

A Definition

A computer program is said to learn from **experience E** with respect to some class of **tasks T** and **performance measure P** , if its performance at tasks in T , as measured by P , improves with experience E .

Tom Mitchell, *Machine Learning* (1997)

Experience | Task | Performance

What is experience?

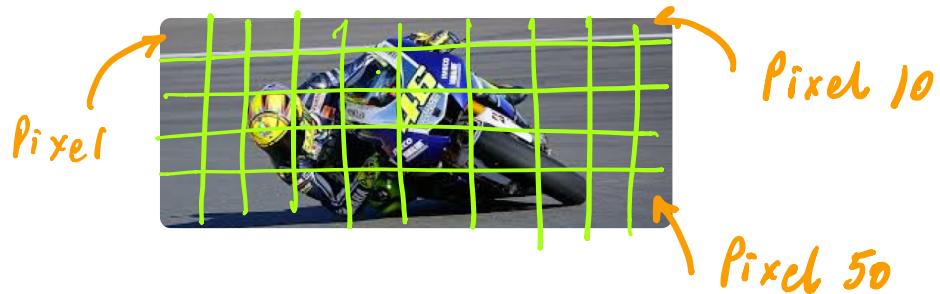
Experience \neq Rules

Experience = Data

Data = Table of Numbers



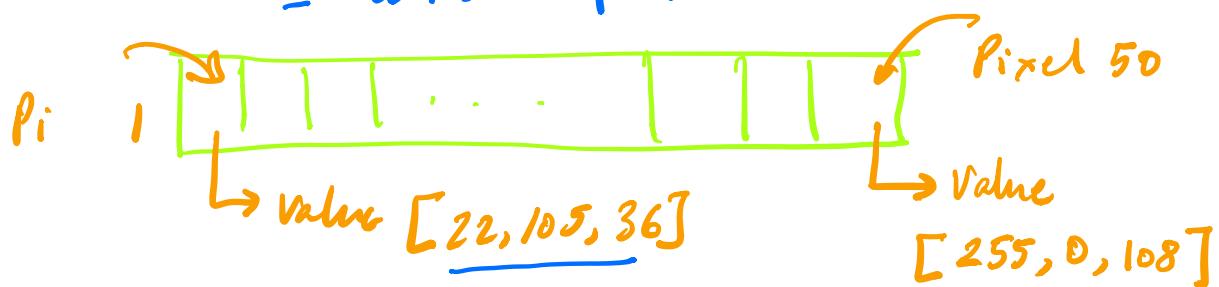
An image is
a grid of pixels



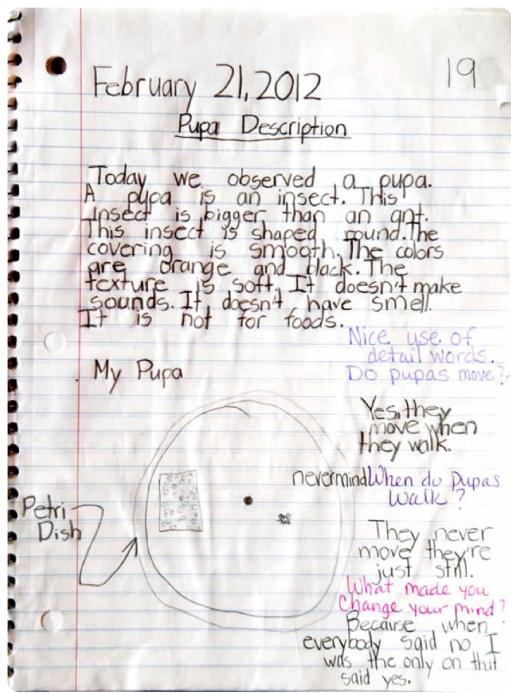
Each pixel is represented
by 3 numbers
each between 0 and 255

