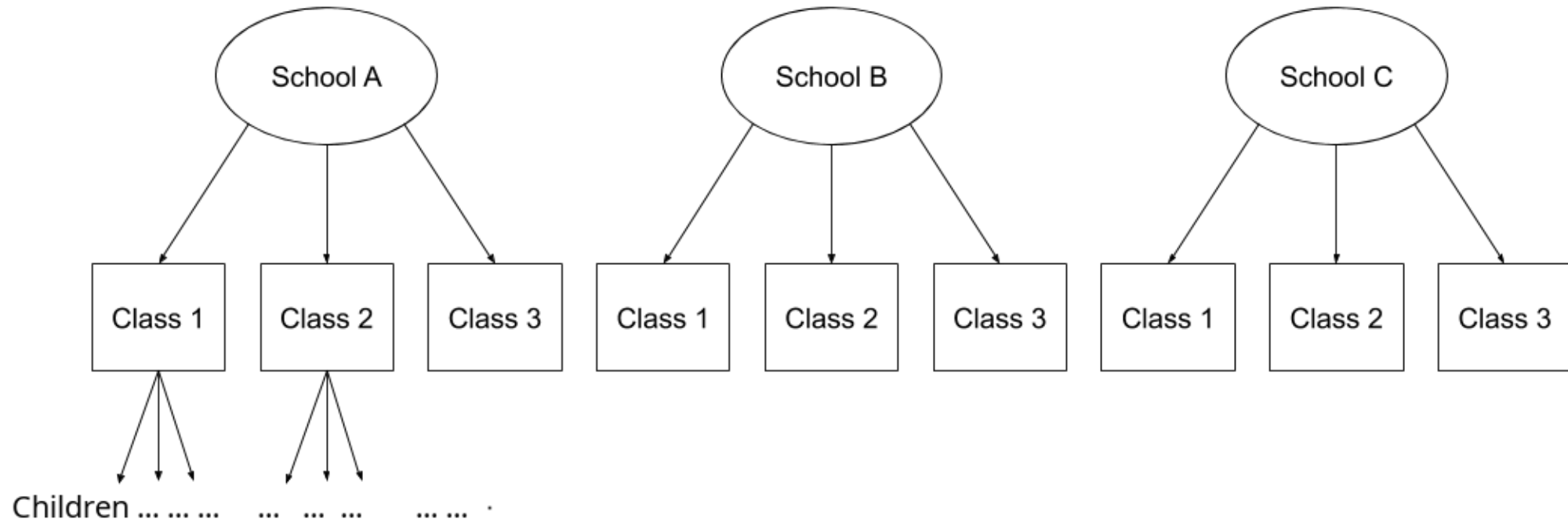
# Nested

- the level  $j$  observations in a level  $i$  group belong **only** to that level  $i$  group.



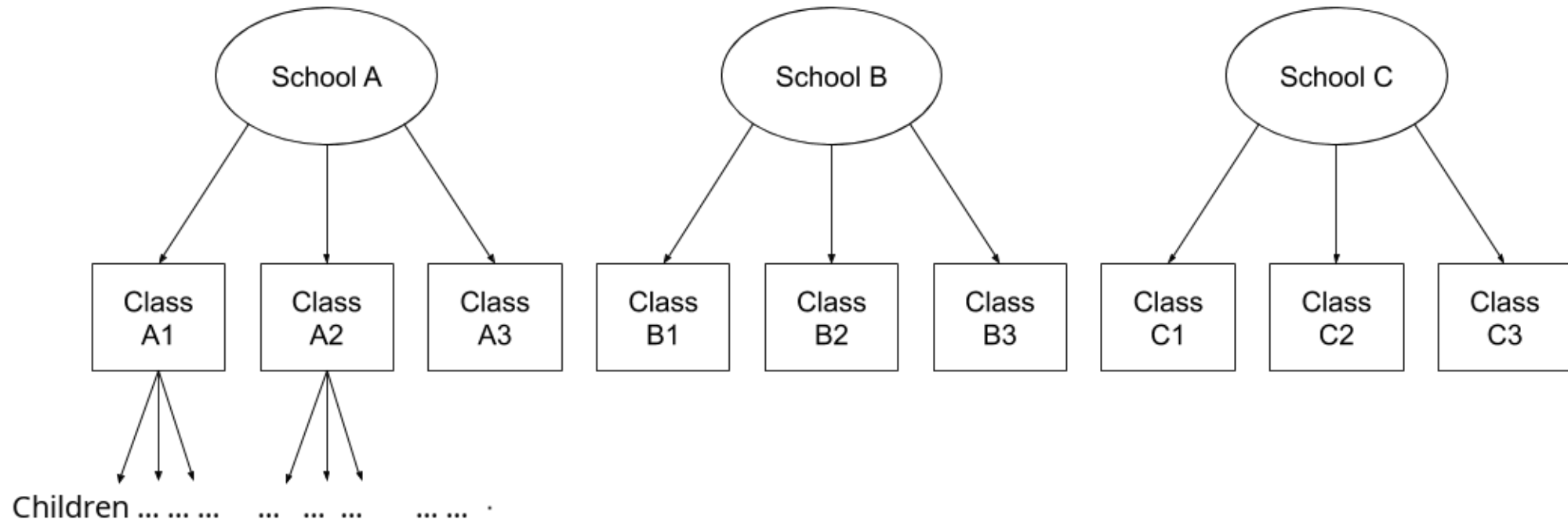
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- (1 | school/class)** or **(1 | school) + (1 | class:school)**



