Enigma Machine Simulator

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# Abstract

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# Introduction

The Enigma Cypher Machine (*Enigma I)* is most well-known for its usage and eventual breaking, during World War 2 (WW2). The machine used several mechanical rotors, a reflect and a plugboard to redirect electrical signals, scrambling a plaintext message into cyphertext. Whilst most have heard of the machine, either from a study of cryptography or through history, many do not understand how the machine functions and its significance in cryptography. By creating a visual tool to demonstrate the inner workings of the Enigma, the aim of the project was to offer a deeper insight into the functionality, significance, but also the weaknesses of the machine.

There already exists a handful of examples of Enigma simulations which tend to offer a skeuomorphic approach to modelling the machine. The challenge I wanted to overcome was to create a tool that teaches the user how the machine functions logically. I began my project by thoroughly researching *Enigma I* to understand the inner workings of the machine and to compile this research into a simpler, abstracted model using Java. I created both a multi-platform command line interface (CLI) and a multi-platform graphical user interface (GUI) to allow the user to interact with the model, the former offering a step-by-step visualisation of the encryption of a message. To complete the project, I developed a second “EnimgaPlus” model which aims to correct the two key cryptographic weaknesses of the machine. I identified the accuracy of my model by comparing with similar products as well as some real-world messages found amongst the German forces during WW2. I also identified the effectiveness of the two Enigma models by using some basic cryptoanalysis.

## Aims and Objectives

The following list adapted from the original project description, however there are some additional objectives I have included myself. For each task I set my own criteria to assess the success of each task’s implementation.

|  |  |
| --- | --- |
| Aim / Objective | Criteria for Success |
| Create a standalone package that simulates *Enigma I* | The package should simulate only the Enigma machine and should be able to be used in different applications. It should also produce the correct output for a given input. The package should allow the Enigma Machine to be fully configurable as the ‘Enigma I’ |
| Create a new “EnigmaPlus” machine with an aim of fixing cryptographic weaknesses of *Enigma I* | The “EnigmaPlus” machine should function similarly to the original Enigma and should be more secure cryptographically |
| Create a basic command line interface | The CLI should be allow full configuration of the machine and allow the user to enter a plaintext message |
| Create a GUI with a visualisation tool | The GUI should have the same capabilities, if not more than the CLI. In addition, it should aim to visually reflect the machine.  The visualisation tool should provide a simplified and informative representation of the encryption steps |
| Support multiple platforms | The application should be compatible with Windows/MacOS/Linux |

# History & Background

## History of the Machine

The Enigma cypher is one of the most famous cipher machines (Enigma n.d.) due to its role in WW2 and the work undertaken at Bletchley Park to crack the code. The Enigma was used extensively by the German forces to transmit coded messages for more secure communication. Whilst most people refer to this machine as “The Enigma”, Enigma is a brand name for a series of cypher machines (Enigma n.d.). The one used most in WW2 was *Enigma I* and was the key focus of this project.

To use the Enigma machine, it had to be configured to an exact setting so that the machine could be correctly decoded by the intended parties. These settings were distributed to the German forces each month in a code book, containing each day’s settings.

TODO : Add more history here

## Design of the Machine

The Enigma Machine was a rotor-based machine and worked with a hybrid of mechanics and electrical signals. *Enigma I* contained 5 key components that worked together to produce cyphertext which were: the keyboard and lampboard, the rotors, the reflector, and the plugboard. The inclusion of all these components aimed to make the machine as unpredictable as possible as well as generating a large key-length of roughly 67 bits (nearly 159 quintillion different settings see Equation 6) (van Manen and Robertsson 2016).

The use of the machine was a simple process. A user would receive a message along with a key denoting the choice of rotors and their respective settings, the plugboard settings and a reflector choice. Each time a key was pressed on the keyboard, a light on the lampboard would emit light as demonstrated in Owen’s animation (Owen 2021) and the user would write down the corresponding letter. Due to the symmetric design of the Enigma machine, as long as two people had the same settings then they could simply input the cyphertext into the machine and receive the plaintext and vice versa. However, this design choice was overlooked and compromised the Enigma’s security (See 3.4) (Thimbleby 2016).



Figure A photo of Enigma I showing the plugboard, keyboard and lampboard. Only a small portion of the rotors are visible, and the reflector is hidden (Enigma n.d.).

