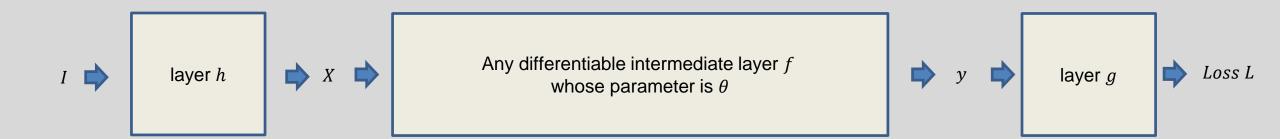


Computer Vision

Lecture 07: Training CNNs with Large Data

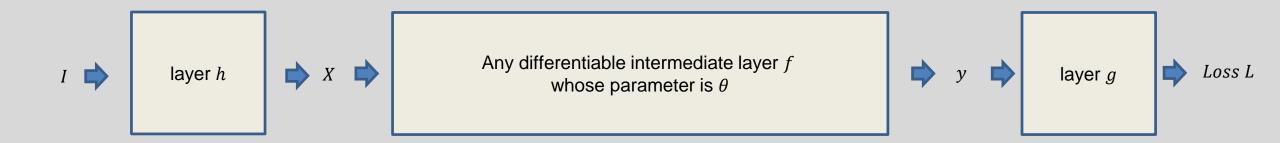
Differentiable layers



We need to implement three things for an intermediate layer f:

forward rule:
$$y = f(X; \theta)$$
 for $g(f(X; \theta)) = L$ backward rule: $\frac{dy}{dX}$ for $\frac{dL}{dX} = \frac{dy}{dX} \times \frac{dL}{dy}$ parameter update rule: $\frac{dy}{d\theta}$ for $\theta^{new} = \theta - \varepsilon \frac{dy}{d\theta} \times \frac{dL}{dy}$

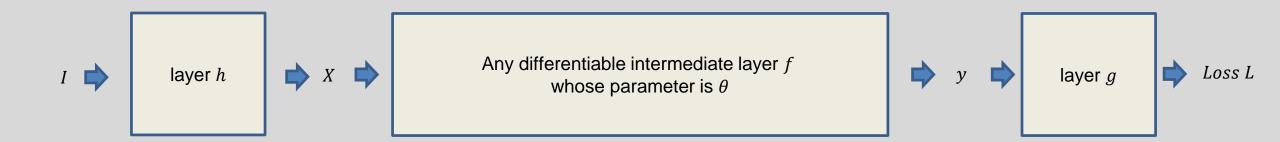
Differentiable layers



We need to implement three things for an intermediate layer f:

forward rule:	$y = f(X; \theta)$	for	$g(f(X;\theta)) = L$	
backward rule:	$\frac{dy}{dX}$	for	$\frac{dL}{dX} = \frac{dy}{dX} \times \frac{dL}{dy}$	PyTorch can do these automatically.
parameter update rule:	$\frac{dy}{d\theta}$	for	$\theta^{new} = \theta - \varepsilon \frac{dy}{d\theta} \times \frac{dL}{dy}$	loss.backward() optimizer.step()

Differentiable layers

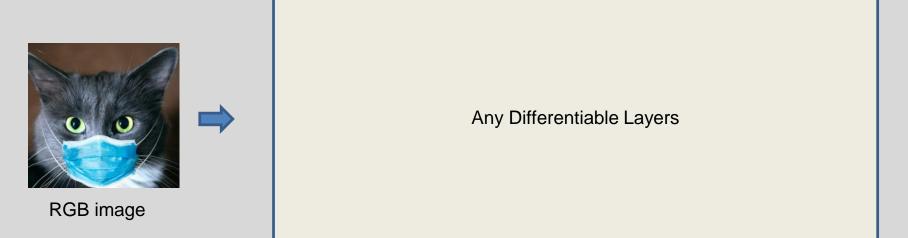


Some layers (e.g. pooling, activation) do not have parameters θ . It requires only two:

forward rule:
$$y = f(X; \theta)$$
 for $g(f(X; \theta)) = L$ backward rule:
$$\frac{dy}{dX}$$
 for
$$\frac{dL}{dX} = \frac{dy}{dX} \times \frac{dL}{dy}$$

In convolutional layers, parameters are convolutional filter kernel's weights.

CNNs

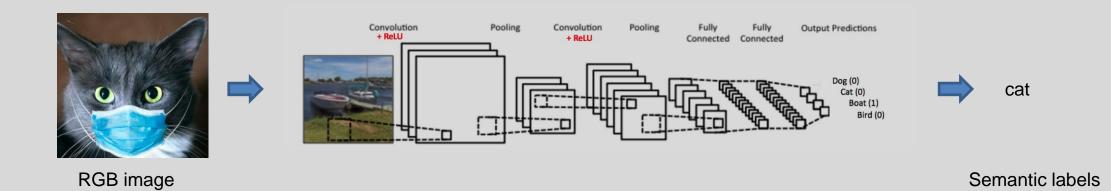




cat

Semantic labels

CNNs



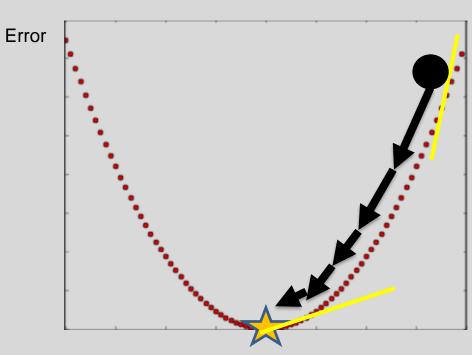


CNN implementation in PyTorch

```
import torch
import torch.nn
class MyCNN (nn.Module):
 def init (self):
    super(). init ()
    self.layer = nn.Sequential(
        nn.Conv2d(1, 16, 5),
        nn.ReLU(),
        nn.Conv2d(16, 32, 5),
        nn.MaxPool2d(2, 2)
        nn.Conv2d(32, 64, 5)
        nn.ReLU()
        nn.MaxPool2d(2,2)
    self.fc layer = nn.Sequential(
        nn.Linear(64*3*3, 10)
        nn.ReLu()
        nn.Linear(100, 10)
 def forward(self, x):
    out = self.layer(x)
    out = out.view*(batch size, -1)
    out = self.fc layer(out)
    return out
```

```
import torch
net = MyCNN()
loss func = torch.nn.MSELoss()
optimizer = torch.optim.SGD(net.parameters(), lr=0.01)
losses = []
for i in range (num epoch):
  optimizer.zero grad()
  output = net(x)
  loss = loss func(output, y)
  loss.backward()
  optimizer.step()
  losses.append(loss.item())
```

