
Search, Compress, Compile: Library Learning in Neurally-Guided Bayesian Program Learning

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Abstract

1 Successful approaches to program induction require a hand-engineered domain-
2 specific language (DSL), constraining the space of allowed programs and imparting
3 prior knowledge of the domain. We contribute a program induction algorithm
4 called SCC that learns a DSL while jointly training a neural network to efficiently
5 search for programs in the learned DSL. We use our model to synthesize functions
6 on lists, edit text, and solve symbolic regression problems, showing how the model
7 learns a domain-specific library of program components for expressing solutions to
8 problems in the domain.

9 1 Introduction

10 Much of everyday human thinking and learning can be understood in terms of program induction:
11 constructing a procedure that maps inputs to desired outputs, based on observing example input-
12 output pairs. People can induce programs flexibly across many different domains, and remarkably,
13 often from just one or a few examples. For instance, if shown that a text-editing program should map
14 “Jane Morris Goodall” to “J. M. Goodall”, we can guess it maps “Richard Erskine Leakey” to “R. E.
15 Leakey”; if instead the first input mapped to “Dr. Jane”, “Goodall, Jane”, or “Morris”, we might have
16 guessed the latter should map to “Dr. Richard”, “Leakey, Richard”, or “Erskine”, respectively.

17 The FlashFill system [1] developed by Microsoft researchers and now embedded in Excel solves
18 problems such as these and is probably the best known practical program-induction algorithm, but
19 researchers in programming languages and AI have built successful program induction algorithms
20 for many applications, such as handwriting recognition and generation [2], procedural graphics [3],
21 question answering [4] and robot motion planning [5], to name just a few. These systems work
22 in different ways, but most hinge upon having a carefully engineered **Domain Specific Language**
23 (**DSL**). This is especially true for systems such as FlashFill that aim to induce a wide range of
24 programs very quickly, in a few seconds or less. DSLs constrain the search over programs with strong
25 prior knowledge in the form of a restricted set of programming primitives tuned to the needs of the
26 domain: for text editing, these are operations like appending strings and splitting on characters.

27 In this work, we consider the problem of building agents that learn to solve program induction tasks,
28 and also the problem of acquiring the prior knowledge necessary to quickly solve these tasks in a new
29 domain. Representative problems in three domains are shown in Table 1. Our solution is an algorithm
30 that grows or bootstraps a DSL while jointly training a neural network to help write programs in the
31 increasingly rich DSL.

32 Because any computable learning problem can in principle be cast as program induction, it is important
33 to delimit our focus. In contrast to computer assisted programming [6] or genetic programming [7],
34 our goal is not to automate software engineering, to learn to synthesize large bodies of code, or to
35 learn complex programs starting from scratch. Ours is a basic AI goal: capturing the human ability

Prior work on program learning has largely assumed a fixed, hand-engineered DSL, both in classic symbolic program learning approaches (e.g., Metagol: [10], FlashFill: [1]), neural approaches (e.g., RobustFill: [11]), and hybrids of neural and symbolic methods (e.g., Neural-guided deductive search: [12], DeepCoder: [13]). A notable exception is the EC algorithm [14], which also learns a library of subroutines. We find EC motivating, and go beyond it and other prior work through the following contributions:

Contributions. (1) We show how to learn-to-learn programs in an expressive Lisp-like programming language, including conditionals, variables, and higher-order recursive functions; (2) We give an algorithm for learning DSLs, built on a formalism known as Fragment Grammars [15]; and (3) We give a hierarchical Bayesian framing of the problem that allows joint inference of the DSL and neural recognition model.

2 The SCC Algorithm

We first mathematically describe our 3-step algorithm as an inference procedure for a hierarchical Bayesian model (Section 2.1), and then describe each step algorithmically in detail (Section 2.2-2.4).

