

```

ClearAll["Global`*"]
A[r_, p_] = (1 / 2) * p * r^2;
grad = D[A[r, p], {{r, p}}];
agrad = Abs[grad];
errorRP = {dr, dp};
errorA = Simplify[agrad.errorRP]
deltaR = Solve[errorA == dA, dr]
deltaR /. {dA -> (1 / 2), dp -> (1 / 100) * (2 * Pi / 360)};
Expand[%];
Simplify[%]
deltaR /. {dA -> (1 / 2), r -> 50, p -> 2 * Pi / 3,
          dp -> (1 / 100) * (2 * Pi / 360)};
Simplify[%]
N[%]

```

$$\text{Out}[*]= \frac{1}{2} dp \text{Abs}[r]^2 + dr \text{Abs}[p r]$$

$$\text{Out}[*]= \left\{ \left\{ dr \rightarrow \frac{2 dA - dp \text{Abs}[r]^2}{2 \text{Abs}[p r]} \right\} \right\}$$

$$\text{Out}[*]= \left\{ \left\{ dr \rightarrow \frac{18000 - \pi \text{Abs}[r]^2}{36000 \text{Abs}[p r]} \right\} \right\}$$

$$\text{Out}[*]= \left\{ \left\{ dr \rightarrow -\frac{1}{480} + \frac{3}{200 \pi} \right\} \right\}$$

$$\text{Out}[*]= \left\{ \left\{ dr \rightarrow 0.00269131 \right\} \right\}$$