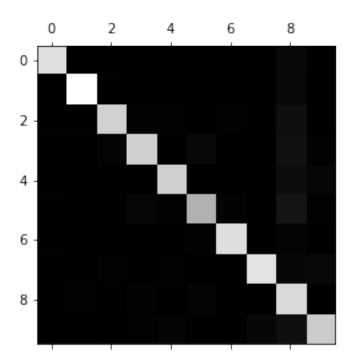
"Determining the Optimal Training Data Size for Recognizing Handwriting"

Elizabeth Chason

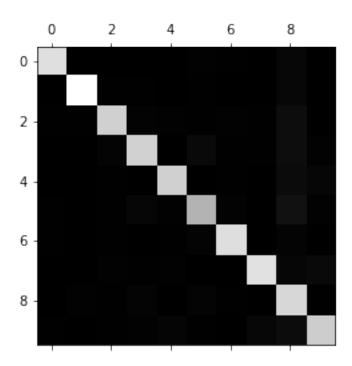
January 19, 2020

```
In [8]: from sklearn.datasets import fetch_openml
In [9]: mnist = fetch_openml('mnist_784', version=1)
In [10]: mnist.keys()
Out[10]: dict_keys(['data', 'target', 'feature_names', 'DESCR', 'details', 'categories', 'url']
In [11]: X, y = mnist["data"], mnist["target"]
         X.shape
Out[11]: (70000, 784)
In [12]:
['5' '0' '4' ... '4' '5' '6']
In [13]: import matplotlib as mpl
         import matplotlib.pyplot as plt
In [17]: import numpy as np
         y = y.astype(np.uint8)
         X_{\text{train}}, X_{\text{test}}, y_{\text{train}}, y_{\text{test}} = X[:60000], X[60000:], y[:60000], y[60000:]
         y_{train_5} = (y_{train} == 5)
         y_{test_5} = (y_{test} == 5)
         from sklearn.linear_model import SGDClassifier
         sgd_clf = SGDClassifier(max_iter=5000, random_state=42)
         from sklearn.preprocessing import StandardScaler
         from sklearn.model_selection import cross_val_predict
         from sklearn.metrics import confusion_matrix
         scaler = StandardScaler()
         X_train_scaled = scaler.fit_transform(X_train.astype(np.float64))
         y_train_pred = cross_val_predict(sgd_clf, X_train_scaled, y_train, cv=3)
         conf_mx = confusion_matrix(y_train, y_train_pred)
         plt.matshow(conf_mx, cmap=plt.cm.gray)
         conf_mx
         plt.show()
```



