Inferring Graphics Programs from Images

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Abstract

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1 Introducing visual programs

- 3 Comment for reader: this paragraph is a little grandiose and goes beyond what we've actually
- 4 done. But these are the kinds of things that motivate the work, and I think that in some form
- 5 these ideas should be in the introduction or the conclusion. How could an agent go from noisy,
- 6 high-dimensional perceptual input to a symbolic, abstract object, like a computer program? Here we
- 7 consider this problem within the context of graphics program synthesis. We develop an approach
- 8 for converting natural images, such as hand drawings, into executable source code for drawing the
- original image. The source code captures not just the objects in the image, but also describes their
- 10 geometric relationships.
- High dimensional perceptual input is ill matched to the abstract semantics of a programming language.
- 12 But programs with constructs like recursion or iteration produce a simpler execution trace of primitive
- 13 actions. Our hypothesis is that the execution trace of the program is better aligned with the perceptual
- input, and that the trace can act as a kind of bridge between perception and programs. We test this
- 15 hypothesis by developing a model that learns to map from an image to the execution trace of the
- graphics program that drew it. With the execution trace in hand, we can bring to bear techniques from
- the program synthesis community to recover the latent graphics program.
- 18 In this work we consider programs that draw diagrams, similar to those found in papers.
- 19 We develop a hybrid architecture for inferring graphics programs. Our approach uses a deep network
- 20 infer an execution trace from an image; this recovers primitive drawing operations like lines, circles,
- 21 or arrows. For added robustness we use the deep network as a proposal distribution for a stochastic
- search over execution traces. Finally we use techniques in the program synthesis community to
- 23 recover the program from its trace.
- 24 Each of these three components the deep network, the stochastic search, the program synthesizer
- 25 confers its own advantages. From the deep network we get a very fast system that can recover
- 26 plausible execution traces in about a minute. From the stochastic search we get added robustness;
- 27 essentially the stochastic search can correct mistakes made by the deep network's proposals. From
- 28 the program synthesizer we get abstraction: our system recovers coordinate transformations, for
- loops, and subroutines, which are useful for downstream tasks.

2 Neural architecture for inferring image parses

- 31 We developed a deep network architecture for efficiently inferring a execution trace, T, from an
- image, I. Our model constructs the trace one drawing command at a time. When predicting the next
- drawing command, the network takes as input the target image I as well as the rendered output of
- 4 previous drawing commands. Intuitively, the network looks at the image it wants to explain, as well

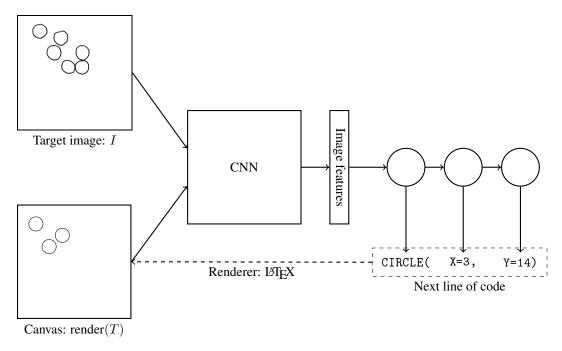


Figure 1: Our neural architecture for inferring the execution trace of a graphics program from its output.

as what it has already drawn. It then decides either to stop drawing or proposes another drawing command to add to the execution trace; if it decides to continue drawing, the predicted primitive is rendered to its "canvas" and the process repeats.

Figure 1 illustrates this architecture. We first pass the target image and a rendering of the trace so far to a convolutional network. Given the features extracted by the convolutionional network, a multilayer perceptron then predicts a distribution over the next drawing command to add to the trace. We predict

the drawing command token-by-token, and condition each token both on the image features and on the previously generated tokens. For example, the network first decides to emit the CIRCLE token conditioned on the image features, then it emits the *x* coordinate of the circle conditioned image features and the CIRCLE token, and finally it predicts the *y* coordinate of the circle conditioned

on the image features, the CIRCLE token, and the \boldsymbol{x} coordinate.