### Keyboard & Lampboard

The keyboard and lampboard were the interface which the user could encode/decode messages. The former was comprised of the 26-letter alphabet omitting any special or numeric characters. Each key on the keyboard could be pressed which would cause a ratchet mechanism to move a lever (pawl) to step the rotors (Hamer 1997). The lampboard was a copy of the keyboard but instead of keys, there were small glass panels which would allow the bulbs underneath to shine through. These panels were also printed with the 26-letter alphabet and upon a keypress, any given lamp could light up to show the plaintext character’s corresponding cyphertext.

### Rotors

The rotors were the heart of the Enigma machine and were responsible for most of its unique properties. They were metal ratchet discs with 26 different positions representing each letter of the alphabet. Each position had a corresponding metal contact (Owen 2021) on both sides of the disk to allow electrical current to flow through the rotor. Inside the rotor, fixed wires were implemented which directed the current from one contact to another, encoding the input.

Rotors also exhibited another property; each rotor had a notch at a fixed position on the ratchet which would allow the levers (pawls) mentioned earlier to ‘step’ the rotor (Hamer 1997). This stepping caused the rotor to rotate by one position. In the machine, three rotors were placed in series to allow current to pass through all three, causing a letter to be scrambled 3 times from one key press. Once a rotor would reach its turnover position (the character shown to the user once the notch position is lined up to the pawl, the latter is not seen by the user of the machine), the rotor to left of the turnover rotor would be stepped as well. The right-most rotor would step every key press, the middle rotor would step with a period of 25 (Grime 2013) (Smart 2016) (one might expect 26, however due to a quirk of the machine known as double stepping, the middle rotor could step twice in a row). The left-most rotor would step with a period of 262. This rotational property of the machine allowed for the encoding for a given letter to change each keypress.

The Enigma rotors could be swapped around and placed in any order in the three slots available. Usually, users were given a box containing 5 different rotors the choice of which to use formed part of the Enigma’s key. Table 1 depicts the 5 rotors that were included with *Enigma I* demonstrating their internal wiring as well as the location of the notch. For example, rotor I will map A to E and B to K provided the rotor is in rest position (Position A and Ring setting A).

|  |  |  |  |
| --- | --- | --- | --- |
| Rotor | Encoding (Position A - Ring setting A) ABCDEFGHIJKLMNOPQRSTUVWXYZ | Notch | Turnover |
| I | EKMFLGDQVZNTOWYHXUSPAIBRCJ | Y | Q |
| II | AJDKSIRUXBLHWTMCQGZNPYFVOE | M | E |
| III | BDFHJLCPRTXVZNYEIWGAKMUSQO | D | V |
| IV | ESOVPZJAYQUIRHXLNFTGKDCMWB | R | J |
| V | VZBRGITYUPSDNHLXAWMJQOFECK | H | Z |

Table 1 "Enigma I" rotor encodings (Enigma wiring n.d.)

Finally, the rotors had an additional setting known as the ring setting. This allowed the internal wires and ratchet to be shifted independently from the letter ring, allowing the notch position to move relative to the letter ring. Whilst generally, the ring setting formed part of the key, it is important to note that it had marginal strength on the strength of the cypher, only affecting the turnover position of the adjacent rotor (How does the Enigma machine work? n.d.).

Much of the complexity of the Enigma was due to these rotors. Alone, with an *Enigma I* model, there were 1054560 different ways to configure the rotors (See Equation 1)

Equation Permutations for rotors (excluding ring setting)

### Reflector

The reflector was a similar component to that of the rotors and together formed the subsystem that does most of the scrambling. The main differences regarding the reflector are that it does not rotate, and the current does not pass through but rather is ‘reflected’, travelling back in the opposite direction. This reflection allows the reflector to act as a similar substitution cypher akin to the rotors.

The design of the reflector was to enable whole machine to be reciprocal, combining encryption and decryption into one operation. This, along with the fact that the reflector could not encode a letter to itself (the design of the rotor prevented the current being passed back through the same metal contact) were crucial flaws exploited (Thimbleby 2016) by the team at Bletchley Park to crack the code during WW2.

The Enigma machine came with a reflector which could be replaced with another but generally remained the same. The three that were available with the *Enigma I* were UKW-A, UKW-B and UKW-C as shown in Table 2. The encodings demonstrate the inner wiring of each reflector, for example UKW-A maps A to the letter E as they have matching indexes.

|  |  |
| --- | --- |
| Reflector | Encoding ABCDEFGHIJKLMNOPQRSTUVWXYZ |
| UKW-A | EJMZALYXVBWFCRQUONTSPIKHGD |
| UKW-B | YRUHQSLDPXNGOKMIEBFZCWVJAT |
| UKW-C | FVPJIAOYEDRZXWGCTKUQSBNMHL |

Table "Enigma I" reflector encodings (Enigma wiring n.d.)

