CSED211: Lab. 2 DataLab2

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POSTECH

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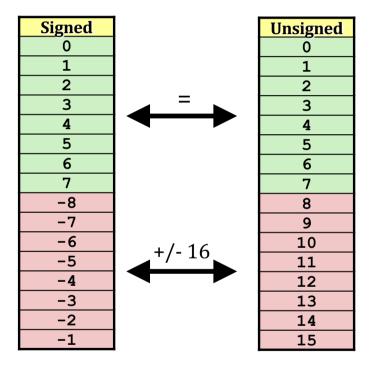
In Last Session

- Linux commands
- Bit and Byte
- Bitwise operation (~, &, |, ^, <<, >>)
- Homeworks about integer

2's Complement

- -x == -x + 1
- Ex) $5 \rightarrow 0100$ -5 $\rightarrow 1100$

Bits
0000
0001
0010
0011
0100
0101
0110
0111
1000
1001
1010
1011
1100
1101
1110
1111



2's Complement Computation

• Addition and subtraction of 2's complement does not need any other operation

$$15 + (-5)$$

Floating Point

- Fractional binary numbers
- IEEE floating point standard



Fractional Binary Numbers

Representation

- Limitations
 - Limitation 1. How can we represent $\frac{1}{3}$, $\frac{1}{7}$, ...?
 - $_{\circ}$ Can only exactly represent numbers of the form $x/2^{k}$
 - Limitation 2. How can we represent 2ⁱ⁺¹?
 - Limited range of numbers

IEEE Floating Point Standard

Representation

$$(-1)^{s} M 2^{E}$$

- S determines whether number is negative or positive
- M normally a fractional value in range [1.0, 2.0)
- E weights value by power of two
- Encoding
 - MSB is a sign bit S
 - Exp field encodes E (not exactly the same as E)
 - Frac field encodes M (not exactly the same as M)

Γ	S	e (exp)	f (frac)
	3	c (cap)) (Hue)

Precisions

■ Single precision: 32 bits

S	e	f
1	8 bits	23 bits

Double precision: 64 bits

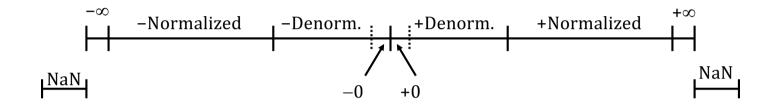
S	e	f
1	11 bits	52 bits

Extended precision: (Intel only): 80 bits

3 E

1 15 bits 63 or 64 bits

Visualization: Floating Point Encoding



- Normalized value
- Denormalized value
- Special value

Normalized Value

When exp != 000...0 and exp != 111...1

$$E = Exp - Bias$$

- Exp: unsinged value exp
- Bias: $2^{k-1}-1$, where k is number of exponent bits
 - ∘ Single precision: 127
 - Double precision: 1023
- M = 1 + f (fraction)
 - $_{\circ}$ Minimum when 000...0 (M = 1.0)
 - $_{\circ}$ Maximum when 111...1 (M = 2.0 ε)

Normalized Encoding Example

```
• Value: float f = 15213.0;
• 15213(10) = 11101101101101(2)
= 1.1101101101101(2) × 213
```

 $v = (-1)^{s} \times M \times 2^{E}$ E = Exp - Bias

Significand

```
• M = 1.\underline{1101101101}_{(2)}
• f = \underline{1101101101}_{00000000000000}
```

Exponent

• E = 13 • Bias = 127 • exp(e) = 140 = 10001100₍₂₎

Result

0	1000 1100	110 1101 1011 0100 0000 0000			
s	exp (e)	f (frac)			

Denormalized Value

■ When exp = 000...0

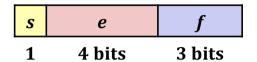
$$E = 1 - Bias$$

- M = 0 + f (fraction)
- Case1) exp = 000...0, frac = 000...0
 - o Represent 0
 - ∘ There exist +0 & -0
- Case2)
 - $_{\circ}\,$ Very small number closes to 0.0

Special Values

- When exp = 111...1
 - Case 1) exp = 111...1, frac = 000...0
 - Infinity
 - Operation that overflow
 - Both positive and negative
 - Case 2) $\exp = 111...1$, frac $\neq 000...0$
 - Not-a-Number (NaN)
 - o Represents case when no numeric value can be determined

Small Example: 8-bit Floating Point



- 8-bit floating point representation
 - The sign bit is in the most significant bit
 - The next four bits are the exponent, with a bias of 7
 - The last three bits are the fraction part
- The same general format as IEEE format
 - For normalized and denormalized numbers
 - For special values to represent 0, NaN, and infinity