red value
green value
blue value

An image is a row of pixel values
= a row of numbers



Actually: a row of lists of numbers

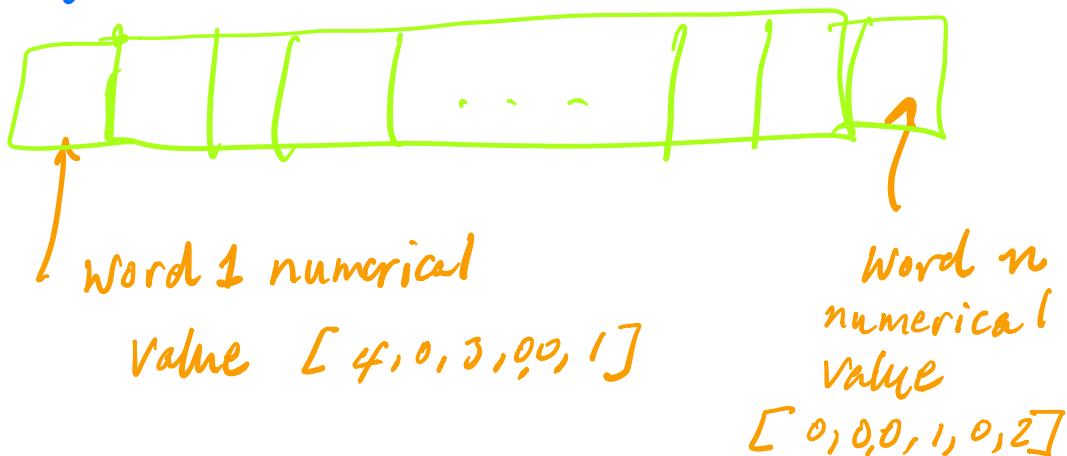


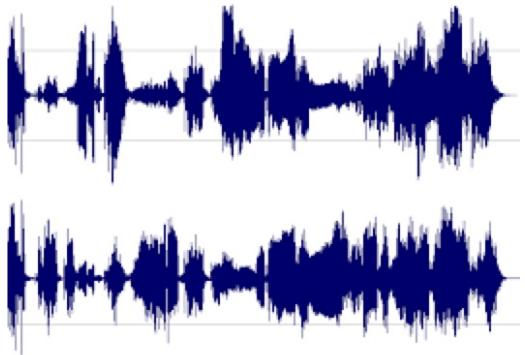
A document is a row of numbers.

Each word in a document is represented by a list of n

We'll see later what these numbers are.)

A document is a row of numbers that represent the words occurring in the document.





An audio Stream
is a row of
numbers.

For example, these numbers can
be [time, amplitude] pairs.



Diagram illustrating a table structure:

1 LastName	2 Sex	3 Age	4 Weight	5 Smoker	6 BloodPressure	7 Trials
'SMITH'	Male	38	176	1	124	93 18
'JOHNSON'	Male	43	163	0	109	77 [11,13,22]
'WILLIAMS'	Female	38	131	0	125	83 []
'JONES'	Female	40	133	0	117	75 [6,12]
'BROWN'	Female	49	119	0	122	80 [14,23]
'DAVIS'	Female	46	142	0	121	70 19
'MILLER'	Female	33	142	1	130	88 13
'WILSON'	Male	40	180	0	115	82 []
'MOORE'	Male	28	183	0	115	78 2
'TAYLOR'	Female	31	132	0	118	86 11

$m \times n$ table
 ↑ ^
 rows columns

A spreadsheet of data is a bunch of rows and columns of numbers.

Words like "Male" and "Female"
 are encoded as numbers.

Similarly, Smoker = 1
 NonSmoker = 0

Inputs / Features

f1	f2	f3	f4	f5	f6	Output

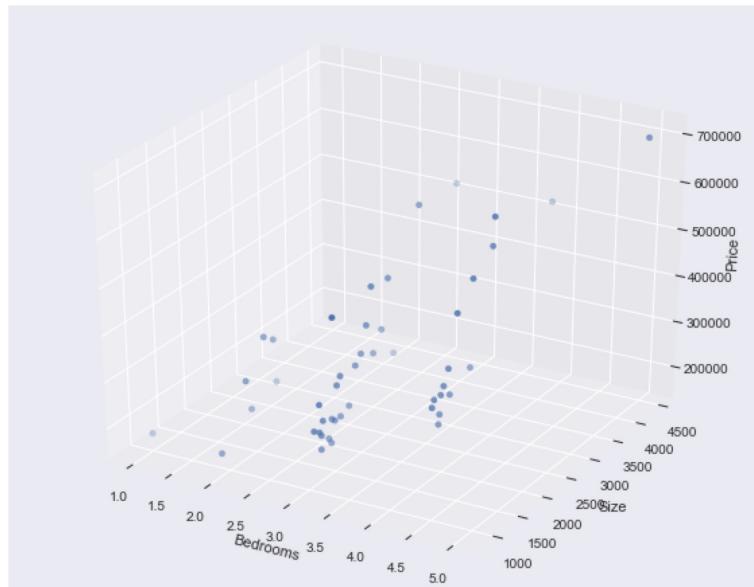
A dataset
is a spreadsheet
of $m \times n$
numbers

n inputs per row (here $n=6$)