Gradient Descent



```
import torch
loss_func = torch.nn.MSELoss()

optimizer = torch.optim.SGD(net.parameters(), lr=0.01)

for i in range(num_epoch):
    optimizer.zero_grad()

    output = net(x)

    loss = loss_func(output, y)

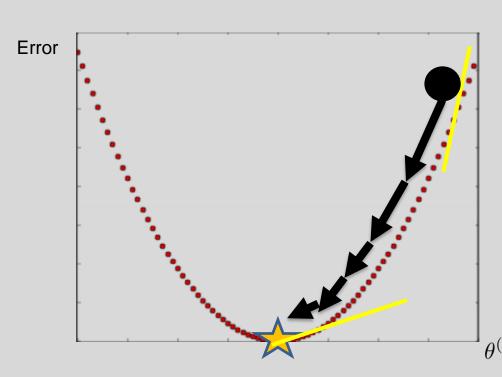
    loss.backward()
    optimizer.step()
```

$$\theta^{(t)} = \{W^{(t)}, b^{(t)}\}$$

Error(W, b) =
$$\frac{1}{3} \sum_{i=1}^{3} (f(x_i; W, b) - y_i)^2$$
,
 $W^{(t+1)} = W^{(t)} - \epsilon \frac{\partial}{\partial W^{(t)}} \text{Error}(W^{(t)}, b^{(t)})$
 $b^{(t+1)} = b^{(t)} - \epsilon \frac{\partial}{\partial b^{(t)}} \text{Error}(W^{(t)}, b^{(t)})$

 ϵ : Learning rate (small value e.g. 0.01)

Stochastic Gradient Descent



import torch
$$loss_func = torch.nn.MSELoss()$$

$$optimizer = torch.optim.SGD(net.parameters(), lr=0.01)$$

$$for i in range(num_epoch):$$

$$for x_batch, y_batch in train_loader:$$

$$optimizer.zero_grad()$$

$$output = net(x_batch)$$

$$loss = loss_func(output, y_batch)$$

$$loss.backward()$$

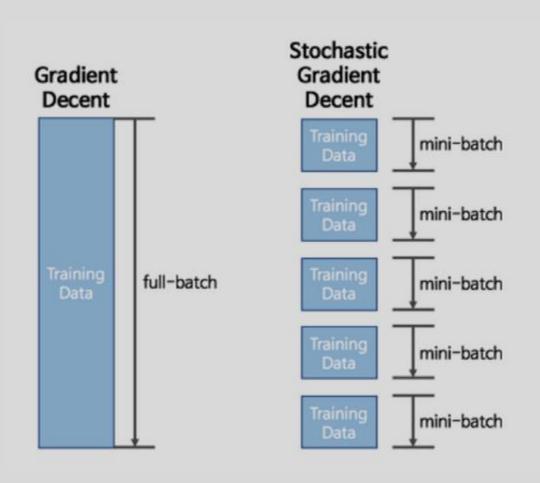
$$optimizer.step()$$

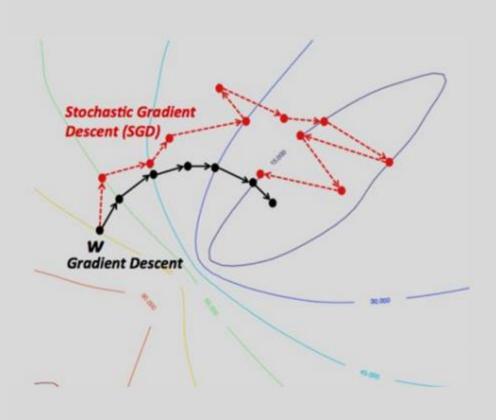
$$\theta^{(t)} = \{W^{(t)}, b^{(t)}\}$$

Error(W, b) =
$$\frac{1}{3} \sum_{i=1}^{3} (f(x_i; W, b) - y_i)^2$$
,
 $W^{(t+1)} = W^{(t)} - \epsilon \frac{\partial}{\partial W^{(t)}} \text{Error}(W^{(t)}, b^{(t)})$
 $b^{(t+1)} = b^{(t)} - \epsilon \frac{\partial}{\partial b^{(t)}} \text{Error}(W^{(t)}, b^{(t)})$

 ϵ : Learning rate (small value e.g. 0.01)

Stochastic Gradient Descent







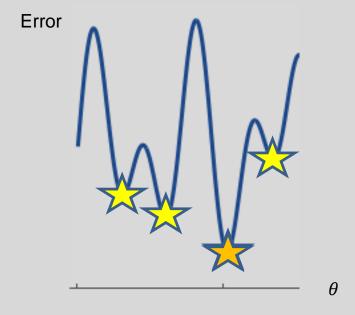
Stochastic Gradient Descent

- Gradient descent
 Calculate for all data (takes large amount of time).
 Go 1 optimal step.
- Stochastic gradient descent
 Calculate gradients for partial data (takes small amount of time).
 Go many non-globally-optimal steps, but converges.

Momentum

For the real-world loss function, it is not so clean.

→ There are many local minima.

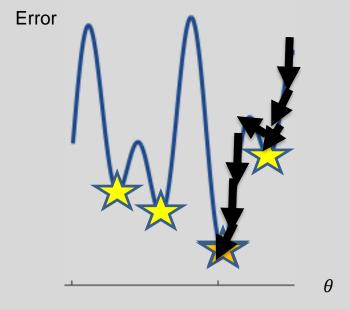


Functions with many local minima

Momentum

For the real-world loss function, it is not so clean.

→ There are many local minima. → Use momentum to climb up small hills.



$$V^{(t+1)} = V^{(t)} * m - \epsilon \frac{\partial}{\partial W^{(t)}} Error(W^{(t)}, b^{(t)})$$

$$U^{(t+1)} = U^{(t)} * m - \epsilon \frac{\partial}{\partial b^{(t)}} Error(W^{(t)}, b^{(t)})$$

$$W^{(t+1)} = W^{(t)} + V^{(t+1)}$$

$$b^{(t+1)} = b^{(t)} + U^{(t+1)}$$

Nesterov Gradient Descent

$$V^{(t+1)} = V^{(t)} * m - \epsilon \frac{\partial}{\partial W^{(t)} + \mu V^{(t)}} Error(W^{(t)} + \mu V^{(t)}, b^{(t)} + \mu U^{(t)})$$

$$U^{(t+1)} = U^{(t)} * m - \epsilon \frac{\partial}{\partial b^{(t)} + \mu U^{(t)}} Error(W^{(t)} + \mu V^{(t)}, b^{(t)} + \mu U^{(t)})$$

$$W^{(t+1)} = W^{(t)} + V^{(t+1)}$$

$$b^{(t+1)} = b^{(t)} + U^{(t+1)}$$

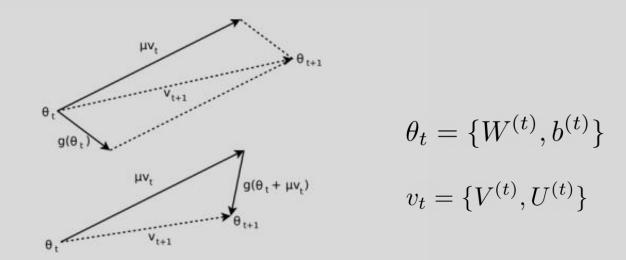
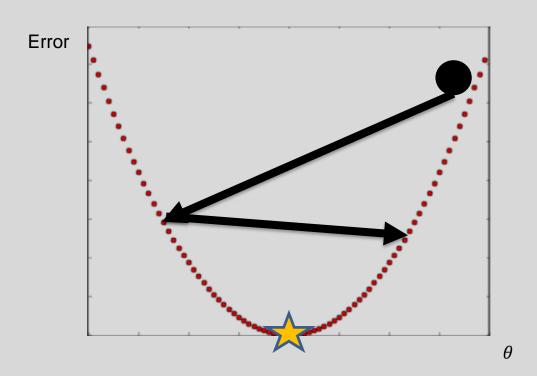
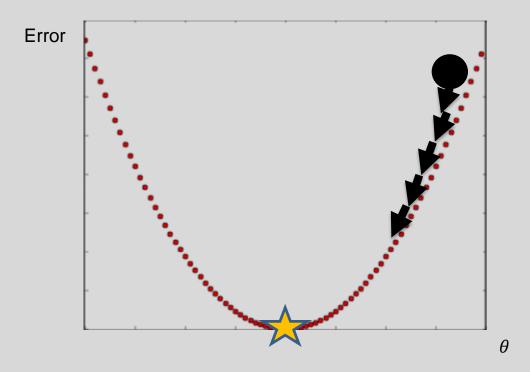


