

Learning Libraries of Subroutines for Neurally-Guided Bayesian Program Learning

Anonymous Author(s)

Affiliation

Address

email

Abstract

Successful approaches to program induction require a hand-engineered domain-specific language (DSL), constraining the space of allowed programs and imparting prior knowledge of the domain. We contribute a program induction algorithm called COCOSEA that learns a DSL while jointly training a neural network to efficiently search for programs in the learned DSL. We use our model to synthesize functions on lists, edit text, and solve symbolic regression problems, showing how the model learns a domain-specific library of program components for expressing solutions to problems in the domain.

1 Introduction

Imagine you are asked to edit some text, and told that you should change the text “Nancy FreeHafer” to “Dr. Nancy”. From this example, you likely infer that “Jane Goodall” goes to “Dr. Jane”, drawing upon your prior knowledge of text, like that words are separated by spaces. Few-shot learning problems like these are commonplace in both human and machine learning. We cast these few-shot learning problems as each being a program synthesis problem. The programming languages and AI communities have built many successful program synthesis algorithms, spanning text editing (e.g., FlashFill [1]), motor programs [30], procedural graphics [2], planning procedures [26], and many others. However, the success of these systems hinges upon a carefully hand-engineered **Domain Specific Language (DSL)**. DSLs impart prior knowledge of a domain by providing a restricted set of finely-tuned programming primitives: for text editing, these are primitives like appending and splitting on characters. In this work, we consider the problem of building agents that solve program learning tasks, and also the problem of acquiring the prior knowledge necessary to quickly solve these tasks (Figure 1). Our solution is an algorithm that learns a DSL while jointly training a neural network to help write programs in the learned DSL.

TASK	<div> Nancy FreeHafer → Dr. Nancy Jane Goodall → ??? </div>
PROGRAM	$f(s) = (f_0 \text{ "Dr." } (f_1 \text{ s ' '}))$
DSL	<div> $f_0(a,b) = (\text{foldr } a \text{ b } (\lambda (x \ y) (\text{cons } x \ y)))$ <i>(f_0: Appends lists (of characters))</i> $f_1(s,c) = (\text{foldr } s \text{ s } (\lambda (x \ a)$ <div>(if (= c x) nil (cons x a))))</div> <i>(f_1: Take characters from s until c reached)</i> </div>

Figure 1: **Task:** Few-shot learning problem. Model solves tasks by writing **programs**, and jointly learns a library of reusable subroutines that are shared across multiple tasks, called a **Domain Specific Language (DSL)**. Program writing is guided by a neural network trained jointly with the library.

59 The new contribution of this work is thus an algorithm for learning DSLs which jointly trains a neural
60 net to search for programs in the DSL.

61 2 The CoCoSEA Algorithm

62 Our goal is to induce a DSL while finding programs solving each of the tasks. We take inspiration
63 primarily from the Exploration-Compression algorithm for bootstrap learning [12]. Exploration-
64 Compression alternates between exploring the space of solutions to a set of tasks, and compressing
65 those solutions to suggest new search primitives for the next exploration stage. We extend these ideas
66 into an inference strategy that iterates through three steps: a **Search** step uses the current DSL and
67 recognition model to search for programs that solve the tasks. The **Compress** and **Compile** steps
68 update the DSL and the recognition model, respectively. Crucially, these steps bootstrap each other:
69 **Search: Solving tasks.** Our program search is informed by both the DSL and the recognition model.
70 When these improve, we can solve more tasks.

71 **Compression: Improving the DSL.** We induce the DSL from the programs found in the search
72 phase, aiming to maximally compress (or, raise the prior probability of) these programs. As we solve
73 more tasks, we hone in on DSLs that more closely match the domain.

74 **Compilation: Learning a neural recognition model.** We update the recognition model by training
75 on two data sources: samples from the DSL (as in the Helmholtz Machine’s “sleep” phase), and
76 programs found by the search procedure during search. As the DSL improves and as search finds
77 more programs, the recognition model gets more data to train on, and better data.