The distribution over the next drawing command factorizes:

$$\mathbb{P}_{\theta}[t_1 t_2 \cdots t_K | I, T] = \prod_{k=1}^K \mathbb{P}_{\theta}[t_k | f_{\theta}(I, \text{render}(T)), \{t_j\}_{j=1}^{k-1}]$$
 (1)

where $t_1t_2\cdots t_K$ are the tokens in the drawing command, I is the target image, T is an execution trace, θ are the parameters of the neural network, and $f_{\theta}(\cdot, \cdot)$ is the image feature extractor (convolutional network). The distribution over execution traces factorizes as:

$$\mathbb{P}_{\theta}[T|I] = \prod_{n=1}^{|T|} \mathbb{P}_{\theta}[T_n|I, T_{1:(n-1)}] \times \mathbb{P}_{\theta}[\mathsf{STOP}|I, T] \tag{2}$$

where |T| is the length of execution trace T, and the STOP token is emitted by the network to signal that the execution trace explains the image.

We train the network by sampling execution traces T and target images I for randomly generated scenes, and maximizing (2) wrt θ by gradient ascent. Despite the architecture being recurrent, training is fully supervised. In a sense, this model is like an autoregressive variant of AIR. When we have the generative model (the rendering function) and treat the trace as fully observed, we need not solve an unsupervised or reinforcement learning problem.

```
\begin{array}{ll} \texttt{CIRCLE}(x,y) & \texttt{Circle at } (x,y) \\ \texttt{RECTANGLE}(x_1,y_1,x_2,y_2) & \texttt{Rectangle with corners at } (x_1,y_1) \ \& \ (x_2,y_2) \\ \texttt{LINE}(x_1,y_1,x_2,y_2,\\ \texttt{arrow} \in \{0,1\}, \texttt{dashed} \in \{0,1\}) & \texttt{Line from } (x_1,y_1) \ \text{to } (x_2,y_2), \text{ optionally with an arrow and/or dashed} \\ \texttt{STOP} & \texttt{Finishes execution trace inference} \end{array}
```

Table 1: The deep network in (1) predicts drawing commands, shown above.

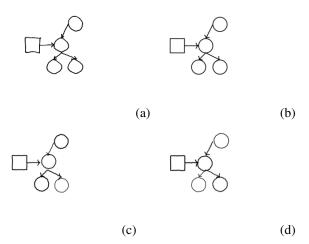


Figure 2: (a): a hand drawing. (b): Rendering of the parse our model infers for (a). We can generalize to hand drawings like these because we train the model on images corrupted by a noise process designed to resemble the kind of noise introduced by hand drawings - see (c) & (d) for noisy renderings of (b).

57 3 Generalizing to hand drawings

58 4 Synthesizing graphics programs from execution traces

59 5 Neural networks for guiding SMC

Let $L(\cdot|\cdot)$: image² $\to \mathcal{R}$ be our likelihood function: it takes two images, an observed target image and a hypothesized program output, and gives the likelihood of the observed image conditioned on the program output. We want to sample from:

$$\mathbb{P}[p|x] \propto L(x|\text{render}(p))\mathbb{P}[p] \tag{3}$$

where $\mathbb{P}[p]$ is the prior probability of program p, and x is the observed image.

```
Program \rightarrow
                 Command; ...; Command
Command \rightarrow
                 CIRCLE(Expression, Expression)
                 RECTANGLE(Expression, Expression, Expression)
Command \rightarrow
Command \rightarrow
                 LINE(Expression, Expression, Expression, Boolean, Boolean)
                 FOR(0 \le Var < Expression)  { Program }
Command \rightarrow
                 REFLECT(Axis) { Program }
Command \rightarrow
                 Z * Var + Z
Expression\rightarrow
        Var \rightarrow
                 A free (unused) variable
          Z\rightarrow
                 an integer
      Axis \rightarrow
                 X = Z
                 Y = Z
      Axis \rightarrow
```

Table 2: Grammar over graphics programs. We allow loops (FOR), vertical/horizontal reflections (REFLECT), and affine transformations (Z * Var + Z).

Algorithm 1 Neurally guided SMC

```
Input: Neural network NN, beam size N, maximum length L, target image x
Output: Samples of the program trace
Set B_0 = \{\text{empty program}\}\
for 1 \le l \le L do
     \text{for } 1 \leq n \leq N \text{ do}
    p_n \sim \text{Uniform}(B_{l-1})
p'_n \sim \text{NN}(\text{render}(p), x)
\text{Define } r_n = p'_n \cdot p_n
\text{Set } \tilde{w}(r_n) = \frac{L(x|r_n)}{L(x|p_n)} \times \frac{\mathbb{P}[p'_n]}{\mathbb{P}[p'_n = \text{NN}(\text{render}(p), x)]}
\text{end for}
\text{Define } w(p) = \frac{\tilde{w}(p)}{\sum_{p'} \tilde{w}(p')}
\text{Set } B_l \text{ to be } N \text{ samples from } r_n \text{ distributed according to } w(\cdot)
return \{p : p \in B_{l < L}, p \text{ is finished}\}
```