Figure 1. (Top) Classical Momentum (Bottom) Nesterov Accelerated Gradient

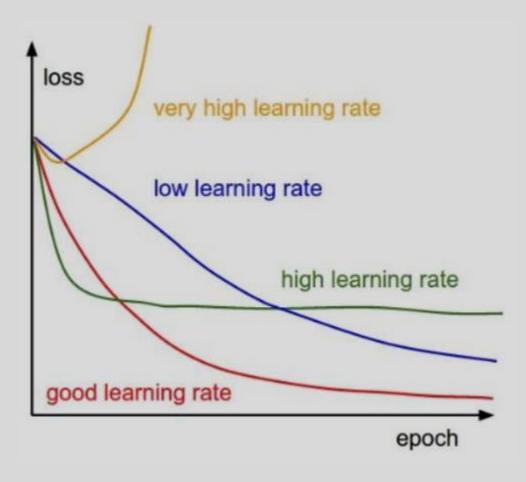




If learning rate is high, it does not converge.

If learning rate is low, too slow to converge.

It is important to decide the proper learning rate.



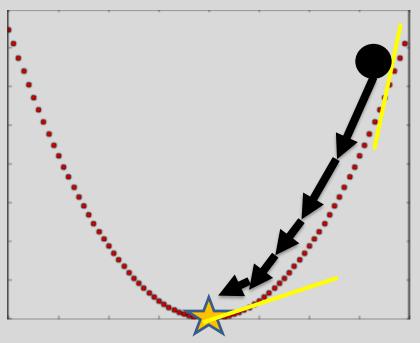
It is important to decide the proper learning rate.

Error

Simple learning rate scheduler defined in the PyTorch:

torch.optim.lr_scheduler.StepLR

- → Multiply gamma(<1) to the learning rate, for every step_size.
- torch.optim.lr_scheduler.ExponentialLR
- → Multiply gamma(<1) to the learning rate, for every epoch.



```
import torch
import torch.nn as nn
import torch.optim.lr scheduler as lr scheduler
net = nn.Sequential(
    nn.Conv2d(in channels = 32, out channels = 64, kernel size = 5, stride = 1, padding = 2)
optimizer = torch.optim.SGD(net.parameters(), lr=0.01)
scheduler = lr scheduler.ExponentialLR(optimizer, gamma=0.99)
for i in range(10):
  scheduler.step()
  print(i, scheduler.get lr())
                                         0 [0.009801]
                                          1 [0.00970299]
                                          2 [0.0096059601]
                                          3 [0.009509900499]
                                          4 [0.00941480149401]
                                          5 [0.0093206534790699]
                                          6 [0.0092274469442792]
                                          7 [0.009135172474836408]
```

8 [0.009043820750088045] 9 [0.008953382542587164]

```
import torch
import torch.nn as nn
import torch.optim.lr_scheduler as lr_scheduler
net = nn.Sequential(
    nn.Conv2d(in_channels = 32, out_channels = 64, kernel_size = 5, stride = 1, padding = 2)
optimizer = torch.optim.SGD(net.parameters(), lr=0.01)
scheduler = lr scheduler.StepLR(optimizer, step size=1, gamma=0.99)
for i in range(10):
  scheduler.step()
  print(i, scheduler.get lr())
                                         0 [0.009801]
                                          1 [0.00970299]
                                          2 [0.0096059601]
                                          3 [0.009509900499]
                                          4 [0.00941480149401]
                                          5 [0.0093206534790699]
                                          6 [0.0092274469442792]
                                          7 [0.009135172474836408]
```

8 [0.009043820750088045] 9 [0.008953382542587164]



```
import torch
import torch.nn as nn
import torch.optim.lr_scheduler as lr_scheduler
net = nn.Sequential(
    nn.Conv2d(in_channels = 32, out_channels = 64, kernel_size = 5, stride = 1, padding = 2)
optimizer = torch.optim.SGD(net.parameters(), lr=0.01)
scheduler = lr scheduler.StepLR(optimizer, step size=3, gamma=0.99)
for i in range(10):
  scheduler.step()
  print(i, scheduler.get lr())
                                    0 [0.01]
                                    1 [0.01]
                                    2 [0.009801]
                                    3 [0.0099]
                                    4 [0.0099]
                                    5 [0.00970299]
                                    6 [0.009801]
                                    7 [0.009801]
                                    8 [0.0096059601]
                                    9 [0.00970299]
```

AdaGrad

Motivation:

Adaptively update gradients for individual parameters.

Update parameters with a large step, whose parameters haven't been changed a lot.

Update parameters with a small step, whose parameters have been changed a lot.

AdaGrad

sgd:
$$\theta^{(t)} = \theta^{(t-1)} - \epsilon \cdot g$$

AdaGrad:

$$\theta^{(t)} = \theta^{(t-1)} - \frac{\epsilon}{\delta + \sqrt{r}} \cdot g$$
$$r = r + g^2$$

RMS Prop

AdaGrad:

$$\theta^{(t)} = \theta^{(t-1)} - \frac{\epsilon}{\delta + \sqrt{r}} \cdot g$$

$$r = r + g^2$$

RMS Prop:

$$\theta^{(t)} = \theta^{(t-1)} - \frac{\epsilon}{\delta + \sqrt{r}} \cdot g$$

$$r = \rho \cdot r + (1 - \rho) \cdot g^2$$

Adam

Motivation:

Jointly tackle 'learning rate' and 'direction' issues.

Combine RMSProp and Momentum methods.

Adam

$$s^{(t)} = \beta_1 \cdot s^{(t-1)} + (1 - \beta_1) \cdot g$$

$$r^{(t)} = \beta_2 \cdot r^{(t-1)} + (1 - \beta_2) \cdot (g \cdot g)$$

$$\hat{s} = \frac{s}{1 - \beta_1^t}$$

$$\hat{r} = \frac{r}{1 - \beta_2^t}$$

$$\theta^{(t)} = \theta^{(t-1)} - \epsilon \frac{\hat{s}}{\sqrt{\hat{r}} + \delta}$$

Adam

PyTorch already offers diverse optimization methods:

```
torch.optim.SGD
torch.optim.RMSProp
torch.optim.AdaGrad
torch.optim.Adam

optimizer = torch.optim.SGD(net.parameters(), lr=0.001)
optimizer = torch.optim.Adam(net.parameters(), lr=0.001, betas=(0.9, 0.999), eps=1e-08)
```

Remarks

There have been several attempts to optimize CNNs well with varied gradients (direction, learning rate).