78 2.1 Hierarchical Bayesian Framing

79 CoCoSEA takes as input a set of *tasks*, written X , each of which is a program synthesis problem. It
80 has at its disposal a domain-specific *likelihood model*, written $\mathbb{P}[x|p]$, which scores the likelihood of
81 a task $x \in X$ given a program p . Its goal is to solve each of the tasks by writing a program, and also
82 to infer a DSL, written \mathcal{D} . We equip \mathcal{D} with a real-valued weight vector θ , and together (\mathcal{D}, θ) define
83 a generative model over programs. We frame our goal as maximum a posteriori (MAP) inference of
84 (\mathcal{D}, θ) given X . Writing J for the joint probability of (\mathcal{D}, θ) and X , we want the \mathcal{D}^* and θ^* solving:

$$J(\mathcal{D}, \theta) \triangleq \mathbb{P}[\mathcal{D}, \theta] \prod_{x \in X} \sum_p \mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta]$$

$$\mathcal{D}^* = \arg \max_{\mathcal{D}} \int J(\mathcal{D}, \theta) d\theta \quad \theta^* = \arg \max_{\theta} J(\mathcal{D}^*, \theta) \quad (1)$$

85 The above equations summarize the problem from the point of view of an ideal Bayesian learner.
86 However, Eq. 1 is wildly intractable because evaluating $J(\mathcal{D}, \theta)$ involves summing over the infinite
87 set of all programs. In practice we will only ever be able to sum over a finite set of programs. So, for
88 each task, we define a finite set of programs, called a *frontier*, and only marginalize over the frontiers:

89 **Definition.** A *frontier of task x* , written \mathcal{F}_x , is a finite set of programs s.t. $\mathbb{P}[x|p] > 0$ for all $p \in \mathcal{F}_x$.

90 Using the frontiers we define the following intuitive lower bound on the joint probability, called \mathcal{L} :

$$J \geq \mathcal{L} \triangleq \mathbb{P}[\mathcal{D}, \theta] \prod_{x \in X} \sum_{p \in \mathcal{F}_x} \mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta] \quad (2)$$

91 CoCoSEA does approximate MAP inference by maximizing this lower bound on the joint probability,
92 alternating maximization w.r.t. the frontiers (Search) and the DSL (Compression):

93 **Program Search: Maxing \mathcal{L} w.r.t. the frontiers.** Here (\mathcal{D}, θ) is fixed and we want to find new
94 programs to add to the frontiers so that \mathcal{L} increases the most. \mathcal{L} most increases by finding programs
95 where $\mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta]$ is large.

96 **DSL Induction: Maxing $\int \mathcal{L} d\theta$ w.r.t. the DSL.** Here $\{\mathcal{F}_x\}_{x \in X}$ is held fixed, and so we can
97 evaluate \mathcal{L} . Now the problem is that of searching the discrete space of DSLs and finding one
98 maximizing $\int \mathcal{L} d\theta$. Once we have a DSL \mathcal{D} we can update θ to $\arg \max_{\theta} \mathcal{L}(\mathcal{D}, \theta, \{\mathcal{F}_x\})$.

99 Searching for programs is hard because of the large combinatorial search space. We ease this
100 difficulty by training a neural recognition model, $q(\cdot|\cdot)$, during the compilation phase: q is trained to
101 approximate the posterior over programs, $q(p|x) \approx \mathbb{P}[p|x, \mathcal{D}, \theta] \propto \mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta]$, thus amortizing
102 the cost of finding programs with high posterior probability.

103 **Neural recognition model: tractably maxing \mathcal{L} w.r.t. the frontiers.** Here we train $q(p|x)$ to
 104 assign high probability to programs p where $\mathbb{P}[x|p]\mathbb{P}[p|\mathcal{D}, \theta]$ is large, because including those
 105 programs in the frontiers will most increase \mathcal{L} .

106 2.2 Searching for Programs

107 Now our goal is to search for programs solving the tasks. We use the simple approach of enumerating
 108 programs from the DSL in decreasing order of their probability, and then checking if a program p
 109 assigns positive probability to a task ($\mathbb{P}[x|p] > 0$); if so, we incorporate p into the frontier \mathcal{F}_x .