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- the level  $j$  observations in a level  $i$  group belong **only** to that level  $i$  group.
- If labels are unique,  $(1 \mid \text{school}) + (1 \mid \text{class})$  is the same as  $(1 \mid \text{school/class})$



# Crossed

- "crossed" = not nested!



# Crossed

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- `(1 | subject) + (1 | task)`

# Fixed or random

Criterion:	Repetition: <i>If the experiment were repeated:</i>	Desired inference: <i>The conclusions refer to:</i>
Fixed effects	Same levels would be used	The levels used
Random effects	Different levels would be used	A population from which the levels used are just a (random) sample

- If only small number of clusters, estimating variance components may be unstable.
- Partialling out cluster-differences as fixed effects *may* be preferable.

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maxmodel <- lmer(emot_dysreg ~ crq + age + int + (1 + crq + age | schoolid), data = crq)
```

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another example: 16 items each occur in 4 different combinations: condition A vs B  $\times$  type 1 vs 2.  
40 participants see all items in all conditions (64 trials each participant).

```
mmod <- lmer(outcome ~ condition * type + (1 + condition * type | ppt) +  
            (1 + condition * type | item), data = kelly)
```

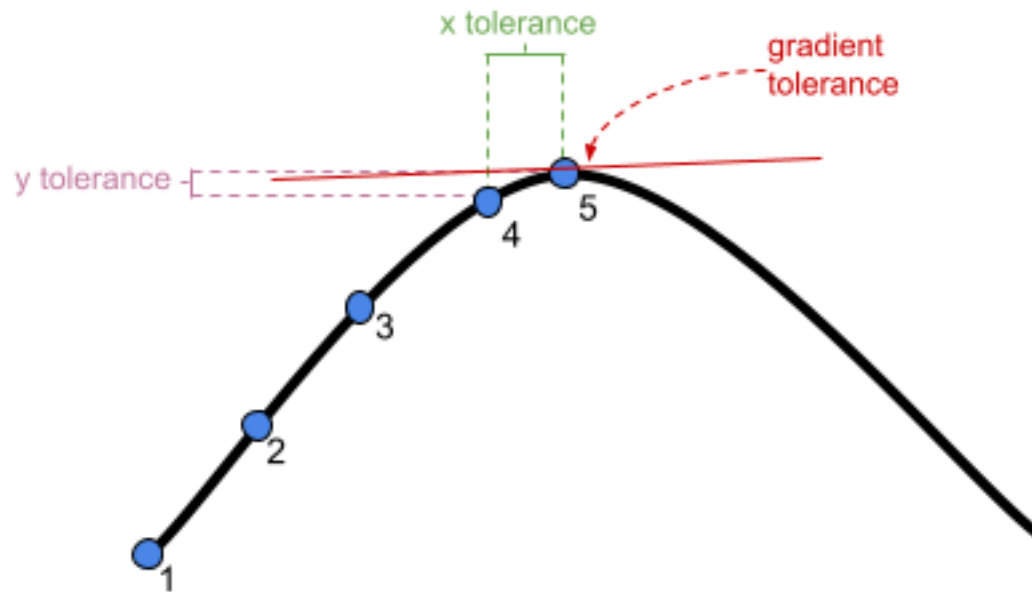
```
## boundary (singular) fit: see ?isSingular
```

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- **No right answer**

# correlations between random effects

##	Groups	Name	Std.Dev.	Corr
##	ppt	(Intercept)	91.7	
##		conditionB	59.1	-0.21
##		type2	27.6	0.25 -0.42
##		conditionB:type2	22.4	-0.32 -0.86 0.26
##	item	(Intercept)	37.0	
##		conditionB	35.8	-0.18
##		type2	20.2	0.14 -0.40
##		conditionB:type2	65.6	0.25 0.27 -0.92
##	Residual		203.2	

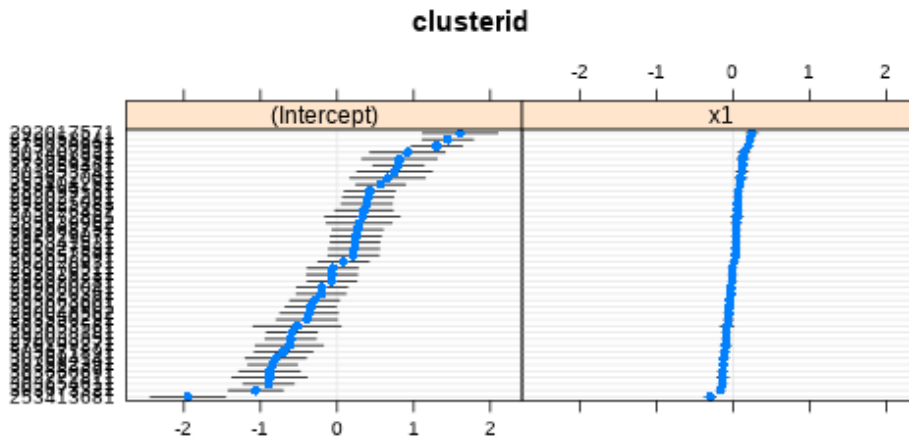
# correlations between random effects

## perfect correlations

