# Sequencing Legal DNA NLP for Law and Political Economy

10. Causal Inference with Text Data

# Research Design

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  - provide credible tests of social-science hypotheses
  - estimate policy parameters to inform policymakers

# **Objectives**

- 1. What is the research question?
- 2. Corpus and Data
- 3. Research design for estimating causal parameters:
  - ▶ What are we trying to estimate?
  - ► What identification strategy / research design will get us there?

# **Objectives**

- 1. What is the research question?
- 2. Corpus and Data
- 3. Research design for estimating causal parameters:
  - ► What are we trying to estimate?
  - What identification strategy / research design will get us there?
- 4. Empirical analysis
  - Show evidence that identification assumptions hold.
  - Produce causal estimates with confidence intervals.
  - Answer the research question.

## Outline

#### The Empirical Problem

#### Adjusting for Confounders without Instruments

Adjustment for Non-Linear Confounding with Double ML Matching / Synthetic Control Adjusting for Text Confounders with BERT Embeddings

Decounfounding with Multiple Treatments

#### Instrumental Variables

Ash, and Morelli, Vannoni (2020): More Laws, More Growth? Galletta-Ash-Chen 2020: Causal Effect of Judicial Sentiment

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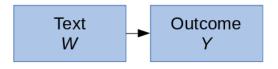
## Learning Treatments from Text

# Setup

▶ *W*, vectorized text

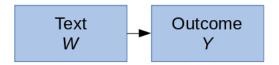
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- ▶ *Y*, outcome from the text
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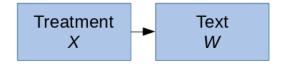


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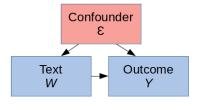
- ▶ W, vectorized text
- Y, outcome from the text
  - e.g., the facts of the case W determine the verdict Y



- X, treatment affecting the text
  - ightharpoonup e.g., judge political preferences X affect the written opinion W

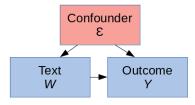


# Empirical Problem: Confounders $(\epsilon)$

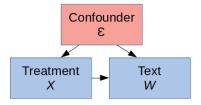


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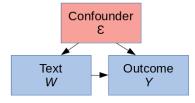


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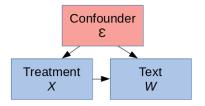


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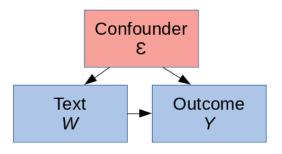


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- $\blacktriangleright$  judge writes opinion W based on characteristics  $\epsilon$  as well as her ideology X.
- ► Key point: a variable is a confounder only if it affects both sides of a regression (both W & Y, or both X & W).

#### **Econometrics**



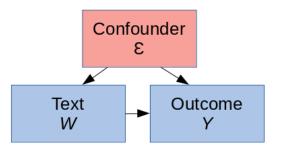
We would like to learn

$$f(W;\theta) = \mathbb{E}\{Y|W\}$$

the conditional expectation function for y, where  $\theta$  represents the true parameter vector.

•  $f(\cdot)$  and  $\theta$  describe the arrow from W to Y.

#### **Econometrics**



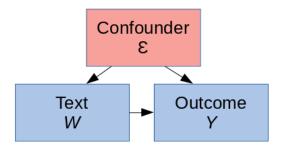
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- $f(\cdot)$  and  $\theta$  describe the arrow from W to Y.
- ▶ If we assume linearity and run OLS, the estimates for  $\hat{\theta}$  are biased because of the confounder.

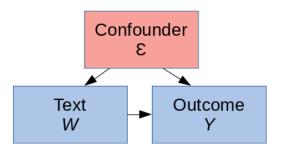
# Econometrics + Machine Learning



$$f(W;\theta) = \mathbb{E}\{Y|W\}$$

- We could take a machine learning (ML) approach and learn a nonlinear approximation  $\hat{f}(W;\theta)$  to predict Y in held-out data.
  - If we obtained more documents  $W_i$  for new individual i, we could form a good prediction about the associated  $Y_i$ .

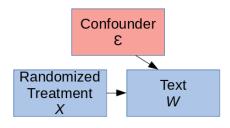
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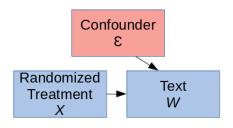
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  - If we obtained more documents  $W_i$  for new individual i, we could form a good prediction about the associated  $Y_i$ .
- **b** But the ML estimates  $\hat{\theta}$  do *not* have a causal interpretation.
  - ▶ i.e., if the case facts W were experimentally changed,  $\hat{\theta}$  would not provide a counterfactual prediction about how the associated outcome Y would change.

# Randomized Experiments



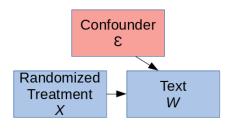
- ► Lab/field experiments provide a gold standard for obtaining causal estimates.
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- ► E.g.:
  - ▶ randomly assign judges from  $X \in \{Party 1, Party 2\}$  to cases.
  - The causal effect is the average difference in their written decisions,  $\mathbb{E}\{W|X=1\}-\mathbb{E}\{W|X=2\}.$

# Empirical Economics and Research Design

- ► In the presence of unobserved confounders, estimating causal parameters presents a significant challenge.
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- ► In the presence of unobserved confounders, estimating causal parameters presents a significant challenge.
  - especially in observational studies where we can't run experiments.
- ► Modern empirical economics puts an emphasis on obtaining causal estimates using **empirical strategies** or **research designs**.
  - this is why Google/Amazon/etc. hire many PhD economists.