110 To make this concrete we need to define what programs actually are and what form $\mathbb{P}[p|\mathcal{D}, \theta]$ takes.
 111 We represent programs as λ -calculus expressions. λ -calculus is a formalism for expressing functional
 112 programs that closely resembles Lisp, including variables, function application, and the ability to
 113 create new functions. Throughout this paper we will write λ -calculus expressions in Lisp syntax. Our
 114 programs are all strongly typed. We use the Hindley-Milner polymorphic typing system [13] which
 115 is used in functional programming languages like OCaml and Haskell. We now define DSLs:

116 **Definition:** (\mathcal{D}, θ) . A DSL \mathcal{D} is a set of typed λ -calculus expressions. A weight vector θ for a DSL
 117 \mathcal{D} is a vector of $|\mathcal{D}| + 1$ real numbers: one number for each DSL element $e \in \mathcal{D}$, written θ_e and
 118 controlling the probability of e occurring in a program, and a weight controlling the probability of a
 119 variable occurring in a program, θ_{var} .

120 Together with its weight vector, a DSL defines a distribution over programs, $\mathbb{P}[p|\mathcal{D}, \theta]$. In the
 121 supplement, we define this distribution by specifying a procedure for drawing samples from $\mathbb{P}[p|\mathcal{D}, \theta]$.

122 Why enumerate, when the program synthesis community has invented many sophisticated algorithms
 123 that search for programs? [14, 15, 3, 16, 4]. We have two reasons: (1) A key point of our work is
 124 that learning the DSL, along with a neural recognition model, can make program induction tractable,
 125 even if the search algorithm is very simple. (2) Enumeration is a general approach that can be applied
 126 to any program induction problem. Many of these more sophisticated approaches require special
 127 conditions on the space of programs.

128 However, a drawback of enumerative search is that we have no efficient means of solving for arbitrary
 129 constants that might occur in a program. In Sec. 4, we will show how to find programs with real-
 130 valued constants by automatically differentiating through the program and setting the constants using
 131 gradient descent.

132 2.3 Compilation: Learning a Neural Recognition Model

133 The purpose of training the recognition model is to amortize the cost of searching for programs. It
 134 does this by learning to predict, for each task, programs with high likelihood according to $\mathbb{P}[x|p]$
 135 while also being probable under the prior (\mathcal{D}, θ) . Concretely, the recognition model q predicts, for
 136 each task $x \in X$, a weight vector $q(x) = \theta^{(x)} \in \mathbb{R}^{|\mathcal{D}|+1}$. Together with the DSL, this defines a
 137 distribution over programs, $\mathbb{P}[p|\mathcal{D}, \theta = q(x)]$. We abbreviate this distribution as $q(p|x)$. The crucial
 138 aspect of this framing is that the neural network leverages the structure of the learned DSL, so it is *not*
 139 responsible for generating programs wholesale. We share this aspect with DeepCoder [8] and [17].

140 How should we get the data to train q ? This is nonobvious because we are considering a weakly
 141 supervised setting (i.e., learning only from tasks and not from (program, task) pairs). One approach
 142 is to sample programs from the DSL, run them to get their input/outputs, and then train q to predict
 143 the program from the input/outputs. This is like how a Helmholtz machine trains its recognition
 144 model during its “sleep” phase [18]. The advantage of “Helmholtz machine” training is that we can
 145 draw unlimited samples from the DSL, training on a large amount of data. Another approach is
 146 self-supervised learning, training q on the (program, task) pairs discovered by search. The advantage
 147 of self-supervised learning is that the training data is much higher quality, because we are training on
 148 the actual tasks. Due to these complementary advantages, we train on both these sources of data.

149 Formally, q should approximate the true posteriors over programs: minimizing the expected KL-
 150 divergence, $\mathbb{E}[\text{KL}(\mathbb{P}[p|x, \mathcal{D}, \theta] \| q(p|x))]$, equivalently maximizing $\mathbb{E}[\sum_p \mathbb{P}[p|x, \mathcal{D}, \theta] \log q(p|x)]$,
 151 where the expectation is taken over tasks. Taking this expectation over the empirical distribution of
 152 tasks gives self-supervised training; taking it over samples from the generative model gives Helmholtz-
 153 machine style training. The objective for a recognition model (\mathcal{L}_{RM}) combines the Helmholtz machine