2.1 Hierarchical Bayesian Framing

SCC takes as input a set of *tasks*, written X , each of which is a program synthesis problem. It has at its disposal a domain-specific *likelihood model*, written $\mathbb{P}[x|p]$, which scores the likelihood of a task $x \in X$ given a program p . Its goal is to solve each of the tasks by writing a program, and also to infer a DSL, written \mathcal{D} . We equip \mathcal{D} with a real-valued weight vector θ , and together (\mathcal{D}, θ) define a generative model over programs. We frame our goal as maximum a posteriori (MAP) inference of (\mathcal{D}, θ) given X . Writing J for the joint probability of (\mathcal{D}, θ) and X , we want the \mathcal{D}^* and θ^* solving:

$$J(\mathcal{D}, \theta) \triangleq \mathbb{P}[\mathcal{D}, \theta] \prod_{x \in X} \sum_p \mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta]$$

$$\mathcal{D}^* = \arg \max_{\mathcal{D}} \int J(\mathcal{D}, \theta) d\theta \quad \theta^* = \arg \max_{\theta} J(\mathcal{D}^*, \theta) \quad (1)$$

The above equations summarize the problem from the point of view of an ideal Bayesian learner. However, Eq. 1 is wildly intractable because evaluating $J(\mathcal{D}, \theta)$ involves summing over the infinite set of all programs. In practice we will only ever be able to sum over a finite set of programs. So, for each task, we define a finite set of programs, called a *frontier*, and only marginalize over the frontiers: **Definition.** A *frontier of task x* , written \mathcal{F}_x , is a finite set of programs s.t. $\mathbb{P}[x|p] > 0$ for all $p \in \mathcal{F}_x$.

Using the frontiers we define the following intuitive lower bound on the joint probability, called \mathcal{L} :

$$J \geq \mathcal{L} \triangleq \mathbb{P}[\mathcal{D}, \theta] \prod_{x \in X} \sum_{p \in \mathcal{F}_x} \mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta] \quad (2)$$

SCC does approximate MAP inference by maximizing this lower bound on the joint probability, alternating maximization w.r.t. the frontiers (Search) and the DSL (Compression):

Program Search: Maxing \mathcal{L} w.r.t. the frontiers. Here (\mathcal{D}, θ) is fixed and we want to find new programs to add to the frontiers so that \mathcal{L} increases the most. \mathcal{L} most increases by finding programs where $\mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta]$ is large.

DSL Induction: Maxing $\int \mathcal{L} d\theta$ w.r.t. the DSL. Here $\{\mathcal{F}_x\}_{x \in X}$ is held fixed, and so we can evaluate \mathcal{L} . Now the problem is that of searching the discrete space of DSLs and finding one maximizing $\int \mathcal{L} d\theta$. Once we have a DSL \mathcal{D} we can update θ to $\arg \max_{\theta} \mathcal{L}(\mathcal{D}, \theta, \{\mathcal{F}_x\})$.

Searching for programs is hard because of the large combinatorial search space. We ease this difficulty by training a neural recognition model, $q(\cdot|\cdot)$, during the compilation phase: q is trained to approximate the posterior over programs, $q(p|x) \approx \mathbb{P}[p|x, \mathcal{D}, \theta] \propto \mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta]$, thus amortizing the cost of finding programs with high posterior probability.

Neural recognition model: tractably maxing \mathcal{L} w.r.t. the frontiers. Here we train $q(p|x)$ to assign high probability to programs p where $\mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta]$ is large, because including those programs in the frontiers will most increase \mathcal{L} .

2.2 Searching for Programs

Now our goal is to search for programs solving the tasks. We use the simple approach of enumerating programs from the DSL in decreasing order of their probability, and then checking if a program p assigns positive probability to a task ($\mathbb{P}[x|p] > 0$); if so, we incorporate p into the frontier \mathcal{F}_x .

To make this concrete we need to define what programs actually are and what form $\mathbb{P}[p|\mathcal{D}, \theta]$ takes. We represent programs as λ -calculus expressions. λ -calculus is a formalism for expressing functional programs that closely resembles Lisp, including variables, function application, and the ability to create new functions. Throughout this paper we will write λ -calculus expressions in Lisp syntax. Our programs are all strongly typed. We use the Hindley-Milner polymorphic typing system [16] which is used in functional programming languages like OCaml and Haskell. We now define DSLs:

Definition: (\mathcal{D}, θ) . A DSL \mathcal{D} is a set of typed λ -calculus expressions. A weight vector θ for a DSL \mathcal{D} is a vector of $|\mathcal{D}| + 1$ real numbers: one number for each DSL element $e \in \mathcal{D}$, written θ_e and controlling the probability of e occurring in a program, and a weight controlling the probability of a variable occurring in a program, θ_{var} .

