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16 February 2023  
Due Tuesday 21 February 2023

**Linear Algebra, Math 2101-002**  
**Homework set #6**

**1.** For each of the following statements indicate if the statement is TRUE or FALSE.  
If it is true, prove the statement. If it is false, give a counter-example.

(a) If  $A$  and  $B$  are nonsingular, then,  $AB = BA$ , i.e., they commute.

(b) If  $A$  and  $B$  are nonsingular, then,  $(AB)^{-1} = B^{-1}A^{-1}$ .

(c) If  $A$  is nonsingular, this implies that  $-A$  is nonsingular.

(d) If  $A$  and  $B$  are nonsingular, then,  $A + B$  is nonsingular.

(e) Let  $A = LU$ , where  $L$  is lower triangular with all diagonal entries equal to one. If  $U$  is nonsingular, then  $A$  is nonsingular.

(f) The inverse of a lower triangular matrix is upper triangular.

**2.–5.** Exercises from the book (pp. 155-156)

- 3.10.1

- 3.10.3

- 3.10.6

Optional, extra credit: - 3.10.7