154 $(\mathcal{L}_{\text{HM}})$ and self supervised $(\mathcal{L}_{\text{SS}})$ objectives, $\mathcal{L}_{\text{RM}} = \mathcal{L}_{\text{SS}} + \mathcal{L}_{\text{HM}}$:

$$\mathcal{L}_{\text{HM}} = \mathbb{E}_{(p,x) \sim (\mathcal{D}, \theta)} [\log q(p|x)] \quad \mathcal{L}_{\text{SS}} = \mathbb{E}_{x \sim X} \left[\sum_{p \in \mathcal{F}_x} \frac{\mathbb{P}[x, p | \mathcal{D}, \theta]}{\sum_{p' \in \mathcal{F}_x} \mathbb{P}[x, p' | \mathcal{D}, \theta]} \log q(p|x) \right]$$

155 2.4 Compression: Learning a Generative Model (a DSL)

156 The purpose of the DSL is to offer a set of abstractions that allow an agent to easily express solutions
 157 to the tasks at hand. Intuitively, we want the algorithm to look at the frontiers and generalize beyond
 158 them, both so the DSL can better express the current solutions, and also so that the DSL might expose
 159 new abstractions which will later be used to discover more programs. Formally, we want the DSL
 160 maximizing $\int \mathcal{L} \, d\theta$ (Sec. 2.1). We replace this marginal with an AIC approximation, giving the
 161 following objective for DSL induction:

$$\log \mathbb{P}[\mathcal{D}] + \arg \max_{\theta} \sum_{x \in X} \log \sum_{p \in \mathcal{F}_x} \mathbb{P}[x|p] \mathbb{P}[p|\mathcal{D}, \theta] + \log \mathbb{P}[\theta|\mathcal{D}] - \|\theta\|_0 \quad (3)$$

162 We induce a DSL by searching lo-
 163 cally through the space of DSLs,
 164 proposing small changes to \mathcal{D} until
 165 Eq. 3 fails to increase. The search
 166 moves work by introducing new λ -
 167 expressions into the DSL. We propose
 168 these new expressions by extracting
 169 fragments of programs already in the
 170 frontiers (Tbl. 2). An important point
 171 here is that we are *not* simply adding
 172 subexpressions of programs to \mathcal{D} , as
 173 done in the EC algorithm [12] and
 174 other prior work [29]. Instead, we are
 175 extracting fragments that unify with
 176 programs in the frontiers. This idea
 177 of storing and reusing fragments of expressions comes from Fragment Grammars [19] and Tree-
 178 Substitution Grammars [20], and is closely related to the idea of antiunification [?].

179 To define the prior distribution over (\mathcal{D}, θ) , we penalize the syntactic complexity of the λ -calculus
 180 expressions in the DSL, defining $\mathbb{P}[\mathcal{D}] \propto \exp(-\lambda \sum_{p \in \mathcal{D}} \text{size}(p))$ where $\text{size}(p)$ measures the size
 181 of the syntax tree of program p , and place a symmetric Dirichlet prior over the weight vector θ .

Algorithm 1 The CoCoSEA Algorithm

Input: Initial DSL \mathcal{D} , set of tasks X , iterations I
Hyperparameters: Enumeration timeout T
 Initialize $\theta \leftarrow \text{uniform}$
for $i = 1$ **to** I **do**
 $\mathcal{F}_x^\theta \leftarrow \{p | p \in \text{enum}(\mathcal{D}, \theta, T) \text{ if } \mathbb{P}[x|p] > 0\}$ (**Search**)
 $q \leftarrow \text{train recognition model, maximizing } \mathcal{L}_{\text{RM}}$ (**Compile**)
 $\mathcal{F}_x^q \leftarrow \{p | p \in \text{enum}(\mathcal{D}, q(x), T) \text{ if } \mathbb{P}[x|p] > 0\}$ (**Search**)
 $\mathcal{D}, \theta \leftarrow \text{induceDSL}(\{\mathcal{F}_x^\theta \cup \mathcal{F}_x^q\}_{x \in X})$ (**Compress**)
end for
return \mathcal{D}, θ, q

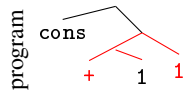
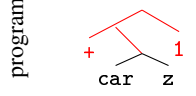
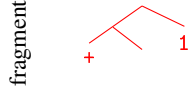
	Example programs in frontiers	Proposed λ -expression
program		$(\lambda (\ell) (\text{map } (\lambda (x) (\text{index } x \ell)) (\text{range } (- (\text{length } \ell) 1))))$ $(\text{map } (\lambda (x) (\text{index } x \ell)) (\text{range } \alpha))$
program		$(\lambda (s) (\text{map } (\lambda (x) (\text{if } (= x \text{'.'}) \text{'-' } x))) s)$ $(\lambda (s) (\text{map } (\lambda (x) (\text{if } (= x \alpha) \beta x))) s)$
fragment		$(\text{if } (= x \text{'-'}) \text{'-' } x)) s)$

Figure 2: **Left:** syntax trees of two programs sharing common structure, highlighted in red, from which we extract a fragment and add it to the DSL (bottom). **Right:** actual programs, from which we extract fragments that (top) slice from the beginning of a list or (bottom) perform character substitutions.