### Plugboard

The plugboard formed the final part of the Enigma’s encryption key and was located at the front of the machine. It displayed another representation of the 26-letter alphabet, each of which had a plug socket. These sockets, and the cables that came with the machine allowed two letters to be connected to each other on the plugboard. This created yet another scrambling of the letter, such that if socket A and socket E were connected then any current passing through the plugboard in wire A, would be directed to wire E and vice versa. Any letter left unconnected to another would result in the plugboard having no effect for that letter. The plugboards letter swapping effect only occurred twice in each encryption, once at the start of the encryption (after the keypress) and once at the end (before the lamp on the lampboard lights up).



Figure A front-facing photo of the Enigma I plugboard with cables in place (Enigma n.d.)

## Enigma Machine and Abstraction

### Enigma’s Encryption

Often the best way to understand the mechanisms of the machine is to focus on a single letter’s encryption. As mentioned in 3.2, the user begins with defining the machine’s key. Upon a keypress on the keyboard, the first notable event is that the rightmost rotor will rotate. Depending on the current rotation, the other rotors may also rotate but only ever by one position. Once this step is completed, an electrical signal will be induced passing through the plugboard towards the rotors. Depending on the plugboard settings, this input signal may be scrambled. This electrical signal then passes through rotors right-to-left with the signal being redirected at each rotor. The output of the three rotor redirections is then transmitted to the reflector where the signal’s direction is reversed and redirected to a different letter’s contact. The signal then passes through all three rotors for a final time, this time from left-to-right, before passing through the plugboard again. Finally, the signal is transmitted to the lampboard where the cyphertext is displayed. Any plaintext letter can be scrambled up to nine times before the cyphertext is displayed.

By representing each of the components of the Enigma as a transformation as demonstrated by Rejewski (Rejewski 1980), such that represents the plugboard, represents the rotor in the left, middle or right position and represents the reflector, an equation, such as Equation 2, can be formulated to describe Enigma’s encryption steps. It is important to note that due to the plugboard’s symmetry, .

Equation The encryption steps of Enigma I

### Abstractions

The Enigma machine is a complex machine. With numerous components working together in both mechanical and electrical forms, it can prove difficult to predict the outcome of an encryption. This section aims to abstract each component into a logical model to help demonstrate the behaviour and weaknesses of the machine.

Firstly, The diagrams provided (Figures 3-7) are inspired by work from Smart (Smart 2016) and Thimbleby (Thimbleby 2016) and depict rectangles with nodes on each side to represent each letter. The connections between these nodes represent the internal wiring of each component or, in a more logical sense, the letter-to-letter mappings of each component. These diagrams are designed such that the any letter is **input on the right** and the **output on the left** is map(x). Consequently, the left can also represent and the right-hand side represents . For example, Figure 3 shows the plugboard in which if the input on the right is “A” then the output will be map(“A”) which is “D”. The reason for representing input on the right-hand side is to better reflect the workings of the Enigma machine. It is important to note that, in the case of rotors, the function refers to the component with no rotational effects.

The plugboard acts as a simple cypher, which aims to swap two letters. This means that letters connected by a cable on the physical machine are encoded to each other; in absence of a cable, no letter scrambling takes place. As shown in Figure 3, sockets on the machine that connected are represented with a connection between nodes such as A and D. Due to the plugboard symmetry, these diagrams exhibit this ‘X’ shapes.

A diagram of lines and dots

Description automatically generated

Figure A wiring diagram to show a plugboards potential encoding

The reflector acts as a substitution cypher with additional constraints being self-coding and reciprocal coding (See Equation 3). Like other components this can be represented using a wiring diagram such as Figure 4 which demonstrates an example of a reflector. In the diagram, A is shown to be connected to F and vice versa such that any input into the reflector will output the letter at the connected node.

Equation An equation and additional constraints to describe the behaviour of an Enigma Reflector

A diagram of a diagram

Description automatically generated

Figure A wiring diagram to show a potential encoding for a reflector

The rotors of the machine are substitution cyphers with no additional constraints. They take an input letter and produce either the same or a different letter. A rotor can be represented using a wiring diagram, however multiple diagrams are needed to convey the rotor’s rotational effects. As demonstrated in Figure 5, the image on the right depicts the same rotor displayed on the left but with a rotation of one. This leads to the connections between nodes to move upwards whereas the ring setting will cause them to move downwards. This effect is easily seen with the horizontal connection between F on the left image. Once the rotor is rotated the same connection is moved upwards in the diagram to become a horizontal connection between E as shown by the image on the right. This effect can be generalised such that any input letter will be mapped to the input letter . In addition, the output of the letter will be shifted by (See Equation 4). It is clear from these generalisations that if the rotation setting was ten and the ring setting was 10, then there would be no effect on a letter’s encryption as mentioned in 3.2.2.