Together with its weight vector, a DSL defines a distribution over programs, $\mathbb{P}[p|\mathcal{D}, \theta]$. In the supplement, we define this distribution by specifying a procedure for drawing samples from $\mathbb{P}[p|\mathcal{D}, \theta]$.

Why enumerate, when the program synthesis community has invented many sophisticated algorithms that search for programs? [6, 17, 18, 19, 20]. We have two reasons: (1) A key point of our work is that learning the DSL, along with a neural recognition model, can make program induction tractable, even if the search algorithm is very simple. (2) Enumeration is a general approach that can be applied to any program induction problem. Many of these more sophisticated approaches require special conditions on the space of programs.

However, a drawback of enumerative search is that we have no efficient means of solving for arbitrary constants that might occur in a program. In Sec. 4, we will show how to find programs with real-valued constants by automatically differentiating through the program and setting the constants using gradient descent.

2.3 Compilation: Learning a Neural Recognition Model

The purpose of training the recognition model is to amortize the cost of searching for programs. It does this by learning to predict, for each task, programs with high likelihood according to $\mathbb{P}[x|p]$ while also being probable under the prior (\mathcal{D}, θ) . Concretely, the recognition model q predicts, for each task $x \in X$, a weight vector $q(x) = \theta^{(x)} \in \mathbb{R}^{|\mathcal{D}|+1}$. Together with the DSL, this defines a distribution over programs, $\mathbb{P}[p|\mathcal{D}, \theta = q(x)]$. We abbreviate this distribution as $q(p|x)$. The crucial aspect of this framing is that the neural network leverages the structure of the learned DSL, so it is *not* responsible for generating programs wholesale. We share this aspect with DeepCoder [13] and [21].

How should we get the data to train q ? This is nonobvious because we are considering a weakly supervised setting (i.e., learning only from tasks and not from (program, task) pairs). One approach is to sample programs from the DSL, run them to get their input/outputs, and then train q to predict the program from the input/outputs. This is like how a Helmholtz machine trains its recognition model during its “sleep” phase [22]. The advantage of “Helmholtz machine” training is that we can draw unlimited samples from the DSL, training on a large amount of data. Another approach is self-supervised learning, training q on the (program, task) pairs discovered by search. The advantage of self-supervised learning is that the training data is much higher quality, because we are training on the actual tasks. Due to these complementary advantages, we train on both these sources of data.

Formally, q should approximate the true posteriors over programs: minimizing the expected KL-divergence, $\mathbb{E}[\text{KL}(\mathbb{P}[p|x, \mathcal{D}, \theta] || q(p|x))]$, equivalently maximizing $\mathbb{E}[\sum_p \mathbb{P}[p|x, \mathcal{D}, \theta] \log q(p|x)]$, where the expectation is taken over tasks. Taking this expectation over the empirical distribution of tasks gives self-supervised training; taking it over samples from the generative model gives Helmholtz-machine style training. The objective for a recognition model (\mathcal{L}_{RM}) combines the Helmholtz machine (\mathcal{L}_{HM}) and self supervised (\mathcal{L}_{SS}) objectives, $\mathcal{L}_{\text{RM}} = \mathcal{L}_{\text{SS}} + \mathcal{L}_{\text{HM}}$:

$$\mathcal{L}_{\text{HM}} = \mathbb{E}_{(p,x) \sim (\mathcal{D}, \theta)} [\log q(p|x)] \quad \mathcal{L}_{\text{SS}} = \mathbb{E}_{x \sim X} \left[\sum_{p \in \mathcal{F}_x} \frac{\mathbb{P}[x, p|\mathcal{D}, \theta]}{\sum_{p' \in \mathcal{F}_x} \mathbb{P}[x, p'|\mathcal{D}, \theta]} \log q(p|x) \right]$$