Let p be a program with L lines, which we will write as $p = (p_1, p_2, \cdots, p_L)$. Assume the prior factors into:

$$\mathbb{P}[p] \propto \prod_{l < L} \mathbb{P}[p_l] \tag{4}$$

Define the distribution $q_L(\cdot)$, which happens to be proportional to the above posterior:

$$q_L(p_1, p_2, \cdots, p_{L-1}, p_L) \propto q_{L-1}(p_1, p_2, \cdots, p_{L-1}) \times \frac{L(x|\text{render}(p_1, p_2, \cdots, p_{L-1}, p_L))}{L(x|\text{render}(p_1, p_2, \cdots, p_{L-1}))} \times \mathbb{P}[p_L]$$
(5)

- Now suppose we have some samples from $q_{L-1}(\cdot)$, and that we then sample a p_L from a distribution proportional to $\frac{L(x|\operatorname{render}(p_1,p_2,\cdots,p_{L-1},p_L))}{L(x|\operatorname{render}(p_1,p_2,\cdots,p_{L-1}))} \times \mathbb{P}[p_L]$. The resulting programs p are distributed according to q_L , and so are also distributed according to $\mathbb{P}[p|x]$.
- How do we sample p_L from a distribution proportional to $\frac{L(x|\text{render}(p_1,p_2,\cdots,p_{L-1},p_L))}{L(x|\text{render}(p_1,p_2,\cdots,p_{L-1}))} \times \mathbb{P}[p_L]$? We have a neural network that takes as input the target image x and the program so far, and produces 70
- 71
- a distribution over next lines of code (p_L) . We write $NN(p_L|p_1,\cdots,p_{L-1};x)$ for the distribution
- output by the neural network. So we can sample from NN and then weight the samples by:

$$w(p_L) = \frac{\mathbb{P}[p_L]}{\text{NN}(p_L|p_1, \cdots, p_{L-1}; x)} \times \frac{L(x|\text{render}(p_1, p_2, \cdots, p_{L-1}, p_L))}{L(x|\text{render}(p_1, p_2, \cdots, p_{L-1}))}$$
(6)

- Then we can resample from these now weighted samples to get a new population of particles (here 74
- programs are particles), where each program now has L lines instead of L-1. 75
- This procedure can be seen as a particle filter, where each successive latent variable is another line of
- 77 code, and the emission probabilities are successive ratios of likelihoods under $L(\cdot|\cdot)$.
- **Comments for Dan.** Right now I'm not actually sampling from the neural network instead, I 78
- enumerate the top few hundred lines of code suggested by the network, and then weight them by their 79
- likelihoods. So actually the form of NN is: 80

$$NN(p_L|p_1, \cdots, p_{L-1}; x) \propto \begin{cases} 1, & \text{if } p_L \in \text{top hundred neural network proposals} \\ 0, & \text{otherwise.} \end{cases}$$
 (7)

- Do you think this is a problem? The neural network puts almost all of its mass on a few guesses. In
- order to get the correct line of code I sometimes need to get something like the 50th top guess, so I
- don't want to literally just sample from the distribution suggested by the neural network. 83

Submission of papers to NIPS 2017

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NIPS requires electronic submissions. The electronic submission site is

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87 Please read carefully the instructions below and follow them faithfully.

88 **6.1** Style

- 89 Papers to be submitted to NIPS 2017 must be prepared according to the instructions presented here.
- 90 Papers may only be up to eight pages long, including figures. This does not include acknowledgments
- 91 and cited references which are allowed on subsequent pages. Papers that exceed these limits will not
- be reviewed, or in any other way considered for presentation at the conference.
- The margins in 2017 are the same as since 2007, which allow for $\sim 15\%$ more words in the paper
- 94 compared to earlier years.
- 95 Authors are required to use the NIPS LATEX style files obtainable at the NIPS website as indicated
- 96 below. Please make sure you use the current files and not previous versions. Tweaking the style files
- 97 may be grounds for rejection.