Equation A function to represent the encoding behaviour of the rotor where x and x` are letters, represents the rotor’s rotation and represents the ring setting.

A diagram of lines and dots

Description automatically generatedA diagram of lines and dots

Description automatically generated

Figure Two wiring diagrams to show a potential rotor encoding. The diagram on the right shows the same rotor as on the left, but with a rotation of one

By abstracting all the electrical and mechanical features of the machine, logical diagrams demonstrating the letter scrambling that takes place in the Enigma machine can be created with greater ease. The diagrams from Figures 3-5 represent each component of the machine and can be combined to create a representation of the entire Enigma machine (See Figures 6-7). These diagrams depict an Enigma machine and demonstrate how the machine works in full. It is important to note that these diagrams only show a single state, upon each key press the rotor wirings will change leading to a potentially different output for the same input.

A diagram of a network

Description automatically generated

Figure A wiring diagram representing a single state of an Enigma I machine. Input is received on the right-hand side before being scrambled by components performing a loop. The electrical signal received back from the plugboard represents the encoded letter. The names of each rotor/reflector do not match the encodings but are given as an example.

A diagram of a network

Description automatically generated

Figure An example of an encryption/decryption taking place in an Enigma I machine. In this case A is encoded to C.

## Design Flaws & Remedies

### Cypher Strength

At a first glance, it may seem like the Enigma machine is unbreakable and indeed the Germans shared this over-confidence (Thimbleby 2016). The Germans became complacent when operating the machine often opting to use the same 3 rotors and neglecting to use more than one reflector (Tang, Lee and Russo 2018). This led to a to a large reduction in the security of communication between operators due to factors that could have been largely avoided (Thimbleby 2016).

Whilst the Enigma machine had a large key space (see Equation 6), it is not the only factor that contributes to a cypher’s strength (How does the Enigma machine work? n.d.). In fact, work from Tang, Lee and Russo (Tang, Lee and Russo 2018) suggests that the Enigma had a theoretical key space of . As suggested by Thimbleby (Thimbleby 2016), by imagining the Enigma machine without its internal components, it can be viewed a substitution cypher with different mappings from keyboard to lamp board. However, this assumes that there are no restrictions with how the mappings can be wired. As mentioned earlier in 3.2, this was not the case for *Enigma I*. The actual number of permutations for the Enigma machine was (See Equation 5). The reduction in permutations by a factor of approximately is due to two features of the machine being self-coding and reciprocal coding (see Equation 3) (Ostwald 2023) (Thimbleby 2016).

Equation Definition of double factorial [CITE]

Equation The number of settings (key space) of Enigma I assuming 10 plugboard cables are used. Ring setting is omitted as it was not changed by the Germans. Based on work from Tang, Lee and Russo (Tang, Lee and Russo 2018).

### Improving the Machine

Clearly, the most obvious solution to improve the *Enigma I* is to increase its key space with more rotors. This can be done by adding an additional slot to the machine to allow for 4 or more rotors to be in use at one time, or even using the usual 3 rotor slots but having a larger collection to choose from. In fact, rotor IV and V were introduced later in 1932 (Ostwald 2023) in order to increase the key space. Other machines that were inspired by Enigma, such as the British Typex, were developed to utilise more than 3 rotors at a time, thus increasing combinatorial complexity (Ostwald 2023). Ostwald’s study (Ostwald 2023) shows numerous additional improvements that either were implemented or could have been implemented to improve the cypher key space.

Thimbleby (Thimbleby 2016) gives examples of multiple circuits that aimed to fix the Enigma’s two main weaknesses mentioned in 3.4.1 demonstrating that the technology at the time period was capable of creating a much stronger cypher. In particular, [FIGURE 6 OF THE PAPER] demonstrates a circuit that only uses 3 rotors omitting both the reflector and the plugboard. By removing these two components, it avoids both self-coding and reciprocal coding by separating encoding and decoding into two distinct functions. For encoding, the current would pass from right to left, and vice versa for decoding. Whilst this model does not include the plugboard, so long as it is only applied once in an encryption, it can still be included and both of the weaknesses avoided. The removal of the reflector does reduce the key space however, this can be mitigated by simply adding another rotor.