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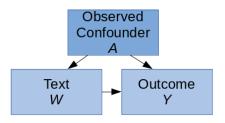
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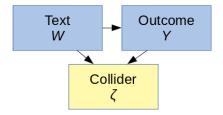
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## Confounder is Observed



- ▶ If confounder *A* is observed, problem solved:
  - include A in your model, or residualize W and Y on A before estimation.
- ▶ Often a strong assumption; ML can help if A is high-dimensional (more on this later).

#### Colliders or "Bad Controls"



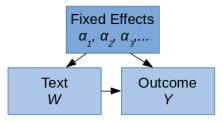
- $\triangleright$   $\zeta$ , colliders (or as most economists would say, "bad controls"), are a third variable that is affected by both your treatment and your outcome.
  - ightharpoonup For example, let  $\zeta$  be the length of the prison sentence, which is affected by the case facts W and the verdict Y.
- ▶ Don't control for colliders! It introduces bias. (also called "conditioning on an outcome".)

## **Fixed Effects**

- ▶ What if all confounders are at the group level?
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#### **Fixed Effects**

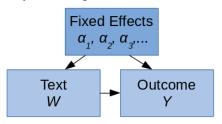
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- in the data, add a dummy variable equaling one for i's cases.
- ▶ Equivalently (almost), can center (de-mean) predictors *W* and outcome *Y* by defendant.
  - With multiple fixed effects (e.g., defendant, judge, and year), can **residualize**: project predictors W and outcome Y onto matrix of dummy variables, and take residuals  $\tilde{W} = W \hat{W}$  and  $\tilde{Y} = Y \hat{Y}$  for use in model training.

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- ► Fixed-effects transformations don't have the same interpretation with non-linear models. Not enough research on this yet.

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# Double/Debiased ML

Chernozhukov, Chetverikov, Duflo, Hansen, Demirer, and Newey (2017)

## Double/Debiased ML

Chernozhukov, Chetverikov, Duflo, Hansen, Demirer, and Newey (2017)

$$Y = \theta T + g(A) + \epsilon$$

- low-dimensional treatment T, high-dimensional set of (observed) confounders A:  $T = m(A) + \eta$ .
- **Decays** Because of confounders, forming a prediction  $\hat{Y} = \hat{\theta}T + \hat{g}(A)$  will be biased.
  - this is the "observed confounders" case, but covariates are high-dimensional and non-linearly related to outcome and treatment.

## Double ML method

Chernozhukov, Chetverikov, Duflo, Hansen, Demirer, and Newey (2017)

1. Predict Y given A:  $\hat{Y}(A)$ , and T given A:  $\hat{T}(A)$ , using any ML method

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- Sample split:
  - ▶ Run (1) on sample a, then run (2) and (3) on sample b, to estimate  $\hat{\theta}_a$
  - ▶ and vice versa (run (1) on sample b, and (2/3) on sample a), to learn a second estimate for  $\hat{\theta}_b$ .
  - average them to get a more efficient estimator:  $\hat{\theta} = \frac{1}{2}(\hat{\theta}_a + \hat{\theta}_b)$ .

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- Note: like double ML, also equivalent to fixed effects or controlling for many observed confounders.
  - but powered up with ML
- Can imagine the text documents associated with individual or groups as a set of covariates for matching
  - e.g., text features from the criminal history of each defendant.

# Adjusting for confounding with text matching

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- Lots of governments try to control online information
- But, censoring the whole internet is hard (# of bloggers >> # of censors)
- Limited external enforcement → self-policing



- ▶ Construct a corpus of chinese blog posts, some of which are censored.
  - ▶ 593 bloggers, 150,000 posts, 6 months

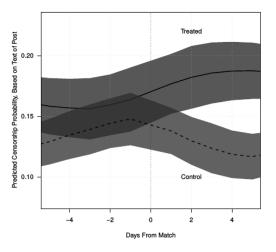
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- Outcome:
  - Using text of subsequent posts, measure how likely they are to be censored (how censorable)
  - Can see whether censorship has a deterrence or backlash effect.

# Censorship has a backlash effect

Roberts, Stewart, and Nielsen (2018)



▶ Bloggers who are censored respond with more censorable content.

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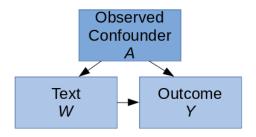
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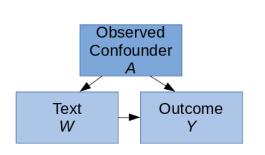
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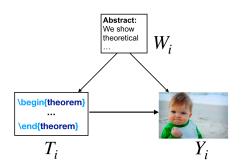
## Sridhar, Veitch, and Blei (2019)



This paper analyzes the problem of the effect of text features on outcomes, where the unobserved confounders are other features of the document.