```
m1 <- lmer(y ~ 1 + x1 +  
            (1 + x1 | clusterid), data = df)  
VarCorr(m1)
```

```
## Groups      Name      Std.Dev. Corr  
## clusterid (Intercept) 0.759  
##           x1          0.117    1.00  
## Residual          0.428
```

```
## $clusterid
```

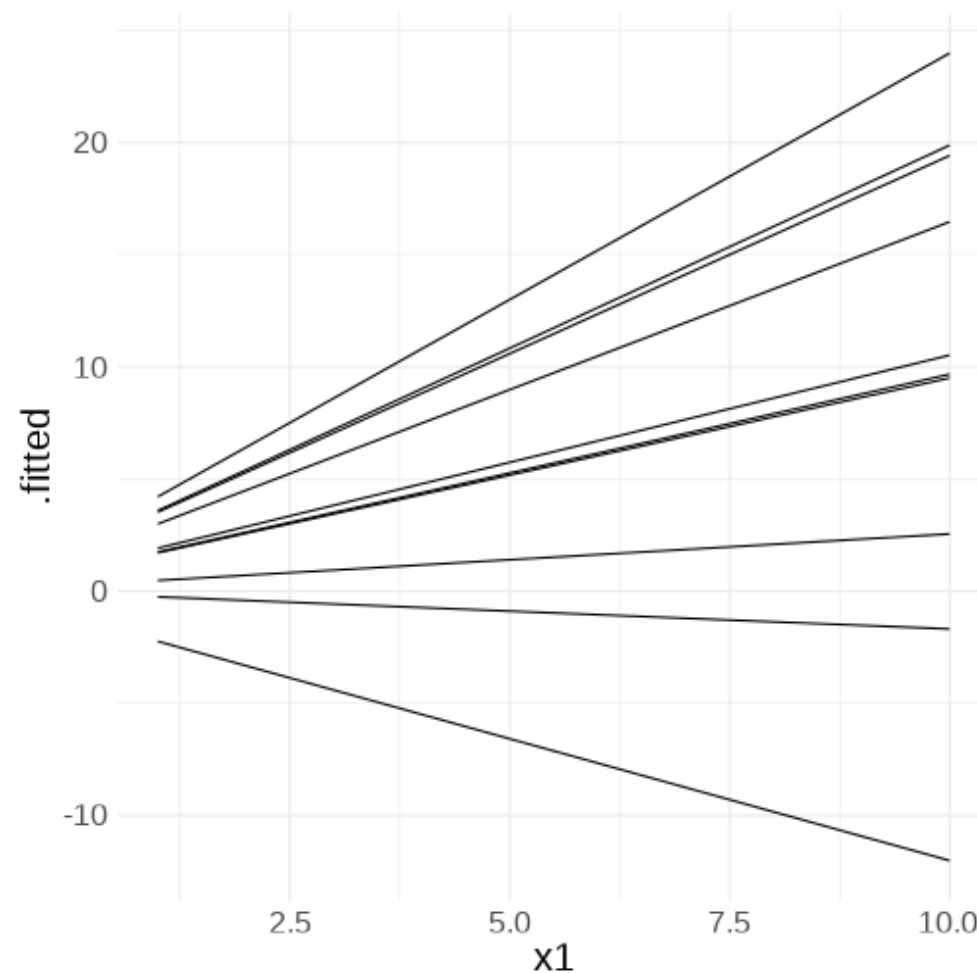
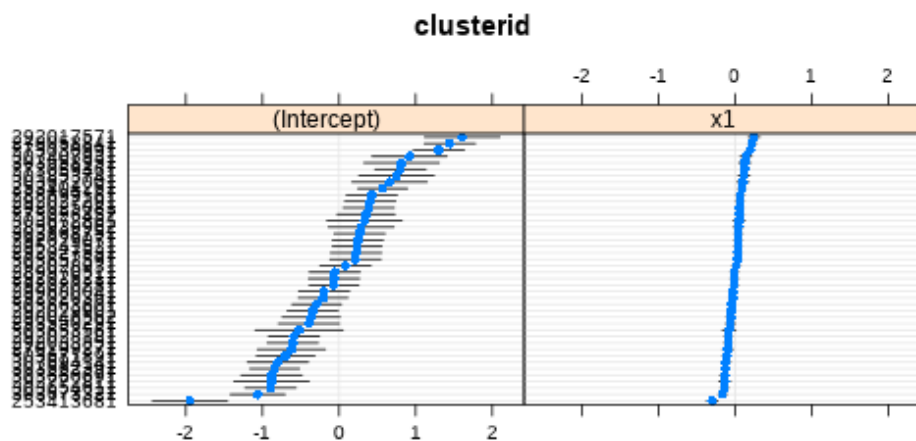


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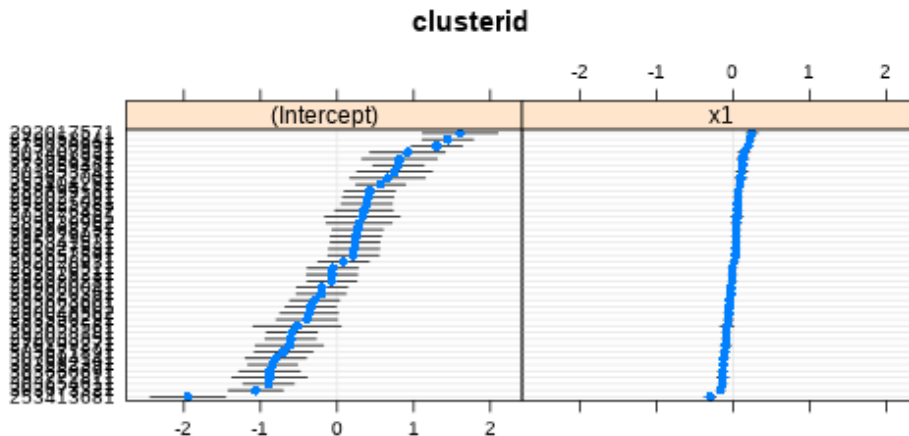
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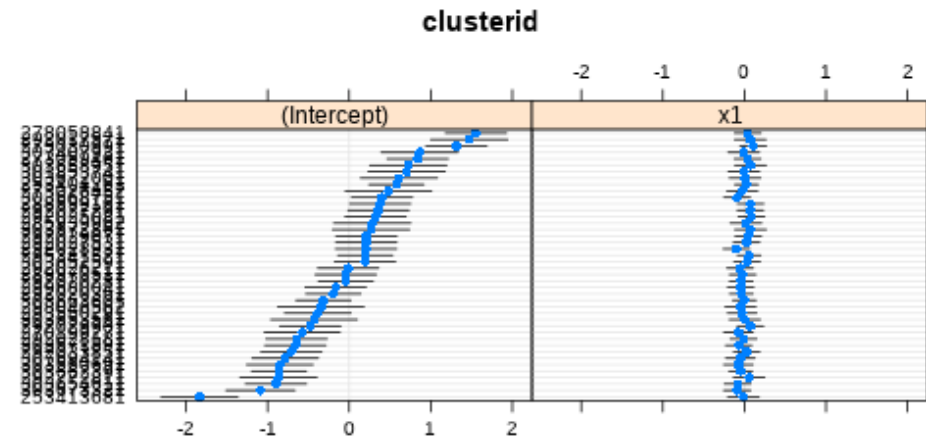


## zero correlations

```
zcpmodel <- lmer(y ~ 1 + x1 +  
                 (1 + x1 || clusterid), data = df)  
VarCorr(zcpmodel)
```

```
## Groups      Name      Std.Dev.  
## clusterid (Intercept) 0.751  
## clusterid.1 x1        0.104  
## Residual              0.432
```

```
## $clusterid
```



# correlations between random effects

When should we remove them?

# correlations between random effects

When should we remove them?

When it makes theoretical sense to do so.



# Summary

- random effect structures can get complicated quite quickly
  - we can have multiple levels of nesting
  - we can have crossed random effects
- the maximal random effect structure is the most complex structure we can fit to the data.
  - it often leads to problems with model convergence
- building MLMs is a balancing act between accounting for different sources of variance and attempting to fit a model that is too complex for our data.

End