Putting all these ingredients together, Alg. 1 describes how we combine program search, recognition model training, and DSL induction.

3 Programs that manipulate sequences

We apply CoCoSEA to list processing (Section 3.1) and text editing (Section 3.2). For both these domains we use a bidirectional GRU [21] for the recognition model, and initially provide the system with a generic set of list processing primitives: `foldr`, `unfold`, `if`, `map`, `length`, `index`, `=`, `+`, `-`, `0`, `1`, `cons`, `car`, `cdr`, `nil`, and `is-nil`.

3.1 List Processing

Synthesizing programs that manipulate data structures is a widely studied problem in the programming languages community [3]. We consider this problem within the context of learning functions that manipulate lists with some involvement of integer arithmetic.

We created 236 human-interpretable list manipulation tasks, each with 15 input/output examples (Tbl. 2). Our data set is interesting in three major ways: many of the tasks require complex solutions; the tasks were not generated from some latent DSL, and the agent must learn to solve these complicated problems from only 236 tasks. Our data set assumes arithmetic operations as well as sequence operations, so we additionally provide our system with the following arithmetic primitives: `mod`, `*`, `>`, `is-square`, `is-prime`.

Name	Input	Output
repeat-2	[7 0]	[7 0 7 0]
drop-3	[0 3 8 6 4]	[6 4]
rotate-2	[8 14 1 9]	[1 9 8 14]
count-head-in-tail	[1 2 1 1 3]	2
keep-mod-5	[5 9 14 6 3 0]	[5 0]
product	[7 1 6 2]	84

Table 2: Some tasks in our list function domain. See the supplement for the complete data set.

We evaluated CoCoSEA on random 50/50 test/train split. Interestingly, we found that the recognition model provided little benefit for the training tasks. However, it yielded faster search times on held out tasks, allowing more tasks to be solved before timing out. The system composed 38 new subroutines, yielding a more expressive DSL more closely matching the domain (left of Tbl. 1, right of Fig. 2). See the supplement for a complete list of DSL primitives discovered by CoCoSEA.

3.2 Text Editing

Synthesizing programs that edit text is a classic problem in the programming languages and AI literatures [17, 22], and algorithms that learn text editing programs ship in Microsoft Excel [1]. This prior work presumes a hand-engineered DSL. We show CoCoSEA can instead start out with generic sequence manipulation primitives and recover many of the higher-level building blocks that have made these other text editing systems successful.

Because our enumerative search procedure cannot generate string constants, we instead enumerate programs with string-valued parameters. For example, to learn a program that prepends “Dr.”, we enumerate $(f_3 \text{ string } s)$ – where f_3 is the learned appending primitive (Fig. 1) – and then define $P[x|p]$ by approximately marginalizing out the string parameters via a simple dynamic program. In Sec. 4, we will use a similar trick to synthesize programs containing real numbers, but using gradient descent instead of dynamic programming.

We trained our system on a corpus of 109 automatically generated text editing tasks, with 4 input/output examples each. After three iterations, it assembles a DSL containing a dozen new functions (center of Fig. 1) that let it solve all of the training tasks.

How well does the learned DSL generalized to real text-editing scenarios? We tested, but did not train, on the 108 text editing problems from the SyGuS [23] program synthesis competition. Before any learning, CoCoSEA solves 3.7% of the problems with an average search time of 235 seconds. After learning, it solves 74.1%, and does so much faster, solving them in an average of 29 seconds. As of the 2017 SyGuS competition, the best-performing algorithm solves 79.6% of the problems.

231 But, SyGuS comes with a different hand-engineered DSL *for each text editing problem*.¹ Here we
 232 learned a single DSL that applied generically to all of the tasks, and perform comparably to the best
 233 prior work.