98 6.2 Retrieval of style files

99 The style files for NIPS and other conference information are available on the World Wide Web at

100 http://www.nips.cc/

- The file nips_2017.pdf contains these instructions and illustrates the various formatting require-
- ments your NIPS paper must satisfy.
- The only supported style file for NIPS 2017 is nips_2017.sty, rewritten for LaTeX 2ε . **Previous**
- style files for LATEX 2.09, Microsoft Word, and RTF are no longer supported!
- The new LATEX style file contains two optional arguments: final, which creates a camera-ready copy,
- and nonatbib, which will not load the natbib package for you in case of package clash.
- 107 At submission time, please omit the final option. This will anonymize your submission and add
- line numbers to aid review. Please do *not* refer to these line numbers in your paper as they will be
- 109 removed during generation of camera-ready copies.
- The file nips_2017.tex may be used as a "shell" for writing your paper. All you have to do is
- replace the author, title, abstract, and text of the paper with your own.
- The formatting instructions contained in these style files are summarized in Sections 7, 8, and 9
- 113 below.

7 General formatting instructions

- The text must be confined within a rectangle 5.5 inches (33 picas) wide and 9 inches (54 picas) long.
- The left margin is 1.5 inch (9 picas). Use 10 point type with a vertical spacing (leading) of 11 points.
- 117 Times New Roman is the preferred typeface throughout, and will be selected for you by default.
- Paragraphs are separated by ½ line space (5.5 points), with no indentation.
- The paper title should be 17 point, initial caps/lower case, bold, centered between two horizontal
- rules. The top rule should be 4 points thick and the bottom rule should be 1 point thick. Allow 1/4 inch
- space above and below the title to rules. All pages should start at 1 inch (6 picas) from the top of the
- 122 page.
- For the final version, authors' names are set in boldface, and each name is centered above the
- corresponding address. The lead author's name is to be listed first (left-most), and the co-authors'
- names (if different address) are set to follow. If there is only one co-author, list both author and
- 126 co-author side by side.
- Please pay special attention to the instructions in Section 9 regarding figures, tables, acknowledgments,
- 128 and references.

29 8 Headings: first level

- All headings should be lower case (except for first word and proper nouns), flush left, and bold.
- First-level headings should be in 12-point type.

132 8.1 Headings: second level

Second-level headings should be in 10-point type.

134 8.1.1 Headings: third level

- 135 Third-level headings should be in 10-point type.
- Paragraphs There is also a \paragraph command available, which sets the heading in bold, flush left, and inline with the text, with the heading followed by 1 em of space.

9 Citations, figures, tables, references

139 These instructions apply to everyone.

140 9.1 Citations within the text

- 141 The natbib package will be loaded for you by default. Citations may be author/year or numeric, as
- long as you maintain internal consistency. As to the format of the references themselves, any style is
- acceptable as long as it is used consistently.
- 144 The documentation for natbib may be found at
- http://mirrors.ctan.org/macros/latex/contrib/natbib/natnotes.pdf
- Of note is the command \citet, which produces citations appropriate for use in inline text. For example,
- 148 \citet{hasselmo} investigated\dots
- 149 produces
- Hasselmo, et al. (1995) investigated...
- If you wish to load the natbib package with options, you may add the following before loading the nips_2017 package:
- 153 \PassOptionsToPackage{options}{natbib}
- 154 If natbib clashes with another package you load, you can add the optional argument nonatbib 155 when loading the style file:
- 156 \usepackage[nonatbib] {nips_2017}
- 157 As submission is double blind, refer to your own published work in the third person. That is, use "In
- the previous work of Jones et al. [4]," not "In our previous work [4]." If you cite your other papers
- that are not widely available (e.g., a journal paper under review), use anonymous author names in the
- citation, e.g., an author of the form "A. Anonymous."

9.2 Footnotes

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- Footnotes should be used sparingly. If you do require a footnote, indicate footnotes with a number 1
- in the text. Place the footnotes at the bottom of the page on which they appear. Precede the footnote
- with a horizontal rule of 2 inches (12 picas).

¹Sample of the first footnote.

Table 3: Sample table title

	Part	
Name	Description	Size (μm)
Dendrite Axon Soma	Input terminal Output terminal Cell body	$\begin{array}{c} \sim \! 100 \\ \sim \! 10 \\ \text{up to } 10^6 \end{array}$

Note that footnotes are properly typeset *after* punctuation marks.²

9.3 Figures

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- All artwork must be neat, clean, and legible. Lines should be dark enough for purposes of reproduction. 167
- The figure number and caption always appear after the figure. Place one line space before the figure 168
- caption and one line space after the figure. The figure caption should be lower case (except for first 169
- word and proper nouns); figures are numbered consecutively. 170
- You may use color figures. However, it is best for the figure captions and the paper body to be legible if the paper is printed in either black/white or in color.