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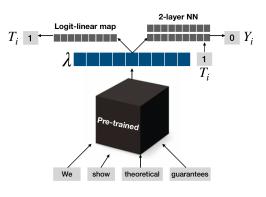




- This paper analyzes the problem of the For example, the effect of putting a effect of text features on outcomes. where the unobserved confounders are other features of the document.
- theorem in your paper on acceptance to a conference/journal.
- This paper is another example of controlling for observed confounds, but in high dimensions.

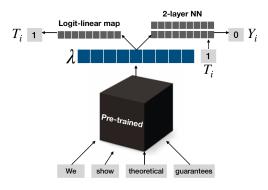
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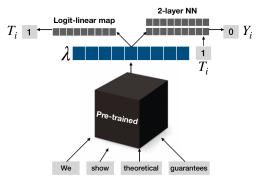
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- ▶ Start with pre-trained BERT embeddings.
- fine-tune them on an additional multitask objective.
- ▶ 1) predict propensity score (probability of treatment given other text features.
- 2) predict outcomes conditional on treatment.

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- ▶ Start with pre-trained BERT embeddings.
- fine-tune them on an additional multitask objective.
- ▶ 1) predict propensity score (probability of treatment given other text features.
- 2) predict outcomes conditional on treatment.
- the resulting embeddings serve as a sufficient statistic for the unobserved confounders.

#### Veitch et al

- ▶ The applications in the paper are not that interesting/convincing.
- ▶ Nice opportunity for an Assignment 3 replication exercise.

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- ▶ In particular, unbiased causal inference is possible if confounders are shared across multiple treatments.
  - ▶ Wang and Blei (2018) provide an ML method to construct a "deconfounder" from the predictors and allow valid inference.

#### How does the deconfounder work?

- ▶ Assume multiple treatments  $A_1, ..., A_m$
- Assume there is a latent factor Z that, when taken out from the  $\vec{A}$ , renders them conditionally independent.

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- ▶ Assume multiple treatments  $A_1, ..., A_m$
- Assume there is a latent factor Z that, when taken out from the  $\vec{A}$ , renders them conditionally independent.
  - ▶ If we can learn Z, this will deconfound the treatments.

### Argument for Deconfounder Z

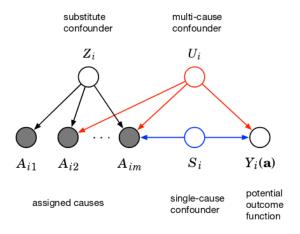


Figure 1: A graphical model argument for the deconfounder. The punchline is that if  $Z_i$  renders the  $A_{ij}$ 's conditionally independent then there cannot be a multi-cause confounder. The proof is by contradiction. Assume conditional independence holds,  $p(a_{i1},...,a_{im}|z_i) = \prod_j p(a_{ij}|z_i)$ ; if there exists a multi-cause confounder  $U_i$  (red) then, by d-separation, conditional independence cannot hold (Pearl, 1988). Note we cannot rule out the single-cause confounder  $S_i$  (blue).

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- Learning the deconfounder is the same as learning any factor model:
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- ➤ To check whether your deconfounder is working, check whether your factor model is capturing distribution of treatment assignment:
  - ▶ fit the factor model on training data; it should be able to predict treatment assignment in the test data.
  - the paper provides a formal test statistic.

#### Best Film Actors: Causal Evidence

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  - Owen Wilson, Nick Cage, Cate Blanchett, Antonio Banderes.
- Most under-valued actors:
  - Stanley Tucci, Willem Dafoe, Susan Sarandon, Ben Affleck, Christopher Walken.

- ▶ This paper also has a not very interesting application.
- ► Another good replication exercise!

#### Outline

#### The Empirical Problem

#### Adjusting for Confounders without Instruments

Adjustment for Non-Linear Confounding with Double MI Matching / Synthetic Control Adjusting for Text Confounders with BERT Embeddings Decounfounding with Multiple Treatments

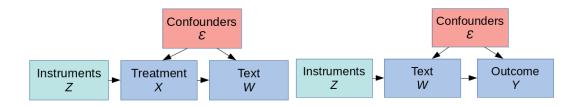
#### Instrumental Variables

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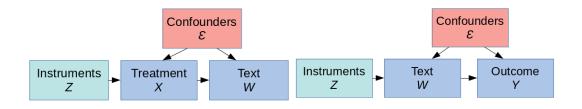
Learning Treatments from Text

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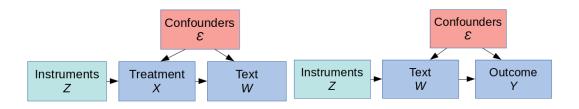
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- Second stage:
  - ▶ Predict  $W(\hat{X}(Z))$  or  $Y(\hat{W}(Z))$

### Random Assignment of Judges $\rightarrow Z$

- ▶ Let Z be a high-dimensional set of characteristics of judges, e.g. political party, cohort, writing style.
- ▶ Let W be the text features of the current case.
- ▶ Let Y be the outcome, e.g., whether the case is appealed.