- Inputs are called "features"
- Inputs & outputs are always numbers.
 - They can be integers - 0, 1, 2, etc.
 - They can be reals - 0.5, 26.4, etc.
 - They can be positive or negative

Tasks

- Predict a number
- Predict a Category / Class



House Prices in Portland

TASK: Predict the price of a
house not in this dataset.

How do we do this task?

Let's start with the data.

Feature 1	Feature 2	Output/target
Num of Br rooms	Size in sq ft.	Price
4	2500	\$350,000
5	3400	\$380,000

Task = Predict output based on features.

Bedrooms	Sq.ft.	Price
$x_1^{(1)}$	$x_2^{(1)}$	$y^{(1)}$
$x_1^{(2)}$	$x_2^{(2)}$	$y^{(2)}$
$x_1^{(3)}$	$x_2^{(3)}$	$y^{(3)}$
$x_1^{(4)}$	$x_2^{(4)}$	$y^{(4)}$
.	.	.

(1) ← row #
← feature #

Notation

$x_1 \leftarrow$ feature #

This is the value of
the first feature on
the first row of the
dataset.

What's the notation for the second feature
in the sixteenth row of the dataset?

To predict the price, we're going to pretend that the price can be constructed by adding and multiplying together some numbers.

$$(w_1 \times \# \text{ bedrooms}) + (w_2 \times \underline{\text{sqr. ft.}}) = \text{price}$$

Parameters Output

features

Actually, for mathematical reasons,
it's like this:

$$w_0 x_0 + w_1 x_1 + w_2 x_2 = y$$

Where w_0 is called the "intercept"
value. [We don't have to worry about
it.]

x_0 is always = 1

Let's look at this from
the standpoint of the
dataset table.

w_0	x_0	w_1	x_1	w_2	x_2	y

we've
 expanded
 the table
 by adding
 columns!

Our dataset now looks like this

row 1	w_0	$x_0^{(1)}$	w_1	$x_1^{(1)}$	w_2	$x_2^{(1)}$	$y^{(1)}$
row 2	w_0	$x_0^{(2)}$	w_1	$x_1^{(2)}$	w_2	$x_2^{(2)}$	$y^{(2)}$
row 3	w_0	$x_0^{(3)}$	w_1	$x_1^{(3)}$	w_2	$x_2^{(3)}$	$y^{(3)}$
row 4	w_0	$x_0^{(4)}$	w_1	$x_1^{(4)}$	w_2	$x_2^{(4)}$	$y^{(4)}$
.
row m	w_0	$x_0^{(m)}$	w_1	$x_1^{(m)}$	w_2	$x_2^{(m)}$	$y^{(m)}$

For each row, we're going to say:

$$\begin{aligned} w_0 x_0^{(1)} + w_1 x_1^{(1)} + w_2 x_2^{(1)} &= \hat{y}^{(1)} \\ w_0 x_0^{(2)} + w_1 x_1^{(2)} + w_2 x_2^{(2)} &= \hat{y}^{(2)} \\ w_0 x_0^{(3)} + w_1 x_1^{(3)} + w_2 x_2^{(3)} &= \hat{y}^{(3)} \\ w_0 x_0^{(4)} + w_1 x_1^{(4)} + w_2 x_2^{(4)} &= \hat{y}^{(4)} \\ \vdots &\quad \vdots \quad \vdots \quad \vdots \end{aligned}$$

w_0 , w_1 , and w_2 do not change from row to row.

Notice: While the x_1 s and x_2 s and \hat{y} s are different in each row, w_0 , w_1 , and w_2 are the SAME in every row.