234 4 Symbolic Regression: Programs from visual input

235 We apply COCOSEA to symbolic regression problems. Here, the agent observes points along the
 236 curve of a function, and must write a program that fits those points. We initially equip our learner with
 237 addition, multiplication, and division, and task it with solving 100 symbolic regression problems, each
 238 either a polynomial of degree 1–4 or a rational function. The recognition model is a convolutional
 239 network that observes an image of the target function’s graph (Fig. 3) – visually, different kinds of
 240 polynomials and rational functions produce different kinds of graphs, and so the recognition model
 241 can learn to look at a graph and predict what kind of function best explains it. A key difficulty,
 242 however, is that these problems are best solved with programs containing real numbers. Our solution
 243 to this difficulty is to allow the system to write programs with real-valued parameters, and then
 244 fit those parameters by automatically differentiating through the programs the system writes and
 245 use gradient descent to fit the parameters. We define the likelihood model, $\mathbb{P}[x|p]$, by assuming a
 246 Gaussian noise model for the input/output examples, and penalize the use of real-valued parameters
 247 using the BIC [24].

248 COCOSEA learns a DSL containing 13 new functions, most of which are templates for polynomials of dif-
 249 ferent orders or ratios of polynomials. It also learns to find programs that minimize the number of contin-
 250 uous degrees of freedom. For example, it learns to represent linear functions with the program `(* real`
 251 `(+ x real))`, which has two continuous degrees of freedom, and represents quartic functions using the
 252 invented DSL primitive f_4 in the rightmost column of Fig. 1 which has five continuous parameters. This
 253 phenomenon arises from our Bayesian framing – both the implicit bias towards shorter programs and the
 254 likelihood model’s BIC penalty.

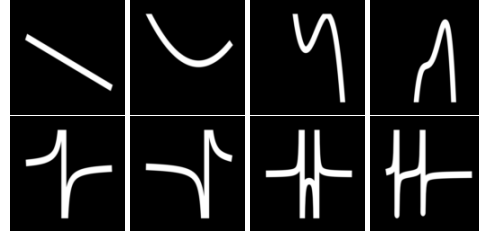


Figure 3: Recognition model input for symbolic regression. DSL learns subroutines for polynomials (top row) and polynomials (bottom row) while the recognition model jointly learns to look at a graph of the function (above) and predict which of those subroutines best explains the observation.

261 5 Quantitative Results

262 We compare with ablations of our model on held out tasks. The purpose of this ablation study is both
 263 to examine the role of each component of COCOSEA, as well as to compare with prior approaches in
 264 the literature: A head-to-head comparison of program synthesizers is complicated by the fact that
 265 each system, including ours, makes idiosyncratic assumptions about the space of programs and the
 266 statement of tasks. Nevertheless, much prior work can be modeled as special cases of our setup. We
 267 compare with the following baselines:

268 **No NN**, which lesions the recognition model.

269 **NPS**, which does not learn the DSL, instead learning the recognition model from samples drawn
 270 from the fixed DSL. We call this NPS (Neural Program Synthesis) because this setup is closest to
 271 how RobustFill [6] and DeepCoder [8] are trained.

272 **SE**, which lesions the recognition model and restricts the DSL learning algorithm to only add
 273 subexpressions of programs in the frontiers to the DSL. This is how prior approaches have learned
 274 libraries of functions [12, 27, 29].

275 **Enum**, which enumerates a frontier without any learning – equivalently, our first search step.

276 For each domain, we are interested both in how many tasks the agent can solve and how quickly
 277 it can find those solutions. Tbl. 3 compares our model against these alternatives. Our full model
 278 consistently improves on the baselines, sometimes dramatically (text editing and symbolic regression).
 279 The recognition model consistently increases the number of solved held-out tasks, and lesioning it
 280 also slows down the convergence of the algorithm, taking more iterations to reach a given number of

¹SyGuS text editing problems also prespecify the set of allowed string constants *for each task*. Our system does not use this assistance.