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- Instrumental variables system:

$$W = g(Z), Y = f(W)$$

- ▶ form ML predictions of  $\hat{g}(\cdot)$
- use those predictions  $\hat{W}$  in predicting  $\hat{f}(\cdot)$

# Regression Discontinuity Design (RDD)

- ▶ RDD's are a special type of IV that exploit threshold rules, where individuals are assigned to treatment if a continuous variable is above some discrete cutoff.
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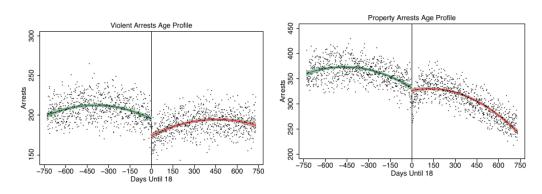
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  - ▶ Income, effect of barely being eligible for poverty subsidy
  - Votes in an election, effect of barely getting a Republican (relative to a Democrat)

#### Increased Penalties at $18 \rightarrow Less$ Crime



Lovett and Zue (2018). California data.

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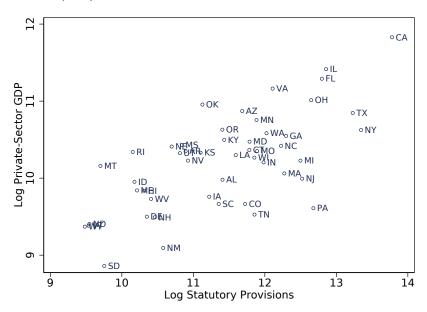
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#### Learning Treatments from Text

#### Laws ↔ Growth

Ash, Morelli, and Vannoni (2020)



$$\Delta \log(Y_{st}) = \rho \Delta \log(W_{st}) + \alpha_{st} + X'_{st}\beta + \varepsilon_{st}$$

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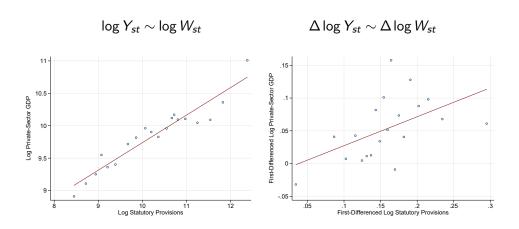
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- $\triangleright$   $\rho$ , causal effect of legislation on growth

# OLS Relationship between Output $Y_{st}$ and Detail $W_{st}$



Binned scatterplots for (log) provisions (horizontal axis) and (log) private sector GDP (vertical axis), residualized on year fixed effects. Left panel: cross-sectional relationship. Right panel: first differences.

▶ We apply latent dirichlet allocation (LDA) to learn topics from text (Blei 2003). Here are 8 most frequent (out of 25):



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- Let  $S_{st}$  be the set of statutes in state s time t. Each statute  $i \in S_{st}$  has a provision count  $w_i$  and a distribution over topics  $v_{il}$ ,  $\forall l \in \{1,...,25\}$ .
- Define legislative flows on topic I in state s during t:

$$W_{slt} = \sum_{i \in S_{st}} v_{il} w_i$$

#### Shift-Share Instruments

- ► Classic application (Bartik 1994):
  - ▶ Instrument for local employment growth with interaction between pre-treatment local sectoral shares and national growth rates by sector.
  - ▶ Isolates changes in employment due to local demand shocks.

#### Shift-Share Instruments

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- Other applications:
  - Market size and drug innovation (Acemoglu and Linn, QJE 2004).
  - China shock (Autor, Dorn, and Hanson, AER 2013).
  - Democracy does cause growth (Acemoglu et al, JPE 2019).

### Constructing Instrument for Legislative Detail

- ► Define:
  - ▶  $W_{slt}$ , number of provisions on legislative topic  $l \in 1,...,25$ } in state  $s \in \{1,...,50\}$  at biennium t.
  - $\triangleright$   $W_{st}$ , total number of legislative provisions in state s at t.
  - $\frac{W_{s/0}}{W_{s0}}$ , topic shares of legislation for first biennium of data (1963-1964).

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- ▶ The instrument:

$$\underbrace{Z_{st}}_{\text{instrument}} = \underbrace{\sum_{l=1}^{25} \frac{W_{sl0}}{W_{s0}}}_{\text{shares}} \underbrace{\sum_{r \neq s} \frac{1}{49} \frac{\Delta W_{rlt}}{W_{rlt-1}}}_{\text{shifts}}$$

- leave-one-out average proportional legislative topic growth in other states, multiplied by this state's pre-treatment topic share.
- standardized to mean zero and variance one.

### First Stage

$$\Delta \log(W_{st}) = \psi Z_{st} + \alpha_{st} + X'_{st}\beta + \eta_{st}$$

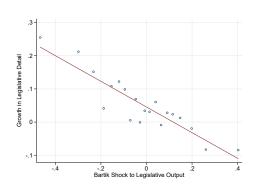
- $V_{st}$ , legal detail in state s at biennium t
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First-Stage Binscatter



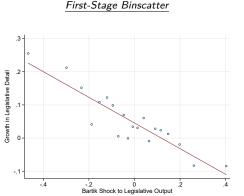
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- $\hat{\psi}$  is statistically significant (p = .003).
- ▶ Robust F-stat in baseline = 46.57.
- $ightharpoonup \hat{\psi}$  is negative:
  - different from standard Bartik.
  - when state has initially low detail on topic, it is more likely to increase detail in response to national trends.
  - e.g., state can borrow legal language at low cost.