The design in [FIGURE 6 OF THE PAPER] was the focus of this project and “EnigmaPlus” as it corrects both weaknesses whilst also exhibiting a similar behaviour to that of *Enigma I*.

TODO : Expand this section – Include logical figure of “EnigmaPlus”

## Related work

Before conducting the research to this product, several similar products were found that simulated the Enigma machine. This project and much of the work done around *Enigma I*were inspired by the similar products. In addition to this, the paper written by Thimbleby (Thimbleby 2016) gave direct inspiration into the creation of “EnigmaPlus”.

“Enigma Machine Emulator” [CITE] is a webpage consisting of a short description about the Enigma machine as well as offering an interactive emulator for the Enigma machine. The emulator follows a skeuomorphic design aiming to present a flat image that resembles the real machine.

“The Enigma Machine” [CITE] presents a sleeker UI allowing the user to configure the machine as well as encode/decode their messages. The design of this webpage strays from the original look and feel of the machine, offering a new and simpler way to interact with it. Much of the design points for my project were inspired by this page.

“Virtual Enigma” [CITE] offers extremely interactive 3D simulation of the Enigma machine. This simulation allows full control of the machine down to each minute detail. Users can open different parts of the machine with their mouse and drag and drop rotors into place on a virtual model of the machine. The level of detail in this simulation offers an authentic experience for the user and is highly recommended for those who would like to experience the machine as a whole.

“The Enigma Machine” [CITE] is the only similar product that I came across that offers a form of visualization to the inner workings of the machine. It represents the Enigma’s encodings as a circular wiring diagram similar to the ones shown in previous sections (Figure 3-7). This particular page was the inspiration of the creation of my visualiser to provide more insight into the machine.

# Design & Implementation

## Tools and Technologies

Description and list of tools used within this project.

* Java to create the application and the model.
* JavaFX – graphics package used to create the GUI + Visualizations.
* GitHub – version control and development tasks
* Maven – build project across multiple platforms.
* XML – Custom component definitions
* Gluon Scene Builder – Used for UI building and FXML creation.

## Enigma Model Design

Talk about the idea of the package, this would be a good place for UML diagrams and a description of how this model is going to work.

### Keyboard & Lamp board

Explanation of how this part does not really need to be modelled, and instead can be represented as input and output.

### Reflector

Description of how this will be modelled.

### Rotors

Description of how this will be modelled.

### Enigma

Description of how this will be modelled.

## Design of the Application

Explain how the application will work, show diagrams in order to show how the interfaces will interact with the model.

### Command Line Interface

A fairly short section, just explain how the interface works and what information will be shown.

### GUI

Larger section explaining the various design stages of the GUI, as well as explaining the MVC implementation. Important to talk about design choices in this section as this is the bulk of the project.

### Visualization

A second part to the GUI, explain the design choices and implementation as well as a section “interpreting the diagram.”

# Results

# Evaluation

## Model Evaluations

* Test Coverage
* Actual German messages
* Permutations compared with improved model.

## GUI Evaluation

* Usability?
* Cross-platform?

# Conclusion

# References

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[Figure 3 Wiring diagram to show a plugboard's potential encoding for a reduced alphabet size e.g. A encodes to D and vice versa. Notice the plugboard wiring diagrams tend to create X shapes. 8](#_Toc158033856)

[Figure 4 Wiring diagram to show an example reflector encoding for a reduced alphabet size e.g. A encodes to F and vice versa. 9](#_Toc158033857)

[Figure 5 Two Wiring diagrams to show an example rotor encoding. The diagram on the right shows the same rotor as on the left, but with a rotation of one. The left diagram shows F encoded to F and the diagram on the right shows E encoded to E. The “wire” is still the same, but the rotation of the rotor will lead to an F input/output, interpreted as E input/output. 10](#_Toc158033858)

[Figure 6 A wiring diagram representing a single state of an Enigma I machine. Input is received on the right-hand side before being scrambled by components in the following order: plugboard, rotor III, rotor II, rotor I, reflector UKW-B, rotor I, rotor II, rotor III, plugboard. The electrical signal received back from the plugboard represents the encoded letter. The names of each rotor/reflector do not match the encodings but are given as an example. 11](#_Toc158033859)

[Figure 7 An example of an encryption/decryption taking place in an Enigma I machine. In this case A is encoded to C. 11](#_Toc158033860)

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[Equation 4 A function to represent the encoding behaviour of the rotor where x and x` are letters, represents the rotor’s rotation and represents the ring setting. The map function returns the input letter’s mapping as if no rotational effects have taken place e.g. in Figure 5, 11](#_Toc158213187)

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