Adam is generally the best solution; but it depends on applications.

Importance of Data

As the supervised learning method, Deep learning requires many (x, y) pairs.

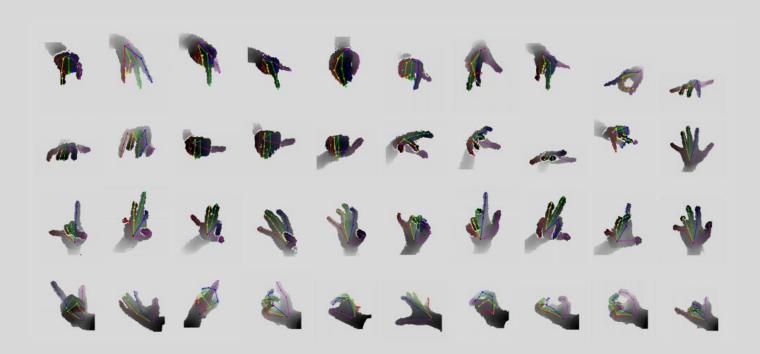
x: Data,

y: Annotation.

Imagine that making your network overfit to large-scale dataset you can see on Earth.

Importance of Data



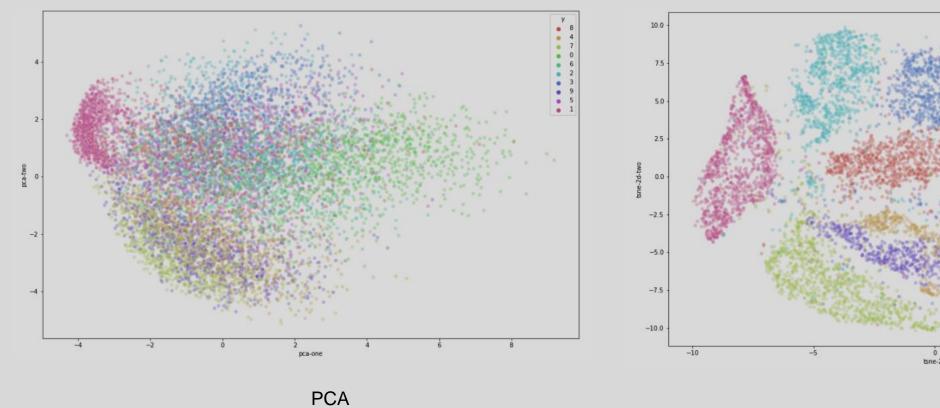


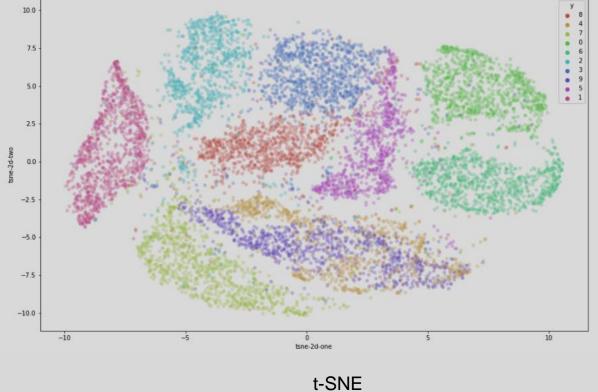
Imagine that your face recognition network learn all human faces on Earth.

Imagine that your hand pose estimation network learn all hand poses on Earth.

Visualizing data

Two popular data visualization techniques: We visualize 784-dimensional data from MNIST in the 2-dimensional space.







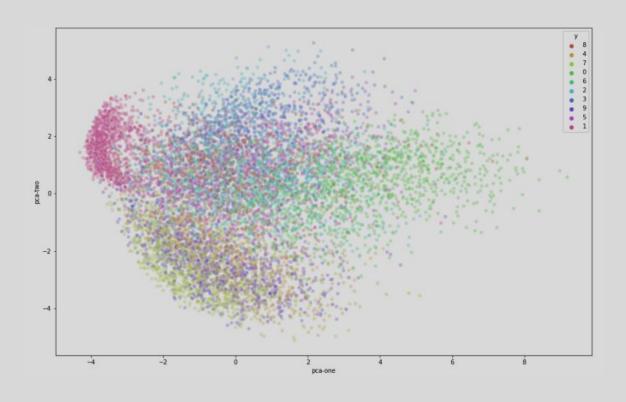
Visualizing data

```
from future import print function
import time
import numpy as np
import pandas as pd
from sklearn.datasets import fetch openml
from sklearn.decomposition import PCA
from sklearn.manifold import TSNE
import matplotlib.pyplot as plt
from mpl toolkits.mplot3d import Axes3D
import seaborn as sns
mnist = fetch openml('mnist 784', version=1, cache=True)
X = mnist.data / 255.0
y = mnist.target
print(X.shape, y.shape)
feat cols = [ 'pixel'+str(i) for i in range(X.shape[1]) ]
df = pd.DataFrame(X,columns=feat cols)
df['y'] = y
df['label'] = df['y'].apply(lambda i: str(i))
N = 10000
df subset = df.loc[rndperm[:N],:].copy()
data subset = df subset[feat cols].values
```



Visualizing data - PCA

```
np.random.seed(42)
rndperm = np.random.permutation(df.shape[0])
pca = PCA(n components=2)
pca result = pca.fit transform(data subset)
df subset['pca-one'] = pca result[:,0]
df subset['pca-two'] = pca result[:,1]
plt.figure(figsize=(16,10))
sns.scatterplot(
    x="pca-one", y="pca-two",
   hue="y",
   palette=sns.color palette("hls", 10),
    data=df.loc[rndperm,:],
    legend="full",
    alpha=0.3
```

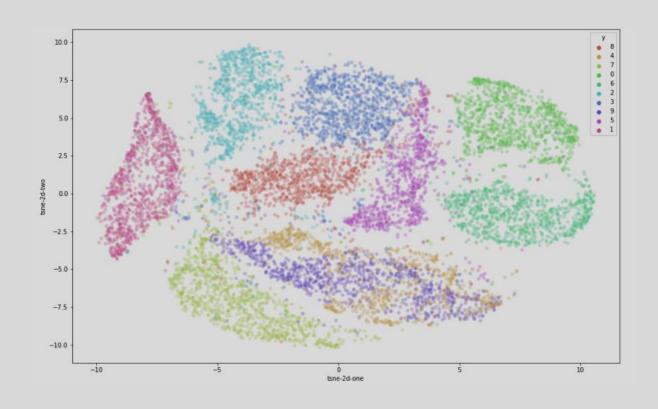


Visualizing data - tSNE

```
tsne = TSNE(n_components=2, verbose=1, perplexity=40, n_iter=300)
tsne_results = tsne.fit_transform(data_subset)

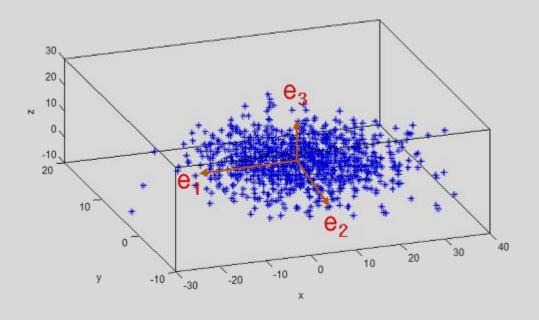
df_subset['tsne-2d-one'] = tsne_results[:,0]
df_subset['tsne-2d-two'] = tsne_results[:,1]

plt.figure(figsize=(16,10))
sns.scatterplot(
    x="tsne-2d-one", y="tsne-2d-two",
    hue="y",
    palette=sns.color_palette("hls", 10),
    data=df_subset,
    legend="full",
    alpha=0.3
)
```



