

2.

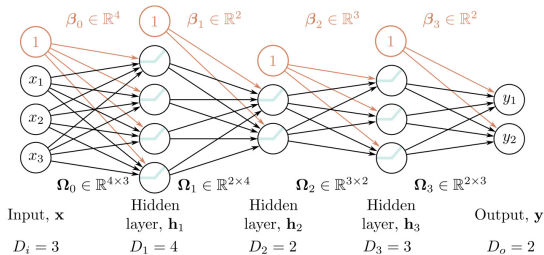
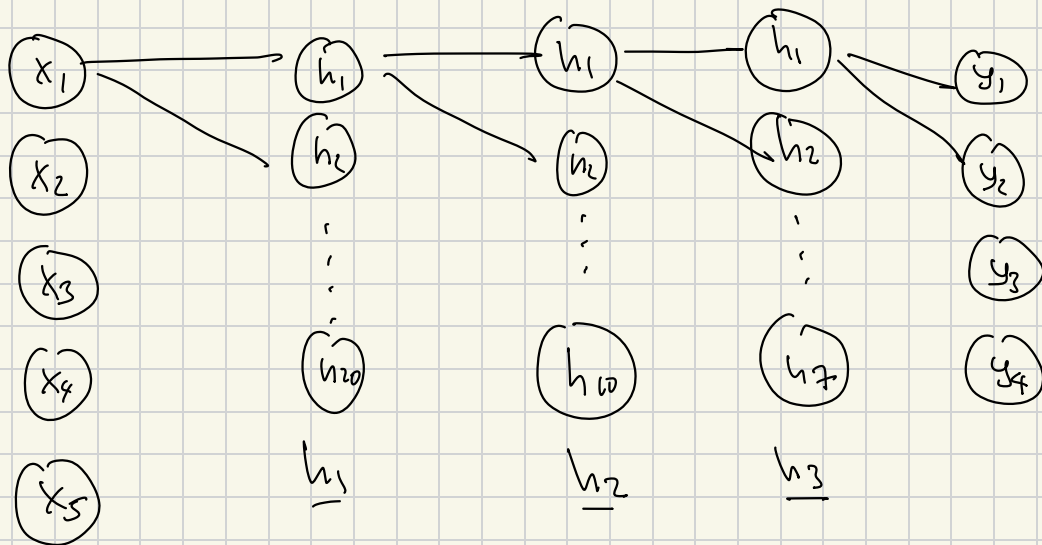


Figure 4.6 Matrix notation for network with $D_i = 3$ -dimensional input x , $D_o = 2$ -dimensional output y , and $K = 3$ hidden layers h_1, h_2 , and h_3 of dimensions $D_1 = 4$, $D_2 = 2$, and $D_3 = 3$ respectively. The weights are stored in matrices Ω_k that multiply the activations from the preceding layer to create the pre-activations at the subsequent layer. For example, the weight matrix Ω_1 that computes the pre-activations at h_2 from the activations at h_1 has dimension 2×4 . It is applied to the four hidden units in layer one and creates the inputs to the two hidden units at layer two. The biases are stored in vectors β_k and have the dimension of the layer into which they feed. For example, the bias vector β_2 is length three because layer h_3 contains three hidden units.

- Number of layers
- Hidden units in layer 1
- Hidden units in layer 2
- Hidden units in layer 3

4.



$$\underline{h}_1 = a[\underline{\beta}_0 + \underline{\Omega}_0 \underline{x}]$$

$$\underline{h}_2 = a[\underline{\beta}_1 + \underline{\Omega}_1 \underline{h}_1]$$

$$\underline{h}_3 = a[\underline{\beta}_2 + \underline{\Omega}_2 \underline{h}_2]$$

$$\underline{y} = o[\underline{\beta}_3 + \underline{\Omega}_3 \underline{h}_3]$$

↑
 some output activation func.

$$\begin{aligned} \underline{x} &\rightarrow 5 \times 1 \\ \underline{\Omega}_0 &\rightarrow 20 \times 5 \\ \underline{\beta}_0 &\rightarrow 20 \times 1 \\ \underline{\Omega}_1 &\rightarrow 10 \times 20 \\ \underline{\beta}_1 &\rightarrow 10 \times 1 \\ \underline{\Omega}_2 &\rightarrow 7 \times 10 \\ \underline{\beta}_2 &\rightarrow 7 \times 1 \\ \underline{\Omega}_3 &\rightarrow 4 \times 7 \\ \underline{\beta}_3 &\rightarrow 4 \times 1 \end{aligned}$$

6. (Consider just weights, not biases).

There are currently,

$$1 \times 10 + 9(10 \times 10) + 1 \times 10 = 10 + 900 + 10 = 920 \text{ weights}$$

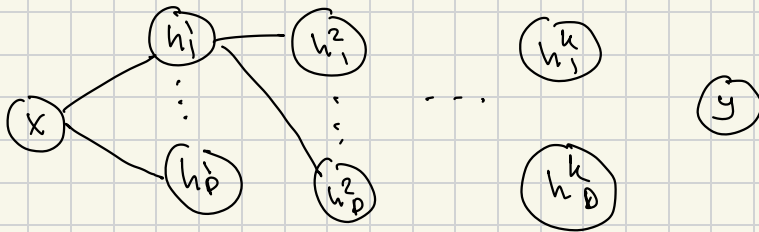
Increasing a layer (depth) gives 100 more weights = 1020 weights
Increasing width (no. nodes in each layer) gives

$$1 \times 11 + 9(11 \times 11) + 1 \times 11 = 1111 \text{ weights.}$$

So, more weights added by increasing width.

8. In the 'odd' answers.

10. Looks like.



Between the input and layer 2 there are $D + D$ params.

Between final layer and output there are $D + 1$ params

In between layers there are $(k-1)(D \times D + D)$ params.

This becomes

$$D + D + D + 1 + (k-1)(D \times D + D) \\ = 3D + 1 + (k-1)D(D+1) \text{ parameters.}$$