1. Assume that **pre-treatment shares are exogenous** (Goldsmith-Pinkham, Sorkin, Swift, 2018; Jaeger, Ruist, Stuhler, 2018).

$$\mathbb{E}\{(\underbrace{\sum_{l=1}^{25}\frac{W_{sl0}}{W_{s0}}})\cdot\epsilon_{st}\}=0$$

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- with state/time fixed effects and state trends (as in our context), global shocks are allowed to be correlated with exposure-weighted averages of unobservables that linearly vary within state (Borusyak & Jaravel, 2017).

### Assessing instrument validity

- ► Following Borusyak & Jaravel (2017) and Adao, Kolesar, Morales (QJE 2019):
  - Instrument is driven by a majority of topics.
  - Economic growth is uncorrelated with future values of the instrument.
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- ► Following Goldsmith-Pinkham, Sorkin, Swift (2018) and Jaeger, Ruist, Stuhler (2018):
  - pre-treatment topic shares uncorrelated with pre-treatment state characteristics.
  - pre-treatment topic shares are uncorrelated with economic growth.

#### Effect of Legislative Detail on Economic Growth

$\Delta \text{ Log } W_{st}$ 0.015* -0.026** 0.071** 0.075** 0. (0.0062) (0.0085) (0.022) (0.022)	(5) (6) (7) (8) (9) 2SLS 2SLS 2SLS 2SLS 2SLS 0.066** 0.095** 0.063** 0.07** 0.078** (0.021) (0.028) (0.021) (0.022) (0.023) 812 846 846 846 796
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01- 046 040 046 046	812 846 846 846 796
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Obs 846 848 846 846	
First-Stage <i>F</i> 46.57 46.47 4	48.49 47.99 45.25 46.26 46.86
State FE X X X X	x x x x x
Time FE X X X X	$x \qquad x \qquad x \qquad x \qquad x$
State Trends X	
Pre $X  imes lpha_t$	X
Pop/Income	X
Govt Expevd	X
Politics	X
Lagged DV	X

Notes: Column 1 shows the results for the OLS regression model. Column 2 shows the results for the reduced form. Column 3 gives the baseline 2SLS estimate and Column 4 adds state-specific linear trends. Column 5 adds a set of covariates (share child and old population, the fraction urban population, and the share of foreign born population) measured in the pre-treatment period interacted with biennium fixed effects. Column 6,7 and 8 add a series of time-varying covariates, respectively: population and income variables, government expenditure variables and political party control variable. Column 9 adds the lagged dependent variable. All specifications include state and biennium fixed effect; standard errors clustered by state.

\*\*P>.01: \*P>.40: +P>.1.

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- Which industries are growing?
  - effect concentrated in construction, manufacturing, and wholesale

#### Other Economic Performance Outcomes

	(1)	(2)	(3)	(4)	(5)
	Log Pop	Log Income	Log Firms	Log Profits	Log Emp
$\Delta$ Log $W_{st}$	0.00007	0.0214*	0.00531	0.128**	0.0744*
	(0.00478)	(0.00904)	(0.0110)	(0.0429)	(0.0328)
Observations	846	846	819	548	819
First Stage F-stat	46.57	46.57	44.02	46.09	44.02
State FE	Х	Х	Х	Х	Х
Time FE	X	Χ	X	Χ	X

Notes: All outcomes in logs. Column 1 uses population as dependent variables. Column 2 uses personal income. Column 3 uses the number of companies. Column 4 and Column 5 use respectively firm profits and employment. All specifications include state and biennium fixed effect, as well as standard errors clustered by state. \*\*p<.01; \*p<.05; +p<.1.

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Learning Treatments from Text

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- but they could be correlated without indicating causation:
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- ➤ Solution: instrumental variables using random assignment of judges, following Belloni et al (2012).
- ▶ We have access to 61 variables that refer to judges' biographical characteristics (age, geographic history, education, occupational history, governmental positions, military service, religion, race, gender, political affiliations, etc)
  - Let  $J_i$  = average characteristics for the three judges assigned to case i.
- Let  $W_i^k$  be the average similarity of case i to target k. Then, the vector of judge characteristics randomly assigned to target k in circuit c during year t is

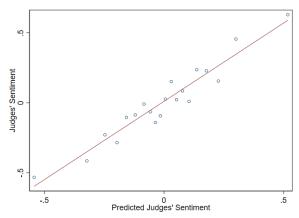
$$\mathbf{J}_{ckt} = \frac{1}{|C_{ct}|} \sum_{i \in C_{ct}} W_i^k \mathbf{J}_i, \tag{1}$$

## The many weak instruments problem

- a well-known limitation of IV is that the instruments have to be sufficiently strong (that is, correlated with the treatment), or else the 2SLS estimator is biased.
- ▶ Recent papers in econometrics have used lasso to select instruments (Belloni et al 2012) or used ridge regression with cross-validated predictions (Hansen and Kozbur 2014).