Dynamic Range (Positive Only)

	s	exp	frac	E	Value	
	0	0000	000	-6	0	
	0	0000	001	-6	1/8*1/64 = 1/512	Closest to zero
Denormalized	0	0000	010	-6	2/8*1/64 = 2/512	
numbers						
	0	0000	110	-6	6/8*1/64 = 6/512	
	0	0000	111	-6	7/8*1/64 = 7/512	Largest denorm.
	0	0001	000	-6	8/8*1/64 = 8/512	
	0	0001	001	-6	9/8*1/64 = 9/512	
	0	0110	110	-1	14/8*1/2 = 14/16	
	0	0110	111	-1	15/8*1/2 = 15/16	Closest to 1 below
Normalized	0	0111	000	0	8/8*1 = 1	
numbers	0	0111	001	0	9/8*1 = 9/8	Closest to 1 above
	0	0111	010	0	10/8*1 = 10/8	
	0	1110	110	7	14/8*128 = 224	
	0	1110	111	7	15/8*128 = 240	
	0	1111	000 cs	SE n/a Intro	oc inf n to Computer Software Systems	Largest norm 15

Quiz

Homework

Lab Homework 2

- Due: 09/25 23:59 (midnight)
- Upload zip file which contains your source file and report
 - Explain your answer in the report
 - File name format (again): [student_#]_[name].c / .pdf, Lab[lab_#]_[student_#]_[name].zip
 - If you unzip in programming server, result should be directory containing .c/.pdf files
- Explain your answer in the report
- Refer to 'writeup_lab2' and following description

Homework Instruction

- Use the minimum number of operators as you can
- You are allowed to use only the following:
 - 1. Integer constants 0 through 255(0xFF)
 - 2. Function arguments and local variables
 - 3. Unary integer operations: !, ~
 - 4. Binary integer operations: &, ^, |, +, <<, >>
- Use dlc program to verify your solution
 - It will tell you whether you break the rule or not

Homework Instruction (cont.)

- You are expressly forbidden to:
 - 1. Use any control constructs: if, do, while, for, switch
 - 2. Define or use any macros
 - 3. Call any functions
 - 4. Use any other operations: &&, | |, -, or?
 - 5. Use any data type other than int (cannot use arrays, structs, or unions)



Homework Instruction (cont.)

- You may assume that your machine:
 - 1. Uses 2's complement, 32-bit representation of integers
 - 2. Performs right shifts arithmetically
 - 3. Has unpredictable behavior when shifting an integer by more than the word size



```
negate – return -x
Example: negate(1) = -1
Legal Ops: !, ~, &, ^, |, +, <<, >>
Max ops: 5
int negate(int x) {
// to be implemented
```

- isLess if x < y then return 1, else return 0
- Examples: isLess(4, 5) = 1
- Legal ops: !, ~, &, ^, |, +, <<, >>
- Max ops: 24

```
int isLess(int x, int y) {
   // to be implemented
}
```

Homework Instruction (Floating Point)

- For this part of the assignment, you will implement some common single-precision floating point operation
- You are allowed to use standard control structures (but not in previous problems)
 - Conditional, loops
- You also use both int and unsigned data types (but not in previous problems)
- You may not use unions, structs, or arrays
- You may not use any floating-point data types, operation, or constants
 - Any floating-point operand will be passed to the function as having type unsigned, and any returned floating-point value will be of type unsigned

- float_abs return absolute value of f
- Legal ops: Any integer/unsigned operations including | |, &&, if, while
- Max ops: 10

```
unsigned float_abs(unsigned uf) {
  // to be implemented
}
```

- float_twice return 2*f
- Legal ops: Any integer/unsigned operations including | |, &&, if, while
- Max ops: 30

```
unsigned float_twice(unsigned uf) {
  // to be implemented
}
```

- float_i2f return (float)x
- Legal ops: Any integer/unsigned operations including | |, &&, if, while
- Max ops: 30

```
unsigned float_i2f(int uf) {
  // to be implemented
}
```

- float_f2i return (int)f
- Legal ops: Any integer/unsigned operations including | |, &&, if, while
- Max ops: 30

```
int float_f2i(unsigned uf) {
   // to be implemented
}
```

How to Do?

- Download "bits.c" file and implement each function
- Use only legal operation and definition of the function
- Please use PLMS Q&A board instead of sending e-mails to TA
 - Do not delete your question after you get your answer

Q & A