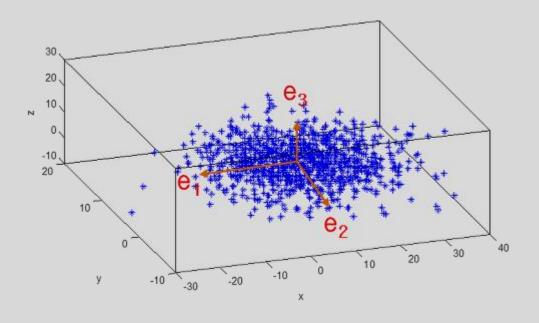


Visualizing the data - PCA



Algorithm to find principal components for data distribution.

Visualizing the data - PCA



What is the principal component here? → Axis, that can represent the largest variance.

Axes are orthogonal to each other.

Visualizing the data - PCA

$$X = \left(\begin{array}{c|cccc} & & & & & \\ & & & & & \\ X_1 & X_2 & X_3 & \cdots & X_d \\ & & & & & \end{array}\right) \in \mathbb{R}^{n \times d}$$

X: data matrix

$$C = \begin{pmatrix} cov(x,x) & cov(x,y) \\ cov(x,y) & cov(y,y) \end{pmatrix}$$

$$= \begin{pmatrix} \frac{1}{n} \sum (x_i - m_x)^2 & \frac{1}{n} \sum (x_i - m_x)(y_i - m_y) \\ \frac{1}{n} \sum (x_i - m_x)(y_i - m_y) & \frac{1}{n} \sum (y_i - m_y)^2 \end{pmatrix}$$

```
C = \begin{pmatrix} cov(x,x) & cov(x,y) \\ cov(x,y) & cov(y,y) \end{pmatrix}
= \begin{pmatrix} \frac{1}{n} \sum (x_i - m_x)^2 & \frac{1}{n} \sum (x_i - m_x)(y_i - m_y) \\ \frac{1}{n} \sum (x_i - m_x)(y_i - m_y) & \frac{1}{n} \sum (y_i - m_y)^2 \end{pmatrix}
Var[X] = E \begin{bmatrix} (X_1 - E[X_1])(X_1 - E[X_1]) & \dots & (X_1 - E[X_1])(X_K - E[X_K]) \\ \vdots & \ddots & \vdots \\ (X_K - E[X_K])(X_1 - E[X_1]) & \dots & (X_K - E[X_K])(X_K - E[X_K]) \end{bmatrix}
= \begin{bmatrix} E[(X_1 - E[X_1])^2] & \dots & E[(X_1 - E[X_1])(X_K - E[X_K]) \\ \vdots & \ddots & \vdots \\ E[(X_K - E[X_K])(X_1 - E[X_1])] & \dots & E[(X_K - E[X_K])^2 \end{bmatrix}
```

Eigenvector Decomposition:

$$C = V\Lambda V^{T}$$

$$= \begin{bmatrix} v_{1} & v_{2} & \cdots & v_{N} \end{bmatrix} \begin{bmatrix} \lambda_{1} & 0 & \cdots & 0 \\ 0 & \lambda_{2} & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \cdots & \lambda_{N} \end{bmatrix} \begin{bmatrix} v_{1}^{T} \\ v_{2}^{T} \\ \vdots \\ v_{N}^{T} \end{bmatrix}$$

$$= \begin{bmatrix} \lambda_1 v_1 & \lambda_2 v_2 & \cdots & \lambda_N v_N \end{bmatrix} \begin{bmatrix} v_1^T \\ v_2^T \\ \vdots \\ v_N^T \end{bmatrix}$$

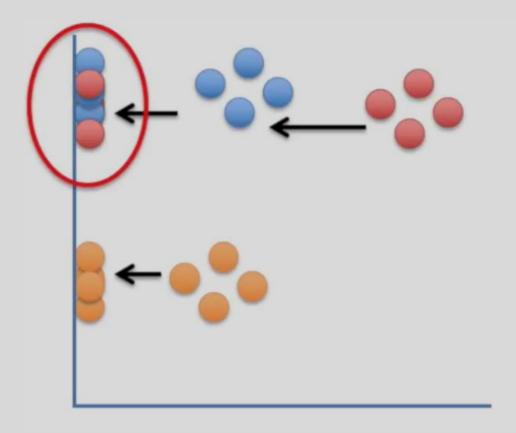
We find eigenvalue/eigenvector for the covariance matrix.

It is mathematically proven that the variance of data samples projected onto an eigenvector is equal to its eigenvalue.

So, we sort eigenvectors in the descending order according to its eigenvalues.

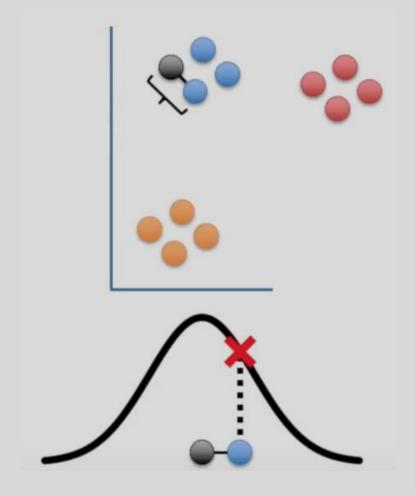
And we choose an eigenvector whose eigenvalue is the largest as the most principled axis e1, choose the second eigenvector as the second principled axis e2 and so on.





Data samples are linearly projected to the principal components.

