

Assignment 6

1. **A.** 7.9

/ \

0.5 8.2

\ \

1.0 9.9

\

6.5

/ \

1.2 7.0

\

2.4

\

5.6

/

3.6

Height = 8

B. Petit Four

/

Cupcake

\

Donut

\

Eclair

\

Froyo

\

Gingerbread

\

Honeycomb

Height = 6

C. 32

/ \

5 94

\ /

10 87

/

85

\

47

/

25

\

29

Height = 5

D. 34

/ \

30 75

```

      /      \
    13      77
   / \      \
  10 20      96
 / \ /
5 11 19
      \
      48
      /
     39
      \
      50
      \
      93
Height = 8

```

2.

```

a.      510
      /   \
    111   372
   / \   / \
  15 108 80 379
   / \   / \
  46 129 87 283
 / \       /

```

36 37 93

\

97

b. No, because the updated node values no longer maintain the BST property, which is $\text{left} < \text{root} < \text{right}$.

c. No, because the balance factor property of AVL trees is not maintained after updating the nodes.

5. 1. initializeCandidates(LinkedList<String> candidates)

- Time: $O(n)$ – iterates once through n candidates to add to the HashMap and ArrayList.
- Space: $O(n)$ – stores each candidate in both the voteCount map and candidateList.

2. castVote(String candidate)

- Time: $O(1)$ – direct access and update in HashMap.
- Space: $O(1)$ – no additional space used.

3. castRandomVote()

- Time: $O(1)$ – random access in a list and then castVote (which is $O(1)$).
- Space: $O(1)$ – no extra space used.

4. rigElection(String candidate)

- Time: $O(n)$ – resets all vote counts (n candidates) and sets one to maxVotes.
- Space: $O(1)$ – no new structures; reuses existing.

5. `getTopKCandidates(int k)`

- Time: $O(n \log n)$ – building the priority queue from n candidates takes $O(n)$, polling top k takes $O(k \log n)$.
- Space: $O(n)$ – stores all entries in a priority queue.

6. `auditElection()`

- Time: $O(n \log n)$ – similar to `getTopKCandidates`, must sort or heapify all n candidates.
- Space: $O(n)$ – creates a maxHeap copy of the entries.