2.4 Compression: Learning a Generative Model (a DSL)

The purpose of the DSL is to offer a set of abstractions that allow an agent to easily express solutions to the tasks at hand. Intuitively, we want the algorithm to look at the frontiers and generalize beyond them, both so the DSL can better express the current solutions, and also so that the DSL might expose new abstractions which will later be used to discover more programs. Formally, we want the DSL maximizing $\int \mathcal{L} d\theta$ (Sec. 2.1). We replace this marginal with an AIC approximation, giving the following objective for DSL induction:

$$\log \mathbb{P}[\mathcal{D}] + \arg \max_{\theta} \sum_{x \in X} \log \sum_{p \in \mathcal{F}_x} \mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta] + \log \mathbb{P}[\theta|\mathcal{D}] - \|\theta\|_0 \quad (3)$$

We induce a DSL by searching locally through the space of DSLs, proposing small changes to \mathcal{D} until Eq. 3 fails to increase. The search moves work by introducing new λ -expressions into the DSL. We propose these new expressions by extracting fragments of programs already in the frontiers (Tbl. 1). An important point here is that we are *not* simply adding subexpressions of programs to \mathcal{D} , as done in the EC algorithm [14] and other prior work [23]. Instead, we are extracting fragments that unify with programs in the frontiers. This idea of storing and reusing fragments of expressions comes from Fragment Grammars [15] and Tree-Substitution Grammars [24], and is closely related to the idea of antiunification [25].

To define the prior distribution over (\mathcal{D}, θ) , we penalize the syntactic complexity of the λ -calculus expressions in the DSL, defining $\mathbb{P}[\mathcal{D}] \propto \exp(-\lambda \sum_{p \in \mathcal{D}} \text{size}(p))$ where $\text{size}(p)$ measures the size of the syntax tree of program p , and place a symmetric Dirichlet prior over the weight vector θ .

Putting all these ingredients together, Alg. 1 describes how we combine program search, recognition model training, and DSL induction.

Algorithm 1 The SCC Algorithm

Input: Initial DSL \mathcal{D} , set of tasks X , iterations I
Hyperparameters: Enumeration timeout T
Initialize $\theta \leftarrow$ uniform
for $i = 1$ **to** I **do**
 $\mathcal{F}_x^\theta \leftarrow \{p | p \in \text{enum}(\mathcal{D}, \theta, T) \text{ if } \mathbb{P}[x|p] > 0\}$ (**Search**)
 $q \leftarrow$ train recognition model, maximizing \mathcal{L}_{RM} (**Compile**)
 $\mathcal{F}_x^q \leftarrow \{p | p \in \text{enum}(\mathcal{D}, q(x), T) \text{ if } \mathbb{P}[x|p] > 0\}$ (**Search**)
 $\mathcal{D}, \theta \leftarrow \text{induceDSL}(\{\mathcal{F}_x^\theta \cup \mathcal{F}_x^q\}_{x \in X})$ (**Compress**)
end for
return \mathcal{D}, θ, q

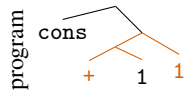
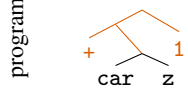
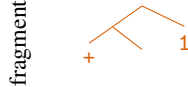
	Example programs in frontiers	Proposed λ -expression
program		$(\lambda (\ell) (\text{map } (\lambda (x) (\text{index } x \ell)) (\text{range } (- (\text{length } \ell) 1))))$ $(\text{map } (\lambda (x) (\text{index } x \ell)) (\text{range } \alpha))$
program		$(\lambda (s) (\text{map } (\lambda (x) (\text{if } (= x \text{'.'}) \text{'-' } x))) s)$ $(\lambda (s) (\text{map } (\lambda (x) (\text{if } (= x \alpha) \beta x))) s)$
fragment		$(\lambda (s) (\text{map } (\lambda (x) (\text{if } (= x \text{'-'}) \text{'.' } x))) s)$

Figure 1: **Left:** syntax trees of two programs sharing common structure, highlighted in red, from which we extract a fragment and add it to the DSL (bottom). **Right:** actual programs, from which we extract fragments that (top) slice from the beginning of a list or (bottom) perform character substitutions.