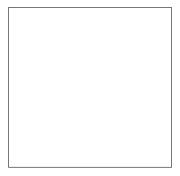


Figure 3: Sample figure caption.

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Tables

- All tables must be centered, neat, clean and legible. The table number and title always appear before the table. See Table 3. 175
- Place one line space before the table title, one line space after the table title, and one line space after 176
- the table. The table title must be lower case (except for first word and proper nouns); tables are 177
- numbered consecutively. 178
- Note that publication-quality tables do not contain vertical rules. We strongly suggest the use of the
- booktabs package, which allows for typesetting high-quality, professional tables: 180

https://www.ctan.org/pkg/booktabs

This package was used to typeset Table 3.

10 Final instructions

- Do not change any aspects of the formatting parameters in the style files. In particular, do not modify the width or length of the rectangle the text should fit into, and do not change font sizes (except
- perhaps in the **References** section; see below). Please note that pages should be numbered.

²As in this example.

11 Preparing PDF files

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- Please prepare submission files with paper size "US Letter," and not, for example, "A4."
- Fonts were the main cause of problems in the past years. Your PDF file must only contain Type 1 or Embedded TrueType fonts. Here are a few instructions to achieve this.
 - You should directly generate PDF files using pdflatex.
 - You can check which fonts a PDF files uses. In Acrobat Reader, select the menu Files>Document Properties>Fonts and select Show All Fonts. You can also use the program pdffonts which comes with xpdf and is available out-of-the-box on most Linux machines.
 - The IEEE has recommendations for generating PDF files whose fonts are also acceptable for NIPS. Please see http://www.emfield.org/icuwb2010/downloads/IEEE-PDF-SpecV32.pdf
 - xfig "patterned" shapes are implemented with bitmap fonts. Use "solid" shapes instead.
 - The \bbold package almost always uses bitmap fonts. You should use the equivalent AMS Fonts:

```
\usepackage{amsfonts}
```

followed by, e.g., \mathbb{R} , \mathbb{R} , \mathbb{R} , or \mathbb{C} . You can also use the following workaround for reals, natural and complex:

```
\newcommand{\RR}{I\!\!R} %real numbers
\newcommand{\Nat}{I\!\!N} %natural numbers
\newcommand{\CC}{I\!\!\!\!C} %complex numbers
```

Note that amsfonts is automatically loaded by the amssymb package.

208 If your file contains type 3 fonts or non embedded TrueType fonts, we will ask you to fix it.

209 11.1 Margins in LATEX

Most of the margin problems come from figures positioned by hand using \special or other commands. We suggest using the command \includegraphics from the graphicx package.

212 Always specify the figure width as a multiple of the line width as in the example below:

```
213     \usepackage[pdftex]{graphicx} ...
214     \includegraphics[width=0.8\linewidth]{myfile.pdf}
```

See Section 4.4 in the graphics bundle documentation (http://mirrors.ctan.org/macros/

216 latex/required/graphics/grfguide.pdf)

217 A number of width problems arise when LATEX cannot properly hyphenate a line. Please give LaTeX

218 hyphenation hints using the \- command when necessary.

219 Acknowledgments

Use unnumbered third level headings for the acknowledgments. All acknowledgments go at the end

of the paper. Do not include acknowledgments in the anonymized submission, only in the final paper.

References

222

- References follow the acknowledgments. Use unnumbered first-level heading for the references. Any
- choice of citation style is acceptable as long as you are consistent. It is permissible to reduce the font
- size to small (9 point) when listing the references. Remember that you can go over 8 pages as
- long as the subsequent ones contain only cited references.
- 227 [1] Alexander, J.A. & Mozer, M.C. (1995) Template-based algorithms for connectionist rule extraction. In
- 228 G. Tesauro, D.S. Touretzky and T.K. Leen (eds.), Advances in Neural Information Processing Systems 7, pp.
- 229 609–616. Cambridge, MA: MIT Press.

- 230 [2] Bower, J.M. & Beeman, D. (1995) *The Book of GENESIS: Exploring Realistic Neural Models with the* 231 *GEneral NEural SImulation System.* New York: TELOS/Springer–Verlag.
- [3] Hasselmo, M.E., Schnell, E. & Barkai, E. (1995) Dynamics of learning and recall at excitatory recurrent synapses and cholinergic modulation in rat hippocampal region CA3. *Journal of Neuroscience* **15**(7):5249-5262.