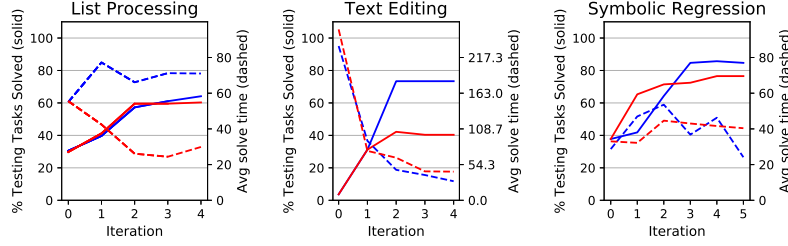


Figure 4: Learning curves for CoCoSEA both with (blue) and without (red) the recognition model. Solid lines: % holdout testing tasks solved. Dashed lines: Average solve time.

tasks solved (Fig. 4). This supports a view of the recognition model as a way of amortizing the cost of searching for programs.

6 Related Work

Our work is far from the first for learning to learn programs, an idea that goes back to Solomonoff [25]:

Deep learning: Much recent work in the ML community has focused on creating neural networks that regress from input/output examples to programs [6, 26, 17, 8]. CoCoSEA’s recognition model draws heavily from this line of work, particularly from [17]. We see these prior works as operating in a different regime: typically, they train with strong supervision (i.e., with annotated ground-truth programs) on massive data sets (i.e., hundreds of millions [6]). Our work considers a weakly-supervised regime where ground truth programs are not provided and the agent must learn from at most a few hundred tasks, which is facilitated by our “Helmholtz machine” style recognition model training (Sec. 2.3).

Inventing new subroutines for program induction: Several program induction algorithms, most prominently the EC algorithm [12], take as their goal to learn new, reusable subroutines that are shared in a multitask setting. We find this work inspiring and motivating, and extend it along two dimensions: (1) we propose a new algorithm for inducing reusable subroutines, based on Fragment Grammars [19]; and (2) we show how to combine these techniques with bottom-up neural recognition models. Other instances of this related idea are [27], Schmidhuber’s OOPS model [28], and predicate invention in Inductive Logic Programming [29].

Bayesian Program Learning: Our work is an instance of Bayesian Program Learning (BPL; see [30, 12, 31, 27]). Previous BPL systems have largely assumed a fixed DSL (but see [27]), and our contribution here is a general way of doing BPL with less hand-engineering of the DSL.

	Ours	No NN	SE	NPS	PCFG	Enum
<i>List Processing</i>						
% solved	79%	76%	71%	35%	62%	37%
Solve time	4.1s	5.8s	10.6s	34.7s	43.4s	20.2s
<i>Text Editing</i>						
% solved	74%	43%	30%	33%	0%	4%
Solve time	29s	65s	38s	80s	–	235s
<i>Symbolic Regression</i>						
% solved	84%	75%	62%	38%	38%	37%
Solve time	24s	40s	28s	31s	55s	29s

Table 3: % solved before timeout. Solve time: averaged over solved tasks. SE: NPS: trained like RobustFill/DeepCoder. PCFG: model w/o structure learning. Enum: model w/o any learning.

7 Contribution and Outlook

We contribute an algorithm, COCOSEA, that learns to program by bootstrapping a DSL with new domain-specific primitives that the algorithm itself discovers, together with a neural recognition model that learns how to efficiently deploy the DSL on new tasks. We believe this integration of top-down symbolic representations and bottom-up neural networks – both of them learned – could help make program induction systems more generally useful for AI. Many directions remain open. Two immediate goals are to integrate more sophisticated neural recognition models [6] and program synthesizers [14], which may improve performance in some domains over the generic methods used here. Another direction is to explore DSL meta-learning: Can we find a *single* universal primitive set that could effectively bootstrap DSLs for new domains, including the three domains considered, but also many others?

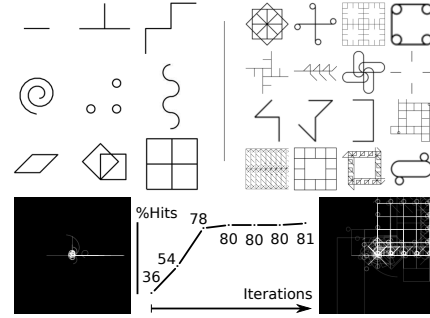


Figure 5: Top left: a few example of the shapes used as targets. Top right: a few examples of discovered new shapes. Bottom: learning curve across iterations in percent in the middle, and on both side average of the compiled new shapes before any training and at the end of the last iteration. See supplementary material for more details.

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