Visualizing the data - tSNE



$$p_{j|i} = \frac{exp(-|x_i - x_j|^2/2\sigma^2)}{\sum_k exp(-|x_i - x_k|^2/2\sigma^2)}$$

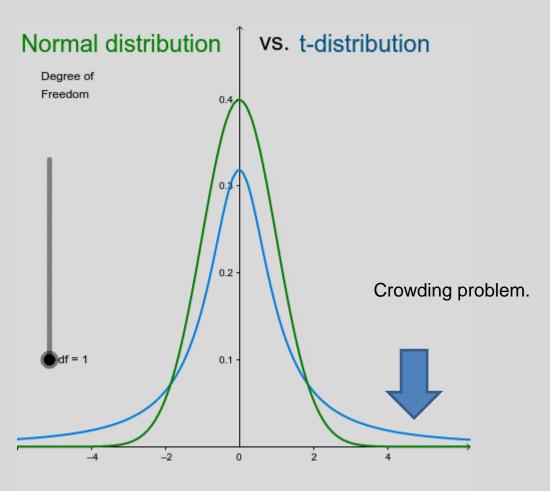
$$q_{j|i} = \frac{e^{-|y_i - y_j|^2}}{\sum_k e^{-|y_i - y_k|^2}}$$

Visualizing the data - tSNE

$$Cost = \sum_{i} KL(P_i||Q_i)$$
$$= \sum_{i} \sum_{j} p_{ij} \log \frac{p_{ij}}{q_{ij}}$$

Minimize the discrepancy between locations in original and reduced spaces.

Visualizing the data - tSNE



$$q_{j|i} = \frac{e^{-|y_i - y_j|^2}}{\sum_k e^{-|y_i - y_k|^2}}$$



$$q_{j|i} = \frac{(1 + |y_i - y_j|^2)^{-1}}{\sum_k (1 + |y_i - y_k|^2)^{-1}}$$



Visualizing large-scale dataset

train	est ICVL	NYU	MSRC	Bighand
ICVL	12.3	35.1	65.8	46.3
NYU	20.1	21.4	64.1	49.6
MSRC	25.3	30.8	21.3	49.7
BigHand	14.9	20.6	43.7	17.1

Table 3. Cross Benchmark comparison. Cross-benchmark average errors, trained with the *Big Hand* data set, the model performs well on ICVL and NYU, while training on ICVL, NYU, and MSRC does not generalize well to other benchmarks.

Dataset	No. frames
ICVL [26]	17,604
NYU [30]	81,009
MSRA15 [24]	76,375
BigHand	2.2M

http://bjornstenger.github.io/papers/yuan_cvpr2017.pdf

Visualizing large-scale dataset

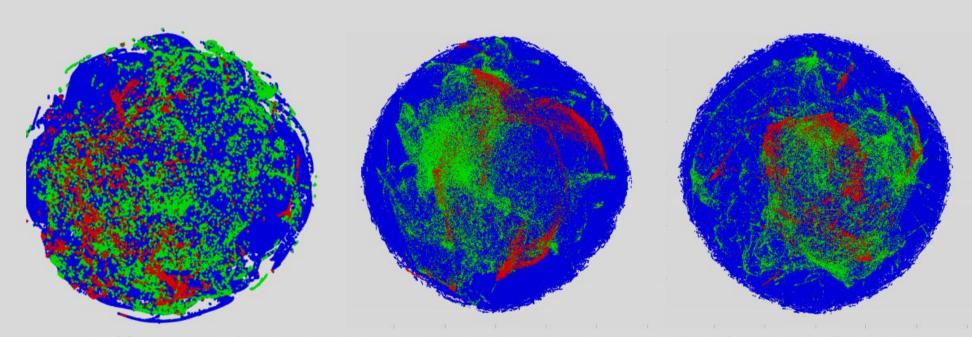
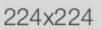


Figure 5. 2D t-SNE embedding of the hand pose space. Big Hand is represented by blue dots, ICVL is represented by red dots. NYU is represented by green dots. The figures show (left) global view point space coverage, (middle) articulation angle space (25D), and (right) hand angle (global orientation and articulation angles) coverage comparison. Compared with existing benchmarks, the *Big Hand* contains a wider range of variation.

http://bjornstenger.github.io/papers/yuan_cvpr2017.pdf

a. No augmentation (= 1 image)









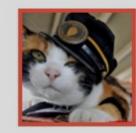
b. Flip augmentation (= 2 images)



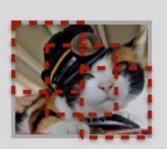
224x224







c. Crop+Flip augmentation (= 10 images)



224x224



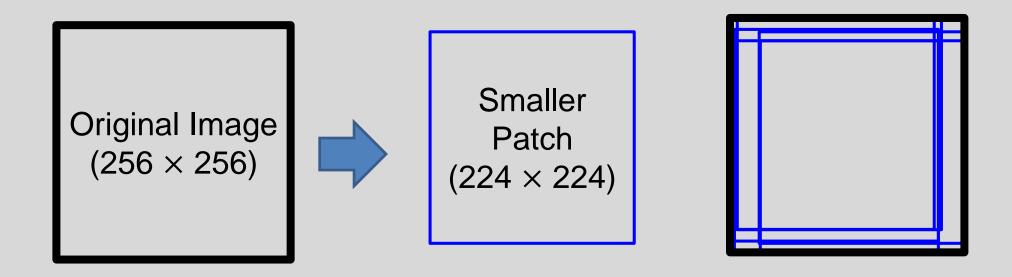






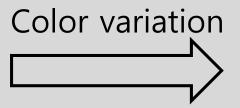






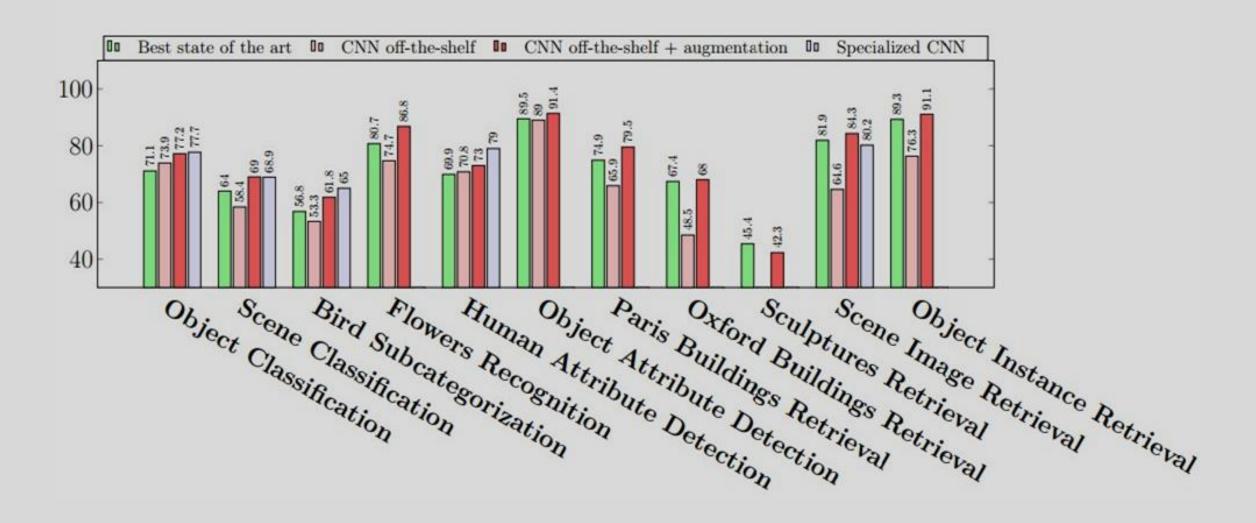
This increases the size of the training set by a factor of 2048 (32 * 32 * 2).