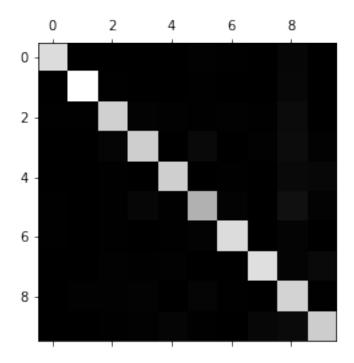
```
In [18]: conf_mx
```

```
Out[18]: array([[5576,
                             Ο,
                                   21,
                                           6,
                                                 9,
                                                       42,
                                                              37,
                                                                      6,
                                                                          225,
                                                                                    1],
                      0, 6398,
                                   38,
                                          23,
                                                       44,
                                                               4,
                                                                          213,
                                                                                   10],
                                                 4,
                                                                      8,
                  26,
                            27, 5242,
                                         90,
                                                71,
                                                       26,
                                                              62,
                                                                     36,
                                                                          371,
                                                                                   7],
                  24,
                            17,
                                  117, 5219,
                                                 2,
                                                      208,
                                                              28,
                                                                     40,
                                                                          406,
                                                                                   70],
                  12,
                            14,
                                   48,
                                          10, 5192,
                                                       10,
                                                              36,
                                                                     26,
                                                                          330,
                                                                                 164],
                  55, 4436,
                                                              76,
                                                                     14,
                                                                          539,
                     28,
                            15,
                                   33,
                                        166,
                                                                                  59],
                  95, 5558,
                     30,
                            14,
                                   41,
                                           2,
                                                43,
                                                                      4,
                                                                          130,
                                                                                    1],
                  21,
                             9,
                                   51,
                                                       12,
                                                                          190,
                                                                                 209],
                                          26,
                                                51,
                                                               3, 5693,
                  17,
                            63,
                                   46,
                                          90,
                                                 3,
                                                      125,
                                                              25,
                                                                     10, 5429,
                                                                         378, 5106]])
                     23,
                            18,
                                   31,
                                         65,
                                               116,
                                                       32,
                                                               1,
                                                                    179,
```



```
In [39]: conf_mx2
```

```
Out[39]: array([[5225,
                             Ο,
                                   21,
                                           6,
                                                  7,
                                                        51,
                                                              36,
                                                                           179,
                                                                                    1],
                                   40,
                                          27,
                                                        45,
                                                               3,
                                                                           179,
                      1, 5992,
                                                  4,
                                                                      7,
                                                                                   10],
                  24,
                            27, 4881,
                                          90,
                                                 65,
                                                        31,
                                                              65,
                                                                     41,
                                                                           325,
                                                                                   11],
                  23,
                            18,
                                  109, 4903,
                                                  1,
                                                      221,
                                                              28,
                                                                     42,
                                                                           313,
                                                                                   70],
                  13,
                            13,
                                   37,
                                          10, 4877,
                                                        14,
                                                              38,
                                                                     19,
                                                                           264,
                                                                                  163],
                  51, 4207,
                                                              74,
                                                                     16,
                                                                           420,
                     26,
                            15,
                                   31,
                                         160,
                                                                                   60],
                  26,
                            15,
                                   41,
                                           2,
                                                 41,
                                                        94, 5201,
                                                                      5,
                                                                           110,
                                                                                    2],
                  17,
                                                                           141,
                                                                                  220],
                            11,
                                   51,
                                          26,
                                                 50,
                                                        11,
                                                               2, 5281,
                  19,
                            58,
                                   46,
                                          94,
                                                  3,
                                                      113,
                                                                      9, 5047,
                                                              27,
                     25,
                            19,
                                   28,
                                          66,
                                               118,
                                                        34,
                                                               1,
                                                                    179,
                                                                           288, 4801]])
```



```
Out[41]: array([[4566,
                            0,
                                  19,
                                         6,
                                                8,
                                                     46,
                                                            34,
                                                                   4,
                                                                        141,
                                                                                 1],
                     0, 5297,
                                  40,
                                        20,
                                                             3,
                                                3,
                                                     40,
                                                                   7,
                                                                        150,
                                                                                10],
                 26,
                           26, 4311,
                                        75,
                                               59,
                                                     23,
                                                            62,
                                                                  34,
                                                                        242,
                                                                                 9],
                 20,
                           18,
                                112, 4272,
                                                2,
                                                    189,
                                                            20,
                                                                  44,
                                                                        252,
                                                                               57],
                 12,
                           12,
                                 33,
                                        10, 4298,
                                                      9,
                                                            33,
                                                                   15,
                                                                        201,
                                                                              150],
                 137,
                                                            64,
                    23,
                           12,
                                  28,
                                               40, 3683,
                                                                  12,
                                                                        340,
                                                                               67],
                 25,
                           15,
                                  38,
                                         2,
                                               37,
                                                     79, 4565,
                                                                   4,
                                                                         89,
                                                                                 1],
                 14,
                                        27,
                                               45,
                                                             4, 4622,
                                                                         93,
                           10,
                                  48,
                                                     10,
                                                                              203],
                           59,
                                  43,
                                        78,
                                                3,
                                                    104,
                    17,
                                                            26,
                                                                   7, 4377,
                                                                                37],
                    20,
                           16,
                                 27,
                                        59,
                                             110,
                                                     34,
                                                             1,
                                                                 150,
                                                                        216, 4258]])
In [48]: flist = []
         for num in range(10):
              recall = conf_mx[num][num] / sum(conf_mx[num])
              lisst = []
              for i in range(10):
                  prec_denom = conf_mx[i][num]
                  lisst.append(prec_denom)
              precision = conf_mx[num] [num] / sum(lisst)
              fone = 2 / ((1/precision) + (1/recall))
              flist.append(fone)
         cumulfone1 = sum(flist)
         meanfone1 = cumulfone / 10
```

In [41]: conf_mx3

meanfone1

```
Out [48]: 0.8985060679733488
In [53]: flist2 = []
         for num in range(10):
             recall2 = conf mx2[num] [num] / sum(conf mx2[num])
             lisst2 = []
             for i in range(10):
                 prec_denom2 = conf_mx2[i][num]
                 lisst2.append(prec_denom2)
             precision2 = conf_mx2[num] [num] / sum(lisst2)
             fone2 = 2 / ((1/precision2) + (1/recall2))
             flist2.append(fone2)
         cumulfone2 = sum(flist2)
         meanfone2 = cumulfone2 / 10
         meanfone2
Out [53]: 0.9006294715151826
In [54]: flist3 = []
         for num in range(10):
             recall3 = conf_mx3[num] [num] / sum(conf_mx3[num])
             lisst3 = []
             for i in range(10):
                 prec_denom3 = conf_mx3[i][num]
                 lisst3.append(prec_denom3)
             precision3 = conf_mx3[num][num] / sum(lisst3)
             fone3 = 2 / ((1/precision3) + (1/recall3))
             flist3.append(fone3)
         cumulfone3 = sum(flist3)
         meanfone3 = cumulfone3 / 10
         meanfone3
Out [54]: 0.9029226433725686
```