3 Programs that manipulate sequences

We apply SCC to list processing (Section 3.1) and text editing (Section 3.2). For both these domains we use a bidirectional GRU [26] for the recognition model, and initially provide the system with a generic set of list processing primitives: `foldr`, `unfold`, `if`, `map`, `length`, `index`, `=`, `+`, `-`, `0`, `1`, `cons`, `car`, `cdr`, `nil`, and `is-nil`.

3.1 List Processing

Synthesizing programs that manipulate data structures is a widely studied problem in the programming languages community [18]. We consider this problem within the context of learning functions that manipulate lists, and which also perform arithmetic operations upon lists of numbers.

We created 236 human-interpretable list manipulation tasks, each with 15 input/output examples (Tbl. 2). Our data set is interesting in three major ways: many of the tasks require complex solutions; the tasks were not generated from some latent DSL, and the agent must learn to solve these complicated problems from only 236 tasks. Our data set assumes arithmetic operations as well as sequence operations, so we additionally provide our system with the following arithmetic primitives: `mod`, `*`, `>`, `is-square`, `is-prime`.

Name	Input	Output
repeat-2	[7 0]	[7 0 7 0]
drop-3	[0 3 8 6 4]	[6 4]
rotate-2	[8 14 1 9]	[1 9 8 14]
count-head-in-tail	[1 2 1 1 3]	2
keep-mod-5	[5 9 14 6 3 0]	[5 0]
product	[7 1 6 2]	84

Table 2: Some tasks in our list function domain. See the supplement for the complete data set.

We evaluated SCC on random 50/50 test/train split. Interestingly, we found that the recognition model provided little benefit for the training tasks. However, it yielded faster search times on held out tasks, allowing more tasks to be solved before timing out. The system composed 38 new subroutines, yielding a more expressive DSL more closely matching the domain (left of Tbl. 1, right of Fig. 1). See the supplement for a complete list of DSL primitives discovered by SCC.

3.2 Text Editing

Synthesizing programs that edit text is a classic problem in the programming languages and AI literatures [21, 27], and algorithms that learn text editing programs ship in Microsoft Excel [1]. This prior work presumes a hand-engineered DSL. We show SCC can instead start out with generic sequence manipulation primitives and recover many of the higher-level building blocks that have made these other text editing systems successful.

Because our enumerative search procedure cannot generate string constants, we instead enumerate programs with string-valued parameters. For example, to learn a program that prepends “Dr.”, we enumerate $(f_3 \text{ string } s)$ – where f_3 is the learned appending primitive (Fig. 1) — and then define $P[x|p]$ by approximately marginalizing out the string parameters via a simple dynamic program. In Sec. 4, we will use a similar trick to synthesize programs containing real numbers, but using gradient descent instead of dynamic programming.

We trained our system on a corpus of 109 automatically generated text editing tasks, with 4 input/output examples each. After three iterations, it assembles a DSL containing a dozen new functions (center of Fig. 1) that let it solve all of the training tasks. But, how well does the learned DSL generalized to real text-editing scenarios? We tested, but did not train, on the 108 text editing problems from the SyGuS [28] program synthesis competition. Before any learning, SCC solves 3.7% of the problems with an average search time of 235 seconds. After learning, it solves 74.1%, and does so much faster, solving them in an average of 29 seconds. As of the 2017 SyGuS competition, the best-performing algorithm solves 79.6% of the problems. But, SyGuS comes with a different hand-engineered DSL for each text editing problem.¹ Here we learned a single DSL that applied generically to all of the tasks, and perform comparably to the best prior work.

¹SyGuS text editing problems also prespecify the set of allowed string constants for each task. For these experiments, our system did not use this assistance.

