

```
In[ ]:= Series[Sin[x], {x, 0, 3}]
```

$$\text{Out[]}= x - \frac{x^3}{6} + O[x]^4$$

```
In[ ]:= Normal[Series[Sin[x], {x, 0, 3}]]
```

$$\text{Out[]}= x - \frac{x^3}{6}$$

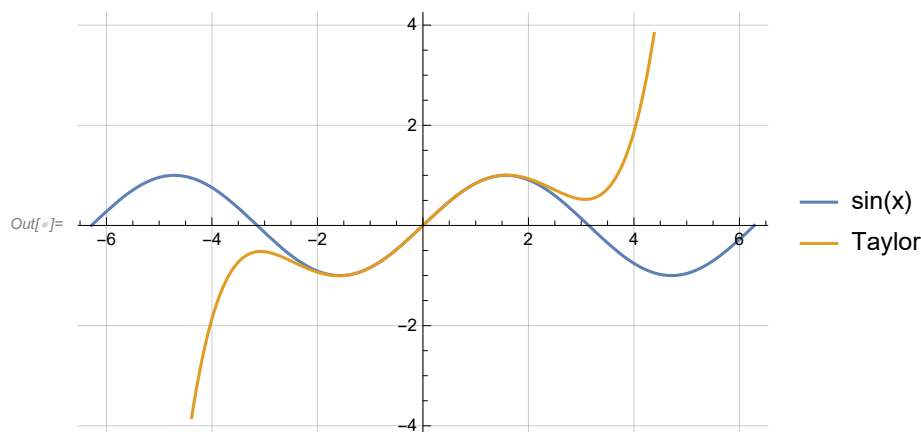
```
In[ ]:= N[Pi, 20]
```

$$\text{Out[]}= 3.1415926535897932385$$

```
In[ ]:= f[x_] = x^2 + 3 * x - 5;
Solve[f[x] == 0, x]
```

$$\text{Out[]}= \left\{ \left\{ x \rightarrow \frac{1}{2} \left(-3 - \sqrt{29} \right) \right\}, \left\{ x \rightarrow \frac{1}{2} \left(-3 + \sqrt{29} \right) \right\} \right\}$$

```
In[ ]:= Normal[Series[Sin[x], {x, 0, 5}]];
Plot[{Sin[x], %}, {x, -2 * Pi, 2 * Pi},
PlotLegends -> {"sin(x)", "Taylor"}, GridLines -> Automatic]
```



```
In[ ]:= ClearAll["Global`*"]
```

```
Ctot[q_] = a * (d/q) + b * (q/2)
der = D[Ctot[q], q]
```

$$\text{Out[]}= \frac{a d}{q} + \frac{b q}{2}$$

$$\text{Out[]}= \frac{b}{2} - \frac{a d}{q^2}$$

```
In[ ]:= Solve[der == 0, q]
qq = %[[2, 1, 2]]
```

$$\text{Out[]}= \left\{ \left\{ q \rightarrow -\frac{\sqrt{2} \sqrt{a} \sqrt{d}}{\sqrt{b}} \right\}, \left\{ q \rightarrow \frac{\sqrt{2} \sqrt{a} \sqrt{d}}{\sqrt{b}} \right\} \right\}$$

$$\text{Out[]}= \frac{\sqrt{2} \sqrt{a} \sqrt{d}}{\sqrt{b}}$$

```
In[ ]:= a * (d/qq) + b * (qq/2)
```

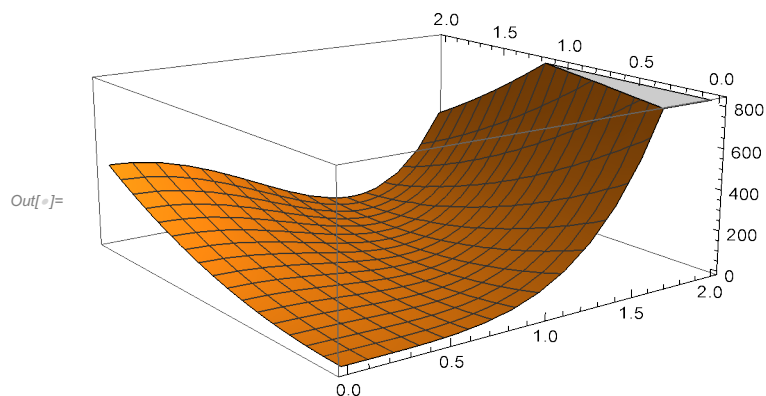
$$\text{Out[]}= \sqrt{2} \sqrt{a} \sqrt{b} \sqrt{d}$$

```
In[ ]:= ClearAll["Global`*"]
f[x_, y_] = 100 * (y - x^2)^2 + (a - x)^2;
grad = D[f[x, y], {{x, y}}];
min = Solve[grad == {0, 0}, {x, y}]
f[x, y] /. {x -> min[[1, 1, 2]], y -> min[[1, 2, 2]]}
```

```
Out[ ]:= {{x -> a, y -> a^2}}
```

```
Out[ ]:= 0
```

```
In[ ]:= a = 1;
pic = Plot3D[f[x, y], {x, 0, 2}, {y, 0, 2}]
```



```
In[ ]:= ClearAll["Global`*"]
f[a_, b_] = (a * b) / (a + b);
grad = D[f[a, b], {{a, b}}];
agrad = Abs[grad];
errorAB = {da, db};
errorF = Simplify[agrad.errorAB]
a = 85;
da = 1;
b = 196;
db = 2;
F = f[a, b]
N[%]
{F - errorF, F + errorF}
N[%]
```

```
Out[ ]:= db Abs[ $\frac{a^2}{(a+b)^2}$ ] + da Abs[ $\frac{b^2}{(a+b)^2}$ ]
```

```
Out[ ]:=  $\frac{16660}{281}$ 
```

```
Out[ ]:= 59.2883
```

```
Out[ ]:= { $\frac{4628594}{78961}$ ,  $\frac{4734326}{78961}$ }
```

```
Out[ ]:= {58.6187, 59.9578}
```

```

ClearAll["Global`*"]
A[r_, p_] = (1/2) * p * r^2;
grad = D[A[r, p], {{r, p}}];
agrad = Abs[grad];
errorRP = {dr, dp};
errorA = Simplify[agrad.errorRP]
deltaR = Solve[errorA == dA, dr]
deltaR /. {dA -> (1/2), dp -> (1/100) * (2 * Pi / 360)};
Expand[%];
Simplify[%]
deltaR /. {dA -> (1/2), r -> 50, p -> 2 * Pi / 3,
  dp -> (1/100) * (2 * Pi / 360)};
Simplify[%]
N[%]

```

$$\text{Out}[*]= \frac{1}{2} dp \text{Abs}[r]^2 + dr \text{Abs}[p r]$$

$$\text{Out}[*]= \left\{ \left\{ dr \rightarrow \frac{2 dA - dp \text{Abs}[r]^2}{2 \text{Abs}[p r]} \right\} \right\}$$

$$\text{Out}[*]= \left\{ \left\{ dr \rightarrow \frac{18000 - \pi \text{Abs}[r]^2}{36000 \text{Abs}[p r]} \right\} \right\}$$

$$\text{Out}[*]= \left\{ \left\{ dr \rightarrow -\frac{1}{480} + \frac{3}{200 \pi} \right\} \right\}$$

$$\text{Out}[*]= \left\{ \left\{ dr \rightarrow 0.00269131 \right\} \right\}$$