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- $ightharpoonup Z_{ckt}$  = the cross-validated prediction for  $S_{ckt}$  using the randomly assigned judge characteristics:



## 2SLS System

► The first stage is

$$S_{ckt} = \gamma_k + \gamma_{ct} + \gamma_Z Z_{ckt} + \eta_{ckt}$$

- $ightharpoonup \gamma_{ck} = \text{dummy variables (fixed effects) for each circuit-year}$
- $ightharpoonup \gamma_k = \text{dummy variables (fixed effects) for each target.}$
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- ► The second stage is

$$Y_{ckt} = \alpha_k + \alpha_{ct} + \beta S_{ckt} + \epsilon_{ckt}$$
 (2)

 $Y_{ckt}$  = thermometer response from ANES in circuit c toward taret k at t.

#### Results

Table 1: Results

	OLS			2SLS		
	(1)	(2)	(3)	(4)	(5)	(6)
Judges' sentiment	-0.138***	-0.137***	-0.135***	-0.139***	-0.167***	-0.122**
	(0.017)	(0.017)	(0.017)	(0.052)	(0.051)	(0.058)
Year FE	Y	Y	Y	Y	Y	Y
Circuit FE	Y	Y	Y	Y	Y	Y
Year FE X Circuit FE	N	Y	Y	N	Y	Y
Target FE	N	N	Y	N	N	Y
F-stat				127.286	124.573	101.201
N observations	2678	2678	2678	2678	2678	2678

Notes: The dependent variable is the thermometer score for all respondents in the ANES by circuit-target-year. Judges' sentiment is the text-based average sentiment by circuit-target-year. All variables are centered and standardized by target. Standard errors clustered by circuit-year in parenthesis. \* p < 0.1, \*\* p < 0.05 and \*\*\* p < 0.01.

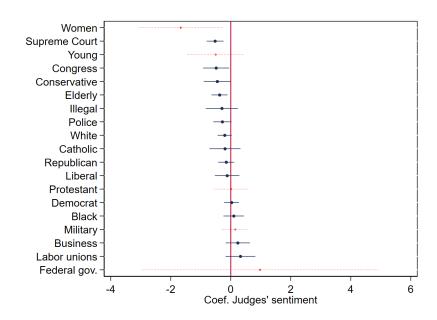
#### Results

Table 2: Results – Leads/Lags of Dep. variable

	2SLS					
	2 years before (1)	Same year (2)	2 years after (3)	4 years after (4)	6 years after (5)	
Judges' sentiment	-0.113 (0.083)	-0.122** (0.058)	-0.215** (0.085)	-0.094 (0.092)	-0.051 (0.189)	
Year FE	Y	Y	Y	Y	Y	
Circuit FE	Y	Y	Y	Y	Y	
Year FE X Circuit FE	Y	Y	Y	Y	Y	
Target FE	Y	Y	Y	Y	Y	
F-stat	65.546	101.201	77.585	46.285	29.677	
N observations	1687	2678	1684	1322	1004	

Notes: The dependent variables are the leads and lags of the thermometer score for all respondents in the ANES by circuit-target-year as reported in columns head. Judges' sentiment is the text-based average sentiment by circuit-target-year. All variables are centered and standardized by target. Standard errors clustered by circuit-year in parenthesis. \* p < 0.1, \*\* p < 0.05 and \*\*\* p < 0.01.

## Effect by group



#### Outline

#### The Empirical Problem

#### Adjusting for Confounders without Instruments

Adjustment for Non-Linear Confounding with Double MI Matching / Synthetic Control Adjusting for Text Confounders with BERT Embeddings Decounfounding with Multiple Treatments

#### Instrumental Variables

Ash, and Morelli, Vannoni (2020): More Laws, More Growth? Galletta-Ash-Chen 2020: Causal Effect of Judicial Sentiment

#### Deep IV (Hartford et al 2017)

Deep IV for Influence of Legal Texts (Ash and Nikolaus 2020)

Learning Treatments from Text

# Deep Instrumental Variables

## Deep Instrumental Variables

- ▶ Deep IV: A Flexible Approach for Counterfactual Prediction
  - use ML algorithms to extend 2SLS to high-dimensional settings

## Deep Instrumental Variables

Hartford, Lewis, Leyton-Brown, and Taddy (2017)

- ▶ Deep IV: A Flexible Approach for Counterfactual Prediction
  - use ML algorithms to extend 2SLS to high-dimensional settings
- Causal effect of interest:

$$f(w;\theta) = \mathbb{E}\{y|w\}$$

▶ Predictors are a function of some instruments:

$$w \sim g(w|z)$$

## First stage

- Deep IV allows arbitrarily high-dimensional w and z.
- In first stage, approximate  $g(w|\gamma(z))$ , the distribution of w:
  - ▶ assume that  $g(\cdot)$  is a mixture density network (a mixture of gaussian distributions) where the parameter vector  $\gamma(\cdot)$  includes the weights, means, and variances (Bishop 2006).

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  - $ightharpoonup \gamma(z)$  is any function of the instruments can use an MLP, for example.
  - $g(\cdot)$  has to be a parametrized distribution because Deep IV requires that the distribution be integrated in the second stage.