240 4 Symbolic Regression: Programs from visual input

241 We apply SCC to symbolic regression problems. Here, the agent observes points along the curve
 242 of a function, and must write a program that fits those points. We initially equip our learner with
 243 addition, multiplication, and division, and task it with solving 100 symbolic regression problems, each
 244 either a polynomial of degree 1–4 or a rational function. The recognition model is a convolutional
 245 network that observes an image of the target function’s graph (Fig. 2) — visually, different kinds of
 246 polynomials and rational functions produce different kinds of graphs, and so the recognition model
 247 can learn to look at a graph and predict what kind of function best explains it. A key difficulty,
 248 however, is that these problems are best solved with programs containing real numbers. Our solution
 249 to this difficulty is to enumerate programs with real-valued parameters, and then fit those parameters
 250 by automatically differentiating through the programs the system writes and use gradient descent to
 251 fit the parameters. We define the likelihood model, $\mathbb{P}[x|p]$, by assuming a Gaussian noise model for
 252 the input/output examples, and penalize the use of real-valued parameters using the BIC [29].

253 SCC learns a DSL containing 13 new functions, most
 254 of which are templates for polynomials of different
 255 orders or ratios of polynomials. It also learns to
 256 find programs that minimize the number of continu-
 257 ous degrees of freedom. For example, it learns to
 258 represent linear functions with the program `(* real`
 259 `(+ x real))`, which has two continuous degrees of
 260 freedom, and represents quartic functions using the
 261 invented DSL primitive f_4 in the rightmost column
 262 of Fig. 1 which has five continuous parameters. This
 263 phenomenon arises from our Bayesian framing —
 264 both the implicit bias towards shorter programs and
 265 the likelihood model’s BIC penalty.

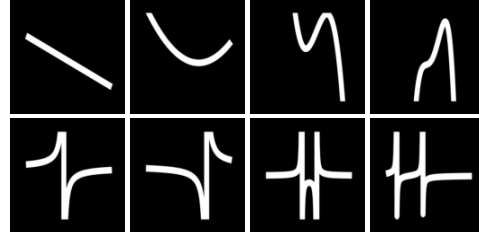


Figure 2: Recognition model input for symbolic regression. DSL learns subroutines for polynomials (top row) and rational functions (bottom row) while the recognition model jointly learns to look at a graph of the function (above) and predict which of those subroutines best explains the observation.

266 5 Quantitative Results

267 We compare with ablations of our model on held out tasks. The purpose of this
 268 ablation study is both to examine the role of each component of SCC, as well as
 269 to compare with prior approaches in the literature: a head-to-head comparison of pro-
 270 gram synthesizers is complicated by the fact that each system, including ours, makes
 271 idiosyncratic assumptions about the space of programs and the statement of tasks.

272 Nevertheless, much prior work can be modeled within our setup. We compare with
 273 the following ablations (Tbl 3; Fig 3):

274 **No NN:** lesions the recognition model.

275 **NPS**, which does not learn the DSL, instead learning the recognition model from
 276 samples drawn from the fixed DSL. We call this NPS (Neural Program Synthesis) be-
 277 cause this is closest to how RobustFill [11] and DeepCoder [13] are trained.

278 **SE**, which lesions the recognition model and restricts the DSL learning algorithm to
 279 only add `SubExpressions` of programs in the frontiers to the DSL. This is how most
 280 prior approaches have learned libraries of functions [14, 30, 23].

281 **PCFG**, which lesions the recognition model and does not learn the DSL, but instead learns the
 282 parameters of the DSL (θ), learning the parameters of a PCFG while not learning any of the structure.

283 **Enum**, which enumerates a frontier without any learning — equivalently, our first search step.

	Ours	No NN	SE	NPS	PCFG	Enum
<i>List Processing</i>						
% solved	79% ²	76%	71%	35%	62%	37%
Solve time	4.1s	5.8s	10.6s	34.7s	43.4s	20.2s
<i>Text Editing</i>						
% solved	74%	43%	30%	33%	0%	4%
Solve time	29s	65s	38s	80s	—	235s
<i>Symbolic Regression</i>						
% solved	84%	75%	62%	38%	38%	37%
Solve time	24s	40s	28s	31s	55s	29s

Table 3: % held-out test tasks solved. Solve time: averaged over solved tasks.

²Due to a last-minute bug we ran the list processing experiments without training the recognition model on “Helmholtz machine” style data. We are rerunning this experiment and anticipate improved quantitative results for list processing — notice the recognition model helps much more for text editing and symbolic regression.