OK, let's get back to our data table and look at the first row.

	w_0	$x_0^{(1)}$	w_1	$x_1^{(1)}$	w_2	$x_2^{(1)}$	$y^{(1)}$	$\hat{y}^{(1)}$
							Size ↓	Price ↓
	?	1	?	4	?	2500	350000	?
							always = 1	

(A) we'd like to calculate $\hat{y}^{(1)}$ - the predicted price by calculating:

$$\hat{y}^{(1)} = (w_0 \times x_0^{(1)}) + (w_1 \times x_1^{(1)}) + (w_2 \times x_2^{(1)})$$

(B) we'd like $\hat{y}^{(1)}$ to be as close to $y^{(1)}$ as possible

Given (A) and (B) what should the values of w_0, w_1 , and w_2 be?

First Try

$$(w_0 \times 1) + (w_1 \times 4) + (w_2 \times 2500) = 350000$$

In other words: Make the prediction exactly equal to the actual price of the house.

Great! We're focused on minimizing the difference between the predicted and the actual price.

But this still leaves us with

too many options for the values of w_0 , w_1 , and w_2

Solution / Approach

Just guess the values
of w_0, w_1, w_2 .

How about

$$w_0 = -10$$

$$w_1 = 500$$

$$w_2 = 120.5$$

This gives us a predicted price

$$\hat{y}^{(1)} = 318,440$$

Compared to $\hat{y}^{(1)}$ - actual

price: 350,000

Not bad. A little lower

than the actual price.

How good is this prediction?

The Thinking How much should we be penalized for this incorrect prediction?

Start With

What is the "cost" of being wrong?

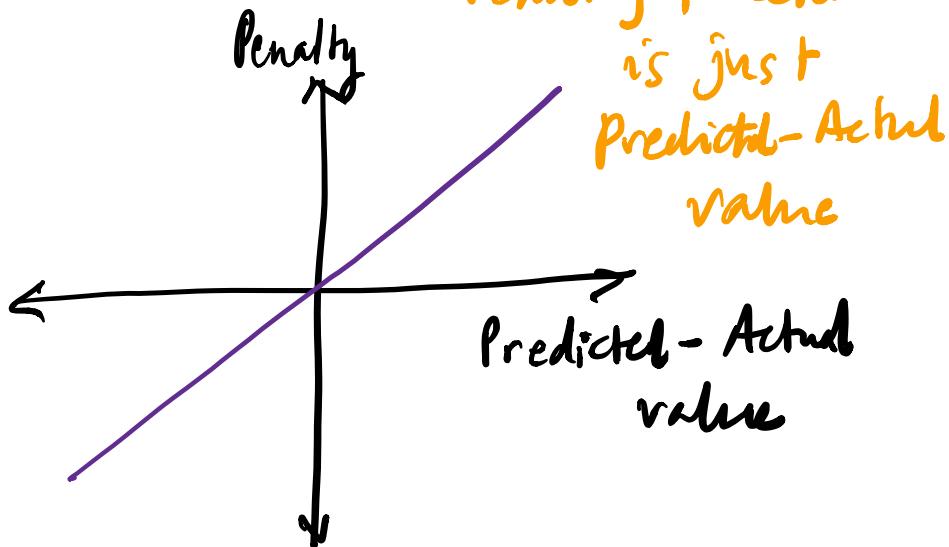
$$\text{Cost} = \frac{\text{Predicted Value}}{\text{Actual Value}}$$

Penalty Functions

How should we construct the penalty? This is a choice we can make / should make based on our knowledge of what's at stake when we make predictions.

A SELECTION OF PENALTY FUNCTIONS

①



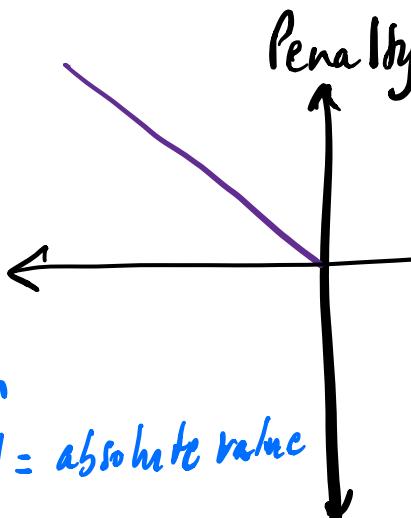
Penalty function
is just
Predicted - Actual
value

Predicted - Actual
value

Is this a good penalty function?

Why or why not?

