

**Assignment #2 [100 points] + 10 Bonus points**  
**Feature Detection, Description, and Matching**

The goal of this assignment is to implement a simple feature detection, description, and matching pipeline that can be used for variety of applications including image registration to object retrieval.

**Part A) Feature detection [30pts]**

**Step-A1:** As described in class and in lecture notes compute the autocorrelation matrix:

$$A = \begin{bmatrix} G(\sigma) \otimes I_x^2 & G(\sigma) \otimes I_x I_y \\ G(\sigma) \otimes I_x I_y & G(\sigma) \otimes I_y^2 \end{bmatrix}$$

You can use built in Python and OpenCV functions for convolution/filtering function (i.e. `cv2.filter2D`).

**Step-A2:** Compute a scalar feature detection measure using one of the formulas discussed in class:

- Shi-Tomasi,
- Harris-Stephens, or
- Harmonic mean.

**Step-A3:** Find local maxima above a certain threshold and report them as detected feature point locations.

Show the detected feature points on the image and include them to the report.

**Part B) Feature matching and evaluation [70pts]**

**Step-B1:** Define and describe a feature descriptor. You can simply use square patches around the detected feature points.

**Step-B2:** Perform feature matching using the feature descriptor you designed and report results for the three matching strategies described in class and lecture notes:

1. distance thresholding,
2. nearest match, and
3. nearest neighbor distance ratio.

**Step-B3:** Use the transformation/homography matrices (H1to2p, H1to3p...) provided with the data and evaluate feature matching performance by reporting TPR (True Positive Rate)

In feature matching, the "true positive rate" (TPR) refers to the proportion of correctly identified corresponding features (true positives) out of all the actual corresponding features present in two images, essentially measuring how well a feature matching algorithm can accurately find

the correct matches between keypoints across different images; a higher true positive rate indicates better matching performance

### Evaluation Process:

1. Apply the given transformation matrix to a point to estimate its location in the second image. Let  $(x_1, y_1)$  and  $(x_2, y_2)$  be the coordinates of a pair of matching points in image-1 and image-2.

Correct position for point  $(x_1, y_1)$  in image 2 is computed using the given transformation  $H_{1 \rightarrow 2}$

$$\begin{bmatrix} x'_2 \\ y'_2 \\ 1 \end{bmatrix} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix} \text{ where } H_{1 \rightarrow 2} = \begin{bmatrix} a & b & c \\ d & e & f \\ g & h & 1 \end{bmatrix}$$

2. Compute pixel distance between the estimated position  $(x'_2, y'_2)$  and the matched point's position  $(x_2, y_2)$ .
3. If the distance is less than  $k$  pixels consider a true positive otherwise label as false positive.

Show the matched points on the input images and include the pictures to your report.

**BONUS [1-12 points]** If you design and implement a better descriptor that is invariant to one or more of the followings:

- [4 pts] scale
- [5 pts] rotation
- [3 pts] brightness-contrast

Demonstrate invariance/robustness of your descriptor by showing results on an appropriate image pair. Specify in the report which invariance you were targeting and whether you were successful.

### Program Structure and Deliveries:

Your program needs to include the following functions:

1. **function [R]=computeFeatureResponse(I,parameters)**  
I: an  $N \times M$  image grayscale measure  
Parameters: additional parameters needed  
R: an  $N \times M$  image, one of the three feature response described in lecture notes (ShiTomasi, Harris, or HarmonicMean).
2. **function [x,y,mask]=FeatureMeasure2Points(R,npoints)**  
R:  $N \times M$  feature response matrix  
npoints: number of feature points that will be returned  
x,y : coordinates of the feature points (npoints $\times$ 1)  
mask : binary mask showing the location of the feature points

3. **function [DList]=generateFeatureDescriptors(I,x,y)**

I : input image

x,y : coordinates of feature points (npointsx1)

Dlist: npointsxDlength descriptor list, where Dlist(i,:) is the feature descriptor vector for the feature point x(i),y(i).

3. **function [Dist]=computeDescriptorDistances(Dlist1,Dlist2)**

Dlist1: descriptor list from first image

Dlist2: descriptor list from second image

Dist: distance matrix, Dist(i,j): distance between ith descriptor in first image and jth descriptor in second image.

4. **Function [MatchList1]=Distance2Matches\_DistThresh(Dist,Th1)**

**Function [MatchList2]=Distance2Matches\_NearestMatch(Dist,Th2)**

**Function [MatchList3]=Distance2Matches\_NearestRatio(Dist,Th3)**

Dist: distance matrix, Dist(i,j): distance between ith descriptor in first image and jth descriptor in second image.

Th1,Th2,Th3: threshold values needed for the methods

MatchList: nx2 matrix of matches where MatchList(i,1) is the index of a feature points in first and and MatchList(i,2) is the index of the matching feature point in the second image.

**Test Data**

Download the file hw2.zip for test data. Your program should get reasonable matches for at least for **bikes\img1** and **bikes\img2**.

With appropriate descriptor design you can get good results for the other images. This will get you bonus points.

**Submission instructions:**

1. **Code:** Code should be organized into functions as described above. Use specific names and inputs/outputs. Non-compliant code will result in reduced points even if the outputs are correct.
2. **Report:** The report should include the following items for at least two image pairs. Include more images to demonstrate how well your pipeline works, particularly if you worked on bonus section.
  - a. Show detected feature points marked on the input images
  - b. For three matching strategies:
    - a. Show matched points connected with a line on the input images
    - b. Show matching statistics as a table

	Distance threshold	Nearest neighbor	Nearest neighbor distance ratio
Threshold used			
Number of detected feature points			
Number of matched points			
TPR (True Positive Rate)			