## Second Stage

Hartford, Lewis, Leyton-Brown, and Taddy (2017)

In second stage, want to predict  $\hat{y}(w;\theta)$ , where  $\hat{y}(w;\theta)$  should be a flexibly specified DNN to allow for non-linearities and interactions.

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- In second stage, want to predict  $\hat{y}(w;\theta)$ , where  $\hat{y}(w;\theta)$  should be a flexibly specified DNN to allow for non-linearities and interactions.
- ▶ Hartford et al (2017) show that causal estimates for  $\theta$  are obtained by minimized the conditional loss function

$$\mathcal{L}(\theta) = \sum_{i} [y_i - \int \hat{y}(w; \theta) d\hat{g}(w|\gamma(z_i))]^2$$

▶ this is true y minus predicted  $\hat{y}$ , but  $\hat{y}$  is conditioned on the instrument-predicted treatment distribution  $\hat{g}$ .

## Second Stage Loss Approximation

Hartford, Lewis, Leyton-Brown, and Taddy (2017)

▶ The integral in  $\mathcal{L}(\theta)$  is approximated by

$$\int \hat{y}(w;\theta)d\hat{g}(w|\gamma(z_i)) \approx \frac{1}{m} \sum_{i}^{m} \hat{y}(\tilde{w}(z_i);\theta)$$

where you make m draws from the estimated treatment distribution given  $z_i$  (the instruments for observation i).

▶ Like 2SLS, a prediction for the endogenous regressor with the instruments is used during second-stage estimation.

### What about relevance/inference?

- Both stages of Deep IV can be validated by out-of-sample prediction in held-out data
  - ▶ in the first stage, this guards against weak-instruments bias in the same way that first-stage F-statistics thresholds do for 2SLS

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# Dataset Overview (n = 71'475 cases, 382 judges)

Outcome  $Y = \log$  citations by future judges.

Treatments X = features of written majority opinions:

- 1. NLP preprocessing of all documents using spaCy
- 2. Training of a word embedding model using word2vec
- 3. Clustering of word embeddings into 200 clusters that are interpreted as topics and arguments of the cases
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Instruments Z = Judge writing style

► The average of the cluster frequencies of all other cases that the judges on the case panel were assigned to.

## Cluster Frequencies

Table: (Hypothetical) Example of Cluster Frequencies

Cluster ID	Words	Freq. Case 1	 Freq. Case 71475
1	word2, word17, word83,	0.00001	 0.00000
2	word5, word89, word1005,	0.00000	 0.00020
		•••	 
199	word19, word33, word100,	0.00023	 0.00190
200	word14, word16, word64,	0.05010	 0.00000

▶ The cluster frequencies of a case sum to 1

## Leveraging Random Assignment

- ► Empirical strategy relies on random assignment of circuit judges, which occurs within the set of judges working on a single court during a year
  - $\triangleright$  To isolate this endogenous variation, we center Y, X, and Z by court-year
- randomization has been verified in previous papers, but we still need to check that it holds in our context.

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- ▶ To analyze features, we use a permutation importance approach to identify text features that move  $\hat{Y}$  the most when scrambled.

# Using Causal Predictions to Analyse the Quality of Judges

- Previous work analyzed the quality of judges using citations directly
- Deep IV provides a means to analyse judge quality based on text-based citation predictions

Court	Judge	Text Quality Rank	Predicted Cites (Deep IV)
5th	Stewart	1	0.3133
5th	Demoss	2	0.2656
5th	Wiener	3	0.2403
5th	Benavides	4	0.1910
5th	Clement	5	0.1817
			***
3rd	Hutchinson	27	0.0861
7th	Posner	28	0.0831
4th	Chapman	29	0.0784
2nd	Harlan	30	0.0773
7th	Easterbrook	31	0.0763
		382	

## Causal Importance of Text Features

- We analyzed the permutation importance of the treatment features (word clusters / topics):
  - higher impact of procedural language on common-law
  - lower impact of case-specific language (e.g. fraud, corporate accounting, debt)
  - some legal concepts turn out not to matter for legal impact (forensic evidence, fact finder / jury)
  - sanity check: "junk" topics and topics containing typo words rank at the bottom of the impact list

Top 4 Cluster Words	Topic	Deep IV Importance	Deep OLS Importance	Rank (D-IV)	Rank (D-OLS)
grant, denying, denial, adjudged	grant/deny	0.0882	0.1631	1	1
adjourn, adjournment, reschedule, continuance	schedule	0.0481	0.0001	3	125
certioari, rehearing, rehear, cert	certioari	0.0365	0.0191	6	20
		***	***		
corrupt, defraud, bogus, fraudulent	fraud	0.0002	0.0005	181	145
Cir1991, cir1985, Cir1996, Cir1987	junk	0.0001	0.0022	194	73
finder, trier, factfinder, inference	jury	0.0000	0.0002	199	178

#### Direction of Treatment Effects

- Use a bootstrap approach to sample from  $\hat{X} \sim F(x|\gamma(c,z;\theta_1))$
- ▶ Fit OLS using sampled treatment  $(Y \sim \hat{X})$ :