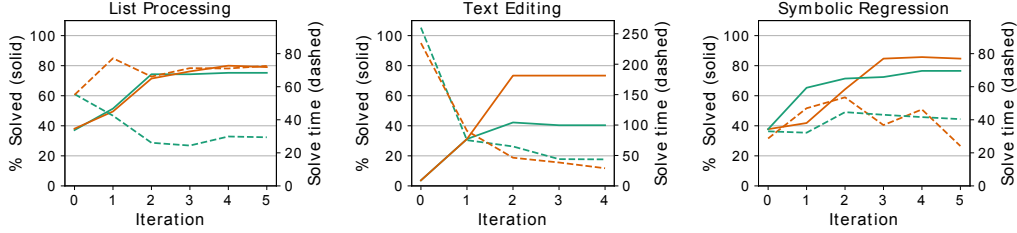


Figure 3: Learning curves for SCC both with (in orange) and without (in teal) the recognition model. Solid lines: % holdout testing tasks solved. Dashed lines: Average solve time.

6 Related Work

Our work is far from the first for learning to learn programs, an idea that goes back to Solomonoff [31]:

Deep learning: Much recent work in the ML community has focused on creating neural networks that regress from input/output examples to programs [11, 5, 21, 13]. SCC’s recognition model draws heavily from this line of work, particularly from [21]. We see these prior works as operating in a different regime: typically, they train with strong supervision (i.e., with annotated ground-truth programs) on massive data sets (i.e., hundreds of millions [11]). Our work considers a weakly-supervised regime where ground truth programs are not provided and the agent must learn from at most a few hundred tasks, which is facilitated by our “Helmholtz machine” style recognition model.

Inventing new subroutines for program induction: Several program induction algorithms, most prominently the EC algorithm [14], take as their goal to learn new, reusable subroutines that are shared in a multitask setting. We find this work inspiring and motivating, and extend it along two dimensions: (1) we propose a new algorithm for inducing reusable subroutines, based on Fragment Grammars [15]; and (2) we show how to combine these techniques with bottom-up neural recognition models. Other instances of this related idea are [30], Schmidhuber’s OOPS model [32], and predicate invention in Inductive Logic Programming [23].

Bayesian Program Learning: Our work is an instance of Bayesian Program Learning (BPL; see [2, 14, 33, 30]). Previous BPL systems have largely assumed a fixed DSL (but see [30]), and our contribution here is a general way of doing BPL with less hand-engineering of the DSL.

7 Discussion

We contribute an algorithm, SCC, that learns to program by bootstrapping a DSL with new domain-specific primitives that the algorithm itself discovers, together with a neural recognition model that learns how to efficiently deploy the DSL on new tasks. We believe this integration of top-down symbolic representations and bottom-up neural networks — both of them learned — helps make program induction systems more generally useful for AI. Many directions remain open. Two immediate goals are to integrate more sophisticated neural recognition models [11] and program synthesizers [6], which may improve performance in some domains over the generic methods used here. We are in the process of applying our algorithm to generative programs and prototyped this with a turtle-like domain: Figure 4 gives some preliminary results for turtle graphics — see Section 1 of the supplementary material for more details. Another direction is to explore DSL meta-learning: can we find a *single* universal primitive set that could effectively bootstrap DSLs for new domains, including the three domains considered, but also many others?

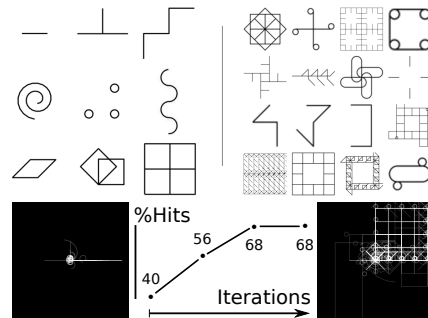


Figure 4: Top left: Example training tasks. Top right: samples from the learned DSL. Bottom: % holdout testing tasks solved (middle), on sides are the averaged samples from the DSL before any training (left) and after last iteration (right).

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