Altered Patch (224 × 224)

Probabilistically, not a single patch will be same at the training phase! (a **factor of infinity**!)





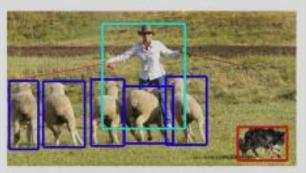
```
import PIL
import numpy as np
import torch
import torchvision
import torchvision.datasets as datasets
from torch.utils.data import DataLoader
import matplotlib.pyplot as plt
from google.colab.patches import cv2 imshow
import cv2
transforms = torchvision.transforms.Compose([
    torchvision.transforms.Resize((224,224)),
    torchvision.transforms.ColorJitter(hue=.05, saturation=.05),
    torchvision.transforms.RandomHorizontalFlip(),
    torchvision.transforms.RandomRotation(20, resample=PIL.Image.BILINEAR),
    torchvision.transforms.ToTensor()
])
for i in range(4):
  train dataset = datasets.MNIST(root = 'mnist data', train=True, transform=transforms, download=True)
  train loader = DataLoader(dataset=train dataset, batch size=1, shuffle=False)
  for x, y in train loader:
    break
  R = np.stack((x[0,0]*255.,x[0,0]*255.,x[0,0]*255.), axis=2)
  cv2 imshow(R)
```



MS COCO dataset



(a) Image classification



(b) Object localization



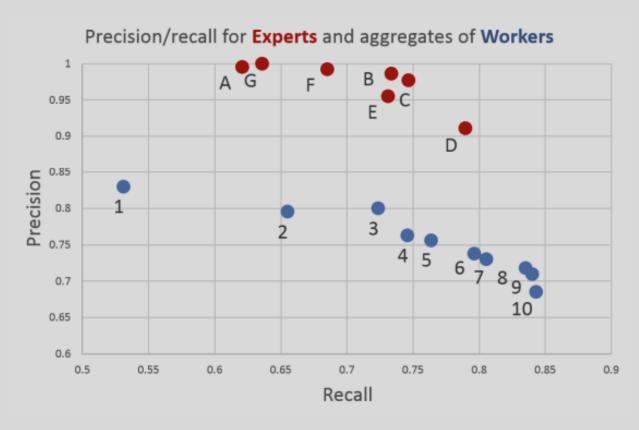
(c) Semantic segmentation (d) This work



Microsoft COCO: Common Objects in Context, ECCV'14

- 328,000 images, 2.5 million object instances from 91 categories.
- Crowd-sourced data by Amazon's Mechanical Turk (AMT).

MS COCO dataset

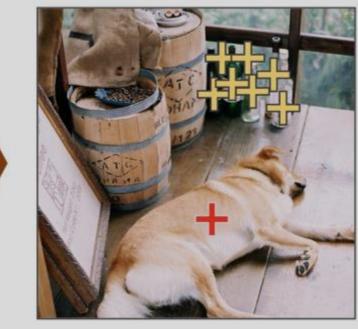


- 8 AMT workers were used to collect data.
- Independent worker annotate well with over 50% prob. $0.5^8 \rightarrow 0.004$
- Ground-truths are generated by majority vote of experts.

MS COCO dataset







(b) Instance spotting



(c) Instance segmentation

• 22 worker hours per 1,000 segmentations

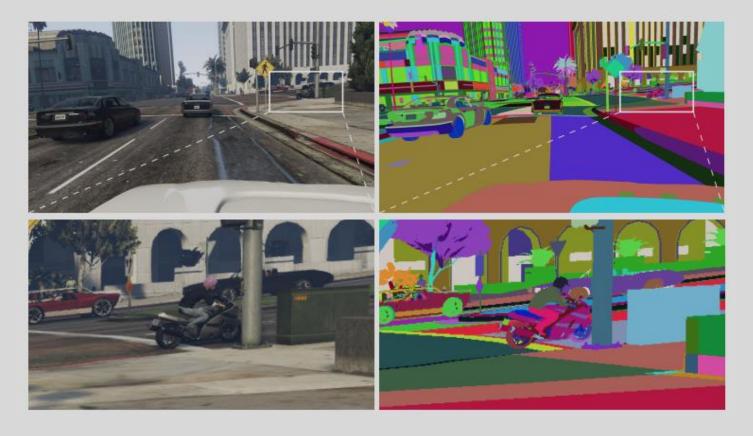
Synthetic data



Learning from synthetic humans, CVPR'17.

Use graphics rendering engines to obtain large-scale datasets.

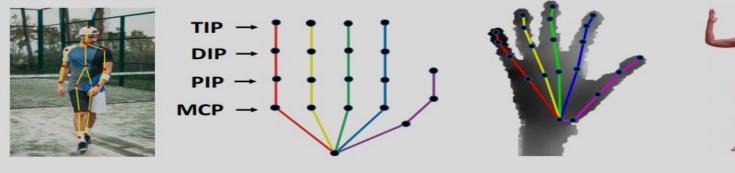
Synthetic data



Playing for Data: Ground Truth from Computer Games, ECCV'16.

Use graphics rendering engines to obtain large-scale datasets.

3D reconstruction task



Hand Skeletons



Body Mesh

Hand Mesh

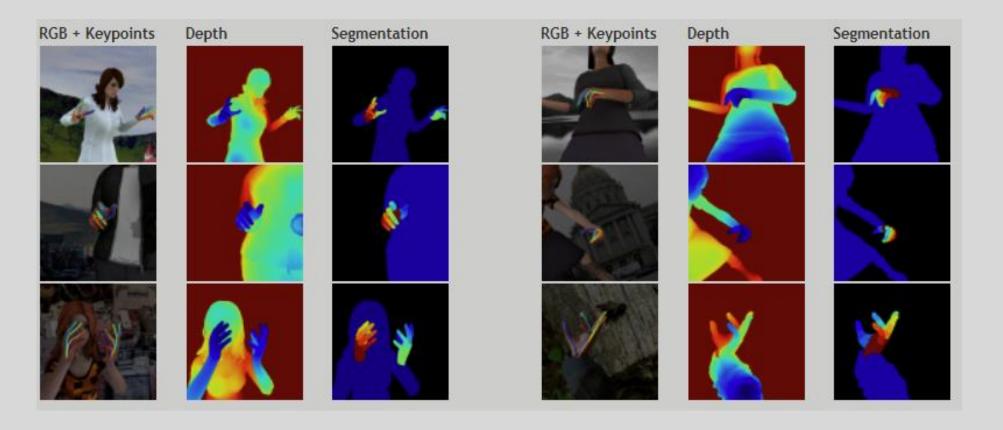


Real-time Joint Tracking of a Hand Manipulating an Object from RGB-D Input, ECCV'16

Non-trivial to collect large-scale accurate annotations via manual efforts.

Body Skeleton

Synthetic data



Learning to Estimate 3D Hand Pose from Single RGB Images, ICCV'17.

Use graphics rendering engines to obtain large-scale datasets.

