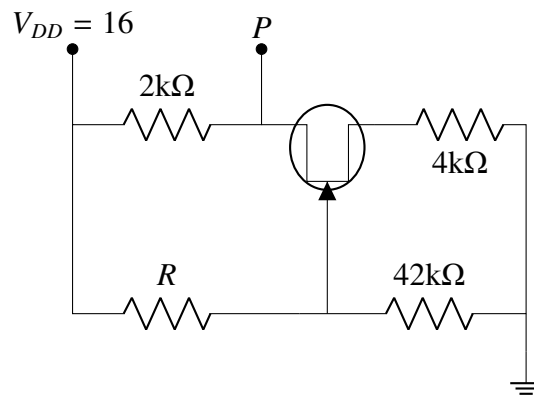


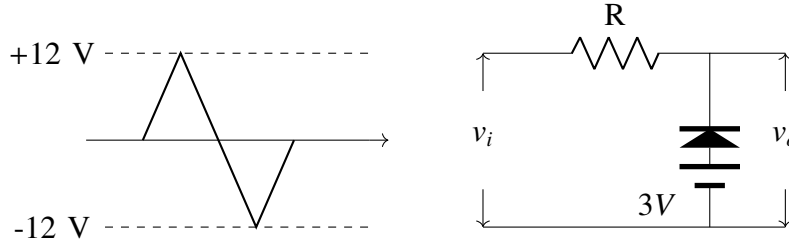
2007 PH 69-85

EE24BTECH11020 - Ellanti Rohith

- 1) In the circuit shown, the voltage at test point P is 12V and the voltage between gate and source is -2V. The value of R (in $k\Omega$) is [GATE 2007]



- a) 42 b) 48 c) 56 d) 70
- 2) When an input voltage V_i , of the form shown, is applied to the circuit given below, the output voltage V_o is of the form [GATE 2007]



- a) c)
- b) d)

Common Data for Questions 71, 72, 73:

A particle of mass m is confined in the ground state of a one-dimensional box, extending from $x = -2L$ to $x = +2L$. The wavefunction of the particle in this state is [GATE 2007]

$$\psi(x) = \psi_0 \cos\left(\frac{\pi x}{4L}\right)$$

where ψ_0 is a constant.

- 3) The normalization factor ψ_0 of this wavefunction is

- a) $\frac{\sqrt{2}}{L}$ b) $\frac{1}{\sqrt{4L}}$ c) $\frac{1}{\sqrt{2L}}$ d) $\frac{1}{\sqrt{L}}$

4) The energy eigenvalue corresponding to this state is

- a) $\frac{\hbar^2 \pi^2}{2mL^2}$ b) $\frac{\hbar^2 \pi^2}{4mL^2}$ c) $\frac{\hbar^2 \pi^2}{16mL^2}$ d) $\frac{\hbar^2 \pi^2}{32mL^2}$

5) The expectation value of p^2 (p is the momentum operator) in this state is

- a) 0 c) $\frac{\hbar^2 \pi^2}{16L^2}$
 b) $\frac{\hbar^2 \pi^2}{32L^2}$ d) $\frac{\hbar^2 \pi^2}{8L^2}$

Common Data for Questions 74, 75:

The Fresnel relations between the amplitudes of incident and reflected electromagnetic waves at an interface between air and a dielectric of refractive index μ_r are [GATE 2007]

$$\frac{E_{\parallel}^{\text{reflected}}}{E_{\parallel}^{\text{incident}}} = \frac{\cos r - \mu \cos i}{\cos r + \mu \cos i}, \quad \frac{E_{\perp}^{\text{reflected}}}{E_{\perp}^{\text{incident}}} = \frac{\mu \cos r - \cos i}{\mu \cos r + \cos i}$$

The subscripts \parallel and \perp refer to polarization, parallel and normal to the plane of incidence respectively. Here, i and r are the angles of incidence and refraction respectively.