Top 4 Cluster Words	Deep IV Effect	Deep IV Rank	Deep OLS Rank
complicate, depend, crucial, illustrate	0.091	1	3
implausible, problematic, exaggeration, skeptical	0.059	2	105
reverse, affirm, vacate, reversed	0.043	3	192
argument, contention, assertion, suggestion	-0.045	195	199
reconsider, reconsideration, remand, modify	-0.060	199	185
4th, 9th, see, 8th (amendments)	-0.070	200	170

- ightharpoonup nuanced legal reasoning ightarrow increased citations
- ▶ procedural aspects → decreased citations

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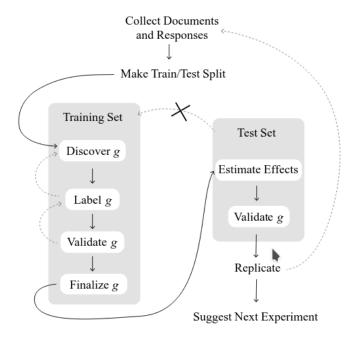
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#### Learning Treatments from Text

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- ▶ Text outcome, non-text treatment:  $W_i = g(X_i; \theta)$
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- ▶ Text outcome, non-text treatment:  $W_i = g(X_i; \theta)$
- ► Text treatment, non-text outcome:  $Y_i = f(W_i; \theta)$
- Learn functional form for  $g(\cdot)$  in half the data, and then run causal inference in the other half.



Egami, Fong, Grimmer, Roberts, and Stewart (2018)

# Sample Split

- ► The insight/emphasis of Egami et al (2018):
  - be the codebook function  $g(\cdot)$  can take any form (you can use any featurization approach you like)
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# Sample Split

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  - but the codebook function  $g(\cdot)$  can take any form (you can use any featurization approach you like)
  - you get valid inference as long as its done in held-out data.
- ► For example, can assume treatments are represented by frequencies over predictive N-grams, by LDA topics, or document embedding clusters.

Fong and Grimmer (2016)

▶ What biographical facts affect voter evaluations?

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- Could run a survey experiment:
  - Document 1: He earned his Juris Doctor in 1997 from Yale Law School, where he operated free legal clinics for low-income residents of New Haven, Connecticut.
  - Document 2: He served in South Vietnam from 1970 to 1971 during the Vietnam War in the Army Rangers' 75th Ranger Regiment, attached to the 173rd Airborne Brigade. He participated in 24 helicopter assaults...

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- But hard to generalize what features drive differences.

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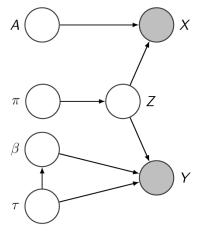
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- 5. In test set: infer treatments and measure their effects

# Supervised Indian Buffet Process

Fong and Grimmer (2016)

# The Supervised Indian Buffet Process (sIBP)



Text and response depend on latent treatments

- Treatment assignment

$$z_{i,k} \sim \operatorname{Bernoulli}(\pi_k)$$
  $\pi_k \sim \prod_{m=1}^k \eta_m$   $\eta_m \sim \operatorname{Beta}(\alpha, 1)$ 

- Document Creation:

$$\mathbf{X}_i \sim \mathsf{MVN}(\mathbf{Z}_i \mathbf{A}, \sigma_X^2 I_D)$$
  
 $\mathbf{A}_k \sim \mathsf{MVN}(\mathbf{0}, \sigma_A^2 I_D)$ 

- Response:

$$Y_i \sim \mathsf{MVN}(Z_i\beta, \tau^{-1})$$
  
 $\beta | \tau \sim \mathsf{MVN}(\mathbf{0}, \tau^{-1}I_K)$   
 $\tau \sim \mathsf{Gamma}(a, b)$ 

### Candidate Biographies on Wikipedia

Fong and Grimmer (2016)

Schumacher was born and raised in the Highlandtown neighborhood of East Baltimore, the eldest of the three daughters of Christine Eleanor (nee Kutz) and William Schumacher. Her parents were both of Polish descent; her immigrant great-grandparents had owned a bakery in Baltimore. During her high school years at the Institute of Notre Dame, she worked in her parents' grocery store...

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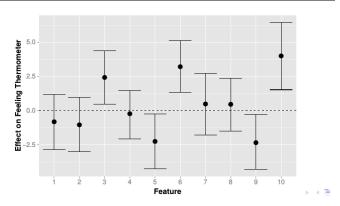
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- ▶ Protocol: Each respondent sees up to 3 texts from the corpus of > 2200 biographies
  - Observe text
  - ► Feeling thermometer rating: 0-100
- ▶ 1,886 participants, 5,303 responses
  - 2,651 training, 2,652 test

# Results

Treatment	Keywords
3	director, university, received, president, phd, policy
5	elected, house, democratic, seat
6	united_states, military, combat, rank
9	law, school_law, law_school, juris_doctor, student
10	war, enlisted, united_states, assigned, army



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  - ▶ These dimensions of heterogeneity may be proxied in text.
  - e.g., Republican judges might be harsher in cases where drug use occurred; Democrats might be harsher in cases where gender discrimination occured.
- ▶ I haven't seen any applications like this, but see Wager and Athey (2017) for some tools for data-driven recovery of heterogeneous effects.
  - another good replication exercise.