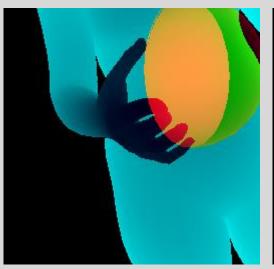
Data generation



RGB image with objects



RGB image without objects

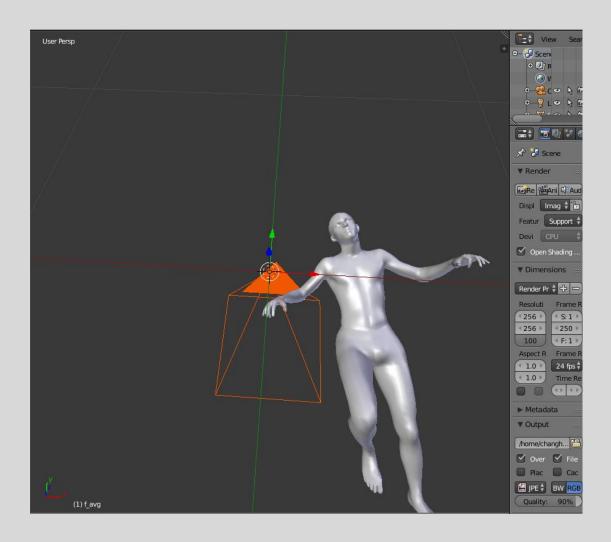


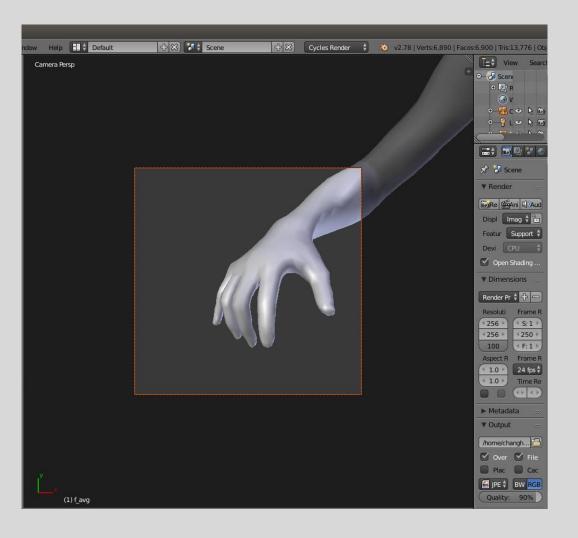
Depth image



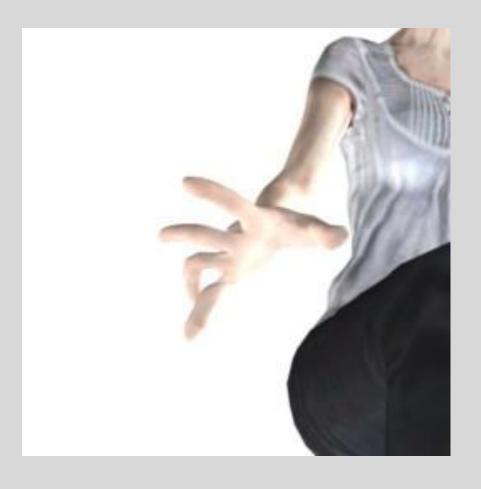
Segmentation mask

Data generation



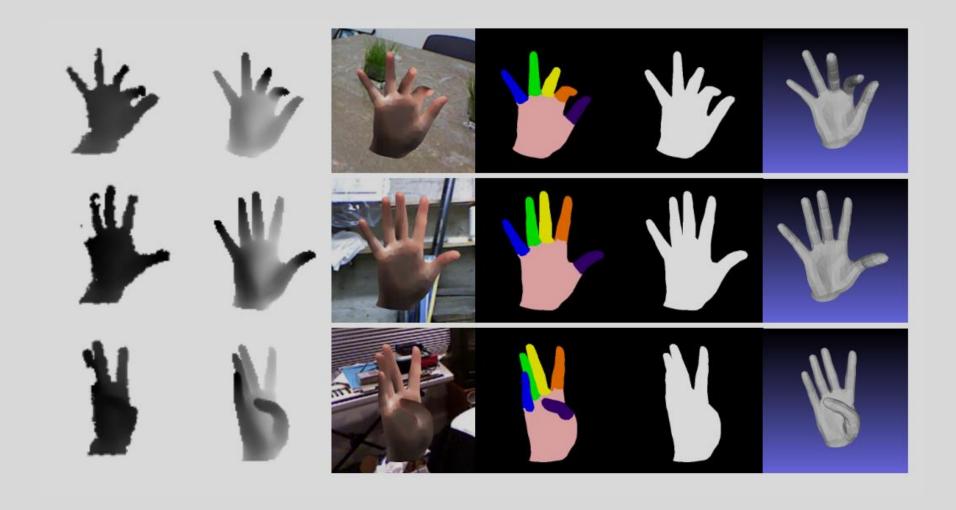


Data generation





Graphics model



Gap between real and synthetic

- 1. Testing data should be real; it means we will use the trained machine/deep learning models on the real-world testing dataset.
- 2. Training could involve synthetic dataset; however machine/deep learning models trained on synthetic dataset does not always generalize well to the real-world dataset, due to the domain gap.

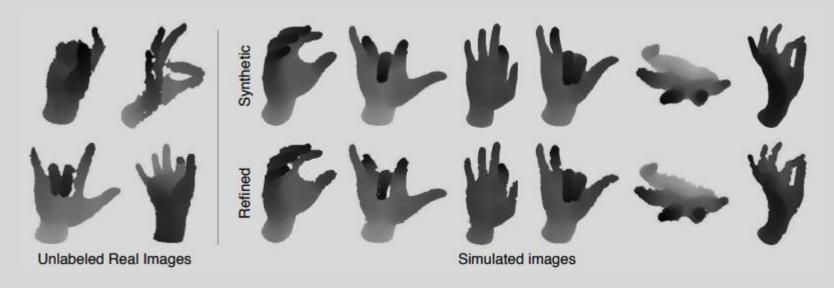
Train model using any supervision. Using synthetic+real datasets.





Test for the real hands.

Gap between real and synthetic

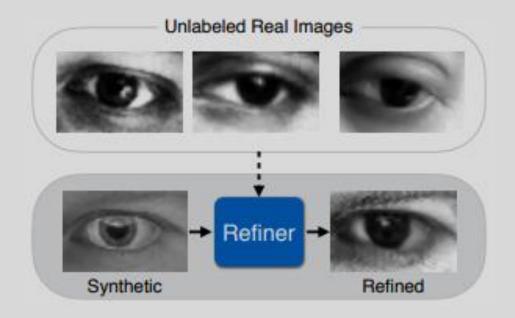


https://openaccess.thecvf.com/content_cvpr_2017/papers/Shrivastava_Learning_From_Simulated_CVPR_2017_paper.pdf



Simulated images

Gap between real and synthetic



Training data	% of images within d	
Synthetic Data	69.7	
Refined Synthetic Data	72.4	
Real Data	74.5	
Synthetic Data 3x	77.7	
Refined Synthetic Data 3x	83.3	

Table 4. Comparison of a hand pose estimator trained on synthetic data, real data, and the output of SimGAN. The results are at distance d=5 pixels from ground truth.