②



Penalty function

$|$

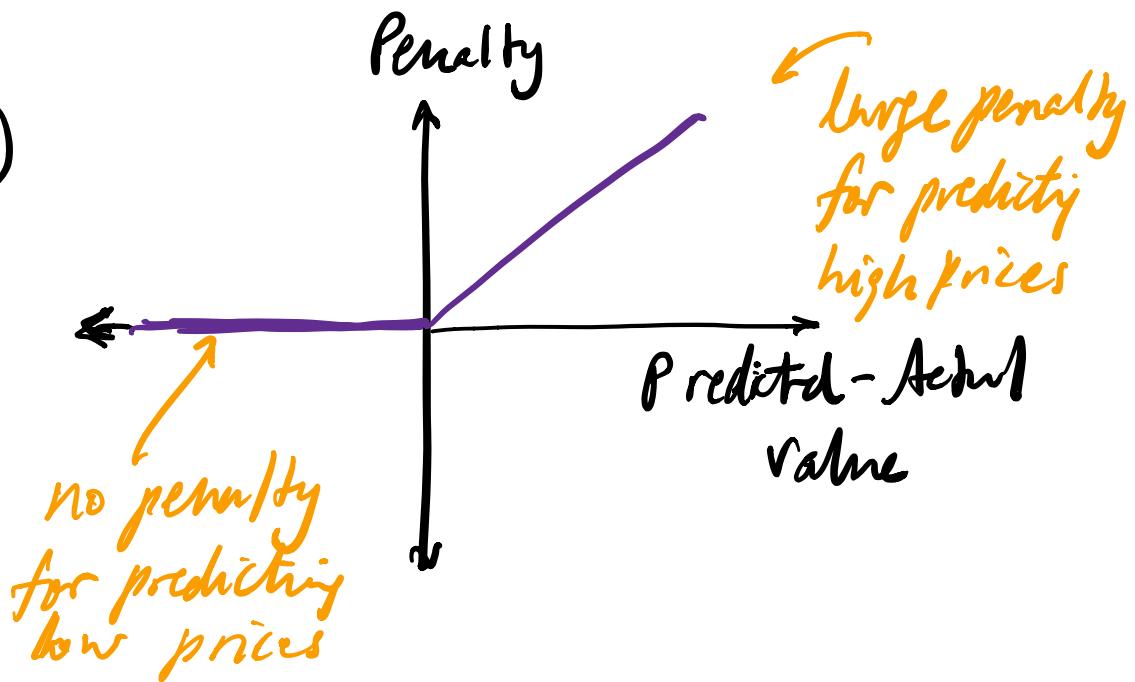
$|$ Predicted - Actual
value

Predicted - Actual
value

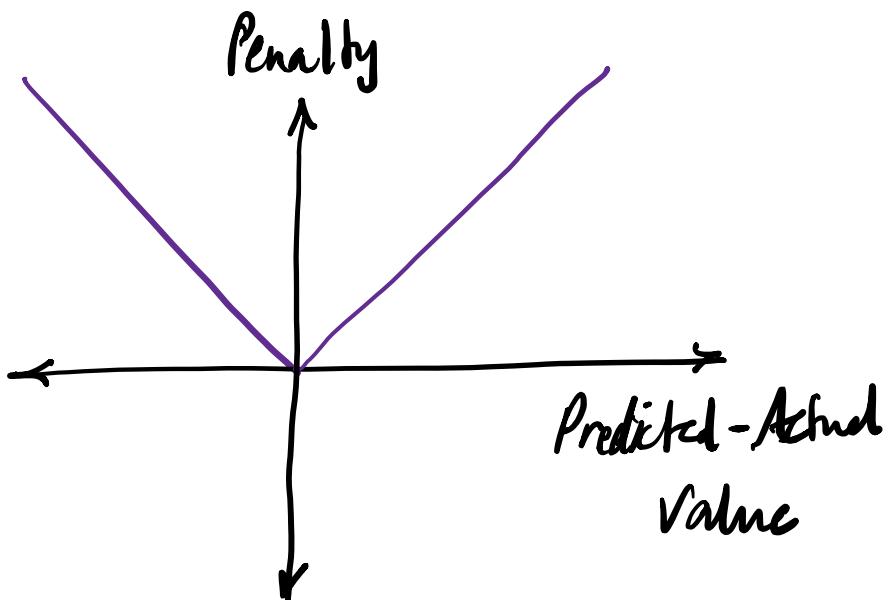
Notation

$| \dots |$ = absolute value

③

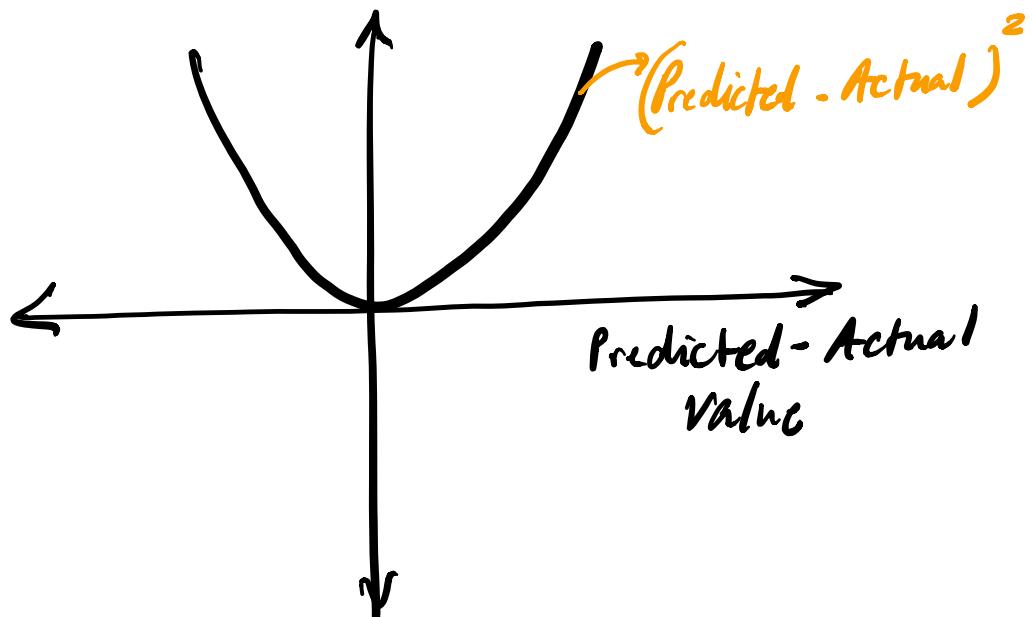


④



Describe this penalty function.
Is it reasonable?

Experience has taught us that some penalty functions work better than others. In particular, one that we'll see a lot of is this one:



$$\text{Penalty} = (\text{Predicted} - \text{Actual})^2$$

[Exercise] Create 3 penalty

functions we have not yet

seen. For each one,

describe it in a sentence

or two.

Let's go back to our data table and expand it to include one more column.

	Parameters			features		Actual	Predicted	Penalty	
	w_0	x_0	w_1	x_1	w_2	x_2	y	\hat{y}	
row1	w_0	1	w_1				y	\hat{y}	
row2	w_0	1	w_1						
:	w_0	1	w_1						
:	w_0	1	w_1						
Row m	w_0	1	w_1						

x_0 is always 1

□ The better the prediction the lower the penalty.

□ The best prediction has the lowest / minimum penalty.

What does it mean to minimize the penalty?

We have the values of w_0 , w_1 , and w_2 to set - they take on the same values for each row.

Let's say we pick the same values as before: $w_0 = -10$
 $w_1 = 500$
 $w_2 = 120.5$

For these values, let's calculate the penalty for every row of the data table.

