

Objective: Propose a model determining the terminal velocity of a raindrop falling from a stationary cloud.

Relevant Variables:

- $v_{\text{terminal}}$ : Terminal velocity of the raindrop (where gravitational force and the drag force are equal)
- $R$ : Raindrop radius
- $\rho_{\text{raindrop}}$ : Raindrop density
- $\rho_{\text{air}}$ : Air density
- $\mu_{\text{air}}$ : Dynamic viscosity of air
- $g$ : Acceleration due to gravity
- $C_d$ : Drag coefficient
- $Re$ : Reynolds number where  $Re = (2 * R * v * \rho_{\text{air}}) / \mu_{\text{air}}$
- $f()$ : A function that combines the relationships among the variables to solve for terminal velocity

Generic model:  $v_{\text{terminal}}(R, \rho_{\text{raindrop}}, \rho_{\text{air}}, g, \mu_{\text{air}}) = f(C_d(Re), Re, R, \rho_{\text{raindrop}}, \rho_{\text{air}}, g, \mu_{\text{air}})$

Assumptions:

- raindrop is a perfect sphere, all the forces acting on the raindrop remain constant throughout its descent, drag coefficient is consistent and uninfluenced during descent

Objective: Propose a model for the volume flow rate  $dV/dt$  of blood flowing in an artery as a function of the pressure  $P$  drop per unit length of artery, the radius  $r$ , the blood density  $\rho$  and the blood viscosity  $\mu$ .

Relevant variables:

- $dV/dt$ : Rate of volume of blood flow in artery
- $\mu$ : Blood viscosity
- $r$ : Artery radius
- $L$ : Length of artery
- $P'$ : Pressure drop per unit length of the artery
- $\rho$ : Blood density
- $v_{\text{avg}}$ : average flow velocity

Generic model:  $dV/dt(r, P', \mu, \rho) = \pi * r^2 * v_{\text{avg}}(P', r, \mu, \rho)$

Assumptions:

- blood flow is laminar; continuous, artery is a cylindrical pipe

Objective: Write a code to solve the wave equations, given the initial and boundary conditions.

Equation:

$$u(x,t)[(1)/(\Delta t^2)-(c^2)/(\Delta x^2)]=(2u(x,t-\Delta t)-u(x,-2\Delta t))/(\Delta t^2)+c^2/((-2u(x-\Delta x,t)+u(x,-2\Delta x,t))/(\Delta x^2))$$

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In [12]: import numpy as np
import matplotlib.pyplot as plt

L_domain = 10
T_sim = 10
Spatial_points = 100
Time_steps = 1000
Wave_speed = 1

dx = L_domain / Spatial_points # spatial step
dt = T_sim / Time_steps # time step

array = np.zeros((Spatial_points, Time_steps))

array[:, 0] = np.sin(np.pi * np.linspace(0, L_domain, Spatial_points)) # ini
array[:, 1] = array[:, 0] + dt * np.zeros(Spatial_points) # initial velocity
array[0, :] = 0 # boundary conditions

# using finite-difference to solve for values of displacement at each postiti
for n in range(1, Time_steps - 1):
    for i in range(1, Spatial_points - 1):
        array[i, n + 1] = (2 * array[i, n] - array[i, n - 1] + Wave_speed**2

plt.imshow(array, extent=[0, T_sim, 0, L_domain], cmap='viridis')
plt.xlabel('Time')
plt.ylabel('Position')
plt.colorbar(label='Displacement')
plt.show()
```