6) The condition for the reflected ray to be completely polarized is

- a) $\mu \cos i = \cos r$ c) $\mu \cos i = -\cos r$
 b) $\cos i = \mu \cos r$ d) $\cos i = -\mu \cos r$

7) For normal incidence at an air-glass interface with $\mu = 1.5$, the fraction of energy reflected is given by

- a) 0.40 b) 0.20 c) 0.16 d) 0.04

Statement for Linked Answer Questions 76 & 77:

In the laboratory frame, a particle P of rest mass m_0 is moving in the positive x direction with a speed of $\frac{5c}{19}$. It approaches an identical particle Q , moving in the negative x direction with a speed of $\frac{2c}{5}$. [GATE 2007]

8) The speed of the particle P in the rest frame of the particle Q is

- a) $\frac{7c}{95}$ b) $\frac{13c}{85}$ c) $\frac{3c}{5}$ d) $\frac{63c}{95}$

9) The energy of the particle P in the rest frame of the particle Q is

- a) $\frac{1}{2}m_0c^2$ b) $\frac{5}{4}m_0c^2$ c) $\frac{19}{13}m_0c^2$ d) $\frac{11}{9}m_0c^2$

Statement for Linked Answer Questions 78 & 79:

The atomic density of a solid is $5.85 \times 10^{28} \text{m}^{-3}$. Its electrical resistivity is $1.6 \times 10^{-8} \Omega \text{m}$. Assume that electrical conduction is described by the Drude model (classical theory), and that each atom contributes one conduction electron. [GATE 2007]

10) The drift mobility (in $\text{m}^2 \text{V}^{-1} \text{s}^{-1}$) of the conduction electrons is

- a) 6.67×10^{-3} b) 6.67×10^{-6} c) 7.63×10^{-3} d) 7.63×10^{-6}

11) The relaxation time (mean free time), in seconds, of the conduction electrons is

- a) 3.98×10^{-15} c) 2.84×10^{-12}
b) 3.79×10^{-14} d) 2.64×10^{-11}

Statement for Linked Answer Questions 80 & 81:

A sphere of radius R carries a polarization $\mathbf{P} = k\mathbf{r}$, where k is a constant and \mathbf{r} is measured from the center of the sphere. [GATE 2007]

12) The bound surface and volume charge densities are given, respectively, by

- a) $-k|r|$ and $3k$ c) $k|r|$ and $-4\pi kR$
b) $k|r|$ and $-3k$ d) $-k|r|$ and $4\pi kR$

13) The electric field \mathbf{E} at a point \mathbf{r} outside the sphere is given by

- a) $\mathbf{E} = 0$ c) $\mathbf{E} = \frac{kR(R^2 - r^2)}{\epsilon_0 r^3} \hat{\mathbf{r}}$
b) $\mathbf{E} = \frac{kR(R^2 - r^2)}{6\epsilon_0 r^3} \hat{\mathbf{r}}$ d) $\mathbf{E} = \frac{3k(r - R)}{4\pi\epsilon_0 r^4} \hat{\mathbf{r}}$

Statement for Linked Answer Questions 82 & 83:

An ensemble of quantum harmonic oscillators is kept at a finite temperature $T = \frac{1}{k_B\beta}$. [GATE 2007]

14) The partition function of a single oscillator with energy levels $(n + \frac{1}{2})\hbar\omega$ is given by

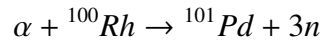
- a) $Z = \frac{e^{-\beta\hbar\omega/2}}{1 - e^{-\beta\hbar\omega}}$ c) $Z = \frac{1}{1 - e^{-\beta\hbar\omega}}$
b) $Z = \frac{e^{-\beta\hbar\omega/2}}{1 + e^{-\beta\hbar\omega}}$ d) $Z = \frac{1}{1 + e^{-\beta\hbar\omega}}$

15) The average number of energy quanta of the oscillators is given by

- a) $\langle n \rangle = \frac{1}{e^{\beta\hbar\omega} - 1}$ c) $\langle n \rangle = \frac{1}{e^{\beta\hbar\omega} + 1}$
b) $\langle n \rangle = \frac{e^{-\beta\hbar\omega}}{e^{\beta\hbar\omega} - 1}$ d) $\langle n \rangle = \frac{e^{-\beta\hbar\omega}}{e^{\beta\hbar\omega} + 1}$

Statement for Linked Answer Questions 84 & 85:

A $16\mu\text{A}$ beam of alpha particles, having cross-sectional area 10^{-4} m^2 , is incident on a rhodium target of thickness $1\mu\text{m}$. This produces neutrons through the reaction:



[GATE 2007]

16) The number of alpha particles hitting the target per second is

- a) 0.5×10^{14} b) 1.0×10^{14} c) 2.0×10^{20} d) 4.0×10^{20}

17) The neutrons are observed at the rate of $1.806 \times 10^8 \text{ s}^{-1}$. If the density of rhodium is approximated as 10^4 kg m^{-3} , the cross-section for the reaction (in barns) is

a) 0.1

b) 0.2

c) 0.4

d) 0.8