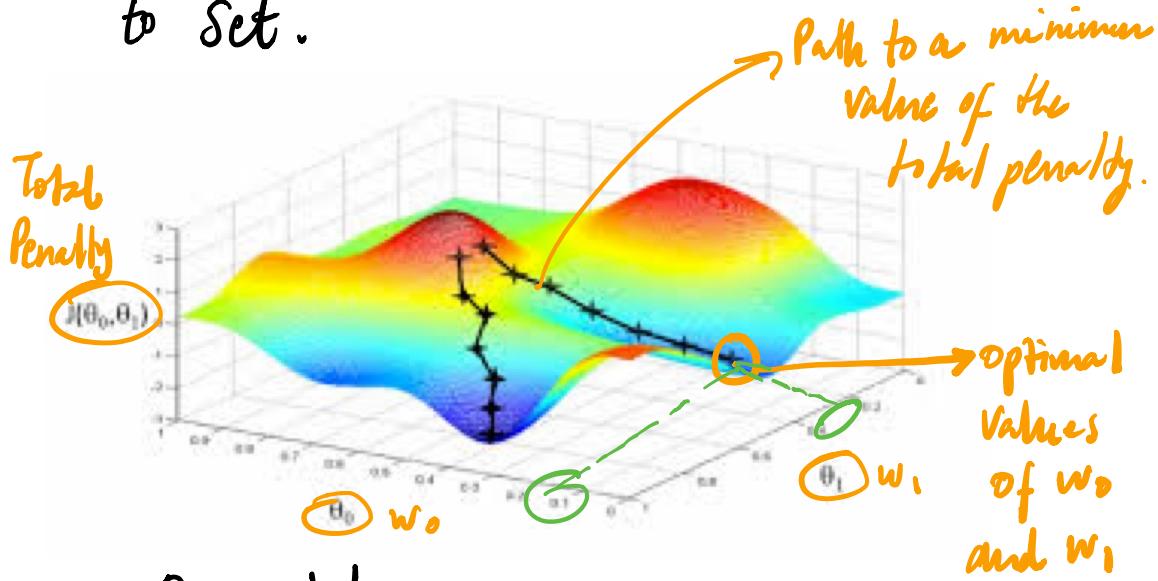
w_0	x_0	w_1	x_1	w_2	x_2	y	\hat{y}	Penalty
-10	$x_0^{(1)}$	500	$x_1^{(1)}$	120.5	$x_2^{(1)}$	$y^{(1)}$	$\hat{y}^{(1)}$	$p^{(1)}$
-10	$x_0^{(2)}$	500	$x_1^{(2)}$	120.5	$x_2^{(2)}$	$y^{(2)}$	$\hat{y}^{(2)}$	$p^{(2)}$
-10	$x_0^{(3)}$	500	$x_1^{(3)}$	120.5	$x_2^{(3)}$	$y^{(3)}$	$\hat{y}^{(3)}$	$p^{(3)}$
-10	$x_0^{(4)}$	500	$x_1^{(4)}$	120.5	$x_2^{(4)}$	$y^{(4)}$	$\hat{y}^{(4)}$	$p^{(4)}$
-10	$x_0^{(5)}$	500	$x_1^{(5)}$	120.5	$x_2^{(5)}$	$y^{(5)}$	$\hat{y}^{(5)}$	$p^{(5)}$
-10	$x_0^{(6)}$	500	$x_1^{(6)}$	120.5	$x_2^{(6)}$	$y^{(6)}$	$\hat{y}^{(6)}$	$p^{(6)}$

⋮

Sum of
 $p^{(1)}, p^{(2)}, p^{(3)}, \dots$

What We Want The values of
 w_0, w_1 , and w_2 that minimizes
the sum of penalties.

Imagine we only had w_0 and w_1 to set.



$$\theta_0 = w_0$$

$$\theta_1 = w_1$$

NOTE The shape of this surface depends on the penalty function we choose.

For each set of w_0 and w_1 values, we plot the penalty (sum of all the penalties in the data set).

This gives us a surface that typically looks like hilly terrain.

A machine learning algorithm is a recipe for finding the path that leads to the minimum value of the total penalty.

The values of w_0 and w_1 at the minimum value of the total penalty are the optimal parameter values.

The computer program has learned these parameter values from experience.

Recap

- 1) Experience = Data (the complete data set)
- 2) Task = Prediction
- 3) Performance = Penalty

best performance = minimize
the sum of
the penalties
across the
entire
dataset.

- 4) The way to get to the best performance values for w_0 , w_1 , and w_2 is to use a machine learning algorithm.

The machine learning algorithm that does this job is simple to write down.

- 1) Pick any set of initial values for w_0 , w_1 , and w_2 .
- 2) Find the total penalty of the dataset.
- 3) Look all around w_0 , w_1 , and w_2 . Find close values that result in a lower total penalty. If none of the close values result in a lower penalty, STOP.
- 4) Repeat 3.

Recap (Continued)

- 5) Machine learning is learning from experience and feedback without having an explicit set of rules.
 - hitting a forehand
 - finding a face in a picture
 - riding a bicycle
- 6) You don't need big data to do machine learning. (But it can help for some problems.)
- 7) Machine learning = giant numerical optimization problem.