

Regression w/ Single Feature ①

The Business Problem

- CEO of a restaurant chain
- Thinking about how to expand the business
- Have data on current restaurants
 - * population of town in which restaurant is located
 - * profit from restaurant per quarter
- Where should the next 5 restaurants be opened to maximize profit growth?

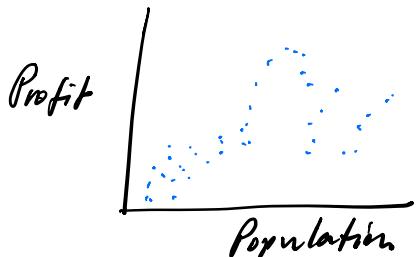
Regression w/ single feature ②

The Data

Population (10,000)	Profit (\$100,000)
6.11	17.59
5.53	9.13
8.52	13.67
.	.
:	:
12.68	15.34

Structure of the data

{ food-truck-profits.txt
97 rows
numerical information (not categorical)
No missing information



Step 1

Scatterplot of the dataset
to visualize it

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STEP 2

Define the task
(w.r.t. the dataset)

Input → the population size

Output → the profit

Task → Given a population size,
predict the profit.

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STEP 3

Define the Model

Feature = input = population size

(later we'll see how features can differ from inputs)

Transform the feature into an output

$(w_0 \times x_0^{(1)}) + (w_1 \times x_1^{(1)}) = \hat{y}^{(1)}$					
Parameter 1	Constant feature	Parameter 2	Feature 1	Predicted output	Actual Output
w_0	x_0	w_1	x_1	$\hat{y}^{(1)}$	$y^{(1)}$
w_0	1	w_1	$x_1^{(1)}$	$\hat{y}^{(1)}$	$y^{(1)}$
w_0	1	w_1	$x_1^{(2)}$	$\hat{y}^{(2)}$	$y^{(2)}$
M rows					
$m = 97$:	:	:	:	:
w_0	1	w_1	$x_1^{(97)}$	$\hat{y}^{(97)}$	$y^{(97)}$

These values don't change from row to row

These values change from row to row

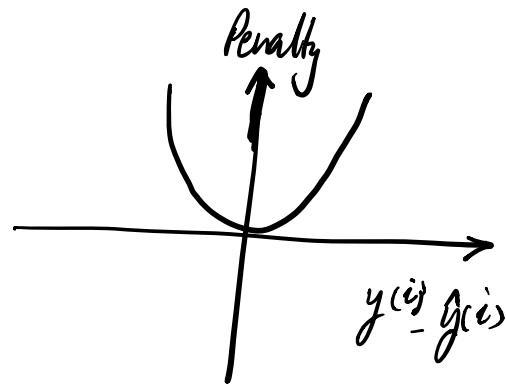
Regression w/ Single Feature (5)

STEP 4

Define the penalty for getting it wrong.

$$\text{Penalty} = \left(\hat{y}^{(i)} - \hat{y}^{(i)} \right)^2$$

for each row

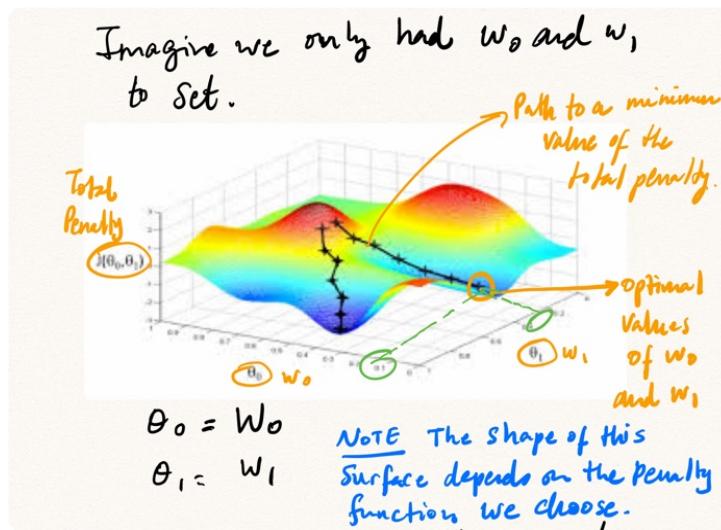


The more we get it wrong, the more we're penalized.

Total Penalty for the entire data set = Sum of penalty of each row.

QUESTION What values of w_0 and w_1 will minimize the total penalty?

Regression w/ Single Feature (6)



Use gradient descent to solve the numerical optimization problem.

- start at an arbitrary point on the surface - pick arbitrary values for w_0 and w_1
- From this point, take a step in the direction where the slope is descending most steeply.
- Do this again and again until you reach a minimum (the "valley floor")

Regression w/ style feature (7)

Recap

Model - transforms the input(s) into the output.

Parameters - these are the fixed values (e.g., w_0, w_1) of the model.

Penalty - for each row of the dataset, what's the penalty/cost/price for being wrong?

Recap (Contd.)

Regression w/ Single Feature ②

Total Penalty - Sum of the penalty of each row of the dataset.

Problem - Find the parameter

values of the model (w_0 and w_i values) that minimize the total penalty.

Approach to Solving the Problem - Gradient Descent.

Hyper-Parameters

Gradient descent can produce different results based on how you set the values of the following parameters.

- Learning Rate. The size of the jump taken at each step.
- The total number of jumps taken.

Regression w/ Single Feature 10

Every machine learning problem has hyperparameters.

Why? Because every machine learning problem is a giant optimization problem - find the optimal values of the model parameters that minimizes the total penalty.

To find these optimal values of w_0 and w_1 (for example), we use a learning algorithm like gradient descent.

Regression w/ Single Feature (1)

Finding the right hyperparameters

is a separate quest - one
that must be solved every time
you apply machine learning to
solve a problem.

In a few sessions we